

Introduction To Data Science

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ASSIGNMENT # 5

Question-1)

Ans:-

S1 : "Sunshine state enjoy sunshine"

S2 : "Brown fox jump high, brown fox run"

S3 : "Sunshine state fox run fast."

BoW Model

output	Sunshine	State	enjoy	Brown	fox	jump	high	run	fast	Total
S1	2	1	1	0	0	0	0	0	0	4
S2	0	0	0	2	2	1	1	1	0	7
S3	1	1	0	0	1	0	0	1	1	5

Vector S1 : [2 1 1 0 0 0 0 0 0 0]

Vector S2 : [0 0 0 2 2 1 1 1 0]

Vector S3 : [1 1 0 0 1 0 0 1 1]

Term Frequency Model

	Sunshine	state	enjoy	Brown	fox	jump	high	run	fast
$T_f - S1$	$\frac{1}{2}$	$\frac{1}{4}$	$\frac{1}{4}$	0	0	0	0	0	0
$T_f - S2$	0	0	0	$\frac{2}{7}$	$\frac{2}{7}$	$\frac{1}{7}$	$\frac{1}{7}$	$\frac{1}{7}$	0
$T_f - S3$	$\frac{1}{5}$	$\frac{1}{5}$	0	0	$\frac{1}{5}$	0	0	$\frac{1}{5}$	$\frac{1}{5}$

IDF Model

	idf
Sunshine	$idf(\text{sunshine}) = \log\left(\frac{3}{2}\right) = 0.18$
State	$idf(\text{state}) = \log\left(\frac{3}{2}\right) = 0.18$
Enjoy	$idf(\text{Enjoy}) = \log\left(\frac{3}{1}\right) = 0.48$
Brown	$idf(\text{Brown}) = \log\left(\frac{3}{1}\right) = 0.48$
Fox	$idf(\text{Fox}) = \log\left(\frac{3}{2}\right) = 0.18$
Jump	$idf(\text{Jump}) = \log\left(\frac{3}{1}\right) = 0.48$
High	$idf(\text{High}) = \log\left(\frac{3}{1}\right) = 0.48$
Run	$idf(\text{Run}) = \log\left(\frac{3}{2}\right) = 0.18$
Fast	$idf(\text{Fast}) = \log\left(\frac{3}{1}\right) = 0.48$

TF-IDF :-

S1)

$$\begin{aligned} \text{tf-idf}(\text{sunshine}) &= \text{tf} * \text{idf} = \frac{1}{2} * 0.18 = 0.09 \\ \text{tf-idf}(\text{Stable}) &= \text{tf} * \text{idf} = \frac{1}{4} * 0.18 = 0.045 \\ \text{tf-idf}(\text{enjoy}) &= \text{tf} * \text{idf} = \frac{1}{4} * 0.48 = 0.12 \end{aligned}$$

S2)

$$\begin{aligned} \text{tf-idf}(\text{Brown}) &= \frac{2}{7} * 0.48 = 0.137 \\ \text{tf-idf}(\text{Fox}) &= \frac{2}{7} * 0.18 = 0.051 \\ \text{tf-idf}(\text{Jump}) &= \frac{1}{7} * 0.48 = 0.07 \\ \text{tf-idf}(\text{High}) &= \frac{1}{7} * 0.48 = 0.07 \\ \text{tf-idf}(\text{Run}) &= \frac{1}{7} * 0.18 = 0.026 \end{aligned}$$

S3)

$$\begin{aligned} \text{tf-idf}(\text{sunshine}) &= \frac{1}{5} * 0.18 = 0.036 \\ \text{tf-idf}(\text{Stable}) &= \frac{1}{5} * 0.18 = 0.036 \\ \text{tf-idf}(\text{Fox}) &= \frac{1}{5} * 0.18 = 0.036 \\ \text{tf-idf}(\text{Run}) &= \frac{1}{5} * 0.18 = 0.036 \\ \text{tf-idf}(\text{Fast}) &= \frac{1}{5} * 0.48 = 0.096 \end{aligned}$$

	idf(s1)	idf(s2)	idf(s3)
Sunshine	0.09	0	0.36
State	0.045	0	0.036
Enjoy	0.12	0	0
Brown	0	0.137	0
For	0	0.051	0.036
Jump	0	0.07	0
High	0	0.07	0
Run	0	0.026	0.036
Fast	0	0	0.096

Question - 2)

Ans:-

Cosine Similarity b/w $S1$ & $S3$

$$\text{Cos}(S1, S3) = \frac{(S1 \cdot S3)}{|S1| |S3|}$$

$$S1 = [2 \ 1 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$$

$$S3 = [1 \ 1 \ 0 \ 0 \ 1 \ 0 \ 0 \ 1 \ 1]$$

$$S1 \cdot S3 = 2 \times 1 + 1 \times 1 + 1 \times 0 + 0 \times 0 + 0 \times 1 + 0 \times 0 + 0 \times 0 + 0 \times 1 + 0 \times 1$$

$$S1 \cdot S3 = 3$$

$$|S1| = \sqrt{2^2 + 1^2 + 1^2 + 0^2 + 0^2 + 0^2 + 0^2 + 0^2 + 0^2} = \sqrt{6} = 2.45$$

$$|S3| = \sqrt{1^2 + 1^2 + 0^2 + 0^2 + 1^2 + 0^2 + 0^2 + 1^2 + 1^2} = \sqrt{5} = 2.24$$

$$\text{Cos}(S1, S3) = \frac{3}{(2.45)(2.24)}$$

$$\text{Cos}(S1, S3) = 0.55$$