

```

from sympy import symbols, And, Or, Not, Implies, to_cnf

# Define constants (entities in the problem)
John, Anil, Harry, Apple, Vegetables, Peanuts, x, y = symbols('John Anil Harry Apple Vegetables Peanuts x y')

# Define predicates as symbols (this works as a workaround)
Food = symbols('Food')
Eats = symbols('Eats')
Likes = symbols('Likes')
Alive = symbols('Alive')
Killed = symbols('Killed')

# Knowledge Base (Premises) in First-Order Logic
premises = [
    # 1. John likes all kinds of food: Food(x) → Likes(John, x)
    Implies(Food, Likes),

    # 2. Apples and vegetables are food: Food(Apple) ∧ Food(Vegetables)
    And(Food, Food),

    # 3. Anything anyone eats and is not killed is food: (Eats(y, x) ∧ ¬Killed(y)) → Food(x)
    Implies(And(Eats, Not(Killed)), Food),

    # 4. Anil eats peanuts and is still alive: Eats(Anil, Peanuts) ∧ Alive(Anil)
    And(Eats, Alive),

    # 5. Harry eats everything that Anil eats: Eats(Anil, x) → Eats(Harry, x)
    Implies(Eats, Eats),

    # 6. Anyone who is alive implies not killed: Alive(x) → ¬Killed(x)
    Implies(Alive, Not(Killed)),

    # 7. Anyone who is not killed implies alive: ¬Killed(x) → Alive(x)
    Implies(Not(Killed), Alive),
]

# Negated conclusion to prove: ¬Likes(John, Peanuts)
negated_conclusion = Not(Likes)

# Convert all premises and the negated conclusion to Conjunctive Normal Form (CNF)
cnf_clauses = [to_cnf(premise, simplify=True) for premise in premises]
cnf_clauses.append(to_cnf(negated_conclusion, simplify=True))

# Function to resolve two clauses
def resolve(clause1, clause2):
    """
    Resolve two CNF clauses to produce resolvents.
    """

```

Resolve two clauses to produce resolvents.

```
"""
clause1_literals = clause1.args if isinstance(clause1, Or) else [clause1]
clause2_literals = clause2.args if isinstance(clause2, Or) else [clause2]
resolvents = []
```

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for literal in clause1_literals:
    if Not(literal) in clause2_literals:
        # Remove the literal and its negation and combine the rest
        new_clause = Or(
            *[l for l in clause1_literals if l != literal],
            *[l for l in clause2_literals if l != Not(literal)]
        ).simplify()
        resolvents.append(new_clause)

return resolvents
```

Function to perform resolution on the set of CNF clauses

```
def resolution(cnf_clauses):
```

```
    """
```

```
    Perform resolution on CNF clauses to check for a contradiction.
```

```
    """
```

```
    clauses = set(cnf_clauses)
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```
    new_clauses = set()
```

```
    while True:
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        clause_list = list(candidates)
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        for i in range(len(clause_list)):
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            for j in range(i + 1, len(clause_list)):
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```
                resolvents = resolve(clause_list[i], clause_list[j])
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                if False in resolvents: # Empty clause found
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                    return True # Contradiction found; proof succeeded
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```
                new_clauses.update(resolvents)
```

```
        if new_clauses.issubset(candidates): # No new information
```

```
            return False # No contradiction; proof failed
```

```
    candidates.update(new_clauses)
```

Perform resolution to check if the conclusion follows

```
result = resolution(cnf_clauses)
```

```
print("Does John like peanuts? ", "Yes, proven by resolution." if result else "No, cannot be proven.")
```



Does John like peanuts? Yes, proven by resolution.

```

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# Define predicates as symbols (this works as a workaround)
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Likes = symbols('Likes')
Alive = symbols('Alive')
Killed = symbols('Killed')

# Knowledge Base (Premises) in First-Order Logic
premises = [
    # 1. John likes all kinds of food:  $\text{Food}(x) \rightarrow \text{Likes}(\text{John}, x)$ 
    Implies(Food, Likes),

    # 2. Apples and vegetables are food:  $\text{Food}(\text{Apple}) \wedge \text{Food}(\text{Vegetables})$ 
    And(Food, Food),

    # 3. Anything anyone eats and is not killed is food:  $(\text{Eats}(y, x) \wedge \neg \text{Killed}(y)) \rightarrow \text{Food}(x)$ 
    Implies(And(Eats, Not(Killed)), Food),

    # 4. Anil eats peanuts and is still alive:  $\text{Eats}(\text{Anil}, \text{Peanuts}) \wedge \text{Alive}(\text{Anil})$ 
    And(Eats, Alive),

    # 5. Harry eats everything that Anil eats:  $\text{Eats}(\text{Anil}, x) \rightarrow \text{Eats}(\text{Harry}, x)$ 
    Implies(Eats, Eats),

    # 6. Anyone who is alive implies not killed:  $\text{Alive}(x) \rightarrow \neg \text{Killed}(x)$ 
    Implies(Alive, Not(Killed)),

    # 7. Anyone who is not killed implies alive:  $\neg \text{Killed}(x) \rightarrow \text{Alive}(x)$ 
    Implies(Not(Killed), Alive),
]

# Negated conclusion to prove:  $\neg \text{Likes}(\text{John}, \text{Peanuts})$ 
negated_conclusion = Not(Likes)

# Convert all premises and the negated conclusion to Conjunctive Normal Form (CNF)
cnf_clauses = [to_cnf(premise, simplify=True) for premise in premises]
cnf_clauses.append(to_cnf(negated_conclusion, simplify=True))

# Function to resolve two clauses
def resolve(clause1, clause2):
    """
    Resolve two CNF clauses to produce resolvents.
    """
    clause1_literals = clause1.args if isinstance(clause1, Or) else [clause1]
    clause2_literals = clause2.args if isinstance(clause2, Or) else [clause2]
    resolvents = []

    for literal in clause1_literals:
        if Not(literal) in clause2_literals:
            # Remove the literal and its negation and combine the rest
            new_clause = Or(
                *[l for l in clause1_literals if l != literal],
                *[l for l in clause2_literals if l != Not(literal)]
            ).simplify()
            resolvents.append(new_clause)

    return resolvents

# Function to perform resolution on the set of CNF clauses
def resolution(cnf_clauses):
    """
    Perform resolution on CNF clauses to check for a contradiction.
    """
    clauses = set(cnf_clauses)
    new_clauses = set()

    while True:
        clause_list = list(clauses)
        for i in range(len(clause_list)):
            for j in range(i + 1, len(clause_list)):
                resolvents = resolve(clause_list[i], clause_list[j])
                if False in resolvents: # Empty clause found
                    return True # Contradiction found; proof succeeded
                new_clauses.update(resolvents)

        if new_clauses.issubset(clauses): # No new information
            return False
    
```

```
        return False # No contradiction; proof failed

    clauses.update(new_clauses)

# Perform resolution to check if the conclusion follows
result = resolution(cnf_clauses)
print("Does John like peanuts? ", "Yes, proven by resolution." if result else "No, cannot be proven.")

→ Does John like peanuts? Yes, proven by resolution.
```