

## INDEX

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29/10/24

## Genetic Algorithm

Algorithm Genetic Algorithm to Maximize  $f(u) = u^2$

Input:

- \* population size (pop-size).
- \* Number of generations (generations).
- \* Mutation rate (mutation-rate).
- \* Crossover rate (crossover-rate).
- \* Range of  $u$  ( $u_{\text{range-low}}, u_{\text{range-high}}$ ).

Output:

- \* Best Solution  $x$  that maximizes  $f(u) = u^2$ .
- \* Best fitness  $f(u)$ .

Procedure:

1. Initialize population of size 'pop-size' with random values in range  $[x_{\text{range-low}}, x_{\text{range-high}}]$ .

2. For generation in range(generations):

a. Evaluate fitness of each individual:

For each individual  $x_i$  in population:

$$\text{fitness}(x_i) = x_i^2.$$

b. Select two parents based on fitness value (roulette-wheel Selection):

total\_fitness = sum of all fitness values.

For each individual  $x_i$  in population:

$$\text{probability}(x_i) = \text{fitness}(x_i) / \text{total\_fitness}$$

Select two parents ( $p_1, p_2$ ) based on probability.

c. Perform crossover with probability 'crossover\_rate':  
if random\_number < crossover\_rate:

$\alpha$  = random value between 0 and 1

$$\text{Offspring 1} = \alpha * p_1 + (1 - \alpha) * p_2$$

$$\text{Offspring 2} = \alpha * p_2 + (1 - \alpha) * p_1$$

else:

$$\text{Offspring 1} = p_1$$

$$\text{Offspring 2} = p_2$$

d. Apply mutation with probability 'mutation\_rate':

For each offspring:

if random\_number < mutation\_rate:

offspring = random value in range [ $x_{\text{range\_low}}$ ,  $x_{\text{range\_high}}$ ]:

e. Update population with new offspring.

3. Terminate after maximum generations or convergence.

4. Output the best individual and fitness value.

~~e. Update population with new offspring~~ ~~Swapping~~ ~~10/10~~

~~new\_population.extend([Offspring 1, Offspring 2])~~

~~population = new\_population[:pop\_size]~~

genetic algorithm(pop\_size, num\_of\_gen, x\_range\_low, x\_range\_high, mutation\_rate, crossover\_rate)

07/11/23

## Particle Swarm Optimization

### 1. Rastrigin function

#### Purpose

The Rastrigin function is a benchmark function used for optimization, it is used to evaluate the fitness of the particles' position during optimization.

#### Algorithm

Given a vector of  $n$  dimension, the Rastrigin function is defined as

$$f(x) = 10n + \sum_{i=1}^n [x_i^2 - 10 \cos(2\pi x_i)]$$

#### pseudo code

function rastrigin( $x$ ):

$n = \text{length of } x$

result =  $10^n$

for  $i = 1$  to  $n$

    result = result +  $(x[i]^2 - 10 \cos(2\pi x[i]))$

return result

### 2. Particle class

#### Purpose

The particle class represents an individual solution (particle) in the Swarm. Each particle has a position, velocity, and the best position it has found so far.

phuedo code

Class particle

function init (dim, bounds)

position = random value in bounds

Velocity = random values between -1 and 1

best\_position = position

best\_value = random (position)

function evaluate():

current\_value = random (position)

If current\_value < best\_value:

best\_value = current\_value

best\_position = position

### 3. PSO Algorithm

purpose

The PSO algorithm is the main procedure that "drives" the swarm to converge towards an optimal solution. It updates particle velocities and positions iteratively based on their own best position and the global best position found by the entire swarm.

function pso(dim, bounds, num\_particles, max\_iter, w) ~~(c)~~

particles = [create particle (dim, bounds) for i=1 to num\_particles]

global\_best\_position = None

global\_best\_value = infinity

for iter=1 to max\_iter:

for each particle in particles:

particle.evaluate()

If  $\text{particle\_best\_value} < \text{global\_best\_value}$   
 $\text{global\_best\_value} = \text{particle\_best\_value}$   
 $\text{global\_best\_position} = \text{particle\_best\_position}$

for each particle in particles:

$$\begin{aligned} \text{Inertia} &= w * \text{particle\_velocity} \\ \text{Cognitive} &= (1 - \text{random value}) * (\text{particle\_best\_position} - \text{particle\_position}) \\ \text{Social} &= c_2 * \text{random value} + (\text{global\_best\_position} - \text{particle\_position}) \end{aligned}$$

$$\text{particle\_Velocity} = \text{Inertia} + \text{Cognitive} + \text{Social}.$$

$$\text{particle\_position} = \text{particle\_position} + \text{particle\_Velocity}$$

$$\text{particle\_position} = \text{clip}(\text{particle\_position}, \text{bound}[0], \text{bound}[1]).$$

return global-best-position, global-best-value

#### 4. Velocity and Position Update

The velocity and position of each particle are updated in each iteration based on three key components: Inertia, Cognitive, and Social.

Phases code:

function update\_velocity\_and\_position(particle, global-best-position, w, c<sub>1</sub>, c<sub>2</sub>, bounds):

$$\text{Inertia} = w * \text{particle\_velocity}$$

$$\text{Cognitive} = (1 - \text{random}) * (\text{particle\_best\_position} - \text{particle\_position})$$

$$\text{Social} = c_2 * \text{random}() * (\text{global\_best\_position} - \text{particle\_position})$$

particle velocity = inertial + cognitive + social.  
~~particle position = random + global + local position~~

particle position = particle, position, particle velocity,  
particle position = clip (particle, position, bounds[0],  
bounds[1])

# Ant Colony Optimization

## for Travelling Salesman Problem,

1) Define the problem - Create a set of cities with coordinates.

pseudoCode

$city = \text{array of city coordinates}$

function calculateDistance( $city$ ):

$\text{num\_city} = \text{length}(city)$

$distance = \text{matrix of size num\_city} \times num\_city$

for each city  $i$ :

for each city  $j$ :

$distance[i][j] = \text{Euclidean distance}$   
between city  $i$  and city  $j$

Explanation: return  $distance$ .

The function calculate-distance computes the pairwise Euclidean distance between all cities. This forms a distance matrix that will be used to help evaluate the length of tour created by ants.

2) Initialize Parameters

pseudoCode

$\text{num\_ants} = \text{number of ants}$

$\alpha = \text{influence of pheromone}$

$\beta = \text{influence of heuristic (inverse distance)}$

$\gamma = \text{evaporation rate of pheromone}$

$\text{num\_iterations} = \text{num of iterations}$

$\text{initial\_pheromone} = \text{initial pheromone value of all edges}$

$distanas = \text{calculate distances}(\text{dist})$

$\text{pheromone\_matrix} = \text{matrix of size num\_city} \times \text{num\_city}$ , filled with initial pheromone.

$eta = \text{matrix of heuristic information } (\frac{1}{\text{distance}})$

Set up the algorithm parameters such as the number of ants, the influence of pheromone and heuristic information, the pheromone evaporation rate, and the number of iterations.

Initialize the pheromone matrix where all values stand with same initial pheromone level.

Calculate the heuristic matrix eta, which is the inverse of the distance matrix. It emphasizes the shorter distance during the construction of solutions.

### 3. Heuristic Information - heuristic function

Function: heuristic( $\text{distances}$ )

Create an empty matrix eta of the same size of distances.

For  $i = 0$  to number of rows in distances;

for  $j = 0$  to number of columns in distances;

If  $\text{distances}[i][j] \neq 0$ :

Set  $\text{eta}[i][j] =$

$\frac{1}{\text{distances}[i][j]}$

Else,

Set  $\text{eta}[i][j]$  to a

large value (to avoid division by zero).

return eta.

The heuristic function computes the inverse of the distance matrix where each element depends on the

denote value for moving from one city to another.  
This value helps the ant favor paths by influencing the probability calculation.

### 3. Choose Next City - chooseNextCity function

pseudo code

Function chooseNextCity(phomone, etc, visited,  
initProb or empty list prob):  
For each city  $j$  from 0 to num cities:  
If city  $j$  has not been visited:  
calculated phomone $=j =$   
phomone[visited[G][T][j]] raised to alpha.  
Calculate heuristic $_j = \text{dist}[\text{visited}[G][T][j]]$   
raised to beta.

Append phomone $_j$  & heuristic $_j$  to prob  
list:

Append 0 to prob.

Normalize prob so that the sum of all probabilities  
equal 1.

return a randomly Selected City Index  
based on the probabilities.

Explanation:

This function Selects the next city for an ant to visit based on a probabilistic approach.

### 4. Construct Solution - constructSolution function

Function constructSolution(phomone, etc):

initialize an empty list tour

Select a random City and add it to the tour  
while the length of tour is less than num cities  
call chooseNextCity to select the next city

Add the selected city to the tour  
within the tour.

\* gift function constructs a complete tour for a single ant.

### 5. Update Pheromone

Function update\_pheromone (pheromone, all\_tour, distance, best\_tour);

Evaporate pheromone by multiplying it by  $(1 - rho)$ .

For each tour in allTour;

Calculate the tour length by summing the distance between consecutive cities in the tour

For each consecutive pair of cities in the tour;

Add  $\frac{1}{\text{tour.length}}$  to pheromone[City 1][City 2]  
Calculate the length of the best tour

For each consecutive pair of cities in the best tour;

Add  $\frac{1}{\text{best.length}}$  to pheromone[City 1][City 2]

\* This function updates the pheromone matrix after each iteration. Pheromone values evaporate (decay) over time, and new pheromones are deposited based on the tour completed by all ants.

### 6. ACO Main loop - run\_aco function

Function run\_aco(distanse, numIterations);

Initialize pheromone matrix with initial pheromone value.

Set best-four to None and best-length to infinity

For iteration = 1 to num\_iterations

Initialize an empty list all-four

For each ant:

Construct a solution (four) using construct\_solution

Add the four to all-four.

Calculate the length of each four in all-four.

Find the best four and best length from all-four.

If the best four found in this iteration is better than the previous best:

Update best-four and best-length.

Update the pheromone matrix using update-pheromone.

Print the best length at the end of this iteration

return best-four and best-length

\* The run\_aro function runs the ACO algorithm over multiple iterations in each iteration.

\* Multiple ants construct their four.

\* The best four is selected, and pheromone are updated accordingly.

\* The algorithm continues until the maximum number of iterations is reached, and the best solution is returned.

3) Plot the Best Route - plot\_route function

function plot\_route(Cities, best-four):

Create a figure for plotting

For each city in Cities:

plot the city at a red point and label it with its index.

Create a list of cities in the best tour,  
including the start city at the end so  
Complete the loop.

plot the cities in the best tour as  
blue lines connecting them.

Set title as "Best tour (length: bestLength)"  
Add labels for N and y-axis.

Show the plot.

# This function visualizes the best tour found  
by the ACO algorithm. It plots the cities as  
red points, connects the cities in the order of  
the best tour with blue lines, and displays  
the result in a plot, showing the route  
and the length of the best tour.

Rishabh

14/11/24

21/11/20

## Cuckoo Search (CS) CS

### 1. Define the problem.

The problem is defined by an objective function,  
and we call it the Sphere function.

$f(x) = \sum x_i^2$  at the function to minimize

parameters

objective function  $f(x) = \sum (x - i)^2$

### 2. Initialize parameters

parameters such as the number of nests, number of iterations, discovery rate, and search space boundaries are initialized.

parameters

$$\text{num\_nest} = 25$$

$$\text{num\_iterations} = 100$$

$$\text{discovery\_rate} = 0.25$$

$$\text{dim} = 5$$

$$\text{lower\_bound} = -10$$

$$\text{upper\_bound} = 10$$

### 3. Initialize Population

A population of nests is randomly initialized within the defined boundaries,

parameters

$\text{nests} = \text{random.uniform(lower\_bound, upper\_bound, num\_nest, dim)}$

$\text{f\_nests} = [\text{evaluate fitness}(x_{i,t}) \text{ for } i \in \text{nests}]$

#### 4. Evaluate fitness

The fitness of each nest is evaluated using the objective function. The best nest is selected based on the lowest fitness value.

fitness<sub>nest</sub>

$$\text{best\_nest} = \min(\text{nest}, \text{by} = \text{fitness})$$

$$\text{best\_fitness} = \min(\text{fitness})$$

#### 5. Generate New Solution (Levy flight)

New Solution are generated via Levy flight, which help explore the search space more efficiently.

fitness<sub>nest</sub>

for each nest:

$$\text{Step\_Size} = \text{Levy\_Flight}(\lambda)$$

$$\text{new\_solution} = \text{nest} + \text{Step\_Size}^{\alpha} (\text{nest} - \text{best\_nest})$$

$$\text{new\_solution} = \text{Clip}(\text{new\_solution}, \text{lower\_bound}, \text{upper\_bound})$$

$$\text{fitness} = \text{evaluate\_fitness}(\text{new\_solution}),$$

#### 6. Abandon Worst nest

Some of the worst nests are abandoned and replaced with new random Solution based on the discovery rate.

fitness<sub>nest</sub>

for each nest with a probability discovery rate;

$$\text{new\_random\_solution} = \text{random\_uniform}(\text{lower\_bound}, \text{upper\_bound}).$$

$$\text{fitness} = \text{evaluate\_fitness}(\text{new\_random\_solution}).$$

### 7. Iteration

The algorithm repeats the process of generating new solutions, updating, and evaluate fitness over multiple iterations.

### Pseudo Code:

```
for iteration in range(num_iterations):
    generate_new_solutions()
    update_best_mutation()
    track_best_fitness()
```

### 8. Output the Best Solution

After completing the iterations, the best mutation found is returned, representing the optimal solution.

### Pseudo Code:

```
return best_mutation, best_fitness
```

### Applications

- Structural optimization, Aerospace design,
- Feature selection, Hyper parameter Tuning, bridge design,
- fruit optimization, noise reduction.

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21/11/24

## Crazy Wolf Optimizer

### 1. Define the problem (objective function).

Define the objective function that takes position of a wolf (a candidate solution) and returns the function's value at that position. The value is called the fitness. Use  $f(x)$  the Sphere function, which calculates the sum of the squares of the position vector components.

Placeholder

FUNCTION Objective function (position):

$$\text{sum} = 0$$

For  $i$  in range(0, len(position)):

$$\text{sum} = \text{position}[i]^2$$

return SUM.

### 2.) Initialize the parameters

Set the number of wolves (population size), the number of iterations and the bounds which the wolves will search for the optimal solution.  
Placeholder

$$\text{num\_wolves} = 30$$

$$\text{num\_dimensions} = 5$$

$$\text{num\_iterations} = 100$$

$$\text{bounds} = [-10, 10]$$

$$\# lb = -10, Ub = 10$$

### 3.) Initialize Population

Generate random positions for all the wolves

in the population within the defined bounds.

pheno\_creat function (int[] alpha\_wolves, num\_wolves,  
num\_dimensions,  
bounds):

Population = []

For i in range(num\_wolves):  
position = []

For d in range(num\_dimensions):  
position[d] = random value  
(bounds)

Population.append(position)  
return Population.

Explanation: Each wolf's position is initialized  
randomly within the search space bounds.  
Each wolf is a candidate solution  
represented by a vector in multi-dimensional space.

g) Evaluate fitness(Rank) wolves at Alpha, Beta, Delta

pheno\_creat

function evaluate\_fitness(population):

alpha\_fitness = infinity

beta\_fitness = infinity

delta\_fitness = infinity

For wolf in population:

fitness = objective function(wolf.position)

If fitness < alpha\_fitness:

alpha\_fitness = Beta\_fitness

Alpha\_position = Beta\_position

$$\begin{aligned}\text{beta-fitness} &= \text{alpha-fitness} \\ \text{beta-position} &= \text{alpha-position}\end{aligned}$$

$$\text{alpha-fitness} = \text{fitness}$$

$$\text{alpha-position} = \text{wolf-position}$$

Else if  $\text{fitness} < \text{beta-fitness}$ :

$$\begin{aligned}\text{delta-fitness} &= \text{beta-fitness} \\ \text{delta-position} &= \text{beta-position}\end{aligned}$$

$$\begin{aligned}\text{beta-fitness} &= \text{fitness} \\ \text{beta-position} &= \text{wolf-position}\end{aligned}$$

Else if  $\text{fitness} < \text{delta-fitness}$ :

$$\begin{aligned}\text{delta-fitness} &= \text{fitness} \\ \text{delta-position} &= \text{wolf-position}\end{aligned}$$

return  $\text{alpha-position}, \text{beta-position}, \text{delta-position}$ .

Explanation: Each wolf's fitness is calculated using the objective function, and the wolves are ranked. The top three wolves (with the best-fitness values) are classified as alpha, beta, and delta wolf.

### 5) Update Position (Simulate wolf Movement)

Procedure

function update\_position(population, alpha-position, beta-position, delta-position, a, bounds):

For each wolf in population:

For  $d$  in range (num-dimensions):

$$A_1 = 2 * a * \text{random\_value}() - a$$

$$A_2 = 2 * a * \text{random\_value}() - a$$

$$A_3 = 2 * a * \text{random\_value}() - a$$

$$(1 = 2 * \text{random\_value})$$

$$(2 = 2 * \text{random\_value})$$

$$(3 = 2 * \text{random\_value})$$

$$D_{\text{alpha}} = \text{abs}((C_1^{\text{alpha}} \cdot \text{alpha\_position}[d]) - 60) / \text{position}(A_1)$$

$$D_{\text{beta}} = \text{abs}((C_2^{\text{beta}} \cdot \text{beta\_position}[d]) - 60) / \text{position}(A_2)$$

$$D_{\text{delta}} = \text{abs}((C_3^{\text{delta}} \cdot \text{delta\_position}[d]) - 60) / \text{position}(A_3)$$

$$\gamma_1 = \text{alpha\_position}[d] - A_1 \cdot D_{\text{alpha}}$$

$$\gamma_2 = \text{beta\_position}[d] - A_2 \cdot D_{\text{beta}}$$

$$\gamma_3 = \text{delta\_position}[d] - A_3 \cdot D_{\text{delta}}$$

$$\text{Wolf\_position}[d] = (\gamma_1 + \gamma_2 + \gamma_3) / 3$$

$$\text{Wolf\_position}[d] = \text{clamp}(\text{Wolf\_position}[d], \text{bounds}[0], \text{bounds}[1])$$

Each wolf's position is updated by calculating the distance from alpha, beta, and delta. Wolf's new position are based on the weighted influence of these three beta wolf. The "a" parameter decreases over time to switch from exploration to exploitation.

### c) generate

for iteration in range(num\_iterations):

    alpha\_position, beta\_position, delta\_position =  
        evaluate\_fitness(population).

$$a = 2 - (\text{iteration} / (\text{num\_iterations}))$$

    update\_population(population, alpha\_position, beta\_position, delta\_position, a, bounds)

Exploration The algorithm runs through multiple iterations, update wolf's position for each iteration. The coefficient "a" decreases over time, shifting the policy from exploration to exploitation. The best solution is printed at each iteration.

## j) Output the Best Solution.

Print "final best solution", alpha-position  
and "Fitness of best solution", alpha-fitness

At the end of the iterations, the best solution  
(alpha wolf's position) and its fitness are reported.  
This is the optimal or near-optimal solution  
found during the optimization process.

### Applications

1- Optimization problem in Engineering, (Structural design).

2- Machine learning and Artificial Intelligence (feature extraction  
and selection).

3- Optimization of Energy Systems, (Renewable energy  
optimization).

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28/11/24

17/12/24

## Parallel Cellular Algorithm

→ objective function

The function is used at Sphere function particularly used in the optimization algorithms.

def Sphere-function(position):

return sum( $position_i^{1/2}$  for each position  $i$  in position)

→ Initialize the Population Grid

This function is used to create a grid of shape and fill with random values uniformly distributed between lower-bound and upper-bound.

def initialize\_population(grid\_size, solution\_dim, lower\_bound, upper\_bound):

Initialize grid with random values in given bounds return grid.

→ Evaluate fitness

This function is used to evaluate the fitness.

for each cell in the grid

def evaluate\_fitness(grid):

for each cell in grid:

Calculate fitness using Sphere-function(cell position)

return fitness grid

→ Get Neighbours of a cell

def get\_neighbours(grid, i, j):

Initialize empty list for neighbour

For each  $(d_i, d_j)$  in  $\{(-1, -1), (-1, 0), (1, 1)\}$   
 excluding  $(0, 0)$ :

$$n_i^j = (i + d_i) \% \text{grid\_size}$$

$$n_j^i = (j + d_j) \% \text{grid\_size}$$

Add  $\text{grid}[n_i^j][n_j^i]$  to neighbour list  
 return neighbour

→ Update State of all Cells in the Grid  
 The function it will get the neighboring cells,  
 Identify the neighbor with best fitness, and move  
 Cells towards the best neighbor's position.

```
def Update_State(grid, fitness, learning_rate):
    Initialize new-grid as a copy of grid
    For each cell(i, j) in grid:
        Get neighbors of cell(i, j)
        Find the best neighbor with minimum
        fitness update cell position:
        new-grid[i, j] = grid[i, j] + learning_rate *
        (best_neighbor_grid[i, j])
```

return new-grid

→ Main parallel Cellular Algorithm

The main algorithm includes initialize the  
 population grid, and for a given number of  
 iterations evaluate fitness, update State based on  
 neighbors & track best solution, and output best  
 solution f fitness.

```
def parallel_cellular_algorithm(grid_size, solution_dim,
    lower_bound, upper_bound, iterations, learning_rate):
    Initialize grid with random positions
    Set best_solution = None and best_fitness = infinity
```

For iteration in range(Iterations):

Evaluate fitness of all cells.

Identify current best solution and fitness of current. If current fitne is better than best-fitne.

Update best-solution and best-fitness.

Update all states using neighbour and learning rate

print current best-fitness

Output best solution and best-fitness

if name == "main":

parallel cellular algorithm(grid\_size = 10, Solution, dim = 2, lower\_bound = 5,

upper\_bound = 5.0, Iterations = 50, learning\_rate = 0.02)

Outputs:

Best Solutions [-0.0095922, 0.03401244]

Best Fitness: 0.00125

## Optimization via Cine Evolution Algorithm

### → Objective function

This function calculates fitness of a given solution using target objective function.

```
def targetfn(x):
    A = 10
```

$$\text{result} = A * \text{length}(x)$$

for each  $x_i$  in  $x$ :

$$\text{result} += (x_i^{12} - A^2 \cos(2\pi p_i x_i))$$

return result

### → Initialize population

Initializes a random population of solutions, each solution represented by a set of genes.

```
def initialize_population(pop_size, num_genes, lower_bound,
                           upper_bound):
```

population = Randomly generate pop\_size individual with num\_genes in range [lower\_bound, upper\_bound]

return population

### → Evaluate fitness

```
def evaluate_fitness(population):
```

fitness → list of targetfn(individual) for each individual in population.

return fitness

### $\hookrightarrow$ Tournament Selection

def tournament\_selection(population, fitness\_tournament\_size):

Selected = for each individual, select the winner of a random tournament from the population.

return Selected

### $\hookrightarrow$ Crossover

Create two offspring from two selected parents by combining their genetic material at a random crossover point.

def crossover(parent1, parent2):

crossover\_point = Randomly choose a point

child1 = Combine parent1 & parent2 at crossover point

child2 = Combine parent2 & parent1 at crossover point  
return child1, child2.

### $\rightarrow$ Mutation

Introduce random mutation in the offspring with a given probability, allow the solution to explore new area of the search space.

def mutate(child, mutation\_rate, lower\_bound, upper\_bound)  
for each gene in child, randomly mutate with probability mutation\_rate.

return mutated child

### $\rightarrow$ Gene Expression Algorithm

This is main loop that evolves the population over several generations, applying selection, crossover, mutation, and finally evaluate to find the best solution.

def gene\_explusion\_algorithm (pop\_size, num\_genet, lower\_bound, upper\_bound, mutation\_rate, crossover\_rate, num\_generations):

population = Initialize population

best\_solution = None, best\_fitness = infinity

for generation = 1 to num\_generations:

fitness = evaluate\_fitness.

Update best Solution if needed

Selected\_population = Tournament Selection

new\_population = for each pair of parents apply crossover and mutation

population = new\_population

return best\_solution, best\_fitness.

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8/12/24