# Statistical Practice in Epidemiology with

# Computer exercises

IARC Lyon 14–20 June 2018

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# Contents

	Prog	gram	•	1		
1	Exe	Exercises 1				
	Intro	oduction to practicals		1		
	1.1	Practice with basic R		2		
	1.2	Reading data into R		15		
	1.3	Tabulation		22		
	1.4	Graphics in R		25		
	1.5	Simple simulation		31		
	1.6	Calculation of rates, RR and RD		33		
	1.7	Logistic regression (GLM)		39		
	1.8	Estimation of effects: simple and more complex		45		
	1.9	Estimation and reporting of curved effects		53		
	1.10			60		
	1.11	Survival analysis: Oral cancer patients		64		
		Time-splitting, time-scales and SMR		73		
		Causal inference		78		
		Nested case-control study and case-cohort study:				
		Risk factors of coronary heart disease		82		
	1.15	Time-dependent variables and multiple states		91		
<b>2</b>	Solutions 99					
	2.3	Tabulation		100		
	2.4	Graphics in R		107		
	2.5	Simple simulation				
	2.6	Calculation of rates, RR and RD				
	2.7	Logistic regression (GLM)				
	2.8	Estimation of effects: simple and more complex				
	2.9	Estimation and reporting of curved effects				
	2.11					
	2.12					
		Causal inference				
		Nested case-control study and case-cohort study:				
		Risk factors of coronary heart disease		227		
	2.15	Time-dependent variables and multiple states				
	_	1		_		

### Program

```
Daily timetable
 9:00 - 9:30
              Recap of yesterday's practicals
 9:30 - 10:30
               Lecture
               Coffee break
10:30 - 11:00
11:00 - 13:00
               Practical
13:00 - 14:00
               Lunch
14:00 - 14:30
               Recap of morning's practical
14:30 - 15:30
               Lecture
15:30 - 16:00
               Tea break
               Practical
16:00 - 18:00
Thursday 14 June
 8:30 - 9:00
              Registration
 9:00 - 9:15
               Welcome (MP)
 9:15 - 10:30
               R History and Ecology (MP)
               Coffeee break
10:30 - 11:00
11:00 - 13:00
               Practical: Practice with basic R
               Simple reading and data input
13:00 - 14:00
               Lunch
14:00 - 14:30
               Recap of morning practical
14:30 - 15:30
               Language, indexing,
                                      subset(),
                                                   ifelse(), attach(), detach(),
               search. Simple simulation. Simple graphics. (KF)
               Tea break
15:30 - 16:00
16:00 - 18:00
               Practical: Simple simulation
               Tabulation
               Introduction to graphs in R
18:00 -
               Welcome reception
Friday 15 June
 9:00 - 9:30
               Recap of yesterday's practicals.
 9:30 - 10:30
               Poisson regression for follow-up studies — likelihood for a constant rate
               Logistic regression for cc-studies (JP)
10:30 - 11:00
               Coffeee break
11:00 - 13:00
               Practical: Rates, rate ratio and rate difference with glm
               Logistic regression with glm
               Lunch
13:00 - 14:00
14:00 - 14:30
               Recap of morning practical
14:30 - 15:45
               Linear and generalized linear models (EL)
               All you ever wanted to know about splines (MP)
               Tea break
15:45 - 16:15
               Practical: Simple estimation of effects
16:15 - 18:00
               Estimation and reporting of linear and curved effects
```

2 SPE practicals

### Saturday 16 June 9:00 - 9:30 Recap of ves

9:00 – 9:30 Recap of yesterday's practicals

9:30 – 10:30 More advanced graphics in R, including ggplot2 (MP)

10:30 - 11:00 Coffee break.

11:00 – 13:00 Practical: Graphical meccano

### Monday 18 June

9:00 - 9:30 Recap of yesterday's practicals

9:30-10:30 Survival analysis: Kaplan Meier & simple Cox-model. Simple competing risks and relative survival. (JP)

10:30 - 11:00 Tea break

11:00 – 13:00 Practical: Survival and competing risks in oral cancer. Relative survival.

13:00 - 14:00 Lunch

14:00 – 14:30 Recap of morning practical

14:30 – 15:30 Dates in R; follow up representation in Lexis objects, time-splitting, multistate model and SMR. (BxC)

15:30 - 16:00 Coffee break.

16:00 – 18:00 Practical: Time-splitting and SMR (Danish diabetes patients)

### Tuesday 19 June

9:00 - 9:30 Recap of yesterday's practicals

9:30 – 10:30 Nested and matched cc-studies & Case-cohort studies (EL)

10:30 - 11:00 Coffee break.

11:00 – 13:00 Practical: CC study: Risk factors for Coronary heart disease

13:00 - 14:00 Lunch

14:00 – 14:30 Recap of morning practical

14:30 - 15:30 Causal inference. (KF)

15:30 - 16:00 Coffee break.

16:00 – 18:00 Practical: Simulation and causal inference

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20:00 – Dinner – restaurant Le Passage

### Wednesday 20 June

9:00 – 9:30 Recap of yesterday's practicals

9:30 – 10:30 Multistate models, Poisson models for rates and simulation of Lexis objects (BxC)

10:30 - 11:00 Coffee break.

11:00 – 12:15 Practical: Multistate-model: Renal complications

12:15 – 12:45 Recap of morning practical

12:54 - 13:00 Wrap-up and farewell.

13:00 - 14:00 Lunch

Further material will appear at this year's course website:

## Chapter 1

### Exercises

### Data sets

Datasets for the practicals in this course, as well as some useful R scripts, will be available on the course homepage, in <a href="http://BendixCarstensen.com/SPE/data">http://BendixCarstensen.com/SPE/data</a>. This is where you will also find the "housekeeping" scripts designed to save you typing.

To get all files in one go, download the zip file http://spe-r.github.io/data.zip.

### Graphical User Interfaces to R

When running the exercises it is a good idea to use a text editor instead of typing your commands directly at the R prompt. On Windows and macOS, R comes with a basic graphical user interface including a built-in text editor. Many people like to use the RStudio interface to R, which includes a very powerful syntax-highlighting editor.

### Keyboard shortcuts

In the past we have found that some participants have had difficulty finding keys for symbols that are commonly used in the R language. In particular, the tilde symbol ~ is used in all modelling functions but not directly available on some keyboards. If this affects you then please consult the Wikipedia page: <a href="http://en.wikipedia.org/wiki/Tilde#Keyboards">http://en.wikipedia.org/wiki/Tilde#Keyboards</a> for advice on the combination of key presses you will need to get tilde.

### Recaps

The R-scripts used during the course for the recaps will be available in <a href="http://BendixCarstensen.com/SPE/recap">http://BendixCarstensen.com/SPE/recap</a>.

### Ask for help

The faculty are here to help you. Ask them for help.

### 1.1 Practice with basic R

The main purpose of this session is to give participants who have not had much (or any) experience with using R a chance to practice the basics and to ask questions. For others, it should serve as a reminder of some of the basic features of the language.

R can be installed on all major platforms (*i.e.* Windows, macOS, Linux). We do not assume in this exercise that you are using any particular platform. Many people like to use the RStudio graphical user interface (GUI), which gives the same look and feel across all platforms.

### 1.1.1 The working directory

A key concept in R is the *working directory* (or *folder* in the terminology of Windows). The working directory is where R looks for data files that you may want to read in and where R will write out any files you create. It is a good idea to keep separate working directories for different projects. In this course we recommend that you keep a separate working directory for each exercise.

If you are working on the command line in a terminal, then you can change to the correct working directory and then launch R by typing "R".

If you are using a GUI then you will typically need to change to the correct working directory after starting R. In RStudio, you can change directory from the "Session" menu. However it is much more useful to create a new *project* to keep your source files and data. When you open a project in the RStudio GUI, your working directory is automatically changed to the directory associated with the project.

You can quit R by typing

q()

at the R command prompt. You will be asked if you want to save your workspace. We recommend that you answer "no" to this question. If you answer "yes" then R will write a file named .RData into the working directory containing all the objects you created during your session so that they will be available next time you start R. This may seem convenient but you will soon find that your workspace becomes cluttered with old objects.

You can display the current working directory with the getwd() function and set it with the setwd() function. The function dir() can be used to see what files you have in the working directory.

### 1.1.2 Read-evaluate-print

The simplest use of R is interactively. R will read in the command you type, evaluate them, then print out the answer. This is called the *read-eval-print loop*, or REPL for people who don't like words. In this exercise, we recommend that you work interactively. As the course evolves you will find that you need to switch to *script files*. We come back to this issue at the end of the exercise.

It is important to remember that R is case sensitive, so that A is different from a. Commands in R are generally separated by a newline, although a semi-colon can also be used.

#### Using R as a calculator 1.1.3

Try using R as a calculator by typing different arithmetic expressions on the command line. Note that R allows you to recall previous commands using the vertical arrow key. You can edit a recalled command and then resubmit it by pressing the return key. Keeping that in mind, try the following:

```
12+16
(12+16)*5
sqrt((12+16)*5) # square root
round(sqrt((12+16)*5),2) # round to two decimal places
```

The hash symbol # denotes the start of a *comment*. Anything after the hash is ignored by R. Round braces are used a lot in R. In the above expressions, they are used in two different ways. Firstly, they can be used to establish the order of operations. In the example

```
> (12+16)*5
[1] 140
```

they ensure that 12 is added to 16 before the result is multiplied by 5. If you omit the braces then you get a different answer

```
> 12+16*5
[1] 92
```

because multiplication has higher precedence than addition. The second use of round braces is in a function call (e.g. sqrt, round). To call a function in R, type the name followed by the arguments inside round braces. Some functions take multiple arguments, and in this case they are separated by commas.

You can see that complicated expressions in R can have several levels of nested braces. To keep track of these, it helps to use a syntax-highlighting editor. For example, in RStudio, when you type an opening bracket "(", RStudio will automatically add a closing bracket ")", and when the cursor moves past a closing bracket, RStudio will automatically highlight the corresponding opening bracket (in grey). Features like this can make it much easier to write R code free from syntax errors.

Instead of printing the result you can store it in an object, say

```
a \leftarrow round(sqrt((12+16)*5),2)
```

In this case R does not print anything to the screen. You can see the results of the calculation, stored in the object a, by typing a and also use a for further calculations, e.g.:

```
exp(a)
log(a)
           # natural logarithm
log10(a)
           # log to the base 10
```

The left arrow expression <-, pronounced "gets", is called the assignment operator, and is obtained by typing < followed by - (with no space in between). It is also possible to use the equals sign = for assignment. Note that some R experts do not like this and recommend to use only "gets" for assignment, reserving = for function arguments,

You can also use a right arrow, as in

```
round(sqrt((12+16)*5),2) \rightarrow a
```

### 1.1.4 Vectors

All commands in R are functions which act on objects. One important kind of object is a vector, which is an ordered collection of numbers, or character strings (e.g. "Charles Darwin"), or logical values (TRUE or FALSE). The components of a vector must be of the same type (numeric, character, or logical). The combine function c(), together with the assignment operator, is used to create vectors. Thus

```
> v \leftarrow c(4, 6, 1, 2.2)
```

creates a vector v with components 4, 6, 1, 2.2 and assigns the result to the vector v.

A key feature of the R language is that many operations are *vectorized*, meaning that you can carry out the same operation on each element of a vector in a single operation. Try

```
> v
> 3+v
> 3*v
```

and you will see that R understands what to do in each case.

R extends ordinary arithmetic with the concept of a *missing value* represented by the symbol NA (Not Available). Any operation on a missing value creates another missing value. You can see this by repeating the same operations on a vector containing a missing value:

```
> v <- c(4, 6, NA)
> 3 + v
> 3 * v
```

The fact that every operation on a missing value produces a missing value can be a nuisance when you want to create a summary statistic for a vector:

```
> mean(v)
[1] NA
```

While it is true that the mean of v is unknown because the value of the third element is missing, we normally want the mean of the non-missing elements. Fortunately the mean function has an optional argument called  $\mathtt{na.rm}$  which can be used for this.

```
> mean(v, na.rm=TRUE)
[1] 5
```

Many functions in R have optional arguments that can be omitted, in which case they take their default value (in this case na.rm=FALSE), or can be explicitly given in the function call to override the default behaviour.

You can get a description of the structure of any object using the function str(). For example, str(v) shows that v is numeric with 4 components. If you just want to know the length of a vector then it is much easier to use the length function.

```
> length(v)
```

### 1.1.5 Sequences

There are short-cut functions for creating vectors with a regular structure. For example, if you want a vector containing the sequence of integers from 1 to 10, you can use

```
> 1:10
```

The seq() function allows the creation of more general sequences. For example, the vector (15, 20, 25, ..., 85) can be created with

```
> seq(from=15, to=85, by=5)
```

The objects created by the ":" operator and the seq() function are ordinary vectors, and can be combined with other vectors using the combine function:

```
> c(5, seq(from=20, to=85, by=5))
```

You can learn more about functions by typing? followed by the function name. For example ?seq gives information about the syntax and usage of the function seq().

- 1. Create a vector w with components 1, -1, 2, -2
- 2. Display this vector
- 3. Obtain a description of w using str()
- 4. Create the vector w+1, and display it.
- 5. Create the vector v with components (5, 10, 15, ..., 75) using seq().
- 6. Now add the components 0 and 1 to the beginning of v using c().
- 7. Find the length of this vector.

### 1.1.6 Displaying and changing parts of a vector (indexing)

Square brackets in R are used to extract parts of vectors. So x[1] gives the first element of vector x. Since R is vectorized you can also supply a vector of integer index values inside the square brackets. Any expression that creates an integer vector will work.

Try the following commands:

```
> x <- c(2, 7, 0, 9, 10, 23, 11, 4, 7, 8, 6, 0)
> x[4]
> x[3:5]
> x[c(1,5,8)]
> x[(1:6)*2]
> x[-1]
```

Negative subscripts mean "drop this element". So x[-1] returns every element of x except the first

Trying to extract an element that is beyond the end of the vector is, surprisingly, not an error. Instead, this returns a missing value

```
> N <- length(x)
> x[N + 1]
[1] NA
```

There is a reason for this behaviour, which we will discuss in the recap. R also allows *logical subscripting*. Try the following

```
> x > 10
> x[x > 10]
```

The first expression creates a logical vector of the same length as  $\mathbf{x}$ , where each element has the value TRUE or FALSE depending on whether or not the corresponding element of  $\mathbf{x}$  is greater than 10. If you supply a logical vector as an index, R selects only those elements for which the conditions is TRUE.

You can combine two logical vectors with the operators & ("logical and") and | ("logical or"). For example, to select elements of x that are between 10 and 20 we combine two one-sided logical conditions for  $x \ge 10$  and  $x \le 20$ :

```
> x[x >= 10 \& x <= 20]
```

The remaining elements of x that are either less than 10 or greater than 20 are selected with

```
> x[x < 10 | x > 20]
```

Indexing can also be used to replace parts of a vector:

```
> x[1] <- 1000
> x
```

This replaces the first element of x. Logical subscripting is useful for replacing parts of a vector that satisfy a certain condition. For example to replace all elements that take the value 0 with the value 1:

```
> x[x==0] <- 1
> x
```

If you want to replace parts of a vector then you need to make sure that the replacement value is either a single value, as in the example above, or a vector equal in length to the number of elements to be replaced. For example, to replace elements 2, 3, and 4 we need to supply a vector of replacement values of length 3.

```
> x[2:4] <- c(0, 8, 1)
> x
```

It is important to remember this when you are using logical subscripting because the number of elements to be replaced is not given explicitly in the R code, and it is easy to get confused about how many values need to be replaced. If we want to add 3 to every element that is less than 3 then we can break the operation down into 3 steps:

```
> y <- x[x < 3]
> y <- y + 3
> x[x < 3] <- y
> x
```

First we extract the values to be modified, then we modify them, then we write back the modified values to the original positions. R experts will normally do this in a single expression.

```
> x[x < 3] < - x[x < 3] + 3
```

Remember, if you are confused by a complicated expression you can usually break it down into simpler steps.

If you want to create an entirely new vector based on some logical condition then use the ifelse() function. This function takes three arguments: the first is a logical vector; the second is the value taken by elements of the logical vector that are TRUE; and the third is the value taken by elements that are FALSE.

In this example, we use the remainder operator % to identify elements of x that have value 0 when divided by 2 (i.e. the even numbers) and then create a new character vector with the labels "even" and "odd":

```
> x %% 2
> ifelse(x %% 2 == 0,"even","odd")
```

Now try the following:

- 8. Display elements that are less than 10, but greater than 4
- 9. Modify the vector x, replacing by 10 all values that are greater than 10
- 10. Modify the vector x, multiplying by 2 all elements that are smaller than 5 (Remember you can do this in steps).

### 1.1.7 Lists

Collections of components of different types are called *lists*, and are created with the list() function. Thus

```
> m <- list(4, TRUE, "name of company")
> m
```

creates a list with 3 components: the first is numeric, the second is logical and the third is character. A list element can be any object, including another list. This flexibility means that functions that need to return a lot of complex information, such as statistical modelling functions, often return a list.

As with vectors, single square brackets are used to take a subset of a list, but the result will always be another list, even if you select only one element

```
> m[1:2] #A list containing first two elements of m > m[3] #A list containing the third element of m
```

If you just want to extract a single element of a list then you must use double square braces:

```
> m[[3]] #Extract third element
```

Lists are more useful when their elements are named. You can name an element by using the syntax name=value in the call to the list function:

This creates a new list with the elements "name", a character vector of names, and "age" a numeric vector of ages. The components of the list can be extracted with a dollar sign \$

```
> mylist$name
> mylist$age
```

### 1.1.8 Data frames

Data frames are a special structure used when we want to store several vectors of the same length, and corresponding elements of each vector refer to the same record. For example, here we create a simple data frame containing the names of some individuals along with their age in years, their sex (coded 1 or 2) and their height in cm.

The construction of a data frame is just like a named list (except that we use the constructor function data.frame instead of list). In fact data frames are lists so, for example, you can extract vectors using the dollar sign or other extraction methods for lists:

```
> mydata$height
> mydata[[4]]
```

On the other hand, data frames are also two dimensional objects:

```
> mydata
  name age sex height
1 Joe 34 1 185
2 Ann 50 2 170
3 Jack 27 1 175
4 Tom 42 1 182
```

When you print a data frame, each variable appears in a separate column. You can use square brackets with two comma-separated arguments to take subsets of rows or columns.

```
> mydata[1,]
> mydata[,c("age", "height")]
> mydata[2,4]
```

We will look into indexing of data frames in more detail below.

Now let's create another data frame with more individuals than the first one:

This new data frame contains the weights of the individuals. The two data sets can be joined together with the merge function.

```
> newdata <- merge(mydata, yourdata)
> newdata
```

The merge function uses the variables common to both data frames – in this case the variable "name" – to uniquely identify each row. By default, only rows that are in both data frames are preserved, the rest are discarded. In the above example, the records for Peter, Sue, and Jane, which are not in mydata are discarded. If you want to keep them, use the optional argument all=TRUE.

```
> newdata <- merge(mydata, yourdata, all=TRUE)
> newdata
```

This keeps a row for all individuals but since Peter, Sue and Jane have no recorded age, height, or sex these are missing values.

### 1.1.9 Working with built-in data frames

We shall use the births data which concern 500 mothers who had singleton births (i.e. no twins) in a large London hospital. The outcome of interest is the birth weight of the baby, also dichotomised as normal or low birth weight. These data are available in the Epi package:

```
> library(Epi)
> data(births)
> objects()
```

The function objects() shows what is in your workspace. To find out a bit more about births try

```
help(births)
```

11. The dataframe "diet" in the Epi package contains data from a follow-up study with coronary heart disease as the end-point. Load these data with

```
> data(diet)
```

and print the contents of the data frame to the screen..

- 12. Check that you now have two objects, births, and diet in your workspace.
- 13. Get help on the object diet.
- 14. Remove the object diet with the command

```
> remove(diet)
```

Check that the object diet is no longer in your workspace.

### 1.1.10 Referencing parts of the data frame (indexing)

Typing births will list the entire data frame – not usually very helpful. You can use the head function to see just the first few rows of a data frame

```
> head(births)
Now try
```

```
> births[1,"bweight"]
```

This will list the value taken by the first subject for the bweight variable. Alternatively

```
> births[1.2]
```

will list the value taken by the first subject for the second variable (which is bweight). Similarly

```
> births[2, "bweight"]
```

will list the value taken by the second subject for bweight, and so on. To list the data for the first 10 subject for the bweight variable, try

```
> births[1:10, "bweight"]
```

and to list all the data for this variable, try

```
> births[, "bweight"]
```

To list the data for the first subject try

```
> births[1, ]
```

An empty index before the comma means "all rows" and an empty index after the comma means "all columns".

- 15. Display the data on the variable gestwks for row 7 in the births data frame.
- 16. Display all the data in row 7.
- 17. Display the first 10 rows for the variable gestwks.

The subset function is another way of getting subsets from a data frame. To select all subjects with height less than 180 cm from the data frame mydata we use

```
> subset(mydata, height < 180)
```

The subset function is usually clearer than the equivalent code using []:

```
> mydata[mydata$height < 180, ]</pre>
```

Another advantage of subset is that it will drop observations with missing values. Compare the following

```
> newdata[newdata$height < 180, ]
> subset(newdata, height < 180)</pre>
```

If height is missing then subset will drop that row. But [] will do something you might not expect. It will include the rows with missing height, but will replace every element in those rows with the missing value NA.

### 1.1.11 Summaries

A good way to start an analysis is to ask for a summary of the data by typing

```
> summary(births)
```

This prints some summary statistics (minimum, lower quartile, mean, median, upper quartile, maximum). For variables with missing values, the number of NAs is also printed.

To see the names of the variables in the data frame try

```
> names(births)
```

Variables in a data frame can be referred to by name, but to do so it is necessary also to specify the name of the data frame. Thus births\$hyp refers to the variable hyp in the births data frame, and typing births\$hyp will print the data on this variable. To summarize the variable hyp try

```
> summary(births$hyp)
```

Alternatively you can use

```
> with(births, summary(hyp))
```

### 1.1.12 Generating new variables

New variables can be produced using assignment together with the usual mathematical operations and functions. For example

```
> logbw <- log(births$bweight)</pre>
```

produces the variable logbw in your workspace, while

```
> births$logbw <- log(births$bweight)</pre>
```

produces the variable logbw in the births data frame.

You can also replace existing variables. For example bweight measures birth weight in grams. To convert the units to kilograms we replace the original variable with a new one:

```
> births$bweight <- births$bweight/1000</pre>
```

### 1.1.13 Turning a variable into a factor

In R categorical variables are known as *factors*, and the different categories are called the *levels* of the factor. Variables such as hyp and sex are originally coded using integer codes, and by default R will interpret these codes as numeric values taken by the variables. Factors will become very important later in the course when we study modelling functions, where factors and numeric variables are treated very differently. For the moment, you can think of factors as "value labels" that are more informative than numeric codes.

For R to recognize that the codes refer to categories it is necessary to convert the variables to be factors, and to label the levels. To convert the variable hyp to be a factor, try

```
> births$hyp <- factor(births$hyp, labels=c("normal", "hyper"))</pre>
```

This takes the original numeric codes (0, 1) and replaces them with informative labels "normal" and "hyper" for normal blood pressure and hypertension, respectively.

18. Convert the variable sex into a factor with labels "M" and "F" for values 1 and 2, respectively

### 1.1.14 Frequency tables

When starting to look at any new data frame the first step is to check that the values of the variables make sense and correspond to the codes defined in the coding schedule. For categorical variables (factors) this can be done by looking at one-way frequency tables and checking that only the specified codes (levels) occur. The most useful function for making simple frequency tables is table. The distribution of the factor hyp can be viewed using

```
> with(births, table(hyp))
```

or by specifying the data frame as in

```
> table(births$hyp)
```

For simple expressions the choice is a matter of taste, but with is shorter for more complicated expressions.

- 19. Find the frequency distribution of sex.
- 20. If you give two or more arguments to the table function then it produces cross-tabulations. Find the two-way frequency distribution of sex and hyp.
- 21. Create a logical variable called early according to whether gestwks is less than 30 or not. Make a frequency table of early.

### 1.1.15 Grouping the values of a numeric variable

For a numeric variable like matage it is often useful to group the values and to create a new factor which codes the groups. For example we might cut the values taken by matage into the groups 20–29, 30–34, 35–39, 40–44, and then create a factor called agegrp with 4 levels corresponding to the four groups. The best way of doing this is with the function cut. Try

```
> births$agegrp <- cut(births$matage, breaks=c(20,30,35,40,45), right=FALSE)
> with(births, table(agegrp))
```

By default the factor levels are labelled [20-25), [25-30), etc., where [20-25) refers to the interval which includes the left hand end (20) but not the right hand end (25). This is the reason for right=FALSE. When right=TRUE (which is the default) the intervals include the right hand end but not the left hand.

Observations which are not inside the range specified by the **breaks** argument result in missing values for the new factor. Hence it is important that the first element in **breaks** is smaller than the smallest value in your data, and the last element is larger than the largest value.

- 22. Summarize the numeric variable gestwks, which records the length of gestation for the baby, and make a note of the range of values.
- 23. Create a new factor gest4 which cuts gestwks at 20, 35, 37, 39, and 45 weeks, including the left hand end, but not the right hand. Make a table of the frequencies for the four levels of gest4.

### 1.1.16 Saving and loading data

As noted in section 1.1.1, at the end of the session, R will offer to save your workspace and, if you accept, it will create a file .RData in your working directory. In fact you can save any R object to disc. For example, to save the data frame births try

```
> save(births, file="births.RData")
```

which will save the births data frame in the file births.RData. If you send this file to a colleague then they can read the data back into R with

```
> load("births.RData")
```

The commands save() and load() can be used with any R objects, but they are particularly useful when dealing with large data frames. The binary format created by the save() functions is the same across all platforms and between R versions.

### 1.1.17 The search path

When you load a package with the library() function, the functions in that package become available for you to use via a mechanism called the *search path*. The command

```
> search()
```

shows the positions on the search path. The first position is ".GlobalEnv". This is the global environment, which is another name for your workspace. The second entry on the search path is the Epi package, the third is a package of commands called methods, the fourth is a package called stats, and so on. To see what is in the workspace try

```
> objects()
```

You should see the objects that you have created in this session. To see what is in the Epi package, try

```
> objects(2)
```

You can also refer to a package by name, not position

```
> objects("package:Epi")
```

When you type the name of an object R looks for it in the order of the search path and will return the first object with this name that it finds.

### 1.1.18 Attaching a data frame

The search path can also be modified by attaching a data frame. For example:

```
> attach(births)
```

This places a copy of the variables in the births data frame in position 2 of the search path. You can verify this with

```
> search()
> objects(2)
```

which shows the objects in this position are the variables from the births data frame.

Attaching a data frame makes the variables in it directly accessible. For example, when you type the command:

```
> hyp
```

you should get the variable hyp from the births data set without having to use the dollar sign. The detach() function removes the data frame from the search path.

```
> detach()
```

when no arguments are given, the detach() function removes the second entry on the search path (after the global environment).

This seems like an attractive feature, especially for people who are used to other statistical software (e.g. SAS, Stata) in which the variables in the "current working dataset" are directly accessible in this way. However, attaching data frames causes more problems than it solves and should be avoided. In particular:

- Since the attached data frame appears second in the search path, it comes after the global environment. If you have an object hyp in the global environment then you will get this, instead of the variable from the births data frame. This is called *masking*. R will warn you about masking, but only once for each variable.
- Attaching a data frame creates a copy of all the variables in it. Subsequent changes to the data frame (e.g. selecting rows or recoding variables) are not reflected in the attached copy, which is a snapshot of the data frame when it was attached.
- If you forget to detach() the data frame when you are finished with it, then you may create multiple attached copies on your search path, especially when using a script.

It is best to stick to using the dollar sign to select variables in a data frame, or to use the with() function. Many R functions (but not all of them) have a data argument which can be used to specify a data frame that should be searched before the search path.

### 1.1.19 Interactive use vs scripting

You can work with R simply by typing function calls at the command prompt and reading the results as they are printed. This is OK for simple use but rapidly becomes cumbersome. If the results of one calculation are used to feed into the next calculation, it can be difficult to go back if you find you have made a mistake, or if you want to repeat the same commands with different data.

When working with R it is best to use a text editor to prepare a batch file (or script) which contains R commands and then to run them from the script. If you are using a GUI then you can use the built-in script editor, or you can use your favourite text editor instead if you prefer.

One major advantage of running all your R commands from a script is that you end up with a record of exactly what you did which can be repeated at any time. This will also help you redo the analysis in the (highly likely) event that your data changes before you have finished all analyses.

#### Reading data into R 1.2

#### 1.2.1 Introduction

"If you want to have rabbit stew, first catch the rabbit" – Old saying, origin unknown

R is a language and environment for data analysis. If you want to do something interesting with it, you need data.

For teaching purposes, data sets are often embedded in R packages. The base R distribution contains a whole package dedicated to data which includes around 100 data sets. This is attached towards the end of the search path, and you can see its contents with

```
> objects("package:datasets")
```

A description of all of these objects is available using the help() function. For example

### > help(Titanic)

gives an explanation of the Titanic data set, along with references giving the source of the data.

The Epi package also contains some data sets. These are not available automatically when you load the Epi package, but you can make a copy in your workspace using the data() function. For example

```
> library(Epi)
> data(bdendo)
```

will create a data frame called bdendo in your workspace containing data from a case-control study of endometrial cancer. Datasets in the Epi package also have help pages: type help(bdendo) for further information.

To go back to the cooking analogy, these data sets are the equivalent of microwave ready meals, carefully packaged and requiring minimal work by the consumer. Your own data will never be able in this form and you must work harder to read it

This exercise introduces you to the basics of reading external data into R. It consists of reading the same data from different formats. Although this may appear repetitive, it allows you to see the many options available to you, and should allow you to recognize when things go wrong.

getting the data: You will need to download the zip file data.zip from the course web site https://spe-r.github.io/data.zip and unpack this in your working directory. This will create a sub-directory data containing (among other things) the files fem.dat, fem-dot.dat, fem.csv, and fem.dta (Reminder: use setwd() to set your working directory).

### 1.2.2 Data sources

Sources of data can be classified into three groups:

- 1. Data in human readable form, which can be inspected with a text editor.
- 2. Data in binary format, which can only be read by a program that understands that format (SAS, SPSS, Stata, Excel, ...).
- 3. Online data from a database management system (DBMS)

This exercise will deal with the first two forms of data. Epidemiological data sets are rarely large enough to justify being kept in a DBMS. If you want further details on this topic, you can consult the "R Data Import/Export" manual that comes with R.

### 1.2.3 Data in text files

Human-readable data files are generally kept in a rectangular format, with individual records in single rows and variables in columns. Such data can be read into a data frame in R.

Before reading in the data, you should inspect the file in a text editor and ask three questions:

- 1. How are columns in the table separated?
- 2. How are missing values represented?
- 3. Are variable names included in the file?

The file fem.dat contains data on 118 female psychiatric patients. The data set contains nine variables.

ID	Patient identifier
AGE	Age in years
IQ	Intelligence Quotient (IQ) score
ANXIETY	Anxiety (1=none, 2=mild, 3=moderate,4=severe)
DEPRESS	Depression (1=none, 2=mild, 3=moderate or severe)
SLEEP	Sleeping normally (1=yes, 2=no)
SEX	Lost interest in sex (1=yes, 2=no)
LIFE	Considered suicide (1=yes, 2=no)
WEIGHT	Weight change (kg) in previous 6 months

Inspect the file fem.dat with a text editor to answer the questions above.

The most general function for reading in free-format data is read.table(). This function reads a text file and returns a data frame. It tries to guess the correct format of each variable in the data frame (integer, double precision, or text).

Read in the table with:

```
> fem <- read.table("./data/fem.dat", header=TRUE)</pre>
```

Note that you must assign the result of read.table() to an object. If this is not done, the data frame will be printed to the screen and then lost.

You can see the names of the variables with

```
> names(fem)
```

The structure of the data frame can be seen with

```
> str(fem)
```

You can also inspect the top few rows with

```
> head(fem)
```

Note that the IQ of subject 9 is -99, which is an illegal value: nobody can have a negative IQ. In fact -99 has been used in this file to represent a missing value. In R the special value NA ("Not Available") is used to represent missing values. All R functions recognize NA values and will handle them appropriately, although sometimes the appropriate response is to stop the calculation with an error message.

You can recode the missing values with

```
> fem IQ[fem IQ == -99] <- NA
```

Of course it is much better to handle special missing value codes when reading in the data. This can be done with the na.strings argument of the read.table() function. See below.

#### Things that can go wrong 1.2.4

Sooner or later when reading data into R, you will make a mistake. The frustrating part of reading data into R is that most mistakes are not fatal: they simply cause the function to return a data frame that is not what you wanted. There are three common mistakes, which you should learn to recognize.

#### 1.2.4.1Forgetting the headers

The first row of the file fem.dat contains the variable names. The read.table() function does not assume this by default so you have to specify this with the argument header=TRUE. See what happens when you forget to include this option:

```
> fem2 <- read.table("data/fem.dat")</pre>
> str(fem2)
> head(fem2)
```

and compare the resulting data frame with fem. What are the names of the variables in the data frame? What is the class of the variables?

Explanation: Remember that read.table() tries to guess the mode of the variables in the text file. Without the header=TRUE option it reads the first row, containing the variable names, as data, and guesses that all the variables are character, not numeric. By default, all character variables are coerced to factors by read.table. The result is a data frame consisting entirely of factors. (You can prevent the conversion of character variables to factors with the argument as.is=TRUE).

If the variable names are not specified in the file, then they are given default names V1, V2, .... You will soon realise this mistake if you try to access a variable in the data frame by, for example

```
> fem2$IQ
```

as the variable will not exist

There is one case where omitting the header=TRUE option is harmless (apart from the situation where there is no header line, obviously). When the first row of the file contains one less value than subsequent lines, read.table() infers that the first row contains the variable names, and the first column of every subsequent row contains its row name.

### 1.2.4.2 Using the wrong separator

By default, read.table assumes that data values are separated by any amount of white space. Other possibilities can be specified using the sep argument. See what happens when you assume the wrong separator, in this case a tab, which is specified using the escape sequence "\t"

```
> fem3 <- read.table("data/fem.dat", sep="\t")
> str(fem3)
```

How many variables are there in the data set?

**Explanation:** If you mis-specify the separator, read.table() reads the whole line as a single character variable. Once again, character variables are coerced to factors, so you get a data frame with a single factor variable.

### 1.2.4.3 Mis-specifying the representation of missing values

The file fem-dot.dat contains a version of the FEM dataset in which all missing values are represented with a dot. This is a common way of representing missing values, but is not recognized by default by the read.table() function, which assumes that missing values are represented by "NA".

Inspect the file with a text editor, and then see what happens when you read the file in incorrectly:

```
> fem4 <- read.table("data/fem-dot.dat", header=TRUE)</pre>
> str(fem4)
```

You should have enough clues by now to work out what went wrong.

You can read the data correctly using the na.strings argument

```
> fem4 <- read.table("data/fem-dot.dat", header=TRUE, na.strings=".")
```

#### 1.2.5 Spreadsheet data

Spreadsheets have become a common way of exchanging data. All spreadsheet programs can save a single sheet in comma-separated variable (CSV) format, which can then be read into R. There are two functions in R for reading in CSV data: read.csv() and read.csv2().

Both of these are wrappers around the read.table() function, i.e. the read.table() function is still doing the work of reading in the data but the read.csv() function provides default argument values for reading in CSV file so all you need to do is specify the file name.

You can see what these default arguments are with the args() function.

```
> args(read.csv)
> args(read.csv2)
```

See if you can spot the difference between read.csv and read.csv2.

**Explanation:** The CSV format is not a single standard. The file format depends on the *locale* of your computer – the settings that determine how numbers are represented. In some countries, the decimal separator is a point "." and the variable separator in a CSV file is a comma ",". In other countries, the decimal separator is a comma "," and the variable separator is a semi-colon ";". This is reflected in the different default values for the arguments sep and dec. The read.csv() function is used for the first format and the read.csv2() function is used for the second format.

The file fem.csv contains the FEM dataset in CSV format. Inspect the file to work out which format is used, and read it into R.

#### 1.2.6 Reading data from the Internet

You can also read in data from a remote web site. The file argument of read.table() does not need to be a local file on your computer; it can be a Uniform Resource Locator (URL), i.e. a web address.

A copy of the file fem.dat is held at https://www.bendixcarstensen.com/SPE/data/fem.dat. You can read it in with

```
> fem6 <- read.table("http://www.bendixcarstensen.com/SPE/data/fem.dat",
+ header=TRUE)
> str(fem6)
```

### 1.2.7 Reading from the clipboard

On Microsoft Windows, you can copy values directly from an open Excel spreadsheet using the clipboard. Highlight the cells you want to copy in the spread sheet and select copy from the pull-down edit menu. Then type read.table(file="clipboard") to read the data in.

There are two reasons why this is a bad idea

- It is not reproducible. In order to read the data in again you need to complete exactly the same sequence of mouse moves and clicks, and there is no record of what you did before.
- Copying from the clipboard loses precision. If you have a value 1.23456789 in your spreadsheet, but have formatted the cell so it is displayed to two decimal places, then the value read into R will be the truncated value 1.23.

### 1.2.8 Binary data

The foreign package allows you to read data in binary formats used by other statistical packages. Since R is an open source project, it can only read binary formats that are themselves "open", in the sense that the standards for reading and writing data are well-documented. For example, there is a function in the foreign package for reading SAS XPORT files, a format that has been adopted as a standard by the US Food and Drug Administration

(http://www.sas.com/govedu/fda/faq.html). However, there is no function in the foreign package for reading native SAS binaries (SAS7BDAT files). Other packages are available from CRAN (http://cran.r-project.org) that offer the possibility of reading SAS binary files: see the haven and sas7bdat packages.

The file fem.dta contains the FEM dataset in the format used by Stata. Read it into R with

```
> library(foreign)
> fem5 <- read.dta("data/fem.dta")
> head(fem5)
```

The Stata data set contains value and variable labels. Stata variables with value labels are automatically converted to factors.

There is no equivalent of variable labels in an R data frame, but the original variable labels are not lost. They are still attached to the data frame as an invisible *attribute*, which you can see with

```
> attr(fem5, "var.labels")
```

A lot of meta-data is attached to the data in the form of attributes. You can see the whole list of attributes with

```
> attributes(fem5)
```

or just the attribute names with

```
> names(attributes(fem5))
```

The read.dta() function can only read data from Stata versions 5-12. The R Core Team has not been able to keep up with changes in the Stata format. You may wish to try the haven package and the readstata13 package, both available from CRAN.

#### Summary 1.2.9

In this exercise we have seen how to create a data frame in R from an external text file. We have also reviewed some common mistakes that result in garbled data.

The capabilities of the foreign package for reading binary data have also been demonstrated with a sample Stata data set.

22 1.3 Tabulation SPE: Exercises

### 1.3 Tabulation

### 1.3.1 Introduction

R and its add-on packages provide several different tabulation functions with different capabilities. The appropriate function to use depends on your goal. There are at least three different uses for tables.

The first use is to create simple summary statistics that will be used for further calculations in R. For example, a two-by-two table created by the table function can be passed to fisher.test, which will calculate odds ratios and confidence intervals. The appearance of these tables may, however, be quite basic, as their principal goal is to create new objects for future calculations.

A quite different use of tabulation is to make "production quality" tables for publication. You may want to generate reports from for publication in paper form, or on the World Wide Web. The package **xtable** provides this capability, but it is not covered by this course.

An intermediate use of tabulation functions is to create human-readable tables for discussion within your work-group, but not for publication. The Epi package provides a function stat.table for this purpose, and this practical is designed to introduce this function.

### 1.3.2 The births data

We shall use the births data which concern 500 mothers who had singleton births in a large London hospital. The outcome of interest is the birth weight of the baby, also dichotomised as normal or low birth weight. These data are available in the Epi package:

```
> library(Epi)
> data(births)
> names(births)
> head(births)
```

In order to work with this data set we need to transform some of the variables into factors. This is done with the following commands:

```
> births$hyp <- factor(births$hyp,labels=c("normal","hyper"))
> births$sex <- factor(births$sex,labels=c("M","F"))
> births$agegrp <- cut(births$matage,breaks=c(20,25,30,35,40,45),right=FALSE)
> births$gest4 <- cut(births$gestwks,breaks=c(20,35,37,39,45),right=FALSE)</pre>
```

Now use str(births) to examine the modified data frame. We have transformed the binary variables hyp and sex into factors with informative labels. This will help when displaying the tables. We have also created grouped variables agegrp and gest4 from the continuous variables matage and gestwks so that they can be tabulated.

IARC, 2018 1.3 Tabulation 23

### 1.3.3 One-way tables

The simplest table one-way table is created by

```
> stat.table(index = sex, data = births)
```

This creates a count of individuals, classified by levels of the factor sex. Compare this table with the equivalent one produced by the table function. Note that stat.table has a data argument that allows you to use variables in a data frame without specifying the frame.

You can display several summary statistics in the same table by giving a list of expressions to the contents argument:

```
> stat.table(index = sex, contents = list(count(), percent(sex)), data=births)
```

Only a limited set of expressions are allowed: see the help page for stat.table for details.

You can also calculate marginal tables by specifying margin=TRUE in your call to stat.table. Do this for the above table. Check that the percentages add up to 100 and the total for count() is the same as the number of rows of the data frame births. To see how the mean birth weight changes with sex, try

```
> stat.table(index = sex, contents = mean(bweight), data=births)
```

Add the count to this table. Add also the margin with margin=TRUE. As an alternative to bweight we can look at lowbw with

```
> stat.table(index = sex, contents = percent(lowbw), data=births)
```

All the percentages are 100! To use the percent function the variable lowbw must also be in the index, as in

```
> stat.table(index = list(sex,lowbw), contents = percent(lowbw), data=births)
```

The final column is the percentage of babies with low birth weight by different categories of gestation.

- 1. Obtain a table showing the frequency distribution of gest4.
- 2. Show how the mean birth weight changes with gest4.
- 3. Show how the percentage of low birth weight babies changes with gest4.

Another way of obtaining the percentage of low birth weight babies by gestation is to use the ratio function:

```
> stat.table(gest4,ratio(lowbw,1,100),data=births)
```

This only works because lowbw is coded 0/1, with 1 for low birth weight.

Tables of odds can be produced in the same way by using ratio(lowbw, 1-lowbw). The ratio function is also very useful for making tables of rates with (say) ratio(D,Y,1000) where D is the number of failures, and Y is the follow-up time. We shall return to rates in a later practical.

24 1.3 Tabulation SPE: Exercises

### 1.3.4 Improving the Presentation of Tables

The stat.table function provides default column headings based on the contents argument, but these are not always very informative. Supply your own column headings using *tagged* lists as the value of the contents argument, within a stat.table call:

```
> stat.table(gest4,contents = list( N=count(),
+ "(%)" = percent(gest4)),data=births)
```

This improves the readability of the table. It remains to give an informative title to the index variable. You can do this in the same way: instead of giving gest4 as the index argument to stat.table, use a named list:

```
> stat.table(index = list("Gestation time" = gest4),data=births)
```

### 1.3.5 Two-way Tables

The following call gives a  $2 \times 2$  table showing the mean birth weight cross-classified by sex and hyp.

```
> stat.table(list(sex,hyp), contents=mean(bweight), data=births)
```

Add the count to this table and repeat the function call using margin = TRUE to calculate the marginal tables. Use stat.table with the ratio function to obtain a 2 × 2 table of percent low birth weight by sex and hyp. You can have fine-grained control over which margins to calculate by giving a logical vector to the margin argument. Use margin=c(FALSE, TRUE) to calculate margins over sex but not hyp. This might not be what you expect, but the margin argument indicates which of the index variables are to be marginalized out, not which index variables are to remain.

### 1.3.6 Printing

Just like every other R function, stat.table produces an object that can be saved and printed later, or used for further calculation. You can control the appearance of a table with an explicit call to print()

There are two arguments to the print method for stat.table. The width argument which specifies the minimum column width, and the digits argument which controls the number of digits printed after the decimal point. This table

```
> odds.tab <- stat.table(gest4, list("odds of low bw" = ratio(lowbw,1-lowbw)),
+ data=births)
> print(odds.tab)
```

shows a table of odds that the baby has low birth weight. Use width=15 and digits=3 and see the difference.

*IARC*, 2018 1.4 Graphics in R 25

### 1.4 Graphics in R

There are three kinds of plotting functions in R:

- 1. Functions that generate a new plot, e.g. hist() and plot().
- 2. Functions that add extra things to an existing plot, e.g. lines() and text().
- 3. Functions that allow you to interact with the plot, e.g. locator() and identify().

The normal procedure for making a graph in R is to make a fairly simple initial plot and then add on points, lines, text etc., preferably in a script.

### 1.4.1 Simple plot on the screen

Load the births data and get an overview of the variables:

```
> library( Epi )
> data( births )
> str( births )
```

Now look at the birthweight distribution with

```
> hist(births$bweight)
```

The histogram can be refined – take a look at the possible options with

```
> help(hist)
```

and try some of the options, for example:

```
> hist(births$bweight, col="gray", border="white")
```

To look at the relationship between birthweight and gestational weeks, try

```
> with(births, plot(gestwks, bweight))
```

You can change the plot-symbol by the option pch=. If you want to see all the plot symbols try:

```
> plot(1:25, pch=1:25)
```

4. Make a plot of the birth weight versus maternal age with

```
> with(births, plot(matage, bweight) )
```

5. Label the axes with

```
> with(births, plot(matage, bweight, xlab="Maternal age", ylab="Birth weight (g)") )
```

### 1.4.2 Colours

There are many colours recognized by R. You can list them all by colours() or, equivalently, colors() (R allows you to use British or American spelling). To colour the points of birthweight versus gestational weeks, try

```
> with(births, plot(gestwks, bweight, pch=16, col="green") )
```

This creates a solid mass of colour in the centre of the cluster of points and it is no longer possible to see individual points. You can recover this information by overwriting the points with black circles using the points() function.

```
> with(births, points(gestwks, bweight, pch=1) )
```

Note: when the number of data points on a scatter plot is large, you may also want to decrease the point size: to get points that are 50% of the original size, add the parameter cex=0.5 (or another number <1 for different sizes).

### 1.4.3 Adding to a plot

The points() function just used is one of several functions that add elements to an existing plot. By using these functions, you can create quite complex graphs in small steps.

Suppose we wish to recreate the plot of birthweight vs gestational weeks using different colours for male and female babies. To start with an empty plot, try

```
> with(births, plot(gestwks, bweight, type="n"))
```

Then add the points with the points function.

```
> with(births, points(gestwks[sex==1], bweight[sex==1], col="blue"))
> with(births, points(gestwks[sex==2], bweight[sex==2], col="red"))
```

To add a legend explaining the colours, try

```
> legend("topleft", pch=1, legend=c("Boys", "Girls"), col=c("blue", "red"))
```

which puts the legend in the top left hand corner.

Finally we can add a title to the plot with

```
> title("Birth weight vs gestational weeks in 500 singleton births")
```

IARC, 2018 1.4 Graphics in R 27

### 1.4.3.1 Using indexing for plot elements

One of the most powerful features of R is the possibility to index vectors, not only to get subsets of them, but also for repeating their elements in complex sequences.

Putting separate colours on males and female as above would become very clumsy if we had a 5 level factor instead of sex.

Instead of specifying one color for all points, we may specify a vector of colours of the same length as the gestwks and bweight vectors. This is rather tedious to do directly, but R allows you to specify an expression anywhere, so we can use the fact that sex takes the values 1 and 2, as follows:

First create a colour vector with two colours, and take look at sex:

```
> c("blue","red")
> births$sex
```

Now see what happens if you index the colour vector by sex:

```
> c("blue", "red")[births$sex]
```

For every occurrence of a 1 in sex you get "blue", and for every occurrence of 2 you get "red", so the result is a long vector of "blue"s and "red"s corresponding to the males and females. This can now be used in the plot:

```
> with(births, plot( gestwks, bweight, pch=16, col=c("blue", "red")[sex]) )
```

The same trick can be used if we want to have a separate symbol for mothers over 40 say. We first generate the indexing variable:

```
> births$oldmum <- ( births$matage >= 40 ) + 1
```

Note we add 1 because ( matage >= 40 ) generates a logic variable, so by adding 1 we get a numeric variable with values 1 and 2, suitable for indexing:

```
> with(births, plot( gestwks, bweight, pch=c(16,3)[oldmum], col=c("blue", "red")[sex] ))
```

so where oldmum is 1 we get pch=16 (a dot) and where oldmum is 2 we get pch=3 (a cross).

R will accept any kind of complexity in the indexing as long as the result is a valid index, so you don't need to create the variable oldmum, you can create it on the fly:

```
> with(births, plot(gestwks, bweight, pch=c(16,3)[(matage>=40)+1], col=c("blue", "red")[
```

### 1.4.3.2 Generating colours

R has functions that generate a vector of colours for you. For example,

```
> rainbow(4)
```

produces a vector with 4 colours (not immediately human readable, though). There are a few other functions that generates other sequences of colours, type ?rainbow to see them. The color function (or colour function if you prefer) returns a vector of the colour names that R knows about. These names can also be used to specify colours.

Gray-tones are produced by the function gray (or grey), which takes a numerical argument between 0 and 1; gray(0) is black and gray(1) is white. Try:

```
> plot( 0:10, pch=16, cex=3, col=gray(0:10/10) )
> points( 0:10, pch=1, cex=3 )
```

### 1.4.4 Saving your graphs for use in other documents

If you need to use the plot in a report or presentation, you can save it in a graphics file. Once you have generated the script (sequence of R commands) that produce the graph (and it looks ok on screen), you can start a non-interactive graphics device and then re-run the script. Instead of appearing on the screen, the plot will now be written directly to a file. After the plot has been completed you will need to close the device again in order to be able to access the file. Try:

```
> pdf(file="bweight_gwks.pdf", height=4, width=4)
> with(births, plot( gestwks, bweight, col=c("blue","red")[sex]) )
> legend("topleft", pch=1, legend=c("Boys","Girls"), col=c("blue","red"))
> dev.off()
```

This will give you a portable document file bweight\_gwks.pdf with a graph which is 4 inches tall and 4 inches wide.

Instead of pdf, other formats can be used (jpg, png, tiff, ...). See help(Devices) for the available options.

In window-based environments (R GUI for Windows, R-Studio) you may also use the menu (File Save as ... or Export) to save the active graph as a file and even copy-paste may work (from R graphics window to Word, for instance) – however, writing it manually into the file is recommended for reproducibility purposes (in case you need to redraw your graph with some modifications).

### 1.4.5 The par() command

It is possible to manipulate any element in a graph, by using the graphics options. These are collected on the help page of par(). For example, if you want axis

*IARC*, 2018 1.4 Graphics in R 29

labels always to be horizontal, use the command par(las=1). This will be in effect until a new graphics device is opened.

Look at the typewriter-version of the help-page with

```
> help(par)
```

```
or better, use the the html-version through \boxed{\text{Help}} \rightarrow \boxed{\text{Html help}} \rightarrow \boxed{\text{Packages}} \rightarrow \boxed{\text{graphics}} \rightarrow \boxed{\text{P}} \rightarrow \boxed{\text{par}}.
```

It is a good idea to take a print of this (having set the text size to "smallest" because it is long) and carry it with you at any time to read in buses, cinema queues, during boring lectures etc. Don't despair, few R-users can understand what all the options are for.

par() can also be used to ask about the current plot, for example par("usr") will give you the exact extent of the axes in the current plot.

If you want more plots on a single page you can use the command

```
> par( mfrow=c(2,3) )
```

This will give you a layout of 2 rows by 3 columns for the next 6 graphs you produce. The plots will appear by row, i.e. in the top row first. If you want the plots to appear columnwise, use par( mfcol=c(2,3) ) (you still get 2 rows by 3 columns).

To restore the layout to a single plot per page use

```
> par(mfrow=c(1,1))
```

If you want a more detailed control over the layout of multiple graphs on a single page look at ?layout.

### 1.4.6 Interacting with a plot

The locator() function allows you to interact with the plot using the mouse. Typing locator(1) shifts you to the graphics window and waits for one click of the left mouse button. When you click, it will return the corresponding coordinates.

You can use locator() inside other graphics functions to position graphical elements exactly where you want them. Recreate the birth-weight plot,

```
> with(births, plot(gestwks, bweight, col = c("blue", "red")[sex]) )
and then add the legend where you wish it to appear by typing
> legend(locator(1), pch=1, legend=c("Boys", "Girls"), col=c("blue", "red") )
```

The identify() function allows you to find out which records in the data correspond to points on the graph. Try

```
> with(births, identify(gestwks, bweight))
```

When you click the left mouse button, a label will appear on the graph identifying the row number of the nearest point in the data frame births. If there is no point nearby, R will print a warning message on the console instead. To end the interaction with the graphics window, right click the mouse: the identify function returns a vector of identified points.

1. Use identify() to find which records correspond to the smallest and largest number of gestational weeks and view the corresponding records:

```
> with(births, births[identify(gestwks, bweight), ])
```

### 1.5 Simple simulation

Monte Carlo methods are computational procedures dealing with simulation of artificial data from given probability distributions with the purpose of learning about the behaviour of phenomena involving random variability. These methods have a wide range of applications in statistics as well as in several branches of science and technology. By solving the following exercises you will learn to use some basic tools of statistical simulation.

1. Whenever using a random number generator (RNG) for a simulation study (or for another purpose, such as for producing a randomization list to be used in a clinical trial or for selecting a random sample from a large cohort), it is a good practice to set first the seed. It is a number that determines the initial state of the RNG, from which it starts creating the desired sequence of pseudo-random numbers. Explicit specification of the seed enables the reproducibility of the sequence. – Instead of the number 5462319 below you may use your own seed of choice.

```
> set.seed(5462319)
```

2. Generate a random sample of size 20 from a normal distribution with mean 100 and standard deviation 10. Draw a histogram of the sampled values and compute the conventional summary statistics

```
> x <- rnorm(20, 100, 10)
> hist(x)
> c(mean(x), sd(x))
```

Repeat the above lines and compare the results.

- 3. Now replace the sample size 20 by 1000 and run again twice the previous command lines with this size but keeping the parameter values as before. Compare the results between the two samples here as well as with those in the previous item.
- 4. Generate 500 observations from a Bernoulli(p) distribution, or Bin(1, p) distribution, taking values 1 and 0 with probabilities p and 1-p, respectively, when p = 0.4:

```
> X <- rbinom(500, 1, 0.4)
> table(X)
```

5. Now generate another 0/1 variable Y, being dependent on previously generated X, so that P(Y = 1|X = 1) = 0.2 and P(Y = 1|X = 0) = 0.1.

```
> Y <- rbinom(500,1,0.1*X+0.1)
> table(X,Y)
> prop.table(table(X,Y),1)
```

6. Generate data obeying a simple linear regression model  $y_i = 5 + 0.1x_i + \varepsilon_i$ , i = 1, ... 100, in which  $\varepsilon_i \sim N(0, 10^2)$ , and  $x_i$  values are integers from 1 to 100. Plot the  $(x_i, y_i)$ -values, and estimate the parameters of that model.

```
> x <- 1:100
> y <- 5 + 0.1*x + rnorm(100,0,10)
> plot(x,y)
> abline(lm(y~x))
> summary(lm(y~x))$coef
```

Are your estimates consistent with the data-generating model? Run the code a couple of times to see the variability in the parameter estimates.

### **1.6 Calculation of rates, RR and RD**

This exercise is *very* prescriptive, so you should make an effort to really understand everything you type into R. Consult the relevant slides of the lecture on "Poisson regression for rates . . ."

#### 1.6.1 Hand calculations for a single rate

Let  $\lambda$  be the true hazard rate or theoretical incidence rate, its estimator being the empirical incidence rate  $\widehat{\lambda} = D/Y =$  'no. cases/person-years'. Recall that the standard error of the empirical rate is  $SE(\widehat{\lambda}) = \widehat{\lambda}/\sqrt{D}$ .

The simplest approximate 95% confidence interval (CI) for  $\lambda$  is given by

$$\widehat{\lambda} \pm 1.96 \times SE(\widehat{\lambda})$$

An alternative approach is based on logarithmic transformation of the empirical rate. The standard error of the log-rate  $\hat{\theta} = \log(\hat{\lambda})$  is  $SE(\hat{\theta}) = 1/\sqrt{D}$ . Thus, a simple approximate 95% confidence interval for the log-hazard  $\theta = \log(\lambda)$  is obtained from

$$\widehat{\theta} \pm 1.96/\sqrt{D} = \log(\widehat{\lambda}) \pm 1.96/\sqrt{D}$$

When taking the exponential from the above limits, we get another approximate confidence interval for the hazard  $\lambda$  itself:

$$\exp\{\log(\widehat{\lambda}) \pm 1.96/\sqrt{D}\} = \widehat{\lambda} \stackrel{\times}{\div} \mathrm{EF},$$

where  $EF = \exp\{1.96 \times SE[\log(\widehat{\lambda})]\}$  is the *error factor* associated with the 95% interval. This approach provides a more accurate approximation with very small numbers of cases. (However, both these methods fail when D = 0, in which case an *exact* method or one based on *profile-likelihood* is needed.)

1. Suppose you have 15 events during 5532 person-years. Let's use R as a simple desk calculator to derive the rate (in 1000 person-years; therefore 5.532) and the first version of an approximate confidence interval:

```
> library( Epi )
> options(digits=4) # to cut down decimal points in the output
> D <- 15
> Y <- 5.532 # thousands of years
> rate <- D / Y
> SE.rate <- rate/sqrt(D)
> c(rate, SE.rate, rate + c(-1.96, 1.96)*SE.rate )
```

2. Compute now the approximate confidence interval using the method based on log-transformation and compare the result with that in item (a)

```
> SE.logr <- 1/sqrt(D)
> EF <- exp( 1.96 * SE.logr )
> c(log(rate), SE.logr)
> c( rate, EF, rate/EF, rate*EF )
```

#### 1.6.2 Poisson model for a single rate with logarithmic link

You are able to estimate  $\lambda$  and compute its CI with a Poisson model, as described in the relevant slides in the lecture handout.

3. Use the number of events as the response and the log-person-years as an offset term, and fit the Poisson model with log-link

```
> m <- glm( D ~ 1, family=poisson(link=log), offset=log(Y) )
> summary( m )
```

What is the interpretation of the parameter in this model?

4. The summary method produces too much output. You can extract CIs for the model parameters directly from the fitted model on the scale determined by the *link* function with the ci.lin()-function. Thus, the estimate, SE, and confidence limits for the log-rate  $\theta = \log(\lambda)$  are obtained by:

```
> ci.lin( m )
```

However, to get the confidence limits for the rate  $\lambda = \exp(\theta)$  on the original scale, the results must be exp-transformed:

```
> ci.lin( m, Exp=T)
```

To get just the point estimate and CI for  $\lambda$  from log-transformed quantities you are recommended to use function ci.exp(), which is actually a wrapper of ci.lin():

```
> ci.exp( m)
> ci.lin( m, Exp=T)[, 5:7]
```

Both functions are found from Epi package. – Note that the test statistic and P-value are rarely interesting quantities for a single rate.

5. There is an alternative way of fitting a Poisson model: Use the empirical rate  $\hat{\lambda} = D/Y$  as a *scaled* Poisson response, and the person-years as *weight* instead of offset (albeit it will give you a warning about non-integer response in a Poisson model, but you can ignore this warning):

```
> mw <- glm( D/Y ~ 1, family=poisson, weight=Y )
> ci.exp( mw )
```

Verify that this gave the same results as above.

### 1.6.3 Poisson model for a single rate with identity link

The advantage of the approach based on weighting is that it allows sensible use of the *identity* link. The response is the same but the parameter estimated is now the rate itself, not the log-rate.

6. Fit the Poisson model with identity link

```
> mi <- glm( D/Y ~ 1, family=poisson(link=identity), weight=Y )
> coef( mi )
```

What is the meaning of the intercept in this model?

Verify that you actually get the same rate estimate as before.

7. Now use ci.lin() to produce the estimate and the confidence intervals from this model:

```
> ci.lin( mi )
> ci.lin( mi )[, c(1,5,6)]
```

## 1.6.4 Poisson model assuming same rate for several periods

Now, suppose the events and person years are collected over three periods.

8. Read in the data and compute period-specific rates

```
> Dx <- c(3,7,5)
> Yx <- c(1.412,2.783,1.337)
> Px <- 1:3
> rates <- Dx/Yx
> rates
```

9. Fit the same model as before, assuming a single rate to the data for the separate periods. Compare the result from previous ones

```
> m3 <- glm( Dx ~ 1, family=poisson, offset=log(Yx) )
> ci.exp( m3 )
```

10. Now test whether the rates are the same in the three periods: Try to fit a model with the period as a factor in the model:

```
> mp <- glm( Dx ~ factor(Px), offset=log(Yx), family=poisson )
```

and compare the two models using anova() with the argument test="Chisq":

```
> anova( m3, mp, test="Chisq" )
```

Compare the test statistic to the deviance of the model mp.

What is the deviance good for?

### 1.6.5 Analysis of rate ratio

We now switch to comparison of two rates  $\lambda_1$  and  $\lambda_0$ , i.e. the hazard in an exposed group vs. that in an unexposed one.

Consider first estimation of the true rate ratio  $\rho = \lambda_1/\lambda_0$  between the groups. Suppose we have pertinent empirical data (cases and person-times) from both groups,  $(D_1, Y_1)$  and  $(D_0, Y_0)$ . The point estimate of  $\rho$  is the empirical rate ratio

$$RR = \frac{D_1/Y_1}{D_0/Y_0}$$

It is known that the variance of  $\log(RR)$ , that is, the difference of the log of the empirical rates  $\log(\widehat{\lambda}_1) - \log(\widehat{\lambda}_0)$  is estimated as

$$var(log(RR)) = var\{log(\widehat{\lambda}_1/\widehat{\lambda}_0)\}$$

$$= var\{log(\widehat{\lambda}_1)\} + var\{log(\widehat{\lambda}_0)\}$$

$$= 1/D_1 + 1/D_0$$

Based on a similar argument as before, an approximate 95% CI for the true rate ratio  $\lambda_1/\lambda_0$  is then:

$$RR \stackrel{\times}{:} \exp\left(1.96\sqrt{\frac{1}{D_1} + \frac{1}{D_0}}\right)$$

Suppose you have 15 events during 5532 person-years in an unexposed group and 28 events during 4783 person-years in an exposed group:

11. Calculate the rate-ratio and CI by direct application of the above formulae:

```
> D0 <- 15 ; D1 <- 28

> Y0 <- 5.532 ; Y1 <- 4.783

> RR <- (D1/Y1)/(D0/Y0)

> SE.lrr <- sqrt(1/D0+1/D1)

> EF <- exp( 1.96 * SE.lrr)

> c( RR, RR/EF, RR*EF )
```

12. Now achieve this using a Poisson model:

```
> D <- c(D0,D1); Y <- c(Y0,Y1); expos <- 0:1
> mm <- glm(D \sim factor(expos), family=poisson, offset=log(Y))
```

What do the parameters mean in this model?

13. You can extract the exponentiated parameters in two ways:

```
> ci.exp( mm )
> ci.lin( mm, E=T )[,5:7]
```

## 1.6.6 Analysis of rate difference

For the true rate difference  $\delta = \lambda_1 - \lambda_0$ , the natural estimator is the empirical rate difference

$$\widehat{\delta} = \widehat{\lambda}_1 - \widehat{\lambda}_0 = D_1/Y_1 - D_0/Y_0 = \text{RD}.$$

Its variance is just the sum of the variances of the two rates (since the latter are based on independent samples):

$$\operatorname{var}(RD) = \operatorname{var}(\widehat{\lambda}_1) + \operatorname{var}(\widehat{\lambda}_0)$$
$$= D_1/Y_1^2 + D_0/Y_0^2$$

14. Use this formula to compute the rate difference and a 95% confidence interval for it:

```
> rd <- diff( D/Y )
> sed <- sqrt( sum( D/Y^2 ) )
> c( rd, rd+c(-1,1)*1.96*sed )
```

15. Verify that this is the confidence interval you get when you fit an additive model with exposure as factor:

```
> ma <- glm( D/Y ~ factor(expos),
+ family=poisson(link=identity), weight=Y )
> ci.lin( ma )[, c(1,5,6)]
```

#### 1.6.7 Optional: Calculations using matrix tools

NB. This subsection requires some familiarity with matrix algebra. Do this only after you have done the other exercise of this session.

16. Explore the function ci.mat(), which lets you use matrix multiplication (operator '%\*%' in R) to produce a confidence interval from an estimate and its standard error (or CIs from whole columns of estimates and SEs):

```
> ci.mat
> ci.mat()
```

As you see, this function returns a  $2 \times 3$  matrix (2 rows, 3 columns) containing familiar numbers.

17. When you combine the single rate and its standard error into a row vector of length 2, i.e. a 1 × 2 matrix, and multiply this by the 2 × 3 matrix above, the computation returns a 1 × 3 matrix containing the point estimate and the confidence limit. – Apply this method to the single rate calculations in 1.6.1; first creating the 1 × 2 matrix and then performing the matrix multiplication.

```
> rateandSE <- c( rate, SE.rate )
> rateandSE
> rateandSE %*% ci.mat()
```

18. When the confidence interval is based on the log-rate and its standard error, the result is obtained by appropriate application of the exp-function on the pertinent matrix product

```
> lograndSE <- c( log(rate), SE.logr )
> lograndSE
> exp( lograndSE %*% ci.mat() )
```

19. For computing the rate ratio and its CI as in 1.6.5, matrix multiplication with ci.mat() should give the same result as there:

```
> exp( c( log(RR), SE.lrr ) %*% ci.mat() )
```

20. The main argument in function ci.mat() is alpha, which sets the confidence level:  $1 - \alpha$ . The default value is alpha = 0.05, corresponding to the level 1 - 0.05 = 95 %. If you wish to get the confidence interval for the rate ratio at the 90 % level (= 1 - 0.1), for instance, you may proceed as follows:

```
> ci.mat( alpha=0.1 )
> exp( c( log(RR), SE.lrr ) %*% ci.mat(alpha=0.1) )
```

21. Look again to the model used to analyse the rate ratio in 1.6.5. Often one would like to get simultaneously both the rates and the ratio between them. This can be achieved in one go using the *contrast matrix* argument ctr.mat to ci.lin() or ci.exp(). Try:

22. Use the same machinery to the additive model to get the rates and the rate-difference in one go. Note that the annotation of the resulting estimates are via the column-names of the contrast matrix.

## 1.7 Logistic regression (GLM)

#### 1.7.1 Malignant melanoma in Denmark

In the mid-80s a case-control study on risk factors for malignant melanoma was conducted in Denmark (Østerlind et al. The Danish case-control study of cutaneous malignant melanoma I: Importance of host factors. *Int J Cancer* 1988; 42: 200-206).

The cases were patients with skin melanoma (excluding lentigo melanoma), newly diagnosed from 1 Oct, 1982 to 31 March, 1985, aged 20-79, from East Denmark, and they were identified from the Danish Cancer Registry.

The controls (twice as many as cases) were drawn from the residents of East Denmark in April, 1984, as a random sample stratified by sex and age (within the same 5 year age group) to reflect the sex and age distribution of the cases. This is called group matching, and in such a study, it is necessary to control for age and sex in the statistical analysis. (Yes indeed: In spite of the fact that stratified sampling by sex and age removed the statistical association of these variables with melanoma from the final case-control data set, the analysis must control for variables which determine the probability of selecting subjects from the base population to the study sample.)

The population of East Denmark is a dynamic one. Sampling the controls only at one time point is a rough approximation of *incidence density sampling*, which ideally would spread out over the whole study period. Hence the exposure odds ratios calculable from the data are estimates of the corresponding hazard rate ratios between the exposure groups.

After exclusions, refusals etc., 474 cases (92% of eligible cases) and 926 controls (82%) were interviewed. This was done face-to-face with a structured questionnaire by trained interviewers, who were not informed about the subject's case-control status.

For this exercise we have selected a few host variables from the study in an ascii-file, melanoma.dat. The variables are listed in table 2.1.

## 1.7.2 Reading the data

Start R and load the Epi package using the function library(). Read the data set from the file melanoma.dat found in the course website to a data frame with name mel using the read.table() function. Remember to specify that missing values are coded ".", and that variable names are in the first line of the file. View the overall structure of the data frame, and list the first 20 rows of mel.

```
> library(Epi)
> mel <- read.table("http://bendixcarstensen.com/SPE/data/melanoma.dat", header=TRUE, na.
> str(mel)
> head(mel, n=20)
```

Table 1.1: Variables in the melanoma dataset.

Variable	Units or Coding	Type	Name
Case-control status	1=case, 0=control	numeric	СС
Sex	1=male, 2=female	numeric	sex
Age at interview	age in years	numeric	age
Skin complexion	0=dark, 1=medium, 2=light	numeric	skin
Hair colour	0=dark brown/black, 1=light brown,		
	2=blonde, 3=red	numeric	hair
eye colour	0=brown, 1=grey, green, 2=blue	numeric	eyes
Freckles	1=many, 2=some, 3=none	numeric	freckles
Naevi, small	no. naevi $< 5$ mm	numeric	nvsmall
Naevi, largs	no. naevi $\geq 5$ mm	numeric	nvlarge

#### 1.7.3 House keeping

The structure of the data frame mel tells us that all the variables are numeric (integer), so first you need to do a bit of house keeping. For example the variables sex, skin, hair, eye need to be converted to factors, with labels, and freckles which is coded 4 for none down to 1 for many (not very intuitive) needs to be recoded, and relabelled.

To avoid too much typing and to leave plenty of time to think about the analysis, these house keeping commands are in a script file called melanoma-house.r. You should study this script carefully before running it. The coding of freckles can be reversed by subtracting the current codes from 4. Once recoded the variable needs to be converted to a factor with labels "none", etc. Age is currently a numeric variable recording age to the nearest year, and it will be convenient to group these values into (say) 10 year age groups, using cut. In this case we choose to create a new variable, rather than change the original.

> source("http://bendixcarstensen.com/SPE/data/melanoma-house.r")

Look again at the structure of the data frame mel and note the changes. Use the command summary (mel) to look at the univariate distributions.

This is enough housekeeping for now - let's turn to something a bit more interesting.

#### 1.7.4 One variable at a time

As a first step it is a good idea to start by looking at the numbers of cases and controls by each variable separately, ignoring age and sex. Try

```
> with(mel, table(cc,skin))
> stat.table(skin, contents=ratio(cc,1-cc), data=mel)
```

to see the numbers of cases and controls, as well as the odds of being a case by skin colour

Now use effx() to get crude estimates of the hazard ratios for the effect of skin colour.

```
> effx(cc, type="binary", exposure=skin, data=mel)
```

• Look at the crude effect estimates of hair, eyes and freckles in the same way.

## 1.7.5 Generalized linear models with binomial family and logit link

The function effx() is just a wrapper for the glm() function, and you can show this by fitting the glm directly with

```
> mf <- glm(cc ~ freckles, family="binomial", data=mel)
> round(ci.exp( mf ),2)
>
```

Comparison with the output from effx() shows the results to be the same.

Note that in effx() the type of response is "binary" whereas in glm() the family of probability distributions used to fit the model is "binomial". There is a 1-1 relationship between type of response and family:

```
metric gaussian
binary binomial
failure/count poisson
```

#### 1.7.6 Controlling for age and sex

Because the probability that a control is selected into the study depends on age and sex it is necessary to control for age and sex. For example, the effect of freckles controlled for age and sex is obtained with

```
> effx(cc, typ="binary", exposure=freckles, control=list(age.cat,sex),data=mel)
or
> mfas <- glm(cc ~ freckles + age.cat + sex, family="binomial", data=mel)
> round(ci.exp(mfas), 2)
```

Do the adjusted estimates differ from the crude ones that you computed with effx()?

#### 1.7.7 Likelihood ratio tests

There are 2 effects estimated for the 3 levels of freckles, and glm() provides a test for each effect separately, but to test for no effect at all of freckles you need a likelihood ratio test. This involves fitting two models, one without freckles and one with, and recording the change in deviance. Because there are some missing values for freckles it is necessary to restrict the first model to those subjects who have values for freckles.

```
> mas <- glm(cc ~ age.cat + sex, family="binomial", data=subset(mel, !is.na(freckles)) )
> anova(mas, mfas, test="Chisq")
```

The change in residual deviance is 1785.9 - 1737.1 = 48.8 on 1389 - 1387 = 2 degrees of freedom. The *P*-value corresponding to this change is obtained from the upper tail of the cumulative distribution of the  $\chi^2$ -distribution with 2 df:

```
> 1 - pchisq(48.786, 2)
```

• There are 3 effects for the 4 levels of hair colour (hair). To obtain adjusted estimates for the effect of hair colour and to test the pertinent null hypothesis fit the relevant models, print the and use anova to test for no effects of hair colour. Compare the estimates with the crude ones and assess the evidence against the null hypothesis.

#### 1.7.8 Relevelling

From the above you can see that subjects at each of the 3 levels light-brown, blonde, and red, are at greater risk than subjects with dark hair, with similar odds ratios. This suggests creating a new variable hair2 which has just two levels, dark and the other three. The Relevel() function in Epi has been used for this in the house keeping script.

• Use effx() to compute the odds-ratio of melanoma between persons with red, blonde or light brown hair versus those with dark hair. Reproduce these results by fitting an appropriate glm. Use also a likelihood ratio test to test for the effect of hair2.

### 1.7.9 Controlling for other variables

When you control the effect of an exposure for some variable you are asking a question about what would the effect be if the variable is kept constant. For example, consider the effect of freckles controlled for hair2. We first stratify by hair2 with

```
> effx(cc, type="binary", exposure=freckles,
+ control=list(age.cat,sex), strata=hair2, data=mel)
```

The effect of freckles is still apparent in each of the two strata for hair colour. Use effx() to control for hair2, too, in addition to age.cat and sex.

```
> effx(cc, type="binary", exposure=freckles,
+ control=list(age.cat,sex,hair2), data=mel)
```

It is tempting to control for variables without thinking about the question you are thereby asking. This can lead to nonsense.

#### 1.7.10 Stratification using glm()

We shall reproduce the output from

```
> effx(cc, type="binary", exposure=freckles,
+ control=list(age.cat,sex), strata=hair2,data=mel)
```

using glm(). To do this requires a nested model formula:

```
> mfas.h <- glm(cc ~ hair2/freckles + age.cat + sex, family="binomial", data=mel)
> ci.exp(mfas.h )
```

In amongst all the other effects you can see the two effects of freckles for dark hair (1.61 and 2.84) and the two effects of freckles for other hair (1.42 and 3.15).

#### 1.7.11 Naevi

The distributions of nvsmall and nvlarge are very skew to the right. You can see this with

```
> with(mel, stem(nvsmall))
> with(mel, stem(nvlarge))
```

Because of this it is wise to categorize them into a few classes

- small naevi into four: 0, 1, 2-4, and 5+;
- large naevi into three: 0, 1, and 2+.

This has been done in the house keeping script.

- Look at the joint frequency distribution of these new variables using with(mel, table()). Are they strongly associated?
- Compute the sex- and age-adjusted OR estimates (with 95% CIs) associated with the number of small naevi first by using effx(), and then by fitting separate glms including sex, age.cat and nvsma4 in the model formula.
- Do the same with large naevi nvlar3.
- Now fit a glm containing age.cat, sex, nvsma4 and nvlar3. What is the interpretation of the coefficients for nvsma4 and nvlar3?

#### 1.7.12 Treating freckles as a numeric exposure

The evidence for the effect of **freckles** is already convincing. However, to demonstrate how it is done, we shall perform a linear trend test by treating freckles as a numeric exposure.

```
> mel$fscore<-as.numeric(mel$freckles)
> effx(cc, type="binary", exposure=fscore, control=list(age.cat,sex), data=mel)
```

You can check for linearity of the log odds of being a case with fscore by comparing the model containing freckles as a factor with the model containing freckles as numeric.

```
> m1 <- glm(cc ~ freckles + age.cat + sex, family="binomial", data=mel)
> m2 <- glm(cc ~ fscore + age.cat + sex, family="binomial", data=mel)
> anova(m2, m1, test="Chisq")
```

There is no evidence against linearity (p = 0.22).

It is sometimes helpful to look at the linearity in more detail with

```
> m1 <- glm(cc ~ C(freckles, contr.cum) + age.cat + sex, family="binomial",data=mel)
> round(ci.exp(m1), 2)
> m2 <- glm(cc ~ fscore + age.cat + sex, family="binomial",data=mel)
> round(ci.exp(m2), 2)
```

The use of C(freckles, contr.cum) makes each odds ratio to compare the odds at that level versus the previous level; not against the baseline (except for the 2nd level). If the log-odds are linear then these odds ratios should be the same (and the same as the odds ratio for fscore in m2.

#### 1.7.13 Graphical displays

The odds ratios (with CIs) can be graphically displayed using function plotEst() in Epi. It uses the value of ci.lin() evaluated on the fitted model object. As the intercept and the effects of age and sex are of no interest, we shall drop the corresponding rows (the 7 first ones) from the matrix produced by ci.lin(), and the plot is based just on the 1st, 5th and the 6th column of this matrix:

```
> m <- glm(cc ~ nvsma4 + nvlar3 + age.cat + sex, family="binomial",data=mel)
> plotEst( exp( ci.lin(m)[ 2:5, -(2:4)] ), xlog=T, vref=1 )
```

The xlog argument makes the OR axis logarithmic.

# 1.8 Estimation of effects: simple and more complex

This exercise deals with analysis of metric or continuous response variables. We start with simple estimation of effects of a binary, categorical or a numeric explanatory variable, the exposure variable of interest. Then evaluation of potential modification confounding and/or by other variables is considered by stratification by and adjustment or control for these variables. Use of function effx() for such tasks is introduced together with functions lm() and glm() that can be used for more general linear and generalized linear models. Finally, more complex polynomial models for the effect of a numeric exposure variable are illustrated.

#### 1.8.1 Response and explanatory variables

Identifying the *response* or *outcome variable* correctly is the key to analysis. The main types are:

- Metric (a measurement taking many values, usually with units)
- Binary (two values coded 1/0)
- Failure (does the subject fail at end of follow-up, coded 1/0, and how long was follow-up, measurement of time)
- Count (aggregated data on failures in a group)

All these response variable are numeric.

Variables on which the response may depend are called *explanatory variables*. They can be categorical factors or numeric variables. A further important aspect of explanatory variables is the role they will play in the analysis.

- Primary role: exposure.
- Secondary role: confounder and/or modifier.

The word *effect* is a general term referring to ways of comparing the values of the response variable at different levels of an explanatory variable. The main measures of effect are:

- Differences in means for a metric response.
- Ratios of odds for a binary response.
- Ratios of rates for a failure or count response.

Other measures of effect include ratios of geometric means for positive-valued metric outcomes, differences and ratios between proportions (risk difference and risk ratio), and differences between failure rates.

#### 1.8.2 Data set births

We shall use the **births** data to illustrate different aspects in estimating effects of various exposures on a metric response variable **bweight** = birth weight, recorded in grams.

1. Load the Epi package and the data set and look at its content

```
> library(Epi)
> data(births)
> str(births)
```

2. Because all variables are numeric we need first to do a little housekeeping. Two of them are directly converted into factors, and categorical versions are created of two continuous variables by function cut().

```
> births$hyp <- factor(births$hyp, labels = c("normal", "hyper"))
> births$sex <- factor(births$sex, labels = c("M", "F"))
> births$agegrp <- cut(births$matage,
+ breaks = c(20, 25, 30, 35, 40, 45), right = FALSE)
> births$gest4 <- cut(births$gestwks,
+ breaks = c(20, 35, 37, 39, 45), right = FALSE)</pre>
```

3. Have a look at univariate summaries of the different variables in the data; especially the location and dispersion of the distribution of bweight.

```
> summary(births)
> with(births, sd(bweight) )
```

### 1.8.3 Simple estimation with effx(), lm() and glm()

We are ready to analyze the "effect" of sex on bweight. A binary exposure variable, like sex, leads to an elementary two-group comparison of group means for a metric response.

4. Comparison of two groups is commonly done by the conventional t-test and the associated confidence interval.

```
> with( births, t.test(bweight ~ sex, var.equal=T) )
```

The *P*-value refers to the test of the null hypothesis that there is no effect of sex on birth weight (quite an uninteresting null hypothesis in itself!). However, t.test() does not provide the point estimate for the effect of sex; only the test result and a confidence interval.

5. The function effx() in Epi is intended to introduce the estimation of effects in epidemiology, together with the related ideas of stratification and controlling, i.e. adjustment for confounding, without the need for familiarity with statistical modelling. It is in fact a wrapper of function glm() that fits generalized linear models. – Now, do the same analysis with effx()

```
> effx(response=bweight, type="metric", exposure=sex, data=births)
```

The estimated effect of sex on birth weight, measured as a difference in means between girls and boys, is -197 g. Either the output from t.test() above or the command

```
> stat.table(sex, mean(bweight), data=births) confirms this (3032.8 - 3229.9 = -197.1).
```

6. The same task can easily be performed by lm() or by glm(). The main argument in both is the *model formula*, the left hand side being the response variable and the right hand side after ~ defines the explanatory variables and their joint effects on the response. Here the only explanatory variable is the binary factor sex. With glm() one specifies the family, i.e. the assumed distribution of the response variable, but in case you use lm(), this argument is not needed, because lm() fits only models for metric responses assuming Gaussian distribution.

```
> m1 <- glm(bweight ~ sex, family=gaussian, data=births)
> summary(m1)
```

Note the amount of output that summary() method produces. The point estimate plus confidence limits can, though, be concisely obtained by ci.lin().

```
> round( ci.lin(m1)[ , c(1,5,6)] , 1)
```

7. Now, use effx() to find the effect of hyp (maternal hypertension) on bweight.

#### 1.8.4 Factors on more than two levels

The variable gest4 became as the result of cutting gestwks into 4 groups with left-closed and right-open boundaries [20,35) [35,37) [37,39) [39,45).

8. We shall find the effects of gest4 on the metric response bweight.

```
> effx(response=bweight,typ="metric",exposure=gest4,data=births)
```

There are now 3 effect estimates:

```
[35,37) vs [20,35) 857
[37,39) vs [20,35) 1360
[39,45) vs [20,35) 1668
```

The command

```
> stat.table(gest4, mean(bweight), data=births)
```

confirms that the effect of agegrp (level 2 vs level 1) is 2590 - 1733 = 857, etc.

9. Compute these estimates by lm() and find out how the coefficients are related to the group means

```
> m2 <- lm(bweight ~ gest4, data = births)
> round( ci.lin(m2)[ , c(1,5,6)] , 1)
```

## 1.8.5 Stratified effects and interaction or effect modification

We shall now examine whether and to what extent the effect of hyp on bweight varies by gest4.

10. The following "interaction plot" shows how the mean bweight depends jointly on hyp and gest4

```
> par(mfrow=c(1,1))
> with( births, interaction.plot(gest4, hyp, bweight) )
```

It appears that the mean difference in **bweight** between normotensive and hypertensive mothers is inversely related to gestational age.

11. Let us get numerical values for the mean differences in the different gest4 categories:

```
> effx(bweight, type="metric", exposure=hyp, strata=gest4,data=births)
```

The estimated effects of hyp in the different strata defined by gest4 thus range from about -100 g among those with  $\geq 39$  weeks of gestation to about -700 g among those with < 35 weeks of gestation. The error margin especially around the latter estimate is quite wide, though. The P-value 0.055 from the test for effect modification indicates weak evidence against the null hypothesis of "no interaction between hyp and gest4". On the other hand, this test may well be not very sensitive given the small number of preterm babies in these data.

12. Stratified estimation of effects can also be done by lm(), and you should get the same results:

```
> m3 <- lm(bweight ~ gest4/hyp, data = births)
> round( ci.lin(m3)[ , c(1,5,6)], 1)
```

13. An equivalent model with an explicit *interaction term* between **gest4** and hyp is fitted as follows

```
> m3I <- lm(bweight ~ gest4 + hyp + gest4:hyp, data = births)
> round( ci.lin(m3I)[ , c(1,5,6)], 1)
```

From this output you would find a familiar estimate -673 g for those < 35 gestational weeks. The remaining coefficients are estimates of the interaction effects such that e.g. 515 = -158 - (-673) g describes the contrast in the effect of hyp on bweight between those 35 to < 37 weeks and those < 35 weeks of gestation.

14. Perhaps a more appropriate reference level for the categorized gestational age would be the highest one. Changing the reference level, here to be the 4th category, can be done by Relevel() function in the Epi package, after which an equivalent interaction model is fitted, now using a shorter expression for it in the model formula:

```
> births$gest4b <- Relevel( births$gest4, ref = 4)
> m3Ib <- lm(bweight ~ gest4b*hyp, data = births)
> round( ci.lin(m3Ib)[ , c(1,5,6)], 1)
```

Notice now the coefficient -91.6 for hyp. It estimates the effect of hyp on bweight among those with  $\geq 39$  weeks of gestation. The estimate -88.5 g = -180.1 - (-91.6) g describes the additional effect of hyp in the category 37 to 38 weeks of gestation upon that in the reference class.

15. At this stage it is interesting to compare the results from the interaction models to those from the corresponding *main effects* model, in which the effect of hyp is assumed not to be modified by gest4:

```
> m3M <- lm(bweight ~ gest4 + hyp, data = births)
> round( ci.lin(m3M)[ , c(1,5,6)], 1)
```

The estimate -201 g describing the overall effect of hyp is obtained as a weighted average of the stratum-specific estimates obtained by effx() above. It is a meaningful estimate adjusting for gest4 insofar as it is reasonable to assume that the effect of hyp is not modified by gest4. This assumption or the "no interaction" null hypothesis can formally be tested by a common deviance test.

```
> anova(m3I, m3M)
```

The *P*-value is practically the same as before when the interaction was tested in effx(). However, in spite of obtaining a "non-significant" result from this test, the possibility of a real interaction should not be ignored in this case.

16. Now, use effx() to stratify (i) the effect of hyp on bweight by sex and then (ii) perform the stratified analysis using the two ways of fitting an interaction model with lm.

Look at the results. Is there evidence for the effect of hyp being modified by sex?

### 1.8.6 Controlling or adjusting for the effect of hyp for sex

The effect of hyp is controlled for – or adjusted for – sex by first looking at the estimated effects of hyp in the two stata defined by sex, and then combining these effects if they seem sufficiently similar. In this case the estimated effects were -496 and -380 which look quite similar (and the P-value against "no interaction" was quite large, too), so we can perhaps combine them, and control for sex.

17. The combining is done by declaring sex as a control variable:

```
> effx(bweight, type="metric", exposure=hyp, control=sex, data=births)
```

18. The same is done with lm() as follows:

```
> m4 <- lm(bweight ~ sex + hyp, data = births)
> ci.lin(m4)[ , c(1,5,6)]
```

The estimated effect of hyp on bweight controlled for sex is thus -448 g. There can be more than one control variable, e.g control=list(sex,agegrp).

Many people go straight ahead and control for variables which are likely to confound the effect of exposure without bothering to stratify first, but usually it is useful to stratify first.

#### 1.8.7 Numeric exposures

If we wished to study the effect of gestation time on the baby's birth weight then gestwks is a numeric exposure.

19. Assuming that the relationship of the response with gestwks is roughly linear (for a metric response) we can estimate the linear effect of gestwks, both with effx() and with lm() as follows:

```
> effx(response=bweight, type="metric", exposure=gestwks,data=births)
> m5 <- lm(bweight ~ gestwks, data=births) ; ci.lin(m5)[ , c(1,5,6)]</pre>
```

We have fitted a simple linear regression model and obtained estimates of the two regression coefficient: intercept and slope. The linear effect of gestwks is thus estimated by the slope coefficient, which is 197 g per each additional week of gestation.

20. You cannot stratify by a numeric variable, but you can study the effects of a numeric exposure stratified by (say) agegrp with

```
> effx(bweight, type="metric", exposure=gestwks, strata=agegrp, data=births)
```

You can control/adjust for a numeric variable by putting it in the control list.

#### 1.8.8 Checking the assumptions of the linear model

At this stage it will be best to make some visual check concerning our model assumptions using plot(). In particular, when the main argument for the *generic function* plot() is a fitted lm object, it will provide you some common diagnostic graphs.

21. To check whether bweight goes up linearly with gestwks try

```
> with(births, plot(gestwks,bweight))
> abline(m5)
```

22. Moreover, take a look at the basic diagnostic plots for the fitted model.

```
> par(mfrow=c(2,2))
> plot(m5)
```

What can you say about the agreement with data of the assumptions of the simple linear regression model, like linearity of the systematic dependence, homoskedasticity and normality of the error terms?

### 1.8.9 Third degree polynomial of gestwks

A common practice to assess possible deviations from linearity is to compare the fit of the simple model with models having higher order polynomial terms. In perinatal epidemiology a popular model for describing the relationship between gestational age and birth weight is a 3rd degree polynomial.

23. For fitting a third degree polynomial of gestwks we can update our previous simple linear model by adding the quadratic and cubic terms of gestwks using the *insulate* operator I()

```
> m6 <- update(m5, . ~ . + I(gestwks^2) + I(gestwks^3))
> round(ci.lin(m6)[, c(1,5,6)], 1)
```

The intercept and linear coefficients are really spectacular – but don't make any sense!

- 24. A more elegant way of fitting polynomial models is to utilize *orthogonal* polynomials, which are linear transformations of the original polynomial terms such that they are mutually uncorrelated. However, they are scaled in such a way that the estimated regression coefficients are also difficult to interpret, apart from the intercept term.
- 25. As function poly() creating orthogonal polynomials does not accepet missing values, we shall only include babies whose value of gestwks is not missing. Let us also perform an F test for the null hypothesis of simple linear effect against the 3rd degree polynomial model

```
> births2 <- subset(births, !is.na(gestwks))
> m.ortpoly <- lm(bweight ~ poly(gestwks, 3), data= births2)
> round(ci.lin(m.ortpoly)[, c(1,5,6)], 1)
> anova(m5, m.ortpoly)
```

Note that the estimated intercept 3138 g has the same value as the mean birth weight among all those babies who are included, i.e. whose gestational age was known.

There seems to be strong evidence against simple linear regression; addition of the quadratic and the cubic term appears to have reduced the residual sum of squares "highly significantly".

26. Irrespective of whether the polynomial terms were orthogonalized or not, the fitted or predicted values for the response variable remain the same. As the next step we shall present graphically the fitted polynomial curve together with 95 % confidence limits for the expected responses as well as 95 % prediction intervals for individual observations in new data comprising gestational weeks from 24 to 45 in steps of 0.25 weeks.

```
> nd <- data.frame(gestwks = seq(24, 45, by = 0.25) )
> fit.poly <- predict( m.ortpoly, newdata=nd, interval="conf" )
> pred.poly <- predict( m.ortpoly, newdata=nd, interval="pred" )
> par(mfrow=c(1,1))
> with( births, plot( bweight ~ gestwks, xlim = c(23, 46), cex.axis= 1.5, cex.lab = > matlines( nd$gestwks, fit.poly, lty=1, lwd=c(3,2,2), col=c('red','blue','blue') )
> matlines( nd$gestwks, pred.poly, lty=1, lwd=c(3,2,2), col=c('red','green','green')
```

The fitted curve fits nicely within the range of observed values of the regressor. However, the tail behaviour in polynomial models tends to be problematic.

We shall continue the analysis in the next practical, in which the apparently curved effect of gestwks is modelled by a *penalized spline*. Also, key details in fitting linear regression models and spline models are covered in the lecture of this afternoon.

#### 1.8.10 Extra (if you have time): Frequency data

Data from very large studies are often summarized in the form of frequency data, which records the frequency of all possible combinations of values of the variables in the study. Such data are sometimes presented in the form of a contingency table, sometimes as a data frame in which one variable is the frequency. As an example, consider the UCBAdmissions data, which is one of the standard R data sets, and refers to the outcome of applications to 6 departments in the graduate school at Berkeley by gender.

27. Let us have a look at the data

#### > UCBAdmissions

You can see that the data are in the form of a  $2 \times 2 \times 6$  contingency table for the three variables Admit (admitted/rejected), Gender (male/female), and Dept (A/B/C/D/E/F). Thus in department A 512 males were admitted while 312 were rejected, and so on. The question of interest is whether there is any bias against admitting female applicants.

28. The next command coerces the contingency table to a data frame, and shows the first 10 lines.

```
> ucb <- as.data.frame(UCBAdmissions)
> head(ucb)
```

The relationship between the contingency table and the data frame should be clear.

29. Let us turn Admit into a numeric variable coded 1 for rejection, 0 for admission

```
> ucb$Admit <- as.numeric(ucb$Admit)-1</pre>
```

The effect of Gender on Admit is crudely estimated by

```
> effx(Admit,type="binary",exposure=Gender,weights=Freq,data=ucb)
```

The odds of rejection for female applicants thus appear to be 1.84 times the odds for males (note the use of weights to take account of the frequencies). A crude analysis therefore suggests there is a strong bias against admitting females.

30. Continue the analysis by stratifying the crude analysis by department - does this still support a bias against females? What is the effect of gender controlled for department?

### 1.9 Estimation and reporting of curved effects

This exercise deals with modelling of curved effects of continuous explanatory variables both on a metric response assuming the Gaussian distribution and on a count or rate outcome based on the Poisson family.

In the first part we continue our analysis on gestational age on birth weight focusing on fitting spline models, both unpenalized and a penalized one.

In the second part we analyse the testisDK data found in the Epi package. It contains the numbers of cases of testis cancer and mid-year populations (person-years) in 1-year age groups in Denmark during 1943–96. In this analysis we apply Poisson regression on the incidence rates treating age and calendar time, first as categorical but then fitting a penalized spline model.

## 1.9.1 Data births: Simple linear regression and 3rd degree polynomial

Recall what was done in items 17 to 24 of the Exercise on simple estimation of effects, in which a simple linear regression and a 3rd degree polynomial were fitted. The main results are also shown on slides 6, 8, 9, and 20 of the lecture on linear models.

1. Make a basic scatter plot and draw the fitted line from a simple linear regression on it.

```
> library(Epi)
> data(births)
> par(mfrow=c(1,1))
> with(births, plot(gestwks, bweight))
> mlin <- lm( bweight ~ gestwks, data = births )
> abline( mlin )
```

2. Repeat also the diagnostic plots of this simple model

```
> par( mfrow=c(2,2) )
> plot( mlin )
```

Some deviation from the linear model is apparent.

### 1.9.2 Fitting a natural cubic spline

A popular approach for flexible modelling is based on natural regression splines, which have more reasonable tail behaviour than polynomial regression.

3. By the following piece of code you can fit a *natural cubic spline* with 5 pre-specified knots to be put at 28, 34, 38, 40 and 43 weeks of gestation, respectively, determining the degree of smoothing.

These regression coefficients are even less interpretable than those in the polynomial model.

4. A graphical presentation of the fitted curve together with the confidence and prediction intervals is more informative:

```
> nd <- data.frame(gestwks = seq(24, 45, by = 0.25) )
> fit.Ns5 <- predict( mNs5, newdata=nd, interval="conf" )
> pred.Ns5 <- predict( mNs5, newdata=nd, interval="pred" )
> par(mfrow=c(1,1))
> with( births, plot(bweight ~ gestwks, xlim=c(23, 46), cex.axis=1.5, cex.lab=1.5 )
> matlines( nd$gestwks, fit.Ns5, lty=1, lwd=c(3,2,2), col=c('red','blue','blue') )
> matlines( nd$gestwks, pred.Ns5, lty=1, lwd=c(3,2,2), col=c('red','green','green') .
```

Compare this with the 3rd order curve previously fitted (see slide 20 of the lecture). In a natural spline the curve is constrained to be linear beyond the extreme knots.

5. Take a look at the basic diagnostic plots from the spline model.

```
> par(mfrow=c(2,2))
> plot(mNs5)
```

How would you interpret these plots?

The choice of the number of knots and their locations can be quite arbitrary, and the results are often sensitive to these choices.

6. To illustrate arbitrariness and associated problems with specification of knots, you may now fit another natural spline model like the one above but now with 10 knots at the following sequence of points: seq(25, 43, by = 2). Display graphically the results The behaviour of the curve is really wild for small values of gestwks!

### 1.9.3 Penalized spline model

One way to go around the arbitrariness in the specification of knots is to fit a *penalized spline* model, which imposes a "roughness penalty" on the curve. Even though a big number of knots are initially allowed, the resulting fitted curve will be optimally smooth.

You cannot fit a penalized spline model with lm() or glm(), Instead, function gam() in package mgcv can be used for this purpose.

- 7. You must first install R package mgcv into your computer.
- 8. When calling gam(), the model formula contains expression 's(X)' for any explanatory variable X, for which you wish to fit a smooth function

```
> library(mgcv)
> mPs <- gam( bweight ~ s(gestwks), data = births)
> summary(mPs)
```

From the output given by summary() you find that the estimated intercept is here, too, equal to the overall mean birth weight in the data. The estimated residual variance is given by "Scale est." or from subobject sig2 of the

fitted gam object. Taking square root you will obtain the estimated residual standard deviation: 445.2 g.

```
> mPs$sig2
> sqrt(mPs$sig2)
```

The degrees of freedom in this model are not computed as simply as in previous models, and they typically are not integer-valued. However, the fitted spline seems to consume only a little more degrees of freedom as the 3rd degree polynomial above.

9. As in previous models we shall plot the fitted curve together with 95 % confidence intervals for the mean responses and 95 % prediction intervals for individual responses. Obtaining these quantities from the fitted gam object requires a bit more work than with 1m objects

The fitted curve is indeed clearly more reasonable than the polynomial.

#### 1.9.4 Testis cancer: Data input and housekeeping

We shall now switch to analyzing the incidence of testis cancer in Denmark during 1943–1998 by age and calendar time or period.

10. Load the data and inspect its structure:

```
> library(Epi )
> data(testisDK)
> str(testisDK)
> summary(testisDK)
> head(testisDK)
```

11. There are nearly 5000 observations from 90 one-year age groups and 54 calendar years. To get a clearer picture of what's going one we do some housekeeping. The age range will be limited to 15–79 years, and age and period are both categorised into 5-year intervals – according to the time-honoured practice in epidemiology.

#### 1.9.5 Some descriptive analysis

Computation and tabulation of incidence rates

12. Tabulate numbers of cases and person-years, and compute the incidence rates (per 100,000 y) in each  $5 \text{ y} \times 5 \text{ y}$  cell using stat.table()

Look at the incidence rates in the column margin and in the row margin. In which age group is the marginal age-specific rate highest? Do the period-specific marginal rates have any trend over time?

13. From the saved table object tab you can plot an age-incidence curve for each period separately, after you have checked the structure of the table, so that you know the relevant dimensions in it.

Is there any common pattern in the age-incidence curves across the periods?

#### 1.9.6 Age and period as categorical factors

We shall first fit a Poisson regression model with log link on age and period model in the traditional way, in which both factors are treated as categorical. The model is additive on the log-rate scale. It is useful to scale the person-years to be expressed in  $10^5$  v.

```
14. > mCat <- glm( D ~ Age + Per, offset=log(Y/100000), family=poisson, data= tdk ) > round( ci.exp( mCat ), 2)
```

What do the estimated rate ratios tell about the age and period effects?

15. A graphical inspection of point estimates and confidence intervals can be obtained as follows. In the beginning it is useful to define shorthands for the pertinent mid-age and mid-period values of the different intervals

```
> plot( c(1943,1998), c(0.6, 6), type='n', log='y', cex.lab = 1.5, cex.axis = 1.5,
    xlab = "Calendar year - 1900", ylab = "Rate ratio")
    lines( pMid,c( 1, ci.exp(mCat)[14:23, 1] ), type = 'o', pch = 16 )
> segments( pMid[-1], ci.exp(mCat)[14:23, 2],
           pMid[-1], ci.exp(mCat)[14:23, 3])
```

16. In the fitted model the reference category for each factor was the first one. As age is the dominating factor, it may be more informative to remove the intercept from the model. As a consequence the age effects describe fitted rates at the reference level of the period factor. For the latter one could choose the middle period 1968-72.

```
> tdk$Per70 <- Relevel(tdk$Per, ref = 6)</pre>
> mCat2 <- glm( D ~ -1 + Age +Per70, offset=log(Y/100000), family=poisson, data= tdk
> round( ci.exp( mCat2 ), 2)
```

We shall plot just the point estimates from the latter model

```
> par(mfrow=c(1,2))
> plot( c(15,80), c(2, 20), type='n', log='y', cex.lab = 1.5, cex.axis = 1.5,
    xlab = "Age (years)", ylab = "Incidence rate (per 100000 y)")
> lines( aMid, c(ci.exp(mCat2)[1:13, 1] ), type = 'o', pch = 16 )
> plot( c(1943,1998), c(0.4, 2), type='n', log='y', cex.lab = 1.5, cex.axis = 1.5,
    xlab = "Calendar year", ylab = "Rate ratio")
> lines( pMid, c(ci.exp(mCat2)[14:18, 1], 1, ci.exp(mCat2)[19:23, 1]),
    type = 'o', pch = 16 )
```

#### Generalized additive model with penalized splines 1.9.7

It is obvious that the age effect on the log-rate scale is highly non-linear, but it is less clear whether the true period effect deviates from linearity. Nevertheless, there are good indications to try fitting smooth continuous functions for both.

17. As the next task we fit a generalized additive model for the log-rate on continuous age and period applying penalized splines with default settings of function gam() in package mgcv. In this fitting an "optimal" value for the penalty parameter is chosen based on an AIC-like criterion known as UBRE.

```
> library(mgcv)
> mPen <- gam( D \sim s(A) + s(P), offset = log(Y/100000),
             family = poisson, data = tdk)
> summary(mPen)
```

The summary is quite brief, and the only estimated coefficient is the intercept, which sets the baseline level for the log-rates, against which the relative age effects and period effects will be contrasted. On the rate scale the baseline level (per 100000 y) is obtained by exp(1.7096)

18. See also the default plot for the fitted curves (solid lines) describing the age and the period effects which are interpreted as contrasts to the baseline level on the log-rate scale.

```
> par(mfrow=c(1,2))
> plot(mPen, seWithMean=TRUE)
> abline(v = 1968, h = 0, lty=3)
```

The dashed lines describe the 95 % confidence band for the pertinent curve. One could get the impression that year 1968 would be some kind of reference value for the period effect, as it was in the categorical model previously fitted. This is not the case, however, because gam() by default parametrizes the spline effects such that the reference level, at which the spline effect is nominally zero, is the overall "grand mean" value of the log-rate in the data. This corresponds to the principle of sum contrasts (contr.sum) for categorical explanatory factors.

From the summary you will also find that the degrees of freedom value required for the age effect is nearly the same as the default dimension k-1=9 of the part of the model matrix (or basis) initially allocated for each smooth function. (Here k refers to the relevant argument that determines the basis dimension when specifying a smooth term by s() in the model formula). On the other hand the period effect takes just about 3 df.

19. It is a good idea to do some diagnostic checking of the fitted model

```
> gam.check(mPen)
```

The four diagnostic plots are analogous to some of those used in the context of linear models for Gaussian responses, but not all of them may be as easy to interpret. – Pay attention to the note given in the printed output about the value of k.

20. Let us refit the model but now with an increased k for age:

```
> mPen2 <- gam( D ~ s(A, k=20) + s(P), offset = log(Y/100000),
+ family = poisson, data = tdk)
> summary(mPen2)
> gam.check(mPen2)
```

With this choice of k the df value for age became about 11, which is well below k-1=19. Let us plot the fitted curves from this fitting, too

```
> par( mfrow=c(1,2) )
> plot( mPen2, seWithMean=TRUE )
> abline( v=1968, h=0, lty=3 )
```

There does not seem to have happened any essential changes from the previously fitted curves, so maybe 8 df could, after all, be quite enough for the age effect.

21. Graphical presentation of the effects can be improved from that supported by plot.gam(). We can, for instance, present the age curve to describe the "mean" incidence rates by age, averaged over the 54 years. For that purpose we need to merge the intercept with the age effect. The period curve will be expressed in terms of rate ratios in relation to the fitted baseline rate, as determined by the model intercept.

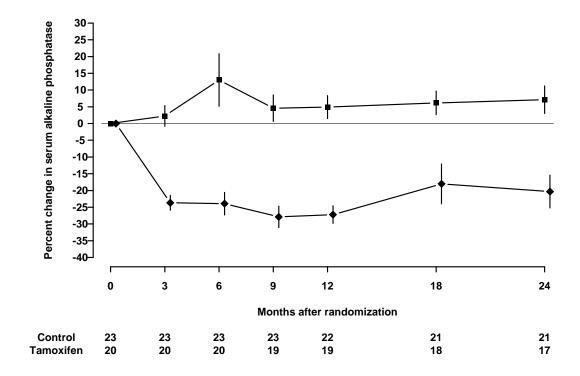
In order to produce these plots one needs to extract certain items from the fitted gam object mPen2 and do some calculations. A source script named "plotPenSplines.R" that does all of that can be found from the /R subdirectory on the course website.

```
> source("http://bendixcarstensen.com/SPE/R/plotPenSplines.R")
```

One could continue the analysis of these data by fitting an age-cohort model as an alternative to the age-period model, as well as an age-cohort-period model.

## 1.10 Graphics meccano

The plot below is from a randomized study of the effect of Tamoxifen treatment on bone mineral metabolism, in a group of patients who were treated for breast cancer.



The data are available in the file alkfos.csv (using comma as separator, so read.csv will read it).

> alkfos <- read.csv("./data/alkfos.csv") # change filename as needed

The purpose of this exercise is to show you how to build a similar graph using base graphics in R. This will take you through a number of fundamental techniques. The exercise will also walk you through creating the graph using ggplot2.

To get started, run the code in the housekeeping script <code>alkfos-house.r</code> . You probably should not study the code in too much detail at this point. The script create the following objects in your workspace.

- times, a vector of length 7 giving the observation times
- means, a 2 × 7 matrix giving the mean percentage change at each time point. Each group has its own row.
- sems, a 2 × 7 matrix giving standard errors of the means, used to create the error bars.
- available, a 2 × 7 matrixing giving the number of participants still available

Use the objects() to see the objects created function to see them.

#### 1.10.1 Base graphics

Now we start building the plot. It is important that you use some form of script to hold the R code since you will frequently have to modify and rerun previously entered code.

- 1. First, plot the means for group 1 (i.e. means[1,]) against times, using type="b" (look up what this does)
- 2. Then *add* a similar curve for group 2 to the plot using points or lines. Notice that the new points are below the y scale of the plot, so you need to revise the initial plot by setting a suitable ylim value.
- 3. Add the error bars using segments. (You can calculate the endpoints using upper <- means + sems etc.). You may have to adjust the ylim again.
- 4. Add the horizontal line at y = 0 using abline
- 5. Use xlab and ylab in the initial plot call to give better axis labels.
- 6. We need a nonstandard x axis. Use xaxt="n" to avoid plotting it at first, then add a custom axis with axis
- 7. The counts below the x axis can be added using mtext on lines 5 and 6 below the bottom of the plot, but you need to make room for the extra lines. Use par(mar=.1 + c(8,4,4,2)) before plotting anything to achieve this.

You now have quite a good reconstruction of the original plot. There are some additional steps you can take to reproduce the published plot exactly. These are advanced exercises so feel free to come back to them later.

- 8. It is not too important here (it was for some other variables in the study), but the S-PLUS plot has the points for the second group offset horizontally by a small amount (.25) to prevent overlap. Redo the plot with this modification.
- 9. Further things to fiddle with: Get rid of the bounding box. Add Control/Tamoxifen labels to the lines of counts. Perhaps use different plotting symbols. Rotate the y axis values. Modify the line widths or line styles.
- 10. Finally, try plotting to the pdf() device and view the results using a PDF viewer (e.g. Adobe Acrobat Reader). You may need to change the pointsize option and/or the plot dimensions for optimal appearance. You might also try saving the plot as a metafile and include it in a Word document.

### 1.10.2 Using ggplot2

The housekeeping script alkfos-house.r also creates a data frame ggdata containing the variables in long format. The code for generating the data frame is shown below, but you do not need to repeat it if you have run the script.

```
> ggdata <- data.frame(
+    times = rep(times, 2),
+    means = c(means[1,], means[2,]),
+    sds = c(sds[1,], sds[2,]),
+    available = c(available[1,], available[2,]),
+    treat = rep(c("placebo","tamoxifen"), each=7)
+    )
> ggdata <- transform(ggdata, sems = sds/sqrt(available))</pre>
```

To create a first approximation to the plot in ggplot2 we use the qplot function (short for "quick plot"). First you must install the ggplot2 package from CRAN and then load it:

```
> library(ggplot2)
> qplot(x=times, y=means, group=treat, geom=c("point", "line") , data=ggdata)
```

The first arguments to qplot are called "aesthetics" in the grammar of graphics. Here we want to plot y=means by x=times grouped by group=treat. The aesthetics are used by the "geometries", which are specified with the geom argument. Here we want to plot both points and lines. The data argument tells qplot to get the aesthetics from the data frame ggdata.

To add the error bars, we add a new geometry "linerange" which uses the aesthetics ymin and ymax

In this case we are saving the output of qplot to an R object p. This means the plot will not appear automatically when we call qplot. Instead, we must explicitly print it.

Note how the y axes are automatically adjusted to include the error bars. This is because they are included in the call to qplot and not added later (as was the case with base graphics).

It remains to give informative axis labels and put the right tick marks on the x-axis. This is done by adding scales to the plot

We can also change the look and feel of the plot by adding a theme (in this case the black and white theme).

```
> p + theme_bw()
```

As an alternative to qplot, we can use the ggplot function to define the data and the common aesthetics, then add the geometries with separate function calls. All the grobs (graphical objects) created by these function calls are combined with the + operator:

```
> p <- ggplot(data=ggdata,</pre>
              aes(x=times, y=means, ymin=means-sems, ymax=means+sems, group=treat)) +
      geom_point() +
+
      geom_line() +
      geom_linerange() +
      geom_hline(yintercept=0, colour="darkgrey") +
      scale_x_continuous(breaks=times[1:7])
```

This call adds another geometry "hline" which uses the aesthetic yintercept to add a horizontal line at 0 on the y-axis. Note that this alternate syntax allows each geometry to have its own aesthetics: here we draw the horizontal line in darkgrey instead of the default black.

#### 1.10.3 Grid graphics

As a final, advanced topic, this subsection shows how viewports from the grid package may be used to display the plot and the table in the same graph. First we create a text table:

```
> tab <- ggplot(data=ggdata, aes(x=times, y=treat, label=available)) +
      geom_text(size=3) + xlab(NULL) + ylab(NULL) +
      scale_x_continuous(breaks=NULL)
> tab
```

Then we create a layout that will contain the graph above the table. Most of the space is taken by the graph. The grid.show.layout allows you to preview the layout.

```
> library(grid)
> Layout <- grid.layout(nrow = 2, ncol = 1, heights = unit(c(2, 0.25),
                                            c("null", "null")))
> grid.show.layout(Layout)
```

The units are relative ("null") units. You can specify exact sizes in centimetres, inches, or lines if you prefer.

We then print the graph and the table in the appropriate viewports

```
> grid.newpage() #Clear the page
> pushViewport(viewport(layout=Layout))
> print(p, vp=viewport(layout.pos.row=1, layout.pos.col=1))
> print(tab, vp=viewport(layout.pos.row=2, layout.pos.col=1))
```

Notice that the left margins do not match. One way to get the margins to match is to use the plot\_grid function from the cowplot package.

```
> library(cowplot)
> plot_grid(p, tab, align="v", ncol=1, nrow=2, rel_heights=c(5,1))
```

#### Survival analysis: Oral cancer patients 1.11

#### 1.11.1Description of the data

File oralca2.txt, that you may access from a url address to be given in the practical, contains data from 338 patients having an oral squamous cell carcinoma diagnosed and treated in one tertiary level oncological clinic in Finland since 1985, followed-up for mortality until 31 December 2008. The dataset contains the following variables:

```
sex, a factor with categories 1 = "Female", 2 = "Male",
sex
            age (years) at the date of diagnosing the cancer,
age
            TNM stage of the tumour (factor): 1 = "I", ..., 4 = "IV", 5 = "unkn",
stage
time
        = follow-up time (in years) since diagnosis until death or censoring,
            event ending the follow-up (numeric):
event
            0 = \text{censoring alive}, 1 = \text{death from oral cancer}, 2 = \text{death from other causes}.
```

#### 1.11.2Loading the packages and the data

11. Load the R packages Epi, mstate, and survival needed in this exercise.

```
> library(Epi)
> library(popEpi)
> library(data.table)
> library(knitr)
> library(survival)
```

12. Read the datafile oralca2.txt from a website, whose precise address will be given in the practical, into an R data frame named orca. Look at the head, structure and the summary of the data frame. Using function table() count the numbers of censorings as well as deaths from oral cancer and other causes, respectively, from the event variable.

```
> orca <- read.table("oralca2.txt", header=T)</pre>
> head(orca) ; str(orca) ; summary(orca)
```

#### 1.11.3 Total mortality: Kaplan–Meier analyses

1. We start our analysis of total mortality pooling the two causes of death into a single outcome. First, construct a survival object orca\$suob from the event variable and the follow-up time using function Surv(). Look at the structure and summary of orca\$suob.

```
> orca$suob <- Surv(orca$time, 1*(orca$event > 0) )
> str(orca$suob)
> summary(orca$suob)
```

2. Create a survfit object s.all, which does the default calculations for a Kaplan–Meier analysis of the overall (marginal) survival curve.

```
> s.all <- survfit(suob ~ 1, data=orca)
```

See the structure of this object and apply print() method on it, too. Look at the results; what do you find?

```
> s.all
> str(s.all)
```

3. The summary method for a survfit object would return a lengthy life table. However, the plot method with default arguments offers the Kaplan-Meier curve for a conventional illustration of the survival experience in the whole patient group. Alternatively, instead of graphing survival proportions, one can draw a curve describing their complements: the cumulative mortality proportions. This curve is drawn together with the survival curve as the result of the second command line below.

```
> plot(s.all)
> lines(s.all, fun = "event", mark.time=F, conf.int=F)
```

The effect of option mark.time=F is to omit marking the times when censorings occurred.

#### 1.11.4 Total mortality by stage

Tumour stage is an important prognostic factor in cancer survival studies.

1. Plot separate cumulative mortality curves for the different stage groups marking them with different colours, the order which you may define yourself. Also find the median survival time for each stage.

```
> s.stg <- survfit(suob ~ stage, data= orca)
> col5 <- c("green", "blue", "black", "red", "gray")
> plot(s.stg, col= col5, fun="event", mark.time=F)
> s.stg
```

2. Create now two parallel plots of which the first one describes the cumulative hazards and the second one graphs the log-cumulative hazards against log-time for the different stages. Compare the two presentations with each other and with the one in the previous item.

```
> par(mfrow=c(1,2))
> plot(s.stg, col= col5, fun="cumhaz", main="cum. hazards")
> plot(s.stg, col= col5, fun="cloglog", main = "cloglog: log cum.haz")
```

- 3. If the survival times were *exponentially* distributed in a given (sub)population the corresponding cloglog-curve should follow an approximately linear pattern. Could this be the case here in the different stages?
- 4. Also, if the survival distributions of the different subpopulations would obey the *proportional hazards* model, the vertical distance between the cloglog-curves should be approximately constant over the time axis. Do these curves indicate serious deviation from the proportional hazards assumption?
- 5. In the lecture handouts (p. 34, 37) it was observed that the crude contrast between males and females in total mortality appears unclear, but the age-adjustment in the Cox model provided a more expected hazard ratio

estimate. We shall examine the confounding by age somewhat closer. First categorize the continuous age variable into, say, three categories by function cut() using suitable breakpoints, like 55 and 75 years, and cross-tabulate sex and age group:

```
> orca$agegr <- cut(orca$age, br=c(0,55,75, 95))
> stat.table( list( sex, agegr), list( count(), percent(agegr) ),
+ margins=T, data = orca )
```

Male patients are clearly younger than females in these data.

Now, plot Kaplan–Meier curves jointly classified by sex and age.

In each ageband the mortality curve for males is on a higher level than that for females.

#### 1.11.5 Event-specific cumulative mortality curves

We move on to analysing cumulative mortalities for the two causes of death separately, first overall and then by prognostic factors.

1. Use the survfit-function in survival package with option type="mstate".

2. One could apply here the plot method of the survfit object to plot the cumulative incidences for each cause. However, we suggest that you use instead a simple function plotCIF() found in the Epi package. The main arguments are

```
data = data frame created by function survfit(), (1.1)
```

$$event = indicator for the event: values 1 or 2.$$
 (1.2)

Other arguments are like in the ordinary plot() function.

3. Draw two parallel plots describing the overall cumulative incidence curves for both causes of death

```
> par(mfrow=c(1,2))
> plotCIF(cif1, 1, main = "Cancer death")
> plotCIF(cif1, 2, main= "Other deaths")
```

4. Compute the estimated cumulative incidences by stage for both causes of death. Now you have to add variable stage to survfit-function.

See the structure of the resulting object, in which you should observe strata variable containing the stage grouping variable. Plot the pertinent curves in two parallel graphs. Cut the y-axis for a more efficient graphical presentation

Compare the two plots. What would you conclude about the effect of stage on the two causes of death?

5. Using another function stackedCIF() in Epi you can put the two cumulative incidence curves in one graph but stacked upon one another such that the lower curve is for the cancer deaths and the upper curve is for total mortality, and the vertical difference between the two curves describes the cumulative mortality from other causes. You can also add some colours for the different zones:

```
> par(mfrow=c(1,1))
> stackedCIF(cif1, colour = c("gray70", "gray85"))
```

#### 1.11.6 Regression modelling of overall mortality.

1. Fit the semiparametric proportional hazards regression model, a.k.a. the Cox model, on all deaths including sex, age and stage as covariates. Use function coxph() in package survival. It is often useful to center and scale continuous covariates like age here. The estimated rate ratios and their confidence intervals can also here be displayed by applying ci.lin() on the fitted model object.

```
> options(show.signif.stars = F)
> m1 <- coxph(suob ~ sex + I((age-65)/10) + stage, data= orca)
> summary( m1 )
> round( ci.exp(m1 ), 4 )
```

Look at the results. What are the main findings?

2. Check whether the data are sufficiently consistent with the assumption of proportional hazards with respect to each of the variables separately as well as globally, using the cox.zph() function.

```
> cox.zph(m1)
```

3. No evidence against proportionality assumption could apparently be found. Moreover, no difference can be observed between stages I and II in the estimates. On the other hand, the group with stage unknown is a complex mixture of patients from various true stages. Therefore, it may be prudent to exclude these subjects from the data and to pool the first two stage groups into one. After that fit a model in the reduced data with the new stage variable.

```
> orca2 <- subset(orca, stage != "unkn")
> orca2$st3 <- Relevel( orca2$stage, list(1:2, 3, 4:5) )
> levels(orca2$st3) = c("I-II", "III", "IV")
> m2 <- update(m1, . ~ . - stage + st3, data=orca2 )
> round( ci.exp(m2 ), 4)
```

4. Plot the predicted cumulative mortality curves by stage, jointly stratified by sex and age, focusing only on 40 and 80 year old patients, respectively, based on the fitted model m2. You need to create a new artificial data frame containing the desired values for the covariates.

## 1.11.7 Modelling event-specific hazards and hazards of the subdistribution

1. Fit the Cox model for the cause-specific hazard of cancer deaths with the same covariates as above. In this case only cancer deaths are counted as events and deaths from other causes are included into censorings.

```
> m2haz1 <- coxph(Surv(time, event==1) ~ sex + I((age-65)/10) + st3 , data=orca2 , > round(ci.exp(m2haz1), 4) > cox.zph(m2haz1)
```

Compare the results with those of model m2. What are the major differences?

2. Fit a similar model for deaths from other causes and compare the results.

```
> m2haz2 <- coxph(Surv(time, event==2) ~ sex + I((age-65)/10) + st3 , data=orca2 , > round(ci.exp(m2haz2), 4) > cox.zph(m2haz2)
```

3. Finally, fit the Fine-Gray model for the hazard of the subdistribution for cancer deaths with the same covariates as above. For this you have to first load package cmprsk, containing the necessary function crr(), and attach the data frame.

```
> library(cmprsk)
> attach(orca2)
> m2fg1 <- crr(time, event, cov1 = model.matrix(m2), failcode=1)
> summary(m2fg1, Exp=T)
```

Compare the results with those of model m2 and m2haz1.

4. Fit a similar model for deaths from other causes and compare the results.

```
> m2fg2 <- crr(time, event, cov1 = model.matrix(m2), failcode=2)
> summary(m2fg2, Exp=T)
```

#### 1.11.8 Analysis of relative survival

1. Load package popEpi for the estimation of relative survival. Use the (simulated) female Finnish breast cancer patients diagnosed between 1993-2012, called sibr.

```
> library(popEpi)
> head(sibr)
```

2. Prepare the data by using lexpand command in the popEpi package, define follow-up time intervals, (calendar time) period that you are interested and where are the population mortality figures. Calculate 5-year observed survival (2008-2012) using period method by Ederer II (default)

```
> ## pretend some are male
> set.seed(1L)
> sire$sex <- rbinom(nrow(sire), 1, 0.01)
> BL <- list(fot = seq(0, 5, 1/12))
> x <- lexpand(sire,
+ birth = bi_date,
+ entry = dg_date,
+ exit = ex_date,
+ status = status,
+ breaks = BL,
+ pophaz = popmort,
+ aggre = list(sex, fot))</pre>
```

3. Calculate 5-year relative survival (2008-2012) using period method by Ederer II (default)

#### 1.11.9 Lexis object with multi-state set-up

Before entering to analyses of cause-specific mortality it might be instructive to apply some Lexis tools to illustrate the competing-risks set-up. More detailed explanation of these tools will be given by Bendix in this afternoon.

1. Form a Lexis object from the data frame and print a summary of it. We shall name the main (and only) time axis in this object as stime.

2. Draw a box diagram of the two-state set-up of competing transitions. Run first the following command line

```
boxes( orca.lex )
```

Now, move the cursor to the point in the graphics window, at which you wish to put the box for "Alive", and click. Next, move the cursor to the point at which you wish to have the box for "Oral ca. death", and click. Finally, do the same with the box for "Other death". If you are not happy with the outcome, run the command line again and repeat the necessary mouse moves and clicks.

#### 1.11.10 Poisson regression as an alternative to Cox model

It can be shown that the Cox model with an unspecified form for the baseline hazard  $\lambda_0(t)$  is mathematically equivalent to the following kind of Poisson regression model. Time is treated as a categorical factor with a dense division of the time axis into disjoint intervals or timebands such that only one outcome event occurs in each timeband. The model formula contains this time factor plus the desired explanatory terms.

A sufficient division of time axis is obtained by first setting the break points between adjacent timebands to be those time points at which an outcome event has been observed to occur. Then, the pertinent lexis object is created and after that it will be split according to those breakpoints. Finally, the Poisson regression model is fitted on the splitted lexis object using function glm() with appropriate specifications.

We shall now demonstrate the numerical equivalence of the Cox model m2haz1 for oral cancer mortality that was fitted above, and the corresponding Poisson regression.

1. First we form the necessary lexis object by just taking the relevant subset of the already available orca.lex object. Upon that the three-level stage factor st3 is created as above.

```
> orca2.lex <- subset(orca.lex, stage != "unkn" )
> orca2.lex$st3 <- Relevel( orca2$stage, list(1:2, 3, 4:5) )
> levels(orca2.lex$st3) = c("I-II", "III", "IV")
```

Then, the break points of time axis are taken from the sorted event times, and the lexis object is split by those breakpoints. The timeband factor is defined according to the splitted survival times stored in variable stime.

```
> cuts <- sort(orca2$time[orca2$event==1])
> orca2.spl <- splitLexis( orca2.lex, br = cuts, time.scale="stime" )
> orca2.spl$timeband <- as.factor(orca2.spl$stime)</pre>
```

As a result we now have an expanded lexis object in which each subject has several rows; as many rows as there are such timebands during which he/she is still at risk. The outcome status lex.Xst has value 0 in all those timebands, over which the subject stays alive, but assumes the value 1 or 2 at his/her last interval ending at the time of death. – See now the structure of the splitted object.

```
> str(orca2.spl)
> orca2.spl[ 1:20, ]
```

2. We are ready to fit the desired Poisson model for oral cancer death as the outcome. The splitted person-years are contained in lex.dur, and the explanatory variables are the same as in model m2haz1. – This fitting may take some time . . .

```
> m2pois1 <- glm( 1*(lex.Xst=="Oral ca. death") ~
+     -1 + timeband + sex + I((age-65)/10) + st3,
+     family=poisson, offset = log(lex.dur), data = orca2.spl)</pre>
```

We shall display the estimation results graphically for the baseline hazard (per 1000 person-years) and numerically for the rate ratios associated with the covariates. Before doing that it is useful to count the length ntb of the block occupied by baseline hazard in the whole vector of estimated parameters. However, owing to how the splitting to timebands was done, the last regression coefficient is necessarily zero and better be omitted when displaying the results. Also, as each timeband is quantitatively named according to its leftmost point, it is good to compute the midpoint values tbmid for the timebands

Compare the regression coefficients and their error margins to those model m2haz1. Do you find any differences? How does the estimated baseline hazard look like?

3. The estimated baseline looks quite ragged when based on 71 separate parameters. A smoothed estimate may be obtained by spline modelling using the tools contained in package splines (see the practical of Saturday 25 May afternoon). With the following code you will be able to fit a reasonable spline model for the baseline hazard and draw the estimated curve (together with a band of the 95% confidence limits about the fitted values). From the same model you should also obtain quite familiar results for the rate ratios of interest.

#### 1.12 Time-splitting, time-scales and SMR

This exercise is about mortaity among Danish Diabetes patients. It is based on the dataset DMlate, a random sample of 10,000 patients from the Danish Diabetes Register (scrambeled dates), all with date of diagnosis after 1994.

1. First load the data and take a look at the data:

```
library( Epi )
library( mgcv )
library( splines )
sessionInfo()
data( DMlate )
str( DMlate )
```

You can get a more detailed explanation of the data by referring to the help page:

```
?DMlate
```

2. Set up the dataset as a Lexis object with age, calendar time and duration of diabetes as timescales, and date of death as event. Make sure that you know what each of the arguments to Lexis mean:

Take a look at the first few lines of the resulting dataset using head().

- 3. Get an overall overview of the mortality by using stat.table to tabulate no. deaths, person-years and the crude mortality rate by sex.
- 4. If we want to assess how mortality depends on age, calendar time and duration or how it relates to population mortality, we should in principle split the follow-up along all three time scales. In practice it is sufficient to split it along one of the time-scales and then use the value of each of the time-scales at the left endpoint of the intervals. Use splitLexis (or splitMulti from the popEpi package) to split the follow-up along the age-axis in sutiable intervals (here set to 1/2 year, but really immaterial as long as it is small):

```
SL \leftarrow splitLexis(LL, breaks=seq(0,125,1/2), time.scale="A") summary(SL)
```

How many records are now in the dataset? How many person-years? Compare to the original Lexis-dataset.

#### SMR

The SMR is the Standardized Mortality Ratio, which is the mortality rate-ratio between the diabetes patients and the general population. In real studies we

74

would subtract the deaths and the person-years among the diabetes patients from those of the general population, but since we do not have access to these, we make the comparison to the general population at large, *i.e.* also including the diabetes patients. We now want to include the population mortality rates as a fixed variable in the split dataset; for each record in the split dataset we attach the value of the population mortality for the relevant sex, and and calendar time. This can be achieved in two ways: Either we just use the current split of follow-up time and allocate the population mortality rates for some suitably chosen (mid-)point of the follow-up in each, or we make a second split by date, so that follow-up in the diabetes patients is in the same classification of age and data as the population mortality table.

5. We will use the former approach, using the dataset split in 6 month intervals, and then include as an extra variable the population mortality as available from the data set M.dk. First create the variables in the diabetes dataset that we need for matching with the population mortality data, that is age, date and sex at the midpoint of each of the intervals (or rater at a point 3 months after the left endpoint of the interval — recall we split the follow-up in 6 month intervals). We need to have variables of the same type when we merge, so we must transform the sex variable in M.dk to a factor, and must for each follow-up interval in the SL data have an age and a period variable that can be used in merging with the population data.

Then match the rates from M.dk into SL — sex, Am and Pm are the common variables, and therefore the match is on these variables:

```
SLr <- merge( SL, M.dk[,c("sex","Am","Pm","rate")] )
dim( SL )
dim( SLr )</pre>
```

This merge (remember to ?merge!) only takes rows that have information from both datasets, hence the slightly fewer rows in SLr than in SL.

- 6. Compute the expected number of deaths as the person-time multiplied by the corresponding population rate, and put it in a new variable, E, say (Expected). Use stat.table to make a table of observed, expected and the ratio (SMR) by age (suitably grouped) and sex.
- 7. Fit a poisson model with sex as the explanatory variable and log-expected as offset to derive the SMR (and c.i.). Some of the population mortality rates are 0, so you need to exclude those records from the analysis.

```
data = subset(SLr,E>0) )
ci.exp( msmr )
```

Recogninse the numbers?

#### Age-specific mortality

8. Now estimate age-specific mortality curves for men and women separately, using splines as implemented in gam. We use k=20 to be sure to catch any irregularities by age.

Make sure you understand all the components on this modeling statement.

9. Now, extract the estimated rates by using the wrapper function ci.pred that computes predicted rates and confidence limits for these. Note that lex.dur is a covariate in the context of prediction; by putting this to 1000 in the prediction dataset we get the rates in units of deaths per 1000 PY:

10. Plot the predicted rates for men and women together - using for example matplot.

```
p.f \leftarrow ci.pred(r.f, newdata = nd)
matplot(nd\$A, cbind(p.m,p.f),
type="l", col=rep(c("blue","red"),each=3), lwd=c(3,1,1), lty=1,
log="y", xlab="Age", ylab="Mortality of DM ptt per 1000 PY")
```

#### Period and duration effects

11. We now want to model the mortality rates among diabetes patients also including current date and duration of diabetes, using penalized splines. Use the argument bs="cr" to s() to get cubic splines indstead of thin plate ("tp") splines which is ithe default, and check if you have a reasonable fit:

Fit the same model for women as well. Are the models reasinable fitting?

12. Plot the estimated effects, using the default plot method for gam objects. Remember that there are three effects estimated, so it is useful set up a multi-panel display, and for the sake of comparability to set ylim to the same for men and women:

```
par( mfrow=c(2,3) )
plot( Mcr, ylim=c(-3,3) )
plot( Fcr, ylim=c(-3,3) )
```

13. Compare the fit of the naive model with just age and the three-factor models, using anova, e.g.:

```
anova( Mcr, r.m, test="Chisq" )
```

14. The model we fitted has three time-scales: current age, current date and current duration of diabetes, so the effects that we report are not immediately interpretable, as they are (as in any kind of multiple regressions) to be interpreted as "all else equal" which they are not, as the three time scales advance simultaneously at the same pace. The reporting would therefore more naturally be *only* on the mortality scale as a function of age, but showing the mortality for persons diagnosed in different ages, using separate displays for separate years of diagnosis. This is most easily done using the ci.pred function with the newdata= argument. So a person diagnosed in age 50 in 1995 will have a mortality measured in cases per 1000 PY as:

Note however, that if you have used the offset=) argument in the mdel specification rather than the + offset() in the model fromula, the offset specification in nd will be ignored, and prediction be made for the scale chosen in the model specification. Now take a look at the result from the ci.pred statement and construct prediction of mortality for men and women diagnosed in a range of ages, say 50, 60, 70, and plot these together in the same graph:

```
cbind( nd, ci.pred( Mcr, newdata=nd ) )
```

15. From figure 2.3 it seems that the duration effect is dramatically over-modeled, so we refit constraining the d.f. to 5:

What do you conclude from the plots?

#### 1.12.1 SMR modeling

- 16. Now model the SMR using age and date of diagnosis and diabetes duration as explanatory variables, including the log-expected-number instead of the log-person-years as offset, using separate models for men and women. You can re-use the code you used for fitting models for the rates, you only need to use the expedtd numbers instead of the person-years. But remember to exclude those units where no deaths in the population occur (that is where the rate is 0) an offset of −∞ will crash gam. Plot the estimated smooth effects from both models using e.g. plot.gam. What do you see?
- 17. Plot the predicted SMRs from the models for men and women diagnosed in ages 50, 60 and 70 as you dif for the rates. What do you see?
- 18. Try to simplify the model to one with a simple sex effect, linear effects of age and date of follow-up, and a smooth effect of duration, giving an estimate of the change in SMR by age and calendar time. How much does SMR change by each year of age? And by each calendar year?
- 19. Use your previous code to plot the predicted mortality from this model too. Are the predicted SMR curves credible?
- 20. (optional) We may deem the curves non-credible and ultimately resort to a brutal parametric assumption without any penalty. If we choose a natural spline for the duration with knost at 0,1,3,6 years we get a model with 3 parameters, try:

```
dim(Ns(SLr\$dur, knots=c(0,1,3,6)))
```

Now fit the same model (also ignoring sex) as above using this:

```
SMRglm \leftarrow glm((lex.Xst=="Dead") \sim I(A-60) + I(P-2000) + Ns(dur, knots=c(0,1,4,8)) + offset(log(E)), family = poisson, \\ data = SLr)
```

Plot the estimated SMRs from this model as before, and give a conclusion on SMR for diabetes patients.

78 1.13 Causal inference SPE: Exercises

#### 1.13 Causal inference

## 1.13.1 Proper adjustment for confounding in regression models

The first exercise of this session will ask you to simulate some data according to pre-specified causal structure (don't take the particular example too seriously) and see how you should adjust the analysis to obtain correct estimates of the causal effects.

Suppose one is interested in the effect of beer-drinking on body weight. Let's assume that in addition to the potential effect of beer on weight, the following is true in reality:

- Men drink more beer than women
- Men have higher body weight than women
- People with higher body weight tend to have higher blood pressure
- Beer-drinking increases blood pressure

The task is to simulate a dataset in accordance with this model, and subsequently analyse it to see, whether the results would allow us to conclude the true association structure.

- 1. Sketch a causal graph (not necessarily with R) to see, how should one generate the data
- 2. Suppose the actual effect sizes are following:
  - The probability of beer-drinking is 0.2 for females and 0.7 for males
  - Men weigh on average 10kq more than women
  - One kg difference in body weight corresponds in average to 0.5mmHg difference in (systolic) blood pressures
  - Beer-drinking increases blood pressure by 10mmHg in average.
  - Beer-drinking has **no** effect on body weight

The R commands to generate the data are:

- 3. Now fit the following models for body weight as dependent variable and beer-drinking as independent variable. Look, what is the estimated effect size:
  - (a) Unadjusted (just simple linear regression)
  - (b) Adjusted for sex
  - (c) Adjusted for sex and blood pressure

IARC, 2018 1.13 Causal inference **79** 

4. What would be the conclusions on the effect of beer on weight, based on the three models? Do they agree? Which (if any) of the models gives an unbiased estimate of the actual causal effect of interest?

- 5. How can the answer be seen from the graph?
- 6. Now change the data-generation algorithm so, that in fact beer-drinking does increase the body weight by 2kg. Look, what are the conclusions in the above models now. Thus the data is generated as before, but the weight variable is computed as:

```
> bdat$weight <- 60 + 10*bdat$sex + 2*bdat$beer + rnorm(1000,0,7)
```

7. Suppose one is interested in the effect of beer-drinking on blood pressure instead, and is fitting a) an unadjusted model for blood pressure, with beer as an only covariate; b) a model with beer, weight and sex as covariates. Would either a) or b) give an unbiased estimate for the effect? (You may double-check whether the simulated data is consistent with your answer).

# 1.13.2 Instrumental variables estimation, Mendelian randomization and assumptions

In the lecture slides it was shown that in a model for blood glucose level (associated with the risk of diabetes), both BMI and FTO genotype were significant. Seeing such result in a real dataset may misleadingly be interpreted as an evidence of a direct effect of FTO genotype on glucose. Conduct a simulation study to verify that one may see a significant genotype effect on outcome in such model if in fact the assumptions for Instrumental Variables estimation (Mendelian Randomization) are valid – genotype has a direct effect on the exposure only, whereas exposure-outcome association is confounded.

1. Start by generating the genotype variable as Binomial(2,p), with p=0.2:

```
> n <- 10000
> mrdat <- data.frame(G = rbinom(n,2,0.2))
> table(mrdat$G)
```

2. Also generate the confounder variable U

```
> mrdat$U <- rnorm(n)</pre>
```

3. Generate a continuous (normally distributed) exposure variable BMI so that it depends on G and U. Check with linear regression, whether there is enough power to get significant parameter estimates. For instance:

```
> mrdat\$BMI \leftarrow with(mrdat, 25 + 0.7*G + 2*U + rnorm(n))
```

4. Finally generate Y ("Blood glucose level") so that it depends on BMI and U (but not on G).

```
> mrdat\$Y \leftarrow with(mrdat, 3 + 0.1*BMI - 1.5*U + rnorm(n,0,0.5))
```

80 1.13 Causal inference SPE: Exercises

5. Verify, that simple regression model for Y, with BMI as a covariate, results in a biased estimate of the causal effect (parameter estimate is different from what was generated) How different is the estimate from 0.1?

- 6. Estimate a regression model for Y with two covariates, G and BMI. Do you see a significant effect of G? Could you explain analytically, why one may see a significant parameter estimate for G there?
- 7. Find an IV (instrumental variables) estimate, using G as an instrument, by following the algorithm in the lecture notes (use two linear models and find a ratio of the parameter estimates). Does the estimate get closer to the generated effect size?

```
> mgx<-lm(BMI ~ G, data=mrdat)
> ci.lin(mgx) # check the instrument effect
> bgx<-mgx$coef[2] # save the 2nd coefficient (coef of G)
> mgy<-lm(Y ~ G, data=mrdat)
> ci.lin(mgy)
> bgy<-mgy$coef[2]
> causeff <- bgy/bgx
> causeff # closer to 0.1?
```

8. A proper simulation study would require the analysis to be run several times, to see the extent of variability in the parameter estimates. A simple way to do it here would be using a for-loop. Modify the code as follows (exactly the same commands as executed so far, adding a few lines of code to the beginning and to the end):

```
> n <- 10000
> # initializing simulations:
> # 30 simulations (change it, if you want more):
> nsim<-30
                    # empty vector for the outcome parameters
> mr<-rep(NA,nsim)</pre>
> for (i in 1:nsim) { # start the loop
+ ### Exactly the same commands as before:
+ mrdat <- data.frame(G = rbinom(n, 2, 0.2))
+ mrdat$U <- rnorm(n)
+ mrdat\$BMI \leftarrow with(mrdat, 25 + 0.7*G + 2*U + rnorm(n))
+ mrdat$Y <- with(mrdat, 3 + 0.1*BMI - 1.5*U + rnorm(n,0,0.5) )
+ mgx<-lm(BMI ~ G, data=mrdat)
+ bgx<-mgx$coef[2]
+ mgy<-lm(Y ~ G, data=mrdat)
+ bgy<-mgy$coef[2]
+ # Save the i'th parameter estimate:
+ mr[i]<-bgy/bgx
      # end the loop
```

Now look at the distribution of the parameter estimate:

```
> summary(mr)
```

9. (optional) Change the code of simulations so that the assumptions are violated: add a weak direct effect of the genotype G to the equation that generates Y:

```
> mrdat\$Y \leftarrow with(mrdat, 3 + 0.1*BMI - 1.5*U + 0.05*G + rnorm(n,0,0.5))
```

Repeat the simulation study to see, what is the bias in the average estimated causal effect of BMI on Y.

IARC, 2018 1.13 Causal inference 81

10. (optional) Using library sem and function tsls, obtain a two-stage least squares estimate for the causal effect. Do you get the same estimate as before?

```
> library(sem)
> summary(tsls(Y ~ BMI, ~G, data=mrdat))
```

#### Why are simulation exercises useful for causal inference?

If we simulate the data, we know the data-generating mechanism and the "true" causal effects. So this is a way to check, whether an analysis approach will lead to estimates that correspond to what is generated. One could expect to see similar phenomena in real data analysis, if the data-generation mechanism is similar to what was used in simulations.

# 1.14 Nested case-control study and case-cohort study:

#### Risk factors of coronary heart disease

In this exercise we shall apply both the nested case-control (NCC) design and the case-cohort (CC) design in sampling control subjects from a defined cohort or closed study population. The case group comprises those cohort members who die from coronary heart disease (CHD) during a > 20 years follow-up of the cohort. The risk factors of interest are cigarette smoking, systolic blood pressure, and total cholesterol level.

Our study population is an occupational cohort comprising 1501 men working in blue-collar jobs in one Nordic country. Eligible subjects had no history of coronary heart disease when recruited to the study in the early 1990s. Smoking habits and many other items were inquired at baseline by a questionnaire, and blood pressure was measured by a research nurse, the values being written down on the questionnaire. Serum samples were also taken from the cohort members at the same time and were stored in a freezer. For some reason, the data in the questionnaires were not entered to any computer file, but the questionnaires were kept in a safe storehouse for further purposes. Also, no biochemical analyses were initially performed for the sera collected from the participants. However, dates of birth and dates of entry to the study were recorded in an electronic file.

In 2010 the study was suddenly reactivated by those investigators of the original team who were still alive then. As the first step mortality follow-up of the cohort members was executed by record linkage to the national population register, from which the dates of death and emigration were obtained. Another linkage was performed with the national register of causes of death in order to get the deaths from coronary heard disease identified. As a result a data file occoh.txt was completed containing the following variables:

id = identification number,
birth = date of birth,
entry = date of recruitment and baseline measurements,
exit = date of exit from mortality follow-up,
death = indicator for vital status at the end of follow-up,
= 1, if dead from any cause, and = 0, if alive,
chdeath = indicator for death from coronary heart disease,
= 1, if "yes", and 0, if "no".

This exercise is divided into five main parts:

- (1) Description of the study base or the follow-up experience of the whole cohort, identification of the cases and illustrating the risk sets.
- (2) Nested case-control study within the cohort: (i) selection of controls by risk set or time-matched sampling using function ccwc() in package Epi, (ii) collection of exposure data for cases and controls from the pertinent data

- base of the whole cohort to the case-control data set using function merge(), and (iii) analysis of case-control data using function clogit() in package survival(),
- (3) Case-cohort study within the cohort: (i) selection of a subcohort by simple random sampling from the cohort, (ii) fitting the Cox model to the data by weighted partial likelihood using function coxph() in package survival() with appropriate weighting and correction of estimated covariance matrix for the model coefficients; also using function cch() in package survival() for the same task.
- (4) Comparison of results from all previous analyses, also with those from a full cohort design.
- (5) Further tasks and homework.

#### Reading the cohort data, illustrating the study base 1.14.1and risk sets

11. Load the packages Epi and survival. Read in the cohort data file and name the resulting data frame as oc. See its structure and print the univariate summaries.

```
> library(Epi)
> library(survival)
> url <- "http://bendixcarstensen.com/SPE/data"</pre>
> oc <- read.table( paste(url, "occoh.txt", sep = "/"), header=TRUE)
> str(oc)
> summary(oc)
```

12. It is convenient to change all the dates into fractional calendar years

```
> oc$ybirth <- cal.yr(oc$birth)</pre>
> oc$yentry <- cal.yr(oc$entry)</pre>
> oc$yexit <- cal.yr(oc$exit)</pre>
```

We shall also compute the age at entry and at exit, respectively, as age will be the main time scale in our analyses.

```
> oc$agentry <- oc$yentry - oc$ybirth
> oc$agexit <- oc$yexit - oc$ybirth
```

13. As the next step we shall create a lexis object from the data frame along the calendar period and age axes, and as the outcome event we specify the coronary death.

```
> oc.lex <- Lexis( entry = list( per = yentry,
                                 age = yentry - ybirth ),
                    exit = list( per = yexit),
+
+
             exit.status = chdeath,
                     id = id, data = oc)
> str(oc.lex)
> summary(oc.lex)
```

14. At this stage it is informative to examine a graphical presentation of the follow-up lines and outcome cases in a conventional Lexis diagram. To rationalize your work we have created a separate source file plots-caco-ex.R to do the graphics for this tas as well as for some forthcoming ones. The source source file is found in the same folder where the data sets are located – Load the source file and have a look at the content of the first function in it

```
> source( paste(url, "plots-caco-ex.R", sep = "/") )
> plot1
```

Function plot1() makes the graph required here. No arguments are needed when calling the function

```
> plot1()
```

15. As age is here the main time axis, we shall illustrate the *study base* or the follow-up lines and outcome events along the age scale, being ordered by age at exit. Function plot2() in the same source file does the work. Vertical lines at those ages when new coronary deaths occur are drawn to identify the pertinent *risk sets*. For that purpose it is useful first to sort the data frame and the lexis object jointly by age at exit & age at entry, and to give a new ID number according to that order.

Using function plot3() in the same source file we now zoom the graphical illustration of the risk sets into event times occurring between 50 to 58 years.

```
> plot3
> plot3()
```

#### 1.14.2 Nested case-control study

We shall now employ the strategy of *risk-set sampling* or *time-matched* sampling of controls, *i.e.* we are conducting a *nested case-control study* within the cohort.

16. The risk sets are defined according to the age at diagnosis of the case. Further matching is applied for age at entry by 1-year agebands. For this purpose we first generate a categorical variable agen2 for age at entry

```
> oc.lex$agen2 <- cut(oc.lex$agentry, br = seq(40, 62, 1) )</pre>
```

Matched sampling from risk sets may be carried out using function <code>ccwc()</code> found in the <code>Epi</code> package. Its main arguments are the times of <code>entry</code> and <code>exit</code> which specify the time at risk along the main time scale (here age), and the outcome variable to be given in the <code>fail</code> argument. The number of

controls per case is set to be two, and the additional matching factor is given. – After setting the RNG seed (with your own number), make a call of this function and see the structure of the resulting data frame cactrl containing the cases and the chosen individual controls.

Check the meaning of the four first columns of the case-control data frame from the help page of function ccwc().

17. Now we shall start collecting data on the risk factors for the cases and their matched controls, including determination of the total cholesterol levels from the frozen sera! The storehouse of the risk factor measurements for the whole cohort is file occoh-Xdata.txt. It contains values of the following variables.

18. In the next step we collect the values of the risk factors for our cases and controls by merging the case-control data frame and the storehouse file. In this operation we utilize function merge() to select columns of two data frames: cactrl (all columns) and ocX (four columns) and to merge these into a single file (see exercise 1.1, subsection 1.1.8, where merge() was introduced). The id variable in both files is used as the key to link each individual case or control with his own data on risk factors.

```
> oc.ncc <- merge(cactrl, ocX[, c("id", "smok", "tchol", "sbp")],
+     by = "id")
> str(oc.ncc)
```

19. We shall treat smoking as categorical and total cholesterol and systolic blood pressure as quantitative risk factors, but the values of the latter will be divided by 10 to get more interpretable effect estimates.

Convert the smoking variable into a factor.

```
> oc.ncc$smok <- factor(oc.ncc$smok,
+ labels = c("never", "ex", "1-14/d", ">14/d"))
```

20. It is useful to start the analysis of case-control data by simple tabulations by the categorized risk factors. Crude estimates of the rate ratios associated with them, in which matching is ignored, can be obtained as instructed in

Janne's lecture on Poisson and logistic models on Saturday 23 May. We shall focus on smoking

21. A proper analysis takes into account matching that was employed in the selection of controls for each case from the pertinent risk set further restricted to subjects who were about the same age at entry as the case was. Also, adjustment for the other risk factors is desirable. In this analysis function clogit() in survival package is utilized. It is in fact a wrapper of function coxph().

Compare these with the crude estimates obtained above.

#### 1.14.3 Case-cohort study

Now we start applying the second major outcome-selective sampling strategy for collecting exposure data from a big study population

22. The subcohort is selected as a simple random sample (n = 260) from the whole cohort. The id-numbers of the individuals that are selected will be stored in vector subcids, and subcind is an indicator for inclusion to the subcohort.

```
> N <- 1501; n <- 260
> set.seed(1579863)
> subcids <- sample(N, n )
> oc.lex$subcind <- 1*(oc.lex$id %in% subcids)</pre>
```

23. We form the data frame oc.cc to be used in the subsequent analysis selecting the union of the subcohort members and the case group from the data frame of the full cohort. After that we collect the data of the risk factors from the data storehouse for the subjects in the case-cohort data

```
> oc.cc <- subset( oc.lex, subcind==1 | chdeath ==1)
> oc.cc <- merge( oc.cc, ocX[, c("id", "smok", "tchol", "sbp")],
+    by ="id")
> str(oc.cc)
```

24. Function plot4() in the same source file creates a graphical illustration of the lifelines contained in the case-cohort data. Lines for the subcohort non-cases are grey without bullet at exit, those for subcohort cases are blue with blue bullet at exit, and for cases outside the subcohort the lines are black and dotted with black bullets at exit.

- > plot4 > plot4()
- 25. Define the categorical smoking variable again.

```
> oc.cc$smok <- factor(oc.cc$smok,</pre>
      labels = c("never", "ex", "1-14/d", ">14/d"))
```

A crude estimate of the hazard ratio for the various smoking categories k vs. non-smokers (k=1) can be obtained by tabulating cases  $(D_k)$  and person-years  $(y_k)$  in the subcohort by smoking and then computing the relevant exposure odds ratio for each category:

$$HR_k^{\text{crude}} = \frac{D_k/D_1}{y_k/y_1}$$

```
> sm.cc <- stat.table( index = smok,
+ contents = list( Cases = sum(lex.Xst), Pyrs = sum(lex.dur) ),
          margins = T, data = oc.cc)
> print(sm.cc, digits = c(sum=0, ratio=1))
> HRcc <- (sm.cc[1, -5]/sm.cc[1, 1])/(sm.cc[2, -5]/sm.cc[2, 1])
> round(HRcc, 3)
```

26. To estimate jointly the rate ratios associated with the categorized risk factors we now fit the pertinent Cox model applying the method of weighted partial likelihood as presented by Ling & Ying (1993) and Barlow (1994). The weights for all cases and non-cases in the subcohort are first computed and added to the data frame.

```
> N.nonc <- N-sum(oc.lex$chdeath) # non-cases in whole cohort
> n.nonc <- sum(oc.cc$subcind * (1-oc.cc$chdeath)) # non-cases in subcohort
> wn <- N.nonc/n.nonc</pre>
                              # weight for non-cases in subcohort
> c(N.nonc, n.nonc, wn)
> oc.cc$w <- ifelse(oc.cc$subcind==1 & oc.cc$chdeath==0, wn, 1)</pre>
```

Next, the Cox model is fitted by the method of weighted partial likelihood using coxph(), such that the robust covariance matrix will be used as the source of standard errors for the coefficients.

```
> oc.cc$surob <- with(oc.cc, Surv(agentry, agexit, chdeath) )</pre>
> cc.we <- coxph( surob \sim smok + I(sbp/10) + tchol, robust = T,
         weight = w, data = oc.cc)
> summary(cc.we)
> round( ci.exp(cc.we), 3)
```

The covariance matrix for the coefficients may also be computed by the dfbeta-method. After that a comparison is made between standard errors from the naive, robust and dfbeta covariance matrix, respectively. You will see that the naive SEs are essentially smaller than those obtained by the robust and the dfbeta method, respectively.

```
> dfbw <- resid(cc.we, type='dfbeta')</pre>
> covdfb.we <- cc.we$naive.var +
     (n.nonc*(N.nonc-n.nonc)/N.nonc)*var(dfbw[ oc.cc$chdeath==0, ] )
> cbind( sqrt(diag(cc.we$naive.var)), sqrt(diag(cc.we$var)),
      sqrt(diag(covdfb.we)) )
```

27. The same analysis can also be done using function cch() in package survival with method = "LinYing" as follows:

```
> cch.LY <- cch( surob ~ smok + I(sbp/10) + tchol, stratum=NULL,
+ subcoh = ~subcind, id = ~id, cohort.size = N, data = oc.cc,
+ method = "LinYing" )
> summary(cch.LY)
```

28. The summary() method for the cch() object does not print the standard errors for the coefficients. The following comparison demonstrates numerically that the method of Lin & Ying is the same as weighted partial likelihood coupled with dfbeta covariance matrix.

#### 1.14.4 Full cohort analysis and comparisons

Finally, suppose the investigators could afford to collect the data of risk factors from the storehouse for the whole cohort.

29. Let us form the data frame corresponding to the full cohort design and convert again smoking to be categorical.

```
> oc.full <- merge( oc.lex, ocX[, c("id", "smok", "tchol", "sbp")],
+ by.x = "id", by.y = "id")
> oc.full$smok <- factor(oc.full$smok,
+ labels = c("never", "ex", "1-14/d", ">14/d"))
```

Juts for comparison with the corresponding analysis in case-cohort data perform a similar crude estimation of hazard ratios associated with smoking.

30. Fit now the Cox model to the full cohort, and there is no need to employ extra tricks upon the ordinary coxph() fit.

31. Lastly, a comparison of the point estimates and standard errors between the different designs, including variants of analysis for the case-cohort design, can be performed.

You will notice that the point estimates of the coefficients obtained from the full cohort, nested case-control, and case-cohort analyses, respectively, are somewhat variable.

However, the standard errors across the NCC and different proper CC analyses are relatively similar. Those from a naive covariance matrix of a CC analysis, though, are practically equal to the SEs from the full cohort analysis, reflecting the fact that the naive analysis implicitly assumes there being as much information available as there is with full cohort data.

#### 1.14.5 Further exercises and homework

- 32. If you have time, you could run both the NCC study and CC study again but now with a larger control group or subcohort; for example 4 controls per case in NCC and n = 520 as the subcohort size in CC. Remember resetting the seed first. Pay attention in the results to how much closer will be the point estimates and the proper SEs to those obtained from the full cohort design.
- 33. Instead of simple linear terms for sbp and tchol you could try to fit spline models to describe their effects.
- 34. A popular alternative to weighted partial likelihood in the analysis of case-cohort data is the pseudo-likelihood method (Prentice 1986), which is based on "late entry" to follow-up of the case subjects not belonging to the subcohort. A longer way of applying this approach, which you could try at home after the course, would first require manipulation of the oc.cc data frame, as outlined on slide 34. Then coxph() would be called like in model object cc.we above but now with weights = 1. Similar corrections on the covariance matrix are needed, too. However, a shorter way is provided by function cch() which you can apply directly to the case-cohort data oc.cc as before but now with method = "Prentice". Try this and compare the results with those obtained by weighted partial likelihood in models cc.we and cch.LY.
- 35. Yet another computational solution for maximizing weighted partial likelihood is provided by a combination of functions twophase() and svycoxph() of the survey package. The approach is illustrated with an example in a vignette "Two-phase designs in epidemiology" by Thomas Lumley (see

http://cran.r-project.org/web/packages/survey/vignettes/epi.pdf, p. 4-7). - You can try this at home and check that you would obtain similar results as with models cc.we and cch.LY.

#### Time-dependent variables and multiple 1.15states

The following practical exercise is based on the data from paper:

P Hovind, L Tarnow, P Rossing, B Carstensen, and HH Parving: Improved survival in patients obtaining remission of nephrotic range albuminuria in diabetic nephropathy. *Kidney Int*, **66**(3):1180–1186, Sept 2004.

You can find a .pdf-version of the paper here: http://BendixCarstensen.com/~bxc/AdvCoh/papers/Hovind.2004.pdf

#### 1.15.1 The renal failure dataset

The dataset renal.dta contains data on follow up of 125 patients from Steno Diabetes Center. They enter the study when they are diagnosed with nephrotic range albuminuria (NRA). This is a condition where the levels of albumin in the urine is exceeds a certain level as a sign of kidney disease. The levels may however drop as a consequence of treatment, this is called remission. Patients exit the study at death or kidney failure (dialysis or transplant).

Table 1.2: Variables in renal.dta.

```
id
        Patient id
        1=male, 2=female
  sex
        Date of birth
  dob
        Date of entry into the study (2.5 years after NRA)
  doe
        Date of remission. Missing if no remission has occurred
  dor
        Date of exit from study
  dox
        Exit status: 1,2,3=event (death, ESRD), 0=censored
event
```

1. The dataset is in Stata-format, so you must read the dataset using read.dta from the foreign package (which is part of the standard R-distribution). At the same time, convert sex to a proper factor. Choose where to read the dataset.

```
library( Epi ) ; clear()
library( foreign )
# renal <- read.dta( "http://BendixCarstensen.com/SPE/data/renal.dta" )</pre>
# renal <- read.dta( "./data/renal.dta" )</pre>
renal$sex <- factor( renal$sex, labels=c("M","F") )</pre>
head( renal )
```

2. Use the Lexis function to declare the data as survival data with age, calendar time and time since entry into the study as timescales. Label any event > 0 as "ESRD", i.e. renal death (death of kidney (transplant or dialysis), or person). Note that you must make sure that the "alive" state

(here NRA) is the first, as Lexis assumes that everyone starts in this state (unless of course entry.status is specified):

Make sure you know what the variables in Lr stand for.

3. Visualize the follow-up in a Lexis-diagram, by using the plot method for Lexis objects.

```
plot( Lr, col="black", lwd=3 )
subset( Lr, age<0 )</pre>
```

What is wrong here? List the data for the person with negative entry age.

4. Correct the data and make a new plot, for example by:

- 5. (Optional, esoteric) We can produce a slightly more fancy Lexis diagram. Note that we have a x-axis of 40 years, and a y-axis of 80 years, so when specifying the output file adjust the total width of the plot so that the use of mai (look up the help page for par) to specify the margins of the plot so that it leaves a plotting area twice as high as wide. The mai argument to par gives the margins in inches, so the total size of the horizontal and vertical margins is 1 inch each, to which we add 80/5 in the height, and 40/5 in the horizontal direction, each giving exactly 5 years per inch in physical size.
- 6. Now make a Cox-regression analysis of the enpoint ESRD with the variables sex and age at entry into the study, using time since entry to the study as time scale.

What is the The hazard ratio between males and females? Between two persons who differ 10 years in age at entry?

- 7. The main focus of the paper was to assess whether the occurrence of remission (return to a lower level of albumin excretion, an indication of kidney recovery) influences mortality. "Remission" is a time-dependent variable which is initially 0, but takes the value 1 when remission occurs. In order to handle this, each person who sees a remission must have two records:
  - One record for the time before remission, where entry is doe, exit is dor, remission is 0, and event is 0.

• One record for the time after remission, where entry is dor, exit is dox, remission is 1, and event is 0 or 1 according to whether the person had an event at dox.

This is accomplished using the cutLexis function on the Lexis object, where we introduce a remission state "Rem". You must declare the "NRA" state as a precursor state, i.e. a state that is *less* severe than "Rem" in the sense that a person who see a remission will stay in the "Rem" state unless he goes to the "ESRD" state. Also use split.state=TRUE to have different ESRD states according to whether a person had had remission or not prioer to ESRD. The statement to do this is:

List the records from a few select persons (choose values for lex.id, using for example subset( Lc, lex.id %in% c(5,7,9) ), or other numbers).

8. Now show how the states are connected and the number of transitions between them by using boxes. This is an interactive command that requires you to click in the graph window:

```
boxes (Lc)
```

It has a couple of fancy arguments, try:

```
boxes( Lc, boxpos=TRUE, scale.R=100, show.BE=TRUE, hm=1.5, wm=1.5)
```

You may even be tempted to read the help page for boxes.Lexis...

9. Plot a Lexis diagram where different coloring is used for different segments of the follow-up. The plot.Lexis function draws a line for each record in the dataset, so you can index the coloring by lex.Cst and lex.Xst as appropriate — indexing by a factor corresponds to indexing by the *index number* of the factor levels, so you must be know which order the factor levels are in:

10. Make Cox-regression of mortality (i.e. endpoint "ESRD" or "ESRD(Rem)") with sex, age at entry and remission as explanatory variables, using time since entry as timescale, and include lex.Cst as time-dependent variable, and indicate that each record represents follow-up from tfi to tfi+lex.dur. Make sure that you know why what goes where here in the call to coxph.

```
 (EP \leftarrow levels(Lc)[3:4]) \\ m1 \leftarrow coxph(Surv(tfi, # from tfi+lex.dur, # to lex.Xst %in% EP) ~ # event \\ sex + I((doe-dob-50)/10) + # fixed covariates \\ (lex.Cst=="Rem"), # time-dependent variable data = Lc) \\ summary( m1 )
```

What is the effect of of remission on the rate of ESRD?

11. The assumption in this model about the two rates of remission is that they are proportional as functions of time since remission. This can tested with the cox.zph function:

```
cox.zph( m1 )
```

Is there indication of non-proportionality between the rates of ESRD?

#### 1.15.2 Splitting the follow-up time

In order to explore the effect of remission on the rate of ESRD, we shall split the data further into small pieces of follow-up. To this end we use the function splitLexis. The rates can then be modeled using a Poisson-model, and the shape of the underlying *rates* be explored. Furthermore, we can allow effects of both time since NRA and current age. To this end we will use splines, so we need the splines and also the mgcv packages.

12. Now split the follow-up time every month after entry, and verify that the number of events and risk time is the same as before and after the split:

```
sLc <- splitLexis( Lc, "tfi", breaks=seq(0,30,1/12) )
summary( Lc, scale=100 )
summary(sLc, scale=100 )</pre>
```

13. Try to fit the Poisson-model corresponding to the Cox-model we fitted previously. The function ns() produces a model matrix corresponding to a piece-wise cubic function, modeling the baseline hazard explicitly (think of the ns terms as the baseline hazard that is not visible in the Cox-model)

How does the effects of sex change from the Cox-model?

14. Try instead using the gam function from the mgcv package — a function that allows s, that optimizes the number as well as the location of the knots:

15. Extract the regression parameters from the models using ci.exp and compare with the estimates from the Cox-model:

```
ci.exp( mx, subset=c("sex","dob","Cst"), pval=TRUE )
ci.exp( m1 )
round( ci.exp( mp, subset=c("sex","dob","Cst") ) / ci.exp( m1 ), 2 )
```

How lare is the difference in estimated regression parameters?

16. The model has the same assumptions as the Cox-model about proportionality of rates, but there is an additional assumption that the hazard is a smooth function of time since entry. It seems to be a sensible assumption (well, restriction) to put on the rates that they vary smoothly by time. No such restriction is made in the Cox model. The gam model optimizes the shape of the smoother by general cross-validation. Try to look at the shape of the estimated effect of tfi:

```
plot( mx )
```

Is this a useful plot?

17. However, plot does not give you the absolute level of the underlying rates because it bypasses the intercept. So try to predict the rates as a function of tfi and the covariates, by setting up a prediction data frame. Note that age in the model specification is entered as doe-dob, hence the prediction data frame must have these two variables and not the age, but it is onlythe difference that matters for the prediction:

Try to overlay with the corresponding prediction from the glm model using ns.

18. Apart from the baseline timescale, time since NRA, the time since remission might be of interest in describing the mortality rate. However this is only relevant for persons who actually have a remission, but there is only 28 persons in this group and 8 events — this can be read of the plot with the little boxes, figure 2.11. With this rather limited number of events we can certainly not expect to be able to model anything more complicated than a linear trend with time since remission. The variable we want to have in the model is current date (per) minus date of remission (dor): per-dor), but

only positive values of it. This can be fixed by using pmax(), but we must also deal with all those who have missing values, so construct a variable which is 0 for persons in "NRA" and time since remission for persons in "Rem":

```
sLc <- transform( sLc, tfr = pmax( (per-dor)/10, 0, na.rm=TRUE ) )</pre>
```

19. Expand the model with this variable:

What can you say about the effect of tinesince remisssion on the rate of ESRD?

#### 1.15.3 Prediction in a multistate model

If we want to make proper statements about the survival and disease probabilities we must know not only how the occurrence of remission influences the rate of death/ESRD, but we must also model the occurrence rate of remission itself.

20. The rates of ESRD were modelled by a Poisson model with effects of age and time since NRA — in the models mp and mx. But if we want to model whole process we must also model the remission rates transition from "NRA" to "Rem", but the number of events is rather small so we restrict covariates in this model to only time since NRA and sex. Note that only the records that relate to the "NRA" state can be used:

What is the remission rate-ration between men and women?

- 21. If we want to predict the probability of being in each of the three states using these estimated rates, we may resort to analytical calculations of the probabilities from the estimated rates, which is doable in this case, but which will be largely intractable for more complicated models. Alternatively we can simulate the life course for a large group of (identical) individuals through a model using the estimated rates. That will give a simulated cohort (in the form of a Lexis object), and we can then just count the number of persons in each state at each of a set of time points. This is accomplished using the function simLexis. The input to this is the initial status of the persons whose life-course we shall simulate, and the transition rates in suitable form:
  - Suppose we want predictions for men aged 50 at NRA. The input is in the form of a Lexis object (where lex.dur and lex.Xst will be ignored). Note that in order to carry over the time.scales and the time.since

attributes, we construct the input object using subset to select columns, and NULL to select rows (see the example in the help file for simLexis):

```
inL <- subset( sLc, select=1:11 )[NULL,]</pre>
str( inL )
timeScales(inL)
inL[1,"lex.id"] <- 1
inL[1,"per"] <- 2000
inL[1,"age"] <- 50</pre>
inL[1,"tfi"] <- 0
inL[1,"lex.Cst"] <- "NRA"</pre>
inL[1,"lex.Xst"] <- NA</pre>
inL[1,"lex.dur"] <- NA</pre>
inL[1,"sex"] <- "M"
inL[1,"doe"] <- 2000
inL[1,"dob"] <- 1950</pre>
inL <- rbind( inL, inL )</pre>
inL[2,"sex"] <- "F"</pre>
inL
str( inL )
```

• The other input for the simulation is the transitions, which is a list with an element for each transient state (that is "NRA" and "Rem"), each of which is again a list with names equal to the states that can be reached from the transient state. The content of the list will be glm objects, in this case the models we just fitted, describing the transition rates:

With this as input we can now generate a cohort, using N=10 to simulate life course of 10 persons (for each set of starting values in inL):

```
( iL <- simLexis( Tr, inL, N=10 ) )
summary( iL, by="sex" )</pre>
```

What type of object have you got as iL. Simulate a couple of thousand persons.

22. Now generate the life course of 5,000 persons, and look at the summary. The system.time command is just to tell you how long it took, you may want to start with 1000 just to see how long that takes.

```
system.time(
sM <- simLexis( Tr, inL, N=5000 ) )
summary( sM, by="sex" )</pre>
```

Why are there so many ESRD-events in the resulting data set?

23. Now count how many persons are present in each state at each time for the first 10 years after entry (which is at age 50). This can be done by using nState. Try:

```
nStm <- nState( subset(sM,sex=="M"), at=seq(0,10,0.1), from=50, time.scale="age") \\ nStf <- nState( subset(sM,sex=="F"), at=seq(0,10,0.1), from=50, time.scale="age") \\ head( nStf )
```

What is to the object nStf?

24. With the counts of persons in each state at the designated time points (in nStm), compute the cumulative fraction over the states, arranged in order given by perm:

```
ppm <- pState( nStm, perm=c(2,1,3,4) )
ppf <- pState( nStf, perm=c(2,1,3,4) )
head( ppf )
tail( ppf )</pre>
```

What do the entries in ppf represent?

25. Try to plot the cumulative probabilities using the plot method for pState objects:

```
plot( ppf )
```

Is this useful?

26. Now try to improve the plot so that it is easier to read, and easier to comapre men and women:

```
par( mfrow=c(1,2) )
plot( ppm, col=c("limegreen","red","#991111","forestgreen") )
lines( as.numeric(rownames(ppm)), ppm[,"Rem"], lwd=4 )
text( 59.5, 0.95, "Men", adj=1, col="white", font=2, cex=1.2 )
axis( side=4, at=0:10/10 )
axis( side=4, at=1:99/100, labels=NA, tck=-0.01 )
plot( ppf, col=c("limegreen","red","#991111","forestgreen"), xlim=c(60,50) )
lines( as.numeric(rownames(ppf)), ppf[,"Rem"], lwd=4 )
text( 59.5, 0.95, "Women", adj=0, col="white", font=2, cex=1.2 )
axis( side=2, at=0:10/10 )
axis( side=2, at=1:99/100, labels=NA, tck=-0.01 )
```

What is the 10-year risk of remission for men and women respectively?

## Chapter 2

### Solutions

There is a chapter for each of the exercises used at the course. This is either a printout of the R-program that performs the analyses, as well as the graphs produced by the programs, or output from an R-weave solution file with a bit more elaborate text.

The code and the output from these programs are also available from the course homepage in <a href="http://BendixCarstensen/SPE/R">http://BendixCarstensen/SPE/R</a>; they are called xxx-s.R; just before each chapter you will find a line with the text xxx-s, indicating that the name of the script will be xxx-s.R.

100 2.3 Tabulation SPE: Solutions

#### 2.3 Tabulation

#### 2.3.1 Introduction

R and its add-on packages provide several different tabulation functions with different capabilities. The appropriate function to use depends on your goal. There are at least three different uses for tables.

The first use is to create simple summary statistics that will be used for further calculations in R. For example, a two-by-two table created by the table function can be passed to fisher.test, which will calculate odds ratios and confidence intervals. The appearance of these tables may, however, be quite basic, as their principal goal is to create new objects for future calculations.

A quite different use of tabulation is to make "production quality" tables for publication. You may want to generate reports from for publication in paper form, or on the World Wide Web. The package **xtable** provides this capability, but it is not covered by this course.

An intermediate use of tabulation functions is to create human-readable tables for discussion within your work-group, but not for publication. The Epi package provides a function stat.table for this purpose, and this practical is designed to introduce this function.

#### 2.3.2 The births data

We shall use the births data which concern 500 mothers who had singleton births in a large London hospital. The outcome of interest is the birth weight of the baby, also dichotomised as normal or low birth weight. These data are available in the Epi package:

```
> library(Epi)
> data(births)
> names(births)
[1] "id"
               "bweight" "lowbw"
                                  "gestwks" "preterm" "matage"
[8] "sex"
> head(births)
  id bweight lowbw gestwks preterm matage hyp sex
        2974
                  0
                      38.52
                                   0
                                          34
  2
                         NA
                                          30
        3270
                  0
                                  NA
3
                                          35
                                                    2
  3
        2620
                  0
                      38.15
                                   0
4
  4
        3751
                  0
                      39.80
                                   0
                                          31
                                               0
                                                    1
5
  5
        3200
                  0
                      38.89
                                   0
                                          33
                                               1
                                                    1
6
        3673
                  0
                      40.97
                                   0
```

The housekeeping file for these data is births-house.r, which you can download from a location to be specified in the practical. Assuming that you have copied the housekeeping file into the subdirectory /data of your working directory, you should now start the session by running this file with the command:

```
> source("data/births-house.r")
```

Make sure you know what the script file has done using str(births).

#### 2.3.3 One-way tables

The simplest table one-way table is created by

```
> stat.table(index = sex, data = births)
-----
sex count()
-----
M 264
F 236
```

This creates a count of individuals, classified by levels of the factor sex. Compare this table with the equivalent one produced by the table function. Note that stat.table has a data argument that allows you to use variables in a data frame without specifying the frame.

You can display several summary statistics in the same table by giving a list of expressions to the contents argument:

Only a limited set of expressions are allowed: see the help page for stat.table for details.

You can also calculate marginal tables by specifying margin=TRUE in your call to stat.table. Do this for the above table. Check that the percentages add up to 100 and the total for count() is the same as the number of rows of the data frame births.

102 2.3 Tabulation SPE: Solutions

To see how the mean birth weight changes with sex, try

```
> stat.table(index = sex, contents = mean(bweight), data=births)
```

sex	mean(bweight)	
M	3229.90	
F	3032.83	

Add the count to this table. Add the margin with margin=TRUE.

sex	 count()	mean(bweight)
	 264	3229.90
F	236	3032.83
Total	500	3136.88

As an alternative to bweight we can look at lowbw with

```
> stat.table(index = sex, contents = percent(lowbw), data=births)
```

```
sex percent(lowbw)

M 100.0
F 100.0
```

All the percentages are 100! To use the percent function the variable lowbw must also be in the index, as in

```
> stat.table(index = list(sex,lowbw), contents = percent(lowbw), data=births)
```

The final column is the percentage of babies with low birth weight by different categories of gestation.

- 1. Obtain a table showing the frequency distribution of gest4.
- 2. Show how the mean birth weight changes with gest4.
- 3. Show how the percentage of low birth weight babies changes with gest4.

> stat.table(index = gest4, contents = count(), data=births)

count()	
31 32 167 260	

> stat.table(index = gest4, contents = mean(bweight), data=births)

```
gest4 mean(bweight)

[20,35) 1733.74
[35,37) 2590.31
[37,39) 3093.77
[39,45) 3401.26
```

> stat.table(index = list(lowbw,gest4), contents = percent(lowbw), data=births)

```
lowbw [20,35) [35,37) [37,39) [39,45)

0 19.4 59.4 89.2 98.8
1 80.6 40.6 10.8 1.2
```

Another way of obtaining the percentage of low birth weight babies by gestation is to use the ratio function:

> stat.table(gest4,ratio(lowbw,1,100),data=births)

gest4	ratio(lowbw, 1, 100)
[20,35) [35,37) [37,39) [39,45)	80.65 40.62 10.78 1.15

This only works because lowbw is coded 0/1, with 1 for low birth weight.

Tables of odds can be produced in the same way by using ratio(lowbw, 1-lowbw). The ratio function is also very useful for making tables of rates with (say) ratio(D,Y,1000) where D is the number of failures, and Y is the follow-up time. We shall return to rates in a later practical.

104 2.3 Tabulation SPE: Solutions

#### 2.3.4 Improving the Presentation of Tables

The stat.table function provides default column headings based on the contents argument, but these are not always very informative. Supply your own column headings using *tagged* lists as the value of the contents argument, within a stat.table call:

```
> stat.table(gest4,contents = list( N=count(),
+ "(%)" = percent(gest4)),data=births)
```

gest4	N	(%)
[20,35) [35,37) [37,39) [39,45)	31 32 167 260	6.3 6.5 34.1 53.1

This improves the readability of the table. It remains to give an informative title to the index variable. You can do this in the same way: instead of giving gest4 as the index argument to stat.table, use a named list:

```
> stat.table(index = list("Gestation time" = gest4),data=births)
```

Gestation time	count()	
[20,35)	31	
[35,37)	32	
[37,39)	167	
[39,45)	260	

#### 2.3.5 Two-way Tables

The following call gives a  $2 \times 2$  table showing the mean birth weight cross-classified by sex and hyp.

```
> stat.table(list(sex,hyp), contents=mean(bweight), data=births)
```

Add the count to this table and repeat the function call using margin = TRUE to calculate the marginal tables.

*IARC*, 2018 2.3 Tabulation **105** 

```
> stat.table(list(sex,hyp), contents=list(count(), mean(bweight)),
+ margin=T, data=births)
```

sex		hyp hyper	Total
М	221 3310.75	43 2814.40	
F	207 3079.50	29 2699.72	
Total	428 3198.90	72 2768.21	500 3136.88

Use stat.table with the ratio function to obtain a  $2 \times 2$  table of percent low birth weight by sex and hyp.

```
> stat.table(list(sex,hyp), contents=list(count(),mean(bweight)),margin=T, data=births)
```

sex	normal	шур	Total
M	221 3310.75	43 2814.40	
F	207 3079.50	29 2699.72	236 3032.83
Total	428 3198.90	72 2768.21	500 3136.88

> stat.table(list(sex,hyp), contents=list(count(),ratio(lowbw,1,100)),margin=T, data=birt

sex	normal	hyp hyper	Total
M	221	43	264
	6.79	27.91	10.23
F	207	29	236
	12.08	27.59	13.98
Total	428	72	500
	9.35	27.78	12.00

You can have fine-grained control over which margins to calculate by giving a logical vector to the margin argument. Use margin=c(FALSE, TRUE) to calculate margins over sex but not hyp. This might not be what you expect, but the margin argument indicates which of the index variables are to be marginalized out, not which index variables are to remain.

106 2.3 Tabulation SPE: Solutions

#### 2.3.6 Printing

Just like every other R function, stat.table produces an object that can be saved and printed later, or used for further calculation. You can control the appearance of a table with an explicit call to print()

There are two arguments to the print method for stat.table. The width argument which specifies the minimum column width, and the digits argument which controls the number of digits printed after the decimal point. This table

```
> odds.tab <- stat.table(gest4, list("odds of low bw" = ratio(lowbw,1-lowbw)),
               data=births)
+
> print(odds.tab)
 _____
         odds of
gest4
          low bw
 [20,35)
           4.17
 [35,37)
             0.68
 [37,39)
            0.12
            0.01
 [39,45)
```

shows a table of odds that the baby has low birth weight. Use width=15 and digits=3 and see the difference.

> print(odds.tab, width=15, digits=3)

gest4	odds	of	low b	)W
[20,35) [35,37) [37,39) [39,45)			4.16 0.68 0.12 0.01	34 21

## 2.4 Graphics in R

There are three kinds of plotting functions in R:

- 1. Functions that generate a new plot, e.g. hist() and plot().
- 2. Functions that add extra things to an existing plot, e.g. lines() and text().
- 3. Functions that allow you to interact with the plot, e.g. locator() and identify().

The normal procedure for making a graph in R is to make a fairly simple initial plot and then add on points, lines, text etc., preferably in a script.

#### 2.4.1 Simple plot on the screen

Load the births data and get an overview of the variables:

```
> library( Epi )
> data( births )
> str( births )
```

Now look at the birthweight distribution with

```
> hist(births$bweight)
```

The histogram can be refined – take a look at the possible options with

```
> help(hist)
```

and try some of the options, for example:

```
> hist(births$bweight, col="gray", border="white")
```

To look at the relationship between birthweight and gestational weeks, try

```
> with(births, plot(gestwks, bweight))
```

You can change the plot-symbol by the option pch=. If you want to see all the plot symbols try:

```
> plot(1:25, pch=1:25)
```

4. Make a plot of the birth weight versus maternal age with

```
> with(births, plot(matage, bweight) )
```

5. Label the axes with

```
> with(births, plot(matage, bweight, xlab="Maternal age", ylab="Birth weight (g)") )
```

#### 2.4.2 Colours

There are many colours recognized by R. You can list them all by colours() or, equivalently, colors() (R allows you to use British or American spelling). To colour the points of birthweight versus gestational weeks, try

```
> with(births, plot(gestwks, bweight, pch=16, col="green") )
```

This creates a solid mass of colour in the centre of the cluster of points and it is no longer possible to see individual points. You can recover this information by overwriting the points with black circles using the points() function.

```
> with(births, points(gestwks, bweight, pch=1) )
```

Note: when the number of data points on a scatter plot is large, you may also want to decrease the point size: to get points that are 50% of the original size, add the parameter cex=0.5 (or another number <1 for different sizes).

#### 2.4.3 Adding to a plot

The points() function just used is one of several functions that add elements to an existing plot. By using these functions, you can create quite complex graphs in small steps.

Suppose we wish to recreate the plot of birthweight vs gestational weeks using different colours for male and female babies. To start with an empty plot, try

```
> with(births, plot(gestwks, bweight, type="n"))
```

Then add the points with the points function.

```
> with(births, points(gestwks[sex==1], bweight[sex==1], col="blue"))
> with(births, points(gestwks[sex==2], bweight[sex==2], col="red"))
```

To add a legend explaining the colours, try

```
> legend("topleft", pch=1, legend=c("Boys", "Girls"), col=c("blue", "red"))
```

which puts the legend in the top left hand corner.

Finally we can add a title to the plot with

```
> title("Birth weight vs gestational weeks in 500 singleton births")
```

#### 2.4.3.1 Using indexing for plot elements

One of the most powerful features of R is the possibility to index vectors, not only to get subsets of them, but also for repeating their elements in complex sequences.

Putting separate colours on males and female as above would become very clumsy if we had a 5 level factor instead of sex.

Instead of specifying one color for all points, we may specify a vector of colours of the same length as the gestwks and bweight vectors. This is rather tedious to do directly, but R allows you to specify an expression anywhere, so we can use the fact that sex takes the values 1 and 2, as follows:

First create a colour vector with two colours, and take look at sex:

```
> c("blue","red")
> births$sex
```

Now see what happens if you index the colour vector by sex:

```
> c("blue", "red")[births$sex]
```

For every occurrence of a 1 in sex you get "blue", and for every occurrence of 2 you get "red", so the result is a long vector of "blue"s and "red"s corresponding to the males and females. This can now be used in the plot:

```
> with(births, plot( gestwks, bweight, pch=16, col=c("blue", "red")[sex]) )
```

The same trick can be used if we want to have a separate symbol for mothers over 40 say. We first generate the indexing variable:

```
> births$oldmum <- ( births$matage >= 40 ) + 1
```

Note we add 1 because ( matage >= 40 ) generates a logic variable, so by adding 1 we get a numeric variable with values 1 and 2, suitable for indexing:

```
> with(births, plot(gestwks, bweight, pch=c(16,3)[oldmum], col=c("blue", "red")[sex] ))
```

so where oldmum is 1 we get pch=16 (a dot) and where oldmum is 2 we get pch=3 (a cross).

R will accept any kind of complexity in the indexing as long as the result is a valid index, so you don't need to create the variable oldmum, you can create it on the fly:

```
> with(births, plot(gestwks, bweight, pch=c(16,3)[(matage>=40)+1], col=c("blue", "red")[
```

#### 2.4.3.2 Generating colours

R has functions that generate a vector of colours for you. For example,

```
> rainbow(4)
```

produces a vector with 4 colours (not immediately human readable, though). There are a few other functions that generates other sequences of colours, type ?rainbow to see them. The color function (or colour function if you prefer) returns a vector of the colour names that R knows about. These names can also be used to specify colours.

Gray-tones are produced by the function gray (or grey), which takes a numerical argument between 0 and 1; gray(0) is black and gray(1) is white. Try:

```
> plot( 0:10, pch=16, cex=3, col=gray(0:10/10) )
> points( 0:10, pch=1, cex=3 )
```

#### 2.4.4 Saving your graphs for use in other documents

If you need to use the plot in a report or presentation, you can save it in a graphics file. Once you have generated the script (sequence of R commands) that produce the graph (and it looks ok on screen), you can start a non-interactive graphics device and then re-run the script. Instead of appearing on the screen, the plot will now be written directly to a file. After the plot has been completed you will need to close the device again in order to be able to access the file. Try:

```
> pdf(file="bweight_gwks.pdf", height=4, width=4)
> with(births, plot( gestwks, bweight, col=c("blue","red")[sex]) )
> legend("topleft", pch=1, legend=c("Boys","Girls"), col=c("blue","red"))
> dev.off()
```

This will give you a portable document file bweight\_gwks.pdf with a graph which is 4 inches tall and 4 inches wide.

Instead of pdf, other formats can be used (jpg, png, tiff, ...). See help(Devices) for the available options.

In window-based environments (R GUI for Windows, R-Studio) you may also use the menu (File Save as ... or Export) to save the active graph as a file and even copy-paste may work (from R graphics window to Word, for instance) – however, writing it manually into the file is recommended for reproducibility purposes (in case you need to redraw your graph with some modifications).

## 2.4.5 The par() command

It is possible to manipulate any element in a graph, by using the graphics options. These are collected on the help page of par(). For example, if you want axis

labels always to be horizontal, use the command par(las=1). This will be in effect until a new graphics device is opened.

Look at the typewriter-version of the help-page with

```
> help(par)
```

```
or better, use the the html-version through |\text{Help}| \rightarrow |\text{Html help}| \rightarrow |\text{Packages}|
graphics \rightarrow P \rightarrow par.
```

It is a good idea to take a print of this (having set the text size to "smallest" because it is long) and carry it with you at any time to read in buses, cinema queues, during boring lectures etc. Don't despair, few R-users can understand what all the options are for.

par() can also be used to ask about the current plot, for example par("usr") will give you the exact extent of the axes in the current plot.

If you want more plots on a single page you can use the command

```
> par( mfrow=c(2,3) )
```

This will give you a layout of 2 rows by 3 columns for the next 6 graphs you produce. The plots will appear by row, i.e. in the top row first. If you want the plots to appear columnwise, use par( mfcol=c(2,3) ) (you still get 2 rows by 3 columns).

To restore the layout to a single plot per page use

```
> par(mfrow=c(1,1))
```

If you want a more detailed control over the layout of multiple graphs on a single page look at ?layout.

#### Interacting with a plot 2.4.6

The locator() function allows you to interact with the plot using the mouse. Typing locator(1) shifts you to the graphics window and waits for one click of the left mouse button. When you click, it will return the corresponding coordinates.

You can use locator() inside other graphics functions to position graphical elements exactly where you want them. Recreate the birth-weight plot,

```
> with(births, plot(gestwks, bweight, col = c("blue", "red")[sex]) )
and then add the legend where you wish it to appear by typing
> legend(locator(1), pch=1, legend=c("Boys", "Girls"), col=c("blue", "red") )
```

The identify() function allows you to find out which records in the data correspond to points on the graph. Try

```
> with(births, identify(gestwks, bweight))
```

When you click the left mouse button, a label will appear on the graph identifying the row number of the nearest point in the data frame births. If there is no point nearby, R will print a warning message on the console instead. To end the interaction with the graphics window, right click the mouse: the identify function returns a vector of identified points.

1. Use identify() to find which records correspond to the smallest and largest number of gestational weeks and view the corresponding records:

```
> with(births, births[identify(gestwks, bweight), ])
```

## 2.5 Simple simulation

Monte Carlo methods are computational procedures dealing with simulation of artificial data from given probability distributions with the purpose of learning about the behaviour of phenomena involving random variability. These methods have a wide range of applications in statistics as well as in several branches of science and technology. By solving the following exercises you will learn to use some basic tools of statistical simulation.

1. Whenever using a random number generator (RNG) for a simulation study (or for another purpose, such as for producing a randomization list to be used in a clinical trial or for selecting a random sample from a large cohort), it is a good practice to set first the seed. It is a number that determines the initial state of the RNG, from which it starts creating the desired sequence of pseudo-random numbers. Explicit specification of the seed enables the reproducibility of the sequence. – Instead of the number 5462319 below you may use your own seed of choice.

```
> set.seed(5462319)
```

2. Generate a random sample of size 20 from a normal distribution with mean 100 and standard deviation 10. Draw a histogram of the sampled values and compute the conventional summary statistics

```
> x <- rnorm(20, 100, 10)
> hist(x)
> c(mean(x), sd(x))
```

Repeat the above lines and compare the results.

```
> x <- rnorm(20, 100, 10)
> hist(x)
> c(mean(x), sd(x))
```

3. Now replace the sample size 20 by 1000 and run again twice the previous command lines with this size but keeping the parameter values as before. Compare the results between the two samples here as well as with those in the previous item.

```
> x <- rnorm(1000, 100, 10)
> hist(x)
> c(mean(x), sd(x))

> x <- rnorm(1000, 100, 10)
> hist(x)
> c(mean(x), sd(x))
```

4. Generate 500 observations from a Bernoulli(p) distribution, or Bin(1, p) distribution, taking values 1 and 0 with probabilities p and 1-p, respectively, when p = 0.4:

```
> X <- rbinom(500, 1, 0.4)
> table(X)
```

5. Now generate another 0/1 variable Y, being dependent on previously generated X, so that P(Y = 1|X = 1) = 0.2 and P(Y = 1|X = 0) = 0.1.

```
> Y <- rbinom(500,1,0.1*X+0.1)
> table(X,Y)
> prop.table(table(X,Y),1)
```

6. Generate data obeying a simple linear regression model  $y_i = 5 + 0.1x_i + \varepsilon_i$ , i = 1, ... 100, in which  $\varepsilon_i \sim N(0, 10^2)$ , and  $x_i$  values are integers from 1 to 100. Plot the  $(x_i, y_i)$ -values, and estimate the parameters of that model.

```
> x <- 1:100
> y <- 5 + 0.1*x + rnorm(100,0,10)
> plot(x,y)
> abline(lm(y~x))
> summary(lm(y~x))$coef
```

Are your estimates consistent with the data-generating model? Run the code a couple of times to see the variability in the parameter estimates.

## **2.6 Calculation of rates, RR and RD**

This exercise is *very* prescriptive, so you should make an effort to really understand everything you type into R. Consult the relevant slides of the lecture on "Poisson regression for rates . . . "

#### 2.6.1 Hand calculations for a single rate

Let  $\lambda$  be the true hazard rate or theoretical incidence rate, its estimator being the empirical incidence rate  $\widehat{\lambda} = D/Y =$  'no. cases/person-years'. Recall that the standard error of the empirical rate is  $SE(\widehat{\lambda}) = \widehat{\lambda}/\sqrt{D}$ .

The simplest approximate 95% confidence interval (CI) for  $\lambda$  is given by

$$\widehat{\lambda} \pm 1.96 \times SE(\widehat{\lambda})$$

An alternative approach is based on logarithmic transformation of the empirical rate. The standard error of the log-rate  $\hat{\theta} = \log(\hat{\lambda})$  is  $SE(\hat{\theta}) = 1/\sqrt{D}$ . Thus, a simple approximate 95% confidence interval for the log-hazard  $\theta = \log(\lambda)$  is obtained from

$$\widehat{\theta} \pm 1.96/\sqrt{D} = \log(\widehat{\lambda}) \pm 1.96/\sqrt{D}$$

When taking the exponential from the above limits, we get another approximate confidence interval for the hazard  $\lambda$  itself:

$$\exp\{\log(\widehat{\lambda}) \pm 1.96/\sqrt{D}\} = \widehat{\lambda} \stackrel{\times}{\div} \text{EF},$$

where  $EF = \exp\{1.96 \times SE[\log(\widehat{\lambda})]\}$  is the *error factor* associated with the 95% interval. This approach provides a more accurate approximation with very small numbers of cases. (However, both these methods fail when D = 0, in which case an *exact* method or one based on *profile-likelihood* is needed.)

1. Suppose you have 15 events during 5532 person-years. Let's use R as a simple desk calculator to derive the rate (in 1000 person-years) and the first version of an approximate confidence interval:

```
> library( Epi )
> options(digits=4)  # cut the number of decimals in the output
> D <- 15
> Y <- 5.532  # thousands of years
> rate <- D / Y
> SE.rate <- rate/sqrt(D)
> c(rate, SE.rate, rate + c(-1.96, 1.96)*SE.rate )
[1] 2.7115 0.7001 1.3393 4.0837
```

2. We then compute the approximate confidence interval using the method based on log-transformation and compare the result with that in item (a)

```
> SE.logr <- 1/sqrt(D)
> EF <- exp( 1.96 * SE.logr )
> c(log(rate), SE.logr)
[1] 0.9975 0.2582
> c( rate, EF, rate/EF, rate*EF )
[1] 2.711 1.659 1.635 4.498
```

#### 2.6.2 Poisson model for a single rate with logarithmic link

We can estimate the rate  $\lambda$  and compute its CI with a Poisson model, as described in the lecture.

3. Use the number of events as the response and the log-person-years as an offset term, and fit the Poisson model with log-link

```
> m <- glm( D ~ 1, family=poisson(link=log), offset=log(Y) )
> summary( m )
glm(formula = D ~ 1, family = poisson(link = log), offset = log(Y))
Deviance Residuals:
[1] 0
Coefficients:
           Estimate Std. Error z value Pr(>|z|)
(Intercept)
             0.998
                         0.258 3.86 0.00011 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
(Dispersion parameter for poisson family taken to be 1)
    Null deviance: 0 on 0 degrees of freedom
Residual deviance: 0 on 0 degrees of freedom
AIC: 6.557
Number of Fisher Scoring iterations: 3
```

What is the interpretation of the parameter in this model?

4. The summary method produces a lot of output, so we extract CIs for the model parameters directly from the fitted model on the scale determined by the link function with the ci.lin()-function. Thus, the estimate, SE, and confidence limits for the log-rate  $\theta = \log(\lambda)$  are obtained by:

However, to get the confidence limits for the rate  $\lambda = \exp(\theta)$  on the original scale, the results must be exp-transformed, we can either do:

or if we just want the point estimate and CI for  $\lambda$  from log-transformed quantities we can use ci.exp(), which is actually a wrapper of ci.lin(); optionally with p-values:

```
exp(Est.) 2.5% 97.5% P
(Intercept) 2.711 1.635 4.498 0.0001119
```

Both functions are found from Epi package. Note that the test statistic and P-value are rarely interesting quantities for a single rate.

5. There is an alternative way of fitting a Poisson model: Use the empirical rate  $\hat{\lambda} = D/Y$  as a *scaled* Poisson response, and the person-years as *weight* instead of offset (albeit it will give you a warning about non-integer response in a Poisson model, but you can ignore this warning):

We see that this gives exactly the same results as above.

#### 2.6.3 Poisson model for a single rate with identity link

The advantage of the approach based on weighting is that it allows sensible use of the *identity* link. The response is the same but the parameter estimated is now the rate itself, not the log-rate.

6. Fit the Poisson model with identity link

What is the meaning of the intercept in this model?

Verify that you actually get the same rate estimate as before.

7. Now use ci.lin() to produce the estimate and the confidence intervals from this model:

The confidence limits are not the same as from the multiplicative model, because they are derived from an approximation of the distribution of the rate being normally distributed, whereas the multiplicative model uses an assumption that the log-rate is normally distributed.

The confidence limits from this model are based on the 2nd derivative of the log-likelihood with respect to the *rate*, and not as before with respect to the *log rate*, and therefore they are different — they are symmetrical on the rate-scale and not on the log-rate scale:

$$\ell(\lambda) = D \ln(\lambda) - \lambda Y \qquad \ell'(\lambda) = D/\lambda - Y \qquad \ell''(\lambda) = -D/\lambda^2 \big|_{\lambda = D/Y} = -Y^2/D$$

Thus the observed information is  $Y^2/D$  and hence the approximate standard deviation of the rate is square root of the inverse of this,  $\sqrt{D}/Y$ , which is exactly the standard deviation you got from the model:

## 2.6.4 Poisson model assuming same rate for several periods

Now, suppose the events and person years are collected over three periods.

8. Read in the data and compute period-specific rates

```
> Dx <- c(3,7,5)
> Yx <- c(1.412,2.783,1.337)
> Px <- 1:3
> rates <- Dx/Yx
> rates
[1] 2.125 2.515 3.740
```

9. We fit the same model as before, assuming a single constant rate across the separate periods; and we get the same result:

10. We can test whether the rates are the same in the three periods by fitting a model with the period as a factor in the model:

```
> mp <- glm( Dx ~ factor(Px), offset=log(Yx), family=poisson ) and comparing the two models using anova() with the argument test="Chisq":
```

We see that the deviance of the model with the constant rates is the same as the likelihood-ratio test versus the model with three separate rates. The deviance is namely in general the likelihood-ratio test of a given model versus the most detailed model possible for the dataset. And in this case, with a dataset of 3 observations, the most detailed model is exactly the one we fitted with one rate per line in the dataset.

#### 2.6.5 Analysis of a rate ratio

We now switch to comparison of two rates  $\lambda_1$  and  $\lambda_0$ , i.e. the hazard in an exposed group vs. that in an unexposed one. Consider first estimation of the true rate ratio  $\rho = \lambda_1/\lambda_0$  between the groups. Suppose we have pertinent empirical data (cases and person-times) from both groups,  $(D_1, Y_1)$  and  $(D_0, Y_0)$ . The point estimate of  $\rho$  is the empirical rate ratio

$$RR = \frac{D_1/Y_1}{D_0/Y_0}$$

It is known that the variance of  $\log(RR)$ , that is, the difference of the log of the empirical rates  $\log(\widehat{\lambda}_1) - \log(\widehat{\lambda}_0)$  is estimated as

$$\text{var}(\log(\text{RR})) = \text{var}\{\log(\widehat{\lambda}_1/\widehat{\lambda}_0)\} 
= \text{var}\{\log(\widehat{\lambda}_1)\} + \text{var}\{\log(\widehat{\lambda}_0)\} 
= 1/D_1 + 1/D_0$$

Based on a similar argument as before, an approximate 95% CI for the true rate ratio  $\lambda_1/\lambda_0$  is then:

$$RR \stackrel{\times}{\div} \exp\left(1.96\sqrt{\frac{1}{D_1} + \frac{1}{D_0}}\right)$$

Suppose you have 15 events during 5532 person-years in an unexposed group and 28 events during 4783 person-years in an exposed group:

11. Calculate the rate-ratio and CI by direct application of the above formulae:

```
> D0 <- 15  ; D1 <- 28
> Y0 <- 5.532 ; Y1 <- 4.783
> RR <- (D1/Y1)/(D0/Y0)
> SE.lrr <- sqrt(1/D0+1/D1)
> EF <- exp( 1.96 * SE.lrr)
> c( RR, RR/EF, RR*EF )
[1] 2.158980 1.153146 4.042153
```

12. Now achieve this using a Poisson model:

```
> D <- c(D0,D1); Y <- c(Y0,Y1); expos <- 0:1
> mm <- glm(D \sim factor(expos), family=poisson, offset=log(Y))
```

What do the parameters mean in this model?

13. You can extract the exponentiated parameters in two ways:

#### 2.6.6 Analysis of rate difference

For the true rate difference  $\delta = \lambda_1 - \lambda_0$ , the natural estimator is the empirical rate difference

$$\widehat{\delta} = \widehat{\lambda}_1 - \widehat{\lambda}_0 = D_1/Y_1 - D_0/Y_0 = \text{RD}.$$

Its variance is just the sum of the variances of the two rates (since the latter are based on independent samples):

$$\operatorname{var}(RD) = \operatorname{var}(\widehat{\lambda}_1) + \operatorname{var}(\widehat{\lambda}_0)$$
$$= D_1/Y_1^2 + D_0/Y_0^2$$

14. Use this formula to compute the rate difference and a 95% confidence interval for it:

```
> rd <- diff( D/Y )
> sed <- sqrt( sum( D/Y^2 ) )
> c( rd, rd+c(-1,1)*1.96*sed )
[1] 3.1425697 0.5764816 5.7086578
```

15. Verify that this is the confidence interval you get when you fit an additive model with exposure as factor:

## 2.6.7 Calculations using matrix tools

- NB. This subsection requires some familiarity with matrix algebra.
- 16. Explore the function ci.mat(), which lets you use matrix multiplication (operator '%\*%' in R) to produce a confidence interval from an estimate and its standard error (or CIs from whole columns of estimates and SEs):

- As you see, this function returns a  $2 \times 3$  matrix (2 rows, 3 columns) containing familiar numbers.
- 17. When you combine the single rate and its standard error into a row vector of length 2, i.e. a  $1 \times 2$  matrix, and multiply this by the  $2 \times 3$  matrix above, the computation returns a  $1 \times 3$  matrix containing the point estimate and the confidence limit. Apply this method to the single rate calculations in 1.6.1; first creating the  $1 \times 2$  matrix and then performing the matrix multiplication.

18. When the confidence interval is based on the log-rate and its standard error, the result is obtained by appropriate application of the exp-function on the pertinent matrix product

19. For computing the rate ratio and its CI as in 1.6.5, matrix multiplication with ci.mat() should give the same result as there:

20. The main argument in function ci.mat() is alpha, which sets the confidence level:  $1 - \alpha$ . The default value is alpha = 0.05, corresponding to the level 1 - 0.05 = 95 %. If you wish to get the confidence interval for the rate ratio at the 90 % level (= 1 - 0.1), for instance, you may proceed as follows:

```
> ci.mat(alpha=0.1)
    Estimate     5.0%     95.0%
[1,]     1    1.000000    1.000000
[2,]     0 -1.644854    1.644854
> exp( c( log(RR), SE.lrr ) %*% ci.mat(alpha=0.1) )
    Estimate     5.0%     95.0%
[1,]     2.15898    1.275491    3.654429
```

21. Look again the model used to analyse the rate ratio in 1.6.5. Often one would like to get simultaneously both the rates and the ratio between them. This can be achieved in one go using the *contrast matrix* argument ctr.mat to ci.lin() or ci.exp(). Try:

```
> CM <- rbind( c(1,0), c(1,1), c(0,1) ) > rownames( CM ) <- c("rate\ 0","rate\ 1","RR\ 1\ vs.\ 0")
             [,1] [,2]
rate 0
              1
rate 1
               1
                     1
RR 1 vs. 0
             0
> mm <- glm( D ~ factor(expos),</pre>
                family=poisson(link=log), offset=log(Y) )
> ci.exp( mm, ctr.mat=CM)
            exp(Est.)
                            2.5%
                                     97.5%
             2.711497 1.634669 4.497678
rate 0
             5.854066 4.041994 8.478512
rate 1
RR 1 vs. 0 2.158980 1.153160 4.042106
```

22. Use the same machinery to the additive model to get the rates and the rate-difference in one go. Note that the annotation of the resulting estimates are via the column-names of the contrast matrix.

```
> rownames( CM ) <- c("rate 0", "rate 1", "RD 1 vs. 0") 
> ma <- glm( D/Y ~ factor(expos), 
+ family=poisson(link=identity), weight=Y ) 
> ci.lin( ma, ctr.mat=CM )[, c(1,5,6)] 
Estimate 2.5% 97.5% 
rate 0 2.711497 1.3393153 4.083678 
rate 1 5.854066 3.6857298 8.022403 
RD 1 vs. 0 3.142570 0.5765288 5.708611
```

## 2.7 Logistic regression (GLM)

#### 2.7.1 Malignant melanoma in Denmark

In the mid-80s a case-control study on risk factors for malignant melanoma was conducted in Denmark (Østerlind et al. The Danish case-control study of cutaneous malignant melanoma I: Importance of host factors. *Int J Cancer* 1988; 42: 200-206).

The cases were patients with skin melanoma (excluding lentigo melanoma), newly diagnosed from 1 Oct, 1982 to 31 March, 1985, aged 20-79, from East Denmark, and they were identified from the Danish Cancer Registry.

The controls (twice as many as cases) were drawn from the residents of East Denmark in April, 1984, as a random sample stratified by sex and age (within the same 5 year age group) to reflect the sex and age distribution of the cases. This is called group matching, and in such a study, it is necessary to control for age and sex in the statistical analysis. (Yes indeed: In spite of the fact that stratified sampling by sex and age removed the statistical association of these variables with melanoma from the final case-control data set, the analysis must control for variables which determine the probability of selecting subjects from the base population to the study sample.)

The population of East Denmark is a dynamic one. Sampling the controls only at one time point is a rough approximation of *incidence density sampling*, which ideally would spread out over the whole study period. Hence the exposure odds ratios calculable from the data are estimates of the corresponding hazard rate ratios between the exposure groups.

After exclusions, refusals etc., 474 cases (92% of eligible cases) and 926 controls (82%) were interviewed. This was done face-to-face with a structured questionnaire by trained interviewers, who were not informed about the subject's case-control status.

For this exercise we have selected a few host variables from the study in an ascii-file, melanoma.dat. The variables are listed in table 2.1.

## 2.7.2 Reading the data

Start R and load the Epi package using the function library(). Read the data set from the file melanoma.dat found in the course website to a data frame with name mel using the read.table() function. Remember to specify that missing values are coded ".", and that variable names are in the first line of the file. View the overall structure of the data frame, and list the first 20 rows of mel.

<sup>&</sup>gt; library(Epi)
> mel <- read.table("http://bendixcarstensen.com/SPE/data/melanoma.dat", header=TRUE, na.
> str(mel)

'data.frame':

\$ cc

Table 2.1: Variables in the melanoma dataset.

Variable	Units or Coding	Type	Name
Case-control status	1=case, 0=control	numeric	CC
Sex	1=male, 2=female	numeric	sex
Age at interview	age in years	numeric	age
Skin complexion	0=dark, 1=medium, 2=light	numeric	skin
Hair colour	0=dark brown/black, 1=light brown,		
	2=blonde, 3=red	numeric	hair
eye colour	0=brown, 1=grey, green, 2=blue	numeric	eyes
Freckles	1=many, 2=some, 3=none	numeric	freckles
Naevi, small	no. naevi < 5mm	numeric	nvsmall
Naevi, largs	no. naevi $\geq 5$ mm	numeric	nvlarge

1400 obs. of 9 variables:

```
$ sex
           : int
                  2 1 2 2 2 2 2 1 2 2 ...
          : int
                  71 68 42 66 36 68 68 39 75 49 ...
 $ age
                  2 2 1 0 1 2 0 2 2 2 ...
 $ skin
          : int
          : int
                  0 0 1 2 0 2 0 0 0 1 ...
$ hair
$ eyes
          : int 2 2 2 1 2 2 1 2 2 2 ...
 $ freckles: int 2 1 3 2 3 2 2 2 1 2 ...
$ nvsmall : int 2 3 22 0 1 0 0 3 5 6 ...
$ nvlarge : int  0 0 1 0 0 0 0 0 0 ...
> head(mel, n=20)
   cc sex age skin hair eyes freckles nvsmall nvlarge
           71
                 2
                           2
1
   1
        2
                      0
                                             2
2
                 2
                      0
                           2
                                     1
                                             3
                                                     0
   1
        1
           68
3
        2
                           2
                                    3
                                            22
    1
           42
                 1
                      1
                                                     1
                                     2
4
    0
        2
           66
                      2
                           1
                                             0
                                                     0
                 0
        2
                           2
                                     3
5
           36
                      0
                                                     0
    1
                 1
                                             1
                                     2
        2
                 2
                      2
                           2
                                             0
6
    0
           68
                                                     0
                                     2
7
        2
    0
           68
                 0
                      0
                           1
                                             0
                                                     0
                           2
                                     2
8
    0
        1
           39
                 2
                      0
                                             3
                                                     0
                           2
2
2
2
9
        2
                 2
                                     1
                                             5
    0
           75
                      0
                                                     0
                                     2
        2
                 2
10
   1
           49
                      1
                                             6
                                                     0
                                     3
    0
        1
           48
                 2
                      1
                                             4
                                                     0
11
                                     2
12
   1
        2
           67
                 0
                      0
                                             1
                                                     0
                           2
        1
                      0
                                     3
                                             4
13
   0
           50
                 1
                                                     0
14
                           1
                                     3
   1
        2
           38
                 2
                      0
                                             8
                                                     0
                           2
15 0
       2
           33
                 2
                      1
                                     2
                                             3
                                                     0
16 0
       2 39
                 1
                      0
                           1
                                    3
                                             0
                                                     2
   0
       2 39
                           2
                                    3
                                             0
                                                     0
17
                 1
                      1
                           1
                                             3
   1
       1 50
                 0
                                    1
                                                     1
18
                           2
        2
                                     2
19 0
           35
                 2
                      0
                                             1
```

: int 1 1 1 0 1 0 0 0 0 1 ...

#### 2.7.3 House keeping

The structure of the data frame mel tells us that all the variables are numeric (integer), so first you need to do a bit of house keeping. For example the variables sex, skin, hair, eye need to be converted to factors, with labels, and freckles which is coded 4 for none down to 1 for many (not very intuitive) needs to be recoded, and relabelled.

To avoid too much typing and to leave plenty of time to think about the analysis, these house keeping commands are in a script file called melanoma-house.r. You should study this script carefully before running it. The coding of freckles can be reversed by subtracting the current codes from 4. Once recoded the variable needs to be converted to a factor with labels "none", etc. Age is currently a numeric variable recording age to the nearest year, and it will be convenient to group these values into (say) 10 year age groups, using cut. In this case we choose to create a new variable, rather than change the original.

```
> source("http://bendixcarstensen.com/SPE/data/melanoma-house.r")
```

Look again at the structure of the data frame mel and note the changes. Use the command summary (mel) to look at the univariate distributions.

#### > str(mel)

```
'data.frame':
                     1400 obs. of 13 variables:
$ cc : int 1 1 1 0 1 0 0 0 0 1 ...
           : Factor w/ 2 levels "M", "F": 2 1 2 2 2 2 2 1 2 2 ...
           : int 71 68 42 66 36 68 68 39 75 49 ...
           : Factor w/ 3 levels "dark", "medium", ...: 3 3 2 1 2 3 1 3 3 3 ...
           : Factor w/ 4 levels "dark", "light_brown", ...: 1 1 2 3 1 3 1 1 1 2 ....
           : Factor w/ 3 levels "brown", "grey-green", ...: 3 3 3 2 3 3 2 3 3 3 ...
$ freckles: Factor w/ 3 levels "none", "some", ...: 2 3 1 2 1 2 2 2 3 2 ...
$ nvsmall : int 2 3 22 0 1 0 0 3 5 6 ...
$ nvlarge : int  0 0 1 0 0 0 0 0 0 .
$ age.cat : Factor w/ 6 levels "[20,30)","[30,40)",..: 6 5 3 5 2 5 5 2 6 3 ...
          : Factor w/ 2 levels "dark", "other": 1 1 2 2 1 2 1 1 1 2 ...
$ hair2
          : Factor w/ 4 levels "[0,1)", "[1,2)", ...: 3 3 4 1 2 1 1 3 4 4 ...
          : Factor w/ 3 levels "[0,1)","[1,2)",..: 1 1 2 1 1 1 1 1 1 1 ...
> summary(mel)
       СС
                  sex
                                               skin
                                                                 hair
        :0.0000
Min.
                  M:584
                          Min.
                                 :21.00
                                          dark :318
                                                        dark
                                                                   :690
1st Qu.:0.0000
                  F:816
                          1st Qu.:42.00
                                          medium:594
                                                        light_brown:548
Median :0.0000
                          Median :53.00
                                          light :478
                                                        blonde
                                                                   : 61
```

```
NA's : 10
Mean
       :0.3386
                         Mean
                                 :52.89
                                                       red
                                                                   :101
3rd Qu.:1.0000
                         3rd Qu.:64.00
       :1.0000
                                :81.00
Max.
                         Max.
                 freckles
                               nvsmall
                                                 nvlarge
        eyes
                                                                    age.cat
          :187
                            Min. : 0.000
                                                    : 0.0000
                                                                 [20,30):61
brown
                 none:633
                                              Min.
grey-green:450
                            1st Qu.: 0.000
                 some:526
                                              1st Qu.: 0.0000
                                                                 [30,40):202
blue
          :757
                 many:237
                            Median : 0.000
                                              Median : 0.0000
                                                                 [40,50):347
NA's
                 NA's: 4
                            Mean : 1.163
                                              Mean : 0.1565
                                                                 [50,60):296
                            3rd Qu.: 1.000
                                                                 [60,70):307
                                              3rd Qu.: 0.0000
```

[70,85):187

[5,50):103

NA's : 7

This is enough housekeeping for now - let's turn to something a bit more interesting.

NA's :

NA's

:7

#### 2.7.4 One variable at a time

As a first step it is a good idea to start by looking at the numbers of cases and controls by each variable separately, ignoring age and sex. Try

```
> with(mel, table(cc,skin))
cc dark medium light
          391
               296
 0 232
   86
          203
               182
> stat.table(skin, contents=ratio(cc,1-cc), data=mel)
skin ratio(cc,
         1 - cc)
_____
dark
           0.37
medium
            0.52
light
             0.61
```

to see the numbers of cases and controls, as well as the odds of being a case by skin colour

Now use effx() to get crude estimates of the hazard ratios for the effect of skin colour.

```
> effx(cc, type="binary", exposure=skin, data=mel)
_____
response : cc
         : binary
       : skin
exposure
skin is a factor with levels: dark / medium / light
baseline is dark
effects are measured as odds ratios
effect of skin on cc
number of observations 1390
```

```
Effect 2.5% 97.5%
medium vs dark 1.40 1.04 1.89 light vs dark 1.66 1.22 2.26
Test for no effects of exposure on 2 df: p-value= 0.00499
• Look at the crude effect estimates of hair, eyes and freckles in the same way.
> with(mel, table(cc,hair))
cc dark light_brown blonde red
 0 490 341 36 59
               207
                       25 42
  1 200
> stat.table(hair, contents=ratio(cc,1-cc), data=mel)
 hair ratio(cc,
              1 - cc)
dark 0.41
light brown 0.61
blonde
                  0.69
 red
> effx(cc,type="binary",exposure=hair,data=mel)
response : cc
type : binary exposure : hair
hair is a factor with levels: dark / light_brown / blonde / red
baseline is dark
effects are measured as odds ratios
effect of hair on cc
number of observations 1400
                 Effect 2.5% 97.5%
blonde vs dark 1.70 0.995 2.91 red vs dark 1.74 1.140 2.68
Test for no effects of exposure on 3 df: p-value= 0.0017
> with(mel, table(cc,eyes))
cc brown grey-green blue
 0 123 312 488
1 64 138 269
> stat.table(eyes, contents=ratio(cc,1-cc), data=mel)
```

```
_____
        ratio(cc,
           1 - cc)
_____
grey-green 0.44 blue 0.52
> effx(cc, type="binary", exposure=eyes, data=mel)
______
response : cc
type : binary
exposure : eyes
eyes is a factor with levels: brown / grey-green / blue
baseline is brown
effects are measured as odds ratios
______
effect of eyes on cc
number of observations 1394
           Effect 2.5% 97.5%
grey-green vs brown 0.85 0.592 1.22 blue vs brown 1.06 0.756 1.48
Test for no effects of exposure on 2 df: p-value= 0.22
> with(mel, table(cc,freckles))
  freckles
cc none some many
 0 466 343 114
 1 167 183 123
> stat.table(freckles, contents=ratio(cc,1-cc),data=mel)
_____
freckles ratio(cc,
         1 - cc)
none 0.36
            0.53
some
many 1.08
> effx(cc, type="binary", exposure=freckles, data=mel)
______
response : cc
type : binary
exposure : freckles
```

freckles is a factor with levels: none / some / many baseline is none effects are measured as odds ratios

```
effect of freckles on cc
number of observations 1396

Effect 2.5% 97.5%
some vs none 1.49 1.16 1.92
many vs none 3.01 2.21 4.11

Test for no effects of exposure on 2 df: p-value= 2.15e-11
```

## 2.7.5 Generalized linear models with binomial family and logit link

The function effx() is just a wrapper for the glm() function, and you can show this by fitting the glm directly with

Comparison with the output from effx() shows the results to be the same.

Note that in effx() the type of response is "binary" whereas in glm() the family of probability distributions used to fit the model is "binomial". There is a 1-1 relationship between type of response and family:

```
metric gaussian
binary binomial
failure/count poisson
```

#### 2.7.6 Controlling for age and sex

Because the probability that a control is selected into the study depends on age and sex it is necessary to control for age and sex. For example, the effect of freckles controlled for age and sex is obtained with

```
effect of freckles on cc
controlled for age.cat sex
number of observations 1396
            Effect 2.5% 97.5%
             1.51 1.17 1.95
some vs none
              3.07 2.24 4.22
many vs none
Test for no effects of exposure on 2 df: p-value= 2.55e-11
or
> mfas <- glm(cc ~ freckles + age.cat + sex, family="binomial", data=mel)
> round(ci.exp(mfas), 2)
              exp(Est.) 2.5% 97.5%
(Intercept)
                   0.41 0.23 0.72
                             1.95
frecklessome
                   1.51 1.17
                   3.07 2.24 4.22
frecklesmany
age.cat[30,40)
                   0.90 0.49 1.67
age.cat[40,50)
                   0.91 0.51 1.62
                   0.97 0.54 1.75
age.cat[50,60)
age.cat[60,70)
                   0.82 0.45 1.48
age.cat[70,85)
                   0.89 0.48 1.65
sexF
                   0.94 0.74 1.19
```

Do the adjusted estimates differ from the crude ones that you computed with effx()?

#### 2.7.7 Likelihood ratio tests

There are 2 effects estimated for the 3 levels of freckles, and glm() provides a test for each effect separately, but to test for no effect at all of freckles you need a likelihood ratio test. This involves fitting two models, one without freckles and one with, and recording the change in deviance. Because there are some missing values for freckles it is necessary to restrict the first model to those subjects who have values for freckles.

The change in residual deviance is 1785.9 - 1737.1 = 48.8 on 1389 - 1387 = 2 degrees of freedom. The *P*-value corresponding to this change is obtained from the upper tail of the cumulative distribution of the  $\chi^2$ -distribution with 2 df:

```
> 1 - pchisq(48.786, 2)
[1] 2.548328e-11
```

• There are 3 effects for the 4 levels of hair colour (hair). To obtain adjusted estimates for the effect of hair colour and to test the pertinent null hypothesis fit the relevant models, print the and use anova to test for no effects of hair colour.

```
exp(Est.) 2.5% 97.5%
(Intercept)
                     0.39 0.22 0.69
hairlight_brown
                     1.50 1.18
                               1.91
hairblonde
                     1.68 0.98
                                2.88
hairred
                     1.78 1.16
                                2.75
age.cat[30,40)
                     0.98 0.53
                               1.79
age.cat[40,50)
                     0.98 0.55
age.cat[50,60)
                     1.17 0.65
age.cat[60,70)
                     0.98 0.55
age.cat[70,85)
                     1.13 0.61
                                2.08
sexF
                     1.00 0.79
                                1.26
Analysis of Deviance Table
Model 1: cc ~ age.cat + sex
Model 2: cc ~ hair + age.cat + sex
  Resid. Df Resid. Dev Df Deviance Pr(>Chi)
1
       1393
                1790.7
                            15.434 0.001481 **
2
       1390
                1775.2 3
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

Compare the estimates with the crude ones and assess the evidence against the null hypothesis.

#### 2.7.8 Relevelling

From the above you can see that subjects at each of the 3 levels light-brown, blonde, and red, are at greater risk than subjects with dark hair, with similar odds ratios. This suggests creating a new variable hair2 which has just two levels, dark and the other three. The Relevel() function in Epi has been used for this in the house keeping script.

• Use effx() to compute the odds-ratio of melanoma between persons with red, blonde or light brown hair versus those with dark hair.

```
> effx(cc, type="binary", exposure=hair2, control=list(age.cat,sex), data=mel)
```

```
response : cc
type : binary
exposure : hair2
control vars : age.cat sex
hair2 is a factor with levels: dark / other
baseline is dark
effects are measured as odds ratios
effect of hair2 on cc
controlled for age.cat sex
number of observations 1400
Effect
         2.5% 97.5%
  1.55 1.24 1.95
Test for no effects of exposure on 1 df: p-value= 0.000124
Reproduce these results by fitting an appropriate glm.
> mh2 <- glm(cc ~ hair2 + age.cat + sex, family="binomial",
               data = subset(mel, !is.na(hair2)) )
> ci.exp(mh2 )
               exp(Est.)
                             2.5%
(Intercept)
               0.3894010 0.2199868 0.6892829
hair2other
               1.5541887 1.2396159 1.9485894
age.cat[30,40) 0.9740838 0.5302331 1.7894756
age.cat[40,50) 0.9872390 0.5539667 1.7593852
age.cat[50,60) 1.1722458 0.6529651 2.1044926
age.cat[60,70) 0.9847738 0.5491367 1.7660074
age.cat[70,85) 1.1277140 0.6121944 2.0773447
               1.0034944 0.7978073 1.2622108
Use also a likelihood ratio test to test for the effect of hair2.
> m1 <- glm(cc ~ age.cat + sex, data = subset(mel, !is.na(hair2)) )</pre>
> anova(m1, mh2,test="Chisq")
Analysis of Deviance Table
Model 1: cc ~ age.cat + sex
Model 2: cc ~ hair2 + age.cat + sex
  Resid. Df Resid. Dev Df Deviance Pr(>Chi)
       1393
               313.17
               1775.93 1 -1462.8
2
       1392
```

#### 2.7.9 Controlling for other variables

When you control the effect of an exposure for some variable you are asking a question about what would the effect be if the variable is kept constant. For example, consider the effect of freckles controlled for hair2. We first stratify by hair2 with

```
> effx(cc, type="binary", exposure=freckles,
     control=list(age.cat,sex), strata=hair2, data=mel)
response : cc
control vars : age.cat sex
stratified by : hair2
freckles is a factor with levels: none / some / many
baseline is none
hair2 is a factor with levels: dark/other
effects are measured as odds ratios
effect of freckles on cc
controlled for age.cat sex
stratified by hair2
number of observations 1396
                               Effect 2.5% 97.5%
strata dark level some vs none 1.61 1.11 2.34
strata other level some vs none 1.42 1.00 2.01
strata dark level many vs none 2.84 1.76 4.58 strata other level many vs none 3.15 2.06 4.80
Test for effect modification on 2 df: p-value= 0.757
The effect of freckles is still apparent in each of the two strata for hair colour. Use
effx() to control for hair2, too, in addition to age.cat and sex.
> effx(cc, type="binary", exposure=freckles,
                   control=list(age.cat,sex,hair2), data=mel)
______
response : cc
type : binary
exposure : freckles
control vars : age.cat sex hair2
freckles is a factor with levels: none / some / many
baseline is none
effects are measured as odds ratios
                                   _____
effect of freckles on cc
controlled for age.cat sex hair2
number of observations 1396
            Effect 2.5% 97.5%

      some vs none
      1.51 1.17 1.95

      many vs none
      3.02 2.19 4.15

Test for no effects of exposure on 2 df: p-value= 6.9e-11
```

It is tempting to control for variables without thinking about the question you are thereby asking. This can lead to nonsense.

#### 2.7.10 Stratification using glm()

We shall reproduce the output from

```
> effx(cc, type="binary", exposure=freckles,
             control=list(age.cat,sex), strata=hair2,data=mel)
______
response : cc
type : binary
exposure : freckles
control vars : age.cat sex
stratified by : hair2
freckles is a factor with levels: none / some / many
baseline is none
hair2 is a factor with levels: dark/other
effects are measured as odds ratios
effect of freckles on cc
controlled for age.cat sex
stratified by hair2
number of observations 1396
                                  Effect 2.5% 97.5%
strata dark level some vs none 1.61 1.11 2.34
strata other level some vs none 1.42 1.00 2.01
strata dark level many vs none 2.84 1.76 4.58
strata other level many vs none 3.15 2.06 4.80
Test for effect modification on 2 df: p-value= 0.757
using glm(). To do this requires a nested model formula:
> mfas.h <- glm(cc ~ hair2/freckles + age.cat + sex, family="binomial", data=mel)
> ci.exp(mfas.h )
                                          2.5%
                           exp(Est.)
                                                     97.5%
(Intercept)
                          0.3169581 0.1725855 0.5821023
hair2other
                          1.5639083 1.0920425 2.2396650
age.cat[30,40) 0.9286674 0.5004220 1.7233920 age.cat[40,50) 0.9573093 0.5328744 1.7198068 age.cat[50,60) 1.0464308 0.5776057 1.8957872 age.cat[60,70) 0.8495081 0.4692660 1.5378570 age.cat[70,85) 0.9351315 0.5020370 1.7418455 sexF 0.9012339 0.7114142 1.1417014
hair2dark:frecklessome 1.6123583 1.1106965 2.3406026
hair2other:frecklessome 1.4196216 1.0015163 2.0122743
hair2dark:frecklesmany 2.8378600 1.7567458 4.5842996
hair2other:frecklesmany 3.1469251 2.0628414 4.8007266
```

In amongst all the other effects you can see the two effects of freckles for dark hair (1.61 and 2.84) and the two effects of freckles for other hair (1.42 and 3.15).

#### 2.7.11 Naevi

The distributions of nvsmall and nvlarge are very skew to the right. You can see this with

```
> with(mel, stem(nvsmall))
The decimal point is at the |
 8 | 0000000000000000000
 10 | 0000000000
 12 | 00
 14 | 0000000
 16
18 | 000
20 | 0
22 | 000
24 | 0
26 |
28 |
30 I
32 L
34 I
36 | 0
38 |
40
42
44
46 | 0
> with(mel, stem(nvlarge))
The decimal point is at the |
 2 | 000000000000000000
 3 | 0000000
 4 | 0000
 5 I 000
 6 |
 7
  1
 8 |
 9
  | 0
10 |
 11 |
12 | 0
13 |
14 I 0
```

Because of this it is wise to categorize them into a few classes

```
- small naevi into four: 0, 1, 2-4, and 5+;
```

<sup>-</sup> large naevi into three: 0, 1, and 2+.

This has been done in the house keeping script.

• Look at the joint frequency distribution of these new variables using with(mel, table()). Are they strongly associated?

> stat.table(list(nvsma4,nvlar3),contents=percent(nvlar3),data=mel)

		-nvlar3	
nvsma4	[0,1)	[1,2)	[2,15)
[0,1) [1,2) [2,5) [5,50)	93.9 89.6 85.8 71.8	4.9 8.3 9.7 16.5	1.2 2.1 4.5 11.7

- > #High frequencies on the diagonal shows a strong association
- Compute the sex- and age-adjusted OR estimates (with 95% CIs) associated with the number of small naevi first by using effx(), and then by fitting separate glms including sex, age.cat and nvsma4 in the model formula.

```
> effx(cc,type="binary",exposure=nvsma4,control=list(age.cat,sex),data=mel)
```

```
response : cc
type : binary
exposure : nvsma4
control vars : age.cat sex
nvsma4 is a factor with levels: [0,1) / [1,2) / [2,5) / [5,50)
baseline is [0,1)
effects are measured as odds ratios
effect of nvsma4 on cc
controlled for age.cat sex
number of observations 1393
                            Effect 2.5% 97.5%
[1,2) vs [0,1) 1.59 1.15 2.21 [2,5) vs [0,1) 2.47 1.77 3.43
[5,50) vs [0,1) 5.06 3.28 7.81
Test for no effects of exposure on 3 df: p-value= <2e-16
> mns <- glm(cc ~ nvsma4 + age.cat + sex, family="binomial",data=mel)
> round(ci.exp(mns), 2)
                         exp(Est.) 2.5% 97.5%

      (Intercept)
      0.36
      0.20
      0.64

      nvsma4[1,2)
      1.59
      1.15
      2.21

      nvsma4[2,5)
      2.47
      1.77
      3.43

      nvsma4[5,50)
      5.06
      3.28
      7.81

      age.cat[30,40)
      0.96
      0.51
      1.80

      age.cat[40,50)
      1.02
      0.56
      1.85
```

```
      age.cat[50,60)
      1.16 0.64 2.13

      age.cat[60,70)
      1.07 0.58 1.96

      age.cat[70,85)
      1.17 0.62 2.21

      sexF
      0.96 0.76 1.21
```

• Do the same with large naevi nvlar3.

```
> effx(cc, type="binary", exposure=nvlar3, control=list(age.cat,sex), data=mel)
response : cc
              : binary
exposure : nvlar3
control vars : age.cat sex
nvlar3 is a factor with levels: [0,1) / [1,2) / [2,15)
baseline is [0,1)
effects are measured as odds ratios
effect of nvlar3 on cc
controlled for age.cat sex
number of observations 1393
                  Effect 2.5% 97.5%
[1,2) vs [0,1)
                   1.82 1.19 2.78
[2,15) vs [0,1)
                  3.58 1.78 7.21
Test for no effects of exposure on 2 df: p-value= 4.81e-05
> mnl <- glm(cc ~ nvlar3 + age.cat + sex, family="binomial", data=mel)
> round(ci.exp(mnl), 2)
(Intercept) 0.49 0.28 0.85 nvlar3[1,2) 1.82 1.19 2.78 nvlar3[2,15) 3.58 1.70

    nvlar3[2,15)
    3.58 1.78 7.21

    age.cat[30,40)
    0.90 0.49 1.66

    age.cat[40,50)
    0.92 0.52 1.63

age.cat[50,60)
                     1.07 0.60 1.91
age.cat[60,70)
                    0.89 0.50 1.60
age.cat[70,85)
                     1.00 0.54 1.84
sexF
                      1.03 0.82 1.29
```

• Now fit a glm containing age.cat, sex, nvsma4 and nvlar3. What is the interpretation of the coefficients for nvsma4 and nvlar3?

```
> mnls <- glm(cc ~ nvsma4 + nvlar3 + age.cat + sex, family="binomial", data=mel)
> # Coeffs for nvsma4 are the effects of nvsma4 controlled for age.cat, sex, and nvlar3.
> # Similarly for the coefficients for nvlar3.
```

138

#### 2.7.12 Treating freckles as a numeric exposure

The evidence for the effect of freckles is already convincing. However, to demonstrate how it is done, we shall perform a linear trend test by treating freckles as a numeric exposure.

You can check for linearity of the log odds of being a case with fscore by comparing the model containing freckles as a factor with the model containing freckles as numeric.

```
> m1 <- glm(cc ~ freckles + age.cat + sex, family="binomial", data=mel)
> m2 <- glm(cc ~ fscore + age.cat + sex, family="binomial", data=mel)
> anova(m2, m1, test="Chisq")
Analysis of Deviance Table

Model 1: cc ~ fscore + age.cat + sex
Model 2: cc ~ freckles + age.cat + sex
   Resid. Df Resid. Dev Df Deviance Pr(>Chi)
1     1388     1738.6
2     1387     1737.1     1     1.5206     0.2175
```

There is no evidence against linearity (p = 0.22).

It is sometimes helpful to look at the linearity in more detail with

```
age.cat [40,50)
                              0.91 0.51
                                         1.62
age.cat[50,60)
                              0.97 0.54
                                         1.75
age.cat[60,70)
                              0.82 0.45
                                         1.48
                                        1.65
age.cat[70,85)
                              0.89 0.48
sexF
                              0.94 0.74
                                        1.19
> m2 <- glm(cc ~ fscore + age.cat + sex, family="binomial",data=mel)</pre>
> round(ci.exp(m2), 2)
               exp(Est.) 2.5% 97.5%
                    0.23 0.12
(Intercept)
                               0.42
fscore
                    1.72 1.47
                                2.00
age.cat[30,40)
                    0.90 0.49
                                1.67
age.cat[40,50)
                    0.91 0.51
                                1.63
age.cat[50,60)
                    0.97 0.54
                               1.75
age.cat[60,70)
                    0.81 0.45
                               1.47
                    0.89 0.48 1.66
age.cat[70,85)
                    0.94 0.74
sexF
                               1.18
```

The use of C(freckles, contr.cum) makes each odds ratio to compare the odds at that level versus the previous level; not against the baseline (except for the 2nd level). If the log-odds are linear then these odds ratios should be the same (and the same as the odds ratio for fscore in m2.

#### 2.7.13 Graphical displays

The odds ratios (with CIs) can be graphically displayed using function plotEst() in Epi. It uses the value of ci.lin() evaluated on the fitted model object. As the intercept and the effects of age and sex are of no interest, we shall drop the corresponding rows (the 7 first ones) from the matrix produced by ci.lin(), and the plot is based just on the 1st, 5th and the 6th column of this matrix:

```
> m <- glm(cc ~ nvsma4 + nvlar3 + age.cat + sex, family="binomial",data=mel)
> plotEst( exp( ci.lin(m)[ 2:5, -(2:4)] ), xlog=T, vref=1 )
```

The xlog argument makes the OR axis logarithmic.

#### 140

# 2.8 Estimation of effects: simple and more complex

This exercise deals with analysis of metric or continuous response variables. We start with simple estimation of effects of a binary, categorical or a numeric explanatory variable, the exposure variable of interest. Then evaluation of potential modification confounding and/or by other variables is considered by stratification by and adjustment or control for these variables. Use of function effx() for such tasks is introduced together with functions lm() and glm() that can be used for more general linear and generalized linear models. Finally, more complex polynomial models for the effect of a numeric exposure variable are illustrated.

#### 2.8.1 Response and explanatory variables

Identifying the *response* or *outcome variable* correctly is the key to analysis. The main types are:

- Metric (a measurement taking many values, usually with units)
- Binary (two values coded 1/0)
- Failure (does the subject fail at end of follow-up, coded 1/0, and how long was follow-up, measurement of time)
- Count (aggregated data on failures in a group)

All these response variable are numeric.

Variables on which the response may depend are called *explanatory variables*. They can be categorical factors or numeric variables. A further important aspect of explanatory variables is the role they will play in the analysis.

- Primary role: exposure.
- Secondary role: confounder and/or modifier.

The word *effect* is a general term referring to ways of comparing the values of the response variable at different levels of an explanatory variable. The main measures of effect are:

- Differences in means for a metric response.
- Ratios of odds for a binary response.
- Ratios of rates for a failure or count response.

Other measures of effect include ratios of geometric means for positive-valued metric outcomes, differences and ratios between proportions (risk difference and risk ratio), and differences between failure rates.

#### 2.8.2 Data set births

We shall use the births data to illustrate different aspects in estimating effects of various exposures on a metric response variable bweight = birth weight, recorded in grams.

1. Load the Epi package and the data set and look at its content

```
> library(Epi)
> data(births)
> str(births)
'data.frame':
                    500 obs. of 8 variables:
$ id : num 1 2 3 4 5 6 7 8 9 10 ...
$ bweight: num
                2974 3270 2620 3751 3200
$ lowbw : num
                0 0 0 0 0 0 0 0 0 0 ...
                38.5 NA 38.2 39.8 38.9 ...
$ gestwks: num
$ preterm: num
               O NA O O O O O O O ...
$ matage : num
                34 30 35 31 33 33 29 37 36 39 ...
         : num
               0 0 0 0 1 0 0 0 0 0 ...
$ sex
         : num
                2 1 2 1 1 2 2 1 2 1 ...
```

2. Because all variables are numeric we need first to do a little housekeeping. Two of them are directly converted into factors, and categorical versions are created of two continuous variables by function cut().

```
> births$hyp <- factor(births$hyp, labels = c("normal", "hyper")) > births$sex <- factor(births$sex, labels = c("M", "F")) > births$agegrp <- cut(births$matage, + breaks = c(20, 25, 30, 35, 40, 45), right = FALSE) > births$gest4 <- cut(births$gestwks, + breaks = c(20, 35, 37, 39, 45), right = FALSE)
```

3. Have a look at univariate summaries of the different variables in the data; especially the location and dispersion of the distribution of bweight.

```
> summary(births)
```

```
gestwks
                   bweight
                                   lowbw
                                                                preterm
      : 1.0
               Min. : 628
                              Min. :0.00
                                             Min. :24.69
Min.
                                                             Min. :0.0000
                1st Qu.:2862
1st Qu.:125.8
                                             1st Qu.:37.94
                               1st Qu.:0.00
                                                             1st Qu.:0.0000
Median :250.5
                Median :3188
                               Median:0.00
                                             Median :39.12
                                                             Median :0.0000
                Mean :3137
                                                    :38.72
Mean :250.5
                               Mean
                                      :0.12
                                             Mean
                                                             Mean
                                                                    :0.1286
                               3rd Qu.:0.00
3rd Qu.:375.2
                3rd Qu.:3551
                                             3rd Qu.:40.09
                                                             3rd Qu.:0.0000
Max. :500.0
                Max. :4553
                                             Max. :43.16
                              Max. :1.00
                                                             Max. :1.0000
                                             NA's
                                                             NA's
                                                    :10
                                                                    :10
    matage
                    hyp
                             sex
                                                      gest4
                                        agegrp
Min.
       :23.00
                normal:428
                             M:264
                                     [20,25): 2
                                                   [20,35):31
1st Qu.:31.00
                hyper: 72
                             F:236
                                     [25,30):68
                                                   [35,37): 32
Median :34.00
                                     [30,35):200
                                                   [37,39):167
Mean
       :34.03
                                     [35,40):194
                                                   [39,45):260
3rd Qu.:37.00
                                     [40,45): 36
                                                  NA's
                                                        : 10
      :43.00
> with(births, sd(bweight) )
[1] 637.4515
```

### 2.8.3 Simple estimation with effx(), lm() and glm()

We are ready to analyze the "effect" of sex on bweight. A binary exposure variable, like sex, leads to an elementary two-group comparison of group means for a metric response.

4. Comparison of two groups is commonly done by the conventional t-test and the associated confidence interval.

The *P*-value refers to the test of the null hypothesis that there is no effect of sex on birth weight (quite an uninteresting null hypothesis in itself!). However, t.test() does not provide the point estimate for the effect of sex; only the test result and a confidence interval.

5. The function effx() in Epi is intended to introduce the estimation of effects in epidemiology, together with the related ideas of stratification and controlling, i.e. adjustment for confounding, without the need for familiarity with statistical modelling. It is in fact a wrapper of function glm() that fits generalized linear models. – Now, do the same analysis with effx()

The estimated effect of sex on birth weight, measured as a difference in means between girls and boys, is -197 g. Either the output from t.test() above or the command

```
> stat.table(sex, mean(bweight), data=births)
```

```
sex mean(bweight)

M 3229.90
F 3032.83
```

confirms this (3032.8 - 3229.9 = -197.1).

6. The same task can easily be performed by lm() or by glm(). The main argument in both is the model formula, the left hand side being the response variable and the right hand side after ~ defines the explanatory variables and their joint effects on the response. Here the only explanatory variable is the binary factor sex. With glm() one specifies the family, i.e. the assumed distribution of the response variable, but in case you use lm(), this argument is not needed, because lm() fits only models for metric responses assuming Gaussian distribution.

Note the amount of output that summary() method produces. The point estimate plus confidence limits can, though, be concisely obtained by ci.lin().

7. Now, use effx() to find the effect of hyp (maternal hypertension) on bweight.

\_\_\_\_\_\_

response : bweight type : metric

#### 2.8.4 Factors on more than two levels

The variable gest4 became as the result of cutting gestwks into 4 groups with left-closed and right-open boundaries [20,35) [35,37) [37,39) [39,45).

8. We shall find the effects of gest4 on the metric response bweight.

```
> effx(response=bweight,typ="metric",exposure=gest4,data=births)
response : bweight
type : metric
exposure : gest4
gest4 is a factor with levels: [20,35) / [35,37) / [37,39) / [39,45)
baseline is [20,35)
effects are measured as differences in means
effect of gest4 on bweight
number of observations 490
                  Effect 2.5% 97.5%
[35,37) vs [20,35) 857 620 1090
[37,39) vs [20,35) 1360 1180 1540
[39,45) vs [20,35) 1670 1490 1850
Test for no effects of exposure on 3 df: p-value= <2e-16
There are now 3 effect estimates:
[35,37) vs [20,35) 857
[37,39) vs [20,35) 1360
[39,45) vs [20,35) 1668
The command
> stat.table(gest4,mean(bweight),data=births)
 _____
 gest4 mean(bweight)
 [20,35) 1733.74
[35,37) 2590.31
```

```
[37,39)
                3093.77
[39,45)
                3401.26
```

confirms that the effect of agegrp (level 2 vs level 1) is 2590 - 1733 = 857, etc.

9. Compute these estimates by lm() and find out how the coefficients are related to the group means

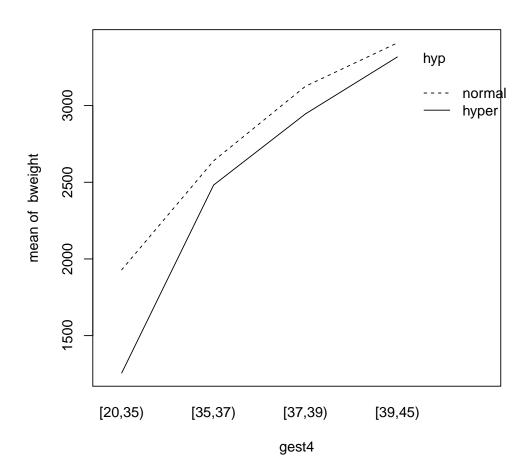
```
> m2 <- lm(bweight ~ gest4, data = births) 
> round( ci.lin(m2)[ , c(1,5,6)] , 1)
                Estimate 2.5% 97.5%
(Intercept)
                  1733.7 1565.3 1902.1
gest4[35,37)
                    856.6 620.3 1092.9
gest4[37,39) 1360.0 1176.7 1543.4
gest4[39,45) 1667.5 1489.4 1845.7
```

#### Stratified effects and interaction or effect 2.8.5 modification

We shall now examine whether and to what extent the effect of hyp on bweight varies by gest4.

10. The following "interaction plot" shows how the mean bweight depends jointly on hyp and gest4

```
> par(mfrow=c(1,1))
> with( births, interaction.plot(gest4, hyp, bweight) )
```



It appears that the mean difference in **bweight** between normotensive and hypertensive mothers is inversely related to gestational age.

11. Let us get numerical values for the mean differences in the different gest4 categories:

```
strata [20,35) level hyper vs normal -673.0 -1040 -307.00
strata [35,37) level hyper vs normal -158.0
                                            -366
strata [37,39) level hyper vs normal -180.0
strata [39,45) level hyper vs normal -91.6
                                            -298
```

Test for effect modification on 3 df: p-value= 0.0553

The estimated effects of hyp in the different strata defined by gest4 thus range from about -100 g among those with  $\geq 39$  weeks of gestation to about -700 g among those with < 35 weeks of gestation. The error margin especially around the latter estimate is quite wide, though. The P-value 0.055 from the test for effect modification indicates weak evidence against the null hypothesis of "no interaction between hyp and gest4". On the other hand, this test may well be not very sensitive given the small number of preterm babies in these data.

12. Stratified estimation of effects can also be done by lm(), and you should get the same results:

```
> m3 <- lm(bweight ~ gest4/hyp, data = births)
> round( ci.lin(m3)[ , c(1,5,6)], 1)
                       Estimate
                                    2.5% 97.5%
(Intercept)
                         1929.1
                                 1732.1 2126.2
gest4[35,37)
                          710.5
                                  431.9 989.2
gest4[37,39)
                         1197.0
                                  984.7 1409.3
gest4[39,45)
                         1479.9 1273.9 1685.8
gest4[20,35):hyphyper -673.0 -1038.8 -307.3
gest4[35,37):hyphyper -158.0 -510.5 194.5
gest4[37,39):hyphyper -180.1 -366.4
                                            6.2
gest4[39,45):hyphyper -91.6 -297.5 114.4
```

13. An equivalent model with an explicit interaction term between gest4 and hyp is fitted as follows

```
> m3I <- lm(bweight ~ gest4 + hyp + gest4:hyp, data = births) > round( ci.lin(m3I)[ , c(1,5,6)], 1)
                        Estimate
                                     2.5% 97.5%
(Intercept)
                          1929.1 1732.1 2126.2
gest4[35,37)
                                   431.9 989.2
                          710.5
                                    984.7 1409.3
gest4[37,39)
                          1197.0
gest4[39,45)
                          1479.9 1273.9 1685.8
hyphyper
                          -673.0 -1038.8 -307.3
gest4[35,37):hyphyper
                          515.0
                                     7.1 1023.0
gest4[37,39):hyphyper
                           492.9
                                     82.5 903.4
gest4[39,45):hyphyper
                           581.5
                                    161.7 1001.2
```

From this output you would find a familiar estimate -673 g for those < 35gestational weeks. The remaining coefficients are estimates of the interaction effects such that e.g. 515 = -158 - (-673) g describes the contrast in the effect of hyp on bweight between those 35 to < 37 weeks and those < 35weeks of gestation.

14. Perhaps a more appropriate reference level for the categorized gestational age would be the highest one. Changing the reference level, here to be the 4th category, can be done by Relevel() function in the Epi package, after which

an equivalent interaction model is fitted, now using a shorter expression for it in the model formula:

```
> births$gest4b <- Relevel( births$gest4, ref = 4)
> m3Ib <- lm(bweight ~ gest4b*hyp, data = births)</pre>
> round( ci.lin(m3Ib)[ , c(1,5,6)], 1)
                      Estimate
                                 2.5%
                                         97.5%
(Intercept)
                        3409.0 3349.1
                                        3468.9
gest4b[20,35)
                        -1479.9 -1685.8 -1273.9
gest4b[35,37)
                        -769.3
                                -975.3
                                        -563.4
                        -282.9 -382.0
gest4b[37,39)
                                        -183.8
hyphyper
                         -91.6 -297.5
                                        114.4
gest4b[20,35):hyphyper
                        -581.5 -1001.2 -161.7
gest4b[35,37):hyphyper
                         -66.4 -474.7
                                         341.8
gest4b[37,39):hyphyper
                         -88.5 -366.3
                                        189.2
```

Notice now the coefficient -91.6 for hyp. It estimates the effect of hyp on bweight among those with  $\geq 39$  weeks of gestation. The estimate -88.5 g = -180.1 - (-91.6) g describes the additional effect of hyp in the category 37 to 38 weeks of gestation upon that in the reference class.

15. At this stage it is interesting to compare the results from the interaction models to those from the corresponding *main effects* model, in which the effect of hyp is assumed not to be modified by gest4:

The estimate -201 g describing the overall effect of hyp is obtained as a weighted average of the stratum-specific estimates obtained by effx() above. It is a meaningful estimate adjusting for gest4 insofar as it is reasonable to assume that the effect of hyp is not modified by gest4. This assumption or the "no interaction" null hypothesis can formally be tested by a common deviance test.

The *P*-value is practically the same as before when the interaction was tested in effx(). However, in spite of obtaining a "non-significant" result from this test, the possibility of a real interaction should not be ignored in this case.

16. Now, use effx() to stratify (i) the effect of hyp on bweight by sex and then (ii) perform the stratified analysis using the two ways of fitting an interaction model with 1m.

```
______
response : bweight
           : metric
exposure : hyp
stratified by : sex
hyp is a factor with levels: normal / hyper
baseline is normal
sex is a factor with levels: M/F
effects are measured as differences in means
effect of hyp on bweight
stratified by sex
number of observations 500
                         Effect 2.5% 97.5%
strata M level hyper vs normal -496 -696 -297
strata F level hyper vs normal -380 -617 -142
Test for effect modification on 1 df: p-value= 0.462
           Estimate 2.5% 97.5%
(Intercept) 3310.7 3230.1 3391.4
             -231.2 -347.2 -115.3
sexF
sexM:hyphyper -496.4 -696.1 -296.6
sexF:hyphyper -379.8 -617.4 -142.2
           Estimate 2.5% 97.5%
(Intercept) 3310.7 3230.1 3391.4
sexF
hyphyper
             -231.2 -347.2 -115.3
```

Look at the results. Is there evidence for the effect of hyp being modified by sex?

#### Controlling or adjusting for the effect of hyp for sex 2.8.6

The effect of hyp is controlled for – or adjusted for – sex by first looking at the estimated effects of hyp in the two stata defined by sex, and then combining these effects if they seem sufficiently similar. In this case the estimated effects were -496 and -380 which look quite similar (and the P-value against "no interaction" was quite large, too), so we can perhaps combine them, and control for sex.

17. The combining is done by declaring sex as a control variable:

-496.4 -696.1 -296.6

sexF:hyphyper 116.6 -193.8 427.0

```
> effx(bweight, type="metric", exposure=hyp, control=sex, data=births)
response : bweight type : metric exposure : hyp
```

```
hyp is a factor with levels: normal / hyper
baseline is normal
effects are measured as differences in means

effect of hyp on bweight
controlled for sex

number of observations 500

Effect 2.5% 97.5%
  -448 -601 -295

Test for no effects of exposure on 1 df: p-value= 9.07e-09
```

18. The same is done with lm() as follows:

The estimated effect of hyp on bweight controlled for sex is thus -448 g. There can be more than one control variable, e.g control=list(sex, agegrp).

Many people go straight ahead and control for variables which are likely to confound the effect of exposure without bothering to stratify first, but usually it is useful to stratify first.

# 2.8.7 Numeric exposures

If we wished to study the effect of gestation time on the baby's birth weight then gestwks is a numeric exposure.

19. Assuming that the relationship of the response with gestwks is roughly linear (for a metric response) we can estimate the linear effect of gestwks, both with effx() and with lm() as follows:

```
2.5% 97.5%
Effect
  197
         180
              214
Test for no effects of exposure on 1 df: p-value= <2e-16
> m5 <- lm(bweight ~ gestwks, data=births); ci.lin(m5)[, c(1,5,6)]
                           2.5%
             Estimate
                                     97.5%
(Intercept) -4489.1398 -5157.2891 -3820.9905
             196.9726 179.7482 214.1971
gestwks
```

We have fitted a simple linear regression model and obtained estimates of the two regression coefficient: intercept and slope. The linear effect of gestwks is thus estimated by the slope coefficient, which is 197 g per each additional week of gestation.

20. You cannot stratify by a numeric variable, but you can study the effects of a numeric exposure stratified by (say) agegrp with

```
> effx(bweight, type="metric", exposure=gestwks, strata=agegrp, data=births)
response : bweight
              : metric
type : metric
exposure : gestwks
stratified by : agegrp
gestwks is numeric
agegrp is a factor with levels: [20,25)/[25,30)/[30,35)/[35,40)/[40,45)
effects are measured as differences in means
effect of an increase of 1 unit in gestwks on bweight
stratified by agegrp
number of observations 490
               Effect 2.5% 97.5%
strata [20,25) 85 -191 361
                  206 167
strata [25,30)
                              245
                  198 171
strata [30,35)
                              225
strata [35,40)
                  202 168
                              235
                  175 124
strata [40,45)
                              226
Test for effect modification on 4 df: p-value= 0.8
```

You can control/adjust for a numeric variable by putting it in the control list.

#### 2.8.8 Checking the assumptions of the linear model

At this stage it will be best to make some visual check concerning our model assumptions using plot(). In particular, when the main argument for the *qeneric* function plot() is a fitted lm object, it will provide you some common diagnostic graphs.

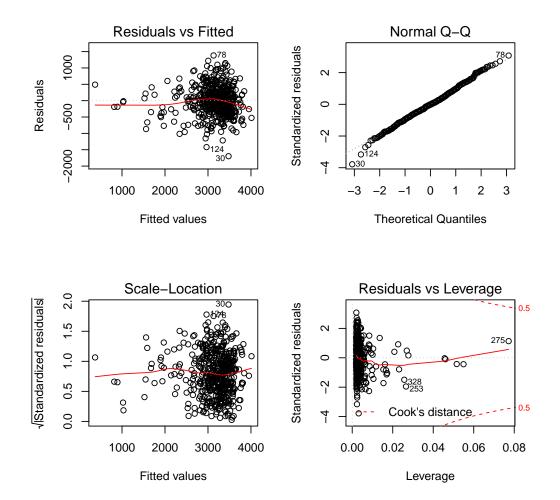
21. To check whether bweight goes up linearly with gestwks try

```
> with(births, plot(gestwks,bweight))
> abline(m5)
```



22. Moreover, take a look at the basic diagnostic plots for the fitted model.

<sup>&</sup>gt; par(mfrow=c(2,2))
> plot(m5)



What can you say about the agreement with data of the assumptions of the simple linear regression model, like linearity of the systematic dependence, homoskedasticity and normality of the error terms?

# 2.8.9 Third degree polynomial of gestwks

A common practice to assess possible deviations from linearity is to compare the fit of the simple model with models having higher order polynomial terms. In perinatal epidemiology a popular model for describing the relationship between gestational age and birth weight is a 3rd degree polynomial.

23. For fitting a third degree polynomial of gestwks we can update our previous simple linear model by adding the quadratic and cubic terms of gestwks using the *insulate* operator I()

- 24. A more elegant way of fitting polynomial models is to utilize *orthogonal* polynomials, which are linear transformations of the original polynomial terms such that they are mutually uncorrelated. However, they are scaled in such a way that the estimated regression coefficients are also difficult to interpret, apart from the intercept term.
- 25. As function poly() creating orthogonal polynomials does not accepet missing values, we shall only include babies whose value of gestwks is not missing. Let us also perform an F test for the null hypothesis of simple linear effect against the 3rd degree polynomial model

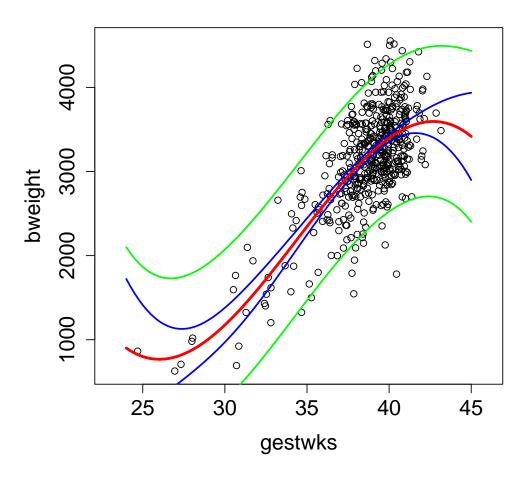
```
> births2 <- subset(births, !is.na(gestwks))</pre>
> m.ortpoly <- lm(bweight ~ poly(gestwks, 3), data= births2 )
> round(ci.lin(m.ortpoly)[, c(1,5,6)], 1)
                  Estimate
                              2.5%
                                     97.5%
                    3138.0 3098.7 3177.4
(Intercept)
poly(gestwks, 3)1 10079.9 9208.9 10950.8
poly(gestwks, 3)2 -740.6 -1611.5
poly(gestwks, 3)3 -1478.5 -2349.4 -607.6
> anova(m5, m.ortpoly)
Analysis of Variance Table
Model 1: bweight ~ gestwks
Model 2: bweight ~ poly(gestwks, 3)
             RSS Df Sum of Sq
                                       Pr(>F)
  Res.Df
   488 98698698
     486 95964282 2 2734416 6.9241 0.001084 **
2
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

Note that the estimated intercept 3138 g has the same value as the mean birth weight among all those babies who are included, i.e. whose gestational age was known.

There seems to be strong evidence against simple linear regression; addition of the quadratic and the cubic term appears to have reduced the residual sum of squares "highly significantly".

26. Irrespective of whether the polynomial terms were orthogonalized or not, the fitted or predicted values for the response variable remain the same. As the next step we shall present graphically the fitted polynomial curve together with 95 % confidence limits for the expected responses as well as 95 % prediction intervals for individual observations in new data comprising gestational weeks from 24 to 45 in steps of 0.25 weeks.

```
> nd <- data.frame(gestwks = seq(24, 45, by = 0.25) )
> fit.poly <- predict( m.ortpoly, newdata=nd, interval="conf" )
> pred.poly <- predict( m.ortpoly, newdata=nd, interval="pred" )
> par(mfrow=c(1,1))
> with( births, plot( bweight ~ gestwks, xlim = c(23, 46), cex.axis= 1.5, cex.lab = > matlines( nd$gestwks, fit.poly, lty=1, lwd=c(3,2,2), col=c('red','blue','blue') )
> matlines( nd$gestwks, pred.poly, lty=1, lwd=c(3,2,2), col=c('red','green','green')
```



The fitted curve fits nicely within the range of observed values of the regressor. However, the tail behaviour in polynomial models tends to be problematic.

We shall continue the analysis in the next practical, in which the apparently curved effect of gestwks is modelled by a *penalized spline*. Also, key details in fitting linear regression models and spline models are covered in the lecture of this afternoon.

# 2.8.10 Extra (if you have time): Frequency data

Data from very large studies are often summarized in the form of frequency data, which records the frequency of all possible combinations of values of the variables in the study. Such data are sometimes presented in the form of a contingency table, sometimes as a data frame in which one variable is the frequency. As an example, consider the UCBAdmissions data, which is one of the standard R data sets, and refers to the outcome of applications to 6 departments in the graduate school at Berkeley by gender.

#### 27. Let us have a look at the data

```
> UCBAdmissions
, , Dept = A
          Gender
          Male Female
  Admitted 512
 Rejected 313
                    19
, , Dept = B
          Gender
           Male Female
Admit
  Admitted 353
                    17
 Rejected 207
, , Dept = C
          Gender
Admit
          Male Female
  Admitted 120
                   202
 Rejected 205
                   391
, , Dept = D
          Gender
          Male Female
Admit
  Admitted 138
                   131
 Rejected 279
                   244
, , Dept = E
          Gender
Admit
           Male Female
  Admitted
            53
 Rejected 138
                   299
, , Dept = F
          Gender
Admit
           Male Female
           22
  Admitted
                    24
 Rejected 351
                   317
```

You can see that the data are in the form of a  $2 \times 2 \times 6$  contingency table for the three variables Admit (admitted/rejected), Gender (male/female), and Dept (A/B/C/D/E/F). Thus in department A 512 males were admitted while 312 were rejected, and so on. The question of interest is whether there is any bias against admitting female applicants.

28. The next command coerces the contingency table to a data frame, and shows the first 10 lines.

```
4 Rejected Female A 19
5 Admitted Male B 353
6 Rejected Male B 207
                                                   19
```

The relationship between the contingency table and the data frame should be

29. Let us turn Admit into a numeric variable coded 1 for rejection, 0 for admission

```
> ucb$Admit <- as.numeric(ucb$Admit)-1</pre>
```

The effect of Gender on Admit is crudely estimated by

```
> effx(Admit,type="binary",exposure=Gender,weights=Freq,data=ucb)
```

```
response : Admit
type : binary
exposure : Gender
```

```
Gender is a factor with levels: Male / Female
baseline is Male
```

effects are measured as odds ratios

```
effect of Gender on Admit
number of observations 24
Effect 2.5% 97.5%
 1.84 1.62 2.09
```

```
Test for no effects of exposure on 1 df: p-value= <2e-16
```

The odds of rejection for female applicants thus appear to be 1.84 times the odds for males (note the use of weights to take account of the frequencies). A crude analysis therefore suggests there is a strong bias against admitting females.

30. Continue the analysis by stratifying the crude analysis by department - does this still support a bias against females? What is the effect of gender controlled for department?

```
response : Admit
type : binary
exposure : Gender
stratified by : Dept
```

```
Gender is a factor with levels: Male / Female
baseline is Male
Dept is a factor with levels: A/B/C/D/E/F
effects are measured as odds ratios
```

```
effect of Gender on Admit
stratified by Dept
```

```
number of observations 24
```

```
### Effect 2.5% 97.5% |

strata A level Female vs Male 0.349 0.209 0.584 |

strata B level Female vs Male 0.803 0.340 1.890 |

strata C level Female vs Male 1.130 0.855 1.500 |

strata D level Female vs Male 0.921 0.686 1.240 |

strata E level Female vs Male 1.220 0.825 1.810 |

strata F level Female vs Male 0.828 0.455 1.510
```

Test for effect modification on 5 df: p-value= 0.00114

\_\_\_\_\_\_

response : Admit type : binary exposure : Gender control vars : Dept

Gender is a factor with levels: Male / Female

baseline is Male

effects are measured as odds ratios

\_\_\_\_\_\_

effect of Gender on Admit controlled for Dept

number of observations 24

Effect 2.5% 97.5% 0.905 0.772 1.060

Test for no effects of exposure on 1 df: p-value= 0.216

# 2.9 Estimation and reporting of curved effects

This exercise deals with modelling of curved effects of continuous explanatory variables both on a metric response assuming the Gaussian distribution and on a count or rate outcome based on the Poisson family.

In the first part we continue our analysis on gestational age on birth weight focusing on fitting spline models, both unpenalized and a penalized one.

In the second part we analyse the testisDK data found in the Epi package. It contains the numbers of cases of testis cancer and mid-year populations (person-years) in 1-year age groups in Denmark during 1943–96. In this analysis we apply Poisson regression on the incidence rates treating age and calendar time, first as categorical but then fitting a penalized spline model.

# 2.9.1 Data births: Simple linear regression and 3rd degree polynomial

Recall what was done in items 17 to 24 of the Exercise on simple estimation of effects, in which a simple linear regression and a 3rd degree polynomial were fitted. The main results are also shown on slides 6, 8, 9, and 20 of the lecture on linear models.

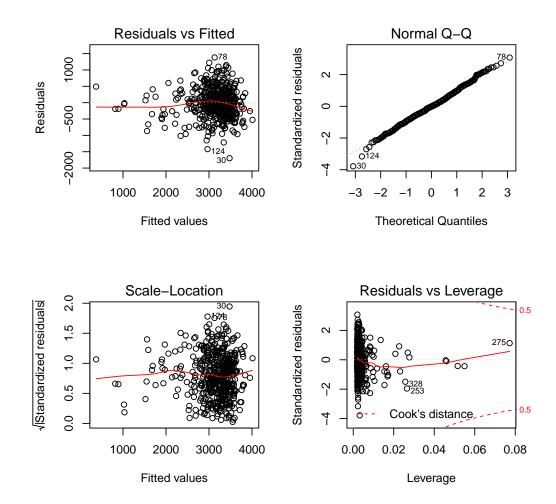
1. Make a basic scatter plot and draw the fitted line from a simple linear regression on it.

```
> library(Epi)
> data(births)
> par(mfrow=c(1,1))
> with(births, plot(gestwks, bweight))
> mlin <- lm(bweight ~ gestwks, data = births )
> abline(mlin)
```



2. Repeat also the diagnostic plots of this simple model

<sup>&</sup>gt; par(mfrow=c(2,2))
> plot(mlin)



Some deviation from the linear model is apparent.

# 2.9.2 Fitting a natural cubic spline

A popular approach for flexible modelling is based on natural regression splines, which have more reasonable tail behaviour than polynomial regression.

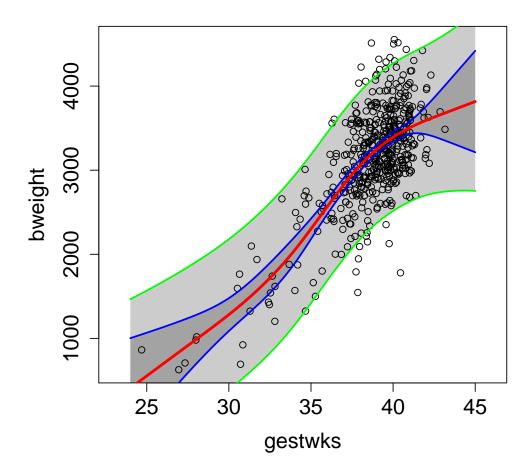
3. By the following piece of code you can fit a *natural cubic spline* with 5 pre-specified knots to be put at 28, 34, 38, 40 and 43 weeks of gestation, respectively, determining the degree of smoothing.

```
> library(splines)
 mNs5 <- lm( bweight ~ Ns( gestwks,
          knots = c(28,34,38,40,43)),
                                       data = births)
> round(ci.lin(mNs5)[ , c(1,5,6)], 1)
                                             Estimate
                                                        2.5%
                                                              97.5%
(Intercept)
                                                987.1
                                                       696.2 1278.1
Ns(gestwks, knots = c(28, 34, 38, 40, 43))1
                                               1996.9 1678.0 2315.8
Ns(gestwks, knots = c(28, 34, 38, 40, 43))2
                                               2234.2 2005.2 2463.2
Ns(gestwks, knots = c(28, 34, 38, 40, 43))3
                                               3271.0 2618.1 3924.0
Ns(gestwks, knots = c(28, 34, 38, 40, 43))4
                                               2265.8 1886.3 2645.3
```

These regression coefficients are even less interpretable than those in the polynomial model.

4. A graphical presentation of the fitted curve together with the confidence and prediction intervals is more informative:

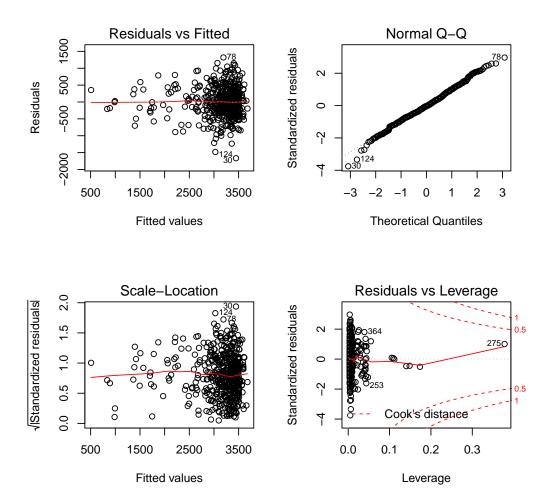
```
> nd <- data.frame(gestwks = seq(24, 45, by = 0.25) )
> fit.Ns5 <- predict( mNs5, newdata=nd, interval="conf" )
> pred.Ns5 <- predict( mNs5, newdata=nd, interval="pred" )
> par(mfrow=c(1,1))
> with(births, plot(bweight ~ gestwks, xlim=c(23, 46),cex.axis= 1.5,cex.lab = 1.5 )
> # matshade gives you semitransparent areas
> matshade( nd$gestwks, fit.Ns5, lwd=2, alpha=0.2 )
> matshade( nd$gestwks, pred.Ns5, lwd=2, alpha=0.2 )
> # matlines puts lines for the intervals
> matlines( nd$gestwks, fit.Ns5, lty=1, lwd=c(3,2,2), col=c('red','blue','blue') )
> matlines( nd$gestwks, pred.Ns5, lty=1, lwd=c(3,2,2), col=c('red','green','green') / pred.Ns5, lty=1, lwd=c(3,2,2), col=c('red','green','green','green') / pred.Ns5, lty=1, lwd=c(3,2,2), col=c('red','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green','green',
```



Compare this with the 3rd order curve previously fitted (see slide 20 of the lecture). In a natural spline the curve is constrained to be linear beyond the extreme knots.

5. Take a look at the basic diagnostic plots from the spline model.

```
> par(mfrow=c(2,2))
> plot(mNs5)
```



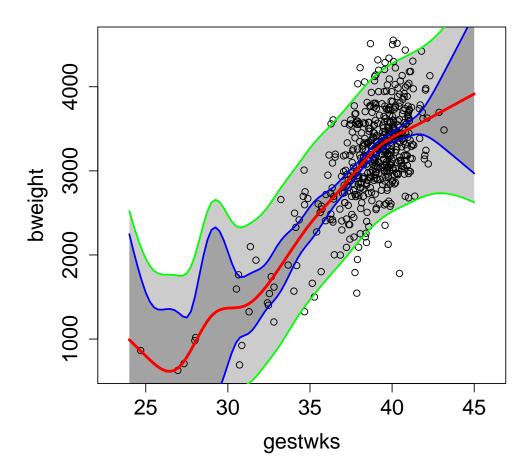
How would you interpret these plots?

The choice of the number of knots and their locations can be quite arbitrary, and the results are often sensitive to these choices.

6. To illustrate arbitrariness and associated problems with specification of knots, you may now fit another natural spline model like the one above but now with 10 knots at the following sequence of points: seq(25, 43, by = 2). Display graphically the results

```
> mNs10 < -lm(bweight ~Ns(gestwks, knots = seq(25, 43, by = 2)),
               data = births)
> round(ci.lin(mNs10)[ , c(1,5,6)], 1)
                                           Estimate
                                                       2.5%
                                                             97.5%
                                                        48.7 1551.1
(Intercept)
                                              799.9
                                              692.5 -1453.2 2838.3
Ns(gestwks, knots = seq(25, 43, by = 2))1
Ns(gestwks, knots = seq(25, 43, by = 2))2
                                              467.2
                                                      -620.5 1554.9
Ns(gestwks, knots = seq(25, 43, by
                                              989.9
                                                         1.8 1978.0
Ns(gestwks, knots = seq(25, 43, by)
                                             1608.1
                                                       762.9 2453.3
Ns(gestwks, knots = seq(25, 43, by
                                             1989.6
                                                      1202.3 2776.9
Ns(gestwks, knots = seq(25, 43, by
                                             2515.0
                                                      1745.8 3284.2
Ns(gestwks, knots = seq(25, 43, by = 2))7
                                             2796.4
                                                     2089.2 3503.7
Ns(gestwks, knots = seq(25, 43, by = 2))8
                                             2508.1
                                                       796.7 4219.4
Ns(gestwks, knots = seq(25, 43, by = 2))9
                                                     2204.7 4030.1
                                             3117.4
```

```
> fit.Ns10 <- predict( mNs10, newdata=nd, interval="conf" )</pre>
> pred.Ns10 <- predict( mNs10, newdata=nd, interval="pred" )</pre>
 par(mfrow=c(1,1))
 with(births, plot(bweight ~ gestwks, xlim = c(23, 46), cex.axis= 1.5, cex.lab =
> matshade( nd$gestwks, fit.Ns10, lwd=2, alpha=0.2 )
> matshade( nd$gestwks, pred.Ns10, lwd=2, alpha=0.2 )
> matlines( nd$gestwks, fit.Ns10, lty=1, lwd=c(3,2,2), col=c('red','blue','blue'))
> matlines( nd$gestwks, pred.Ns10, lty=1, lwd=c(3,2,2), col=c('red','green','green')
```



The behaviour of the curve is really wild for small values of gestwks!

#### 2.9.3 Penalized spline model

One way to go around the arbitrariness in the specification of knots is to fit a penalized spline model, which imposes a "roughness penalty" on the curve. Even though a big number of knots are initially allowed, the resulting fitted curve will be optimally smooth.

You cannot fit a penalized spline model with lm() or glm(), Instead, function gam() in package mgcv can be used for this purpose.

7. You must first install R package mgcv into your computer.

8. When calling gam(), the model formula contains expression 's(X)' for any explanatory variable X, for which you wish to fit a smooth function

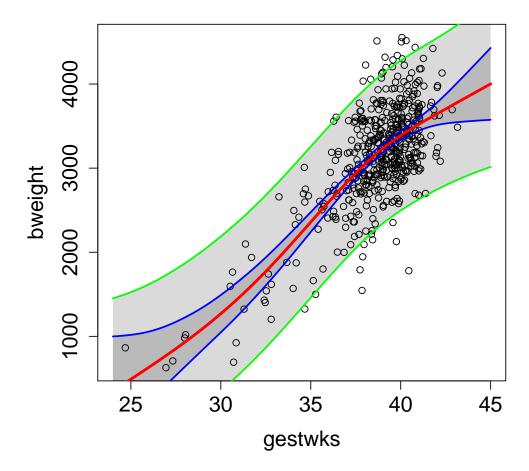
```
> library(mgcv)
> mPs <- gam( bweight ~ s(gestwks), data = births)
> summary(mPs)
Family: gaussian
Link function: identity
Formula:
bweight ~ s(gestwks)
Parametric coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 3138.01
                         20.11
                                  156 <2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
Approximate significance of smooth terms:
            edf Ref.df
                           F p-value
s(gestwks) 3.321 4.189 124.7 <2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
R-sq.(adj) = 0.516
                     Deviance explained = 51.9%
GCV = 1.9995e+05 Scale est. = 1.9819e+05 n = 490
```

From the output given by summary() you find that the estimated intercept is here, too, equal to the overall mean birth weight in the data. The estimated residual variance is given by "Scale est." or from subobject sig2 of the fitted gam object. Taking square root you will obtain the estimated residual standard deviation: 445.2 g.

```
> mPs$sig2
[1] 198186
> sqrt(mPs$sig2)
[1] 445.1808
```

The degrees of freedom in this model are not computed as simply as in previous models, and they typically are not integer-valued. However, the fitted spline seems to consume only a little more degrees of freedom as the 3rd degree polynomial above.

9. As in previous models we shall plot the fitted curve together with 95 % confidence intervals for the mean responses and 95 % prediction intervals for individual responses. Obtaining these quantities from the fitted gam object requires a bit more work than with 1m objects



The fitted curve is indeed clearly more reasonable than the polynomial.

# 2.9.4 Testis cancer: Data input and housekeeping

We shall now switch to analyzing the incidence of testis cancer in Denmark during 1943–1998 by age and calendar time or period.

10. Load the data and inspect its structure:

```
$ P: num 1943 1943 1943 1943 ...
$ D: num 1 1 0 1 0 0 0 0 0 0 ...
$ Y: num 39650 36943 34588 33267 32614 ...
 summary( testisDK )
                   Р
                                 D
      : 0.0 Min. :1943 Min. : 0.000 Min. : 471.7
1st Qu.:22.0 1st Qu.:1956 1st Qu.: 0.000
                                          1st Qu.:18482.2
Median: 44.5 Median: 1970 Median: 1.000
                                         Median :28636.0
Mean :44.5 Mean :1970 Mean : 1.812
                                         Mean :26239.8
                                           3rd Qu.:36785.5
3rd Qu.:67.0 3rd Qu.:1983 3rd Qu.: 2.000
Max. :89.0 Max. :1996 Max. :17.000
                                           Max. :47226.8
> head( testisDK )
 Α
   PD
1 0 1943 1 39649.50
2 1 1943 1 36942.83
3 2 1943 0 34588.33
4 3 1943 1 33267.00
5 4 1943 0 32614.00
6 5 1943 0 32020.33
```

11. There are nearly 5000 observations from 90 one-year age groups and 54 calendar years. To get a clearer picture of what's going one we do some housekeeping. The age range will be limited to 15–79 years, and age and period are both categorised into 5-year intervals – according to the time-honoured practice in epidemiology.

# 2.9.5 Some descriptive analysis

Computation and tabulation of incidence rates

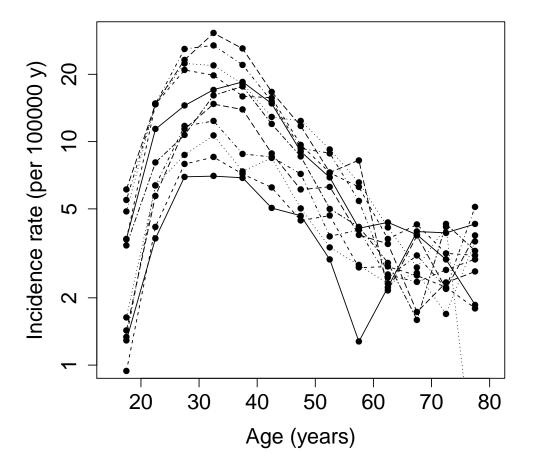
12. Tabulate numbers of cases and person-years, and compute the incidence rates (per 100,000 y) in each  $5 \text{ y} \times 5 \text{ y}$  cell using stat.table()

```
Age [1943,1948) [1948,1953) [1953,1958) [1958,1963) [1963,1968) [1968,1973) [1953,1963] [1953,1963] [1963,1968] [1968,1973] [1953,1963] [1963,1968] [1968,1973] [1953,1963] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1963,1968] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1968,1973] [1
```

[20,25)	30	31	46	49	55	85
	813	745	722	771	960	1054
	3.7	4.2	6.4	6.4	5.7	8.1
[25,30)	55	62	63	82	87	103
	791	782	723	699	765	963
	7.0	7.9	8.7	11.7	11.4	10.7
[30,35)	56	66	82	88	103	124
	799	775	769	712	700	770
	7.0	8.5	10.7	12.4	14.7	16.1
[35,40)	53	56	56	67	99	124
	769	783	760	760	712	702
	6.9	7.2	7.4	8.8	13.9	17.7
[40,45)	35	47	65	64	67	85
	694	754	768	750	757	710
	5.0	6.2	8.5	8.5	8.9	12.0
[45,50)	29	30	37	54	45	64
	622	677	738	753	738	746
	4.7	4.4	5.0	7.2	6.1	8.6
[50,55)	16	28	22	27	46	36
	539	600	654	715	733	718
	3.0	4.7	3.4	3.8	6.3	5.0
[55,60)	6	14	16	25	26	29
	471	513	571	623	681	698
	1.3	2.7	2.8	4.0	3.8	4.2
[60,65)	9	12	11	13	20	18
	403	435	475	528	573	627
	2.2	2.8	2.3	2.5	3.5	2.9
[65,70)	13	9	10	13	8	8
	328	358	386	420	463	501
	4.0	2.5	2.6	3.1	1.7	1.6
[70,75)	9	6	5	7	8	16
	230	269	295	317	342	374
	3.9	2.2	1.7	2.2	2.3	4.3
[75,80]	6	3	7	11	6	8
	140	167	196	215	229	246
	4.3	1.8	3.6	5.1	2.6	3.2
Total	327	371	433	513	585	733
	7375	7601	7851	8236	8703	9070
	4.4	4.9	5.5	6.2	6.7	8.1

Look at the incidence rates in the column margin and in the row margin. In which age group is the marginal age-specific rate highest? Do the period-specific marginal rates have any trend over time?

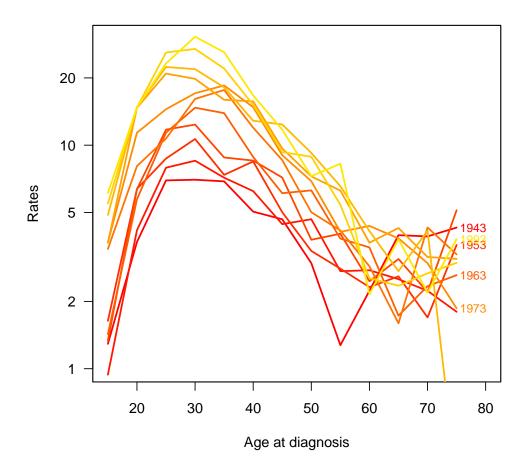
13. From the saved table object tab you can plot an age-incidence curve for each period separately, after you have checked the structure of the table, so that you know the relevant dimensions in it.



There is also a function rateplot that does default plotting of rate tables (see the help page for rateplot):

```
> par( mfrow=c(1,1) )
> rateplot( tab[3,1:nAge,1:nPer], "ap", ylim=c(1,30),
```

```
age = seq(15,75,5), per=seq(1943,1993,5),
col=heat.colors(16), ann=TRUE )
```



Is there any common pattern in the age-incidence curves across the periods?

# 2.9.6 Age and period as categorical factors

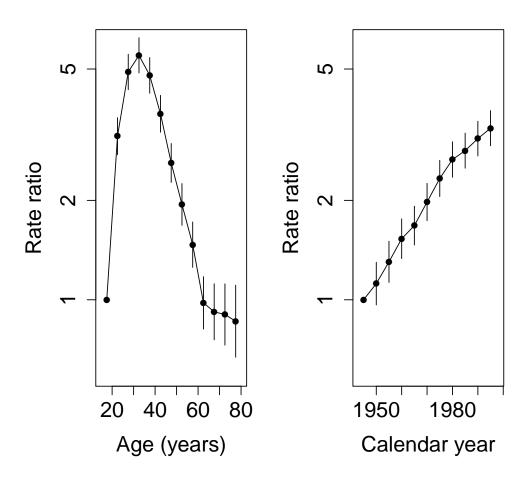
We shall first fit a Poisson regression model with log link on age and period model in the traditional way, in which both factors are treated as categorical. The model is additive on the log-rate scale. It is useful to scale the person-years to be expressed in  $10^5$  y.

```
14. > mCat <- glm(D ~ Age + Per, offset=log(Y/100000), family=poisson, data= tdk)
    > round( ci.exp( mCat ), 2)
                   exp(Est.) 2.5% 97.5%
                        1.47 1.26
    (Intercept)
                                   1.72
   Age[20,25)
                        3.13 2.75
                                    3.56
   Age [25,30)
                        4.90 4.33
   Age [30,35)
                        5.50 4.87
   Age [35,40)
                        4.78 4.22
                        3.66 3.22
   Age [40,45)
                                    4.16
   Age [45,50)
                        2.60 2.27
                                   2.97
```

```
Age [50,55)
                    1.94 1.68
                               2.25
Age [55,60)
                    1.47 1.25
                               1.72
Age [60,65)
                    0.98 0.82
                               1.18
Age [65,70)
                    0.92 0.76
                              1.12
                              1.12
Age [70,75)
                    0.90 0.73
Age[75,80]
                    0.86 0.67
                              1.11
Per[1948,1953)
                    1.12 0.96 1.30
Per[1953,1958)
                    1.30 1.13 1.50
Per[1958,1963)
                    1.53 1.33 1.76
Per[1963,1968)
                    1.68 1.47 1.92
Per[1968,1973)
                    1.98 1.74 2.25
Per[1973,1978)
                    2.33 2.05 2.64
Per[1978,1983)
                    2.66 2.35 3.01
Per[1983,1988)
                    2.83 2.50 3.20
Per[1988,1993)
                    3.08 2.73 3.47
Per[1993,1998]
                   3.31 2.93 3.74
```

What do the estimated rate ratios tell about the age and period effects?

15. A graphical inspection of point estimates and confidence intervals can be obtained as follows. In the beginning it is useful to define shorthands for the pertinent mid-age and mid-period values of the different intervals



16. In the fitted model the reference category for each factor was the first one. As age is the dominating factor, it may be more informative to remove the intercept from the model. As a consequence the age effects describe fitted rates at the reference level of the period factor. For the latter one could choose the middle period 1968-72.

2.16

1.98

0.44

3.18

2.63

2.51

0.51

Age [70,75)

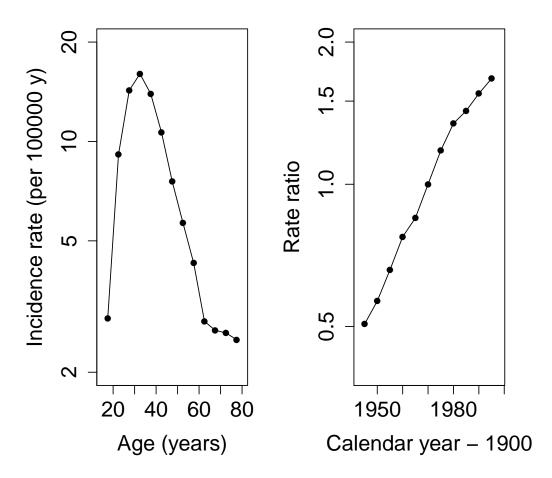
Age [75,80]

Per70[1943,1948)

```
> tdk$Per70 <- Relevel(tdk$Per, ref = 6)
> mCat2 <- glm( D ~ -1 + Age +Per70, offset=log(Y/100000), family=poisson, data= tdk
> round( ci.exp( mCat2 ), 2)
                  exp(Est.)
                              2.5% 97.5%
Age[15,20)
                       2.91
                              2.55 3.33
Age [20,25)
                       9.12
                             8.31 10.01
Age [25,30)
                      14.28 13.11 15.55
Age [30,35)
                      16.03 14.72 17.46
Age [35,40)
                      13.94 12.76 15.23
Age [40,45)
                              9.71 11.71
                      10.66
Age [45,50)
                       7.57
                              6.83
                                    8.39
Age [50,55)
                              5.05
                                    6.36
                       5.67
Age [55,60)
                       4.28
                              3.75
Age [60,65)
                       2.85
                              2.43
                                    3.35
                              2.25
Age [65,70)
                       2.68
```

```
Per70[1948,1953)
                       0.57
                              0.50
                                    0.64
Per70[1953,1958)
                       0.66
                              0.58
                                    0.74
Per70[1958,1963)
                       0.77
                              0.69
                                    0.87
Per70[1963,1968)
                              0.76
                       0.85
                                    0.95
Per70[1973,1978)
                       1.18
                              1.07
                                    1.30
Per70[1978,1983)
                       1.35
                              1.22
                                    1.48
Per70[1983,1988)
                       1.43
                              1.30
                                    1.57
Per70[1988,1993)
                       1.56
                              1.42
                                    1.70
Per70[1993,1998]
                              1.53
                                    1.84
                       1.67
```

We shall plot just the point estimates from the latter model



# 2.9.7 Generalized additive model with penalized splines

It is obvious that the age effect on the log-rate scale is highly non-linear, but it is less clear whether the true period effect deviates from linearity. Nevertheless, there are good indications to try fitting smooth continuous functions for both.

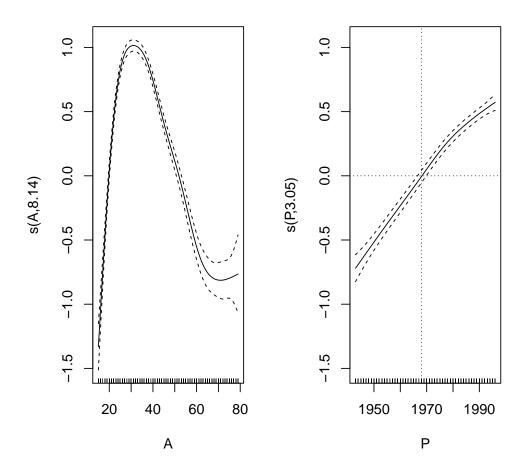
17. As the next task we fit a generalized additive model for the log-rate on continuous age and period applying penalized splines with default settings of function gam() in package mgcv. In this fitting an "optimal" value for the penalty parameter is chosen based on an AIC-like criterion known as UBRE.

```
> library(mgcv)
> mPen <- gam( D ~ s(A) + s(P), offset = log(Y/100000),
            family = poisson, data = tdk)
> summary(mPen)
Family: poisson
Link function: log
Formula:
D \sim s(A) + s(P)
Parametric coefficients:
           Estimate Std. Error z value Pr(>|z|)
(Intercept) 1.70960 0.01793 95.33 <2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Approximate significance of smooth terms:
      edf Ref.df Chi.sq p-value
s(A) 8.143 8.765
                  2560 <2e-16 ***
s(P) 3.046 3.790
                   1054 <2e-16 ***
Signif. codes: 0 '***, 0.001 '**, 0.01 '*, 0.05 '., 0.1 ', 1
R-sq.(adj) = 0.714 Deviance explained = 53.6%
UBRE = 0.082051 Scale est. = 1
                               n = 3510
```

The summary is quite brief, and the only estimated coefficient is the intercept, which sets the baseline level for the log-rates, against which the relative age effects and period effects will be contrasted. On the rate scale the baseline level (per 1000000 y) is obtained by  $\exp(1.7096)$ 

18. See also the default plot for the fitted curves (solid lines) describing the age and the period effects which are interpreted as contrasts to the baseline level on the log-rate scale.

```
> par(mfrow=c(1,2))
> plot(mPen, seWithMean=TRUE)
> abline(v = 1968, lty=3)
> abline(h = 0, lty=3)
```



The dashed lines describe the 95 % confidence band for the pertinent curve. One could get the impression that year 1968 would be some kind of reference value for the period effect, as it was in the categorical model previously fitted. This is not the case, however, because gam() by default parametrizes the spline effects such that the reference level, at which the spline effect is nominally zero, is the overall "grand mean" value of the log-rate in the data. This corresponds to the principle of sum contrasts (contr.sum) for categorical explanatory factors.

From the summary you will also find that the degrees of freedom value required for the age effect is nearly the same as the default dimension k-1=9 of the part of the model matrix (or basis) initially allocated for each smooth function. (Here k refers to the relevant argument that determines the basis dimension when specifying a smooth term by s() in the model formula). On the other hand the period effect takes just about 3 df.

19. It is a good idea to do some diagnostic checking of the fitted model

```
> gam.check(mPen)
```

```
Method: UBRE Optimizer: outer newton full convergence after 7 iterations. Gradient range [-8.706859e-10,1.34696e-06] (score 0.0820511 & scale 1).
```

Method: UBRE

```
Hessian positive definite, eigenvalue range [0.0002209238,0.0003823692].
   Model rank = 19 / 19
   Basis dimension (k) checking results. Low p-value (k-index<1) may
   indicate that k is too low, especially if edf is close to k'.
          k' edf k-index p-value
   s(A) 9.00 8.14 0.93 <2e-16 ***
                   0.95
   s(P) 9.00 3.05
                           0.095 .
   Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
   The four diagnostic plots are analogous to some of those used in the context
   of linear models for Gaussian responses, but not all of them may be as easy
   to interpret. – Pay attention to the note given in the printed output about
   the value of k.
20. Let us refit the model but now with an increased k for age:
   > mPen2 <- gam( D ~ s(A, k=20) + s(P), offset = log(Y/100000),
                family = poisson, data = tdk)
   > summary(mPen2)
   Family: poisson
   Link function: log
   Formula:
   D \sim s(A, k = 20) + s(P)
   Parametric coefficients:
               Estimate Std. Error z value Pr(>|z|)
   (Intercept) 1.70863
                         0.01795 95.17 <2e-16 ***
   Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
   Approximate significance of smooth terms:
           edf Ref.df Chi.sq p-value
   s(A) 11.132 13.406 2553 <2e-16 ***
   s(P) 3.045 3.788 1054 <2e-16 ***
   Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
   R-sq.(adj) = 0.714 Deviance explained = 53.7%
   UBRE = 0.081809 Scale est. = 1
   > gam.check(mPen2)
```

Optimizer: outer newton

Hessian positive definite, eigenvalue range [0.00022158,0.0009322223].

Basis dimension (k) checking results. Low p-value (k-index<1) may indicate that k is too low, especially if edf is close to k'.

0.1 .

Signif. codes: 0 '\*\*\* 0.001 '\*\* 0.01 '\* 0.05 '.' 0.1 ' ' 1

full convergence after 6 iterations.

(score 0.08180917 & scale 1).

Model rank = 29 / 29

s(P) 9.00 3.05

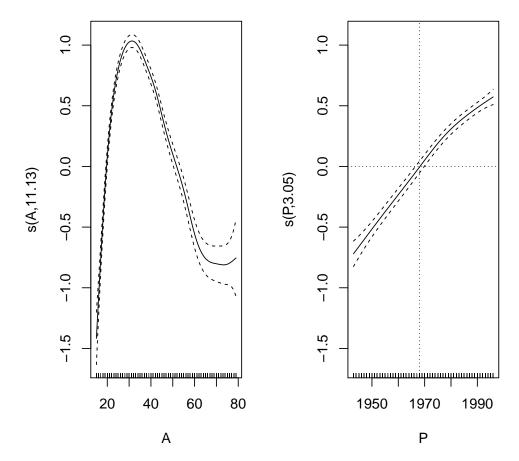
Gradient range [-1.546248e-12,4.091392e-09]

k' edf k-index p-value s(A) 19.00 11.13 0.93 <2e-16 \*\*\*

0.95

With this choice of k the df value for age became about 11, which is well below k-1=19. Let us plot the fitted curves from this fitting, too

```
> par(mfrow=c(1,2))
> plot(mPen2, seWithMean=TRUE)
> abline(v = 1968, lty=3)
> abline(h = 0, lty=3)
```

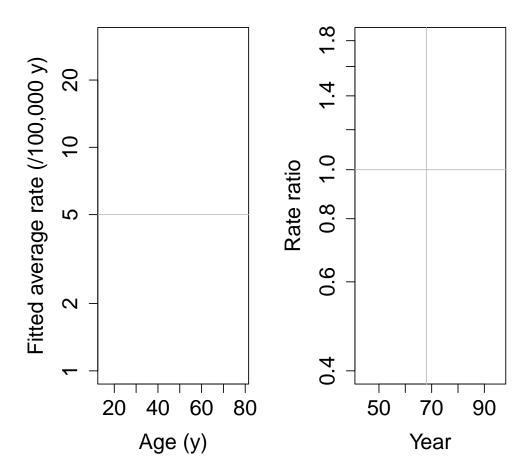


There does not seem to have happened any essential changes from the previously fitted curves, so maybe 8 df could, after all, be quite enough for the age effect.

21. Graphical presentation of the effects can be improved from that supported by plot.gam(). We can, for instance, present the age curve to describe the "mean" incidence rates by age, averaged over the 54 years. For that purpose we need to merge the intercept with the age effect. The period curve will be expressed in terms of rate ratios in relation to the fitted baseline rate, as determined by the model intercept.

In order to produce these plots one needs to extract certain items from the fitted gam object mPen2 and do some calculations. A source script named "plotPenSplines.R" that does all of that can be found from the /R subdirectory on the course website.

```
> source("http://bendixcarstensen.com/SPE/R/plotPenSplines.R")
num [1:66, 1:3] 2.22e-16 2.22e-16 2.22e-16 2.22e-16 2.22e-16 ...
- attr(*, "dimnames")=List of 2
    ..$ : chr [1:66] "1" "2" "3" "4" ...
    ..$ : chr [1:3] "Estimate" "2.5%" "97.5%"
```



One could continue the analysis of these data by fitting an age-cohort model as an alternative to the age-period model, as well as an age-cohort-period model.

## 2.11 Survival analysis: Oral cancer patients

#### 2.11.1 Description of the data

File oralca2.txt, that you may access from a url address to be given in the practical, contains data from 338 patients having an oral squamous cell carcinoma diagnosed and treated in one tertiary level oncological clinic in Finland since 1985, followed-up for mortality until 31 December 2008. The dataset contains the following variables:

#### 2.11.2 Loading the packages and the data

22. Load the R packages Epi, and survival needed in this exercise.

```
> library(Epi)
> library(survival)
```

23. Read the datafile oralca2.txt from a website, whose precise address will be given in the practical, into an R data frame named orca. Look at the head, structure and the summary of the data frame. Using function table() count the numbers of censorings as well as deaths from oral cancer and other causes, respectively, from the event variable.

```
> orca <- read.table("./data/oralca2.txt", header=T)</pre>
> head(orca) ; str(orca) ; summary(orca)
              age stage time event
   Male 65.42274 unkn 5.081
2 Female 83.08783
                    III 0.419
                                  1
                                  2
                     II 7.915
   Male 52.59008
   Male 77.08630
                     I 2.480
   Male 80.33622
                     IV 2.500
6 Female 82.58132
                     IV 0.167
'data.frame':
                     338 obs. of 5 variables:
$ sex : Factor w/ 2 levels "Female", "Male": 2 1 2 2 2 1 2 2 1 2 ...
$ age : num 65.4 83.1 52.6 77.1 80.3 ...
  stage: Factor w/ 5 levels "I", "III", "III", ...: 5 3 2 1 4 4 2 5 4 2 ....
$ time : num 5.081 0.419 7.915 2.48 2.5 ...
  event: int 0 1 2 2 1 2 0 1 1 0 ...
                               stage
                                             time
                                                              event
Female:152
                    :15.15
                              I :50
                                              : 0.085
                                                         Min. :0.0000
             Min.
                                        Min.
                              II :77
Male :186
              1st Qu.:53.24
                                        1st Qu.: 1.333
                                                         1st Qu.:0.0000
                              III:72
             Median :64.86
                                        Median : 3.869
                                                         Median :1.0000
             Mean
                   :63.51
                              IV :68
                                        Mean
                                               : 5.662
                                                         Mean
                                                                 :0.9941
              3rd Qu.:74.29
                              unkn:71
                                        3rd Qu.: 8.417
                                                         3rd Qu.:2.0000
              Max.
                    :92.24
                                        Max.
                                               :23.258
                                                         Max.
                                                                :2.0000
```

#### 2.11.3 Total mortality: Kaplan–Meier analyses

1. We start our analysis of total mortality pooling the two causes of death into a single outcome. First, construct a *survival object* orca\$suob from the event variable and the follow-up time using function Surv(). Look at the structure and summary of orca\$suob.

```
> orca$suob <- Surv(orca$time, 1*(orca$event > 0) )
> str(orca$suob)
 'Surv' num [1:338, 1:2] 5.081+
                                 0.419
                                          7.915
                                                  2.480
                                                          2.500
                                                                  0.167
                                                                          5.925+ 1.5
 - attr(*, "dimnames")=List of 2
  ..$ : NULL
  ..$ : chr [1:2] "time" "status"
 - attr(*, "type")= chr "right"
> summary(orca$suob)
     time
                     status
       : 0.085
                 Min. :0.0000
Min.
1st Qu.: 1.333
                 1st Qu.:0.0000
Median : 3.869
                 Median :1.0000
Mean : 5.662
                 Mean
                         :0.6775
3rd Qu.: 8.417
                 3rd Qu.:1.0000
       :23.258
                 Max.
                         :1.0000
```

2. Create a survfit object s.all, which does the default calculations for a Kaplan–Meier analysis of the overall (marginal) survival curve.

```
> s.all <- survfit(suob ~ 1, data=orca)</pre>
```

- attr(\*, "class")= chr "survfit"

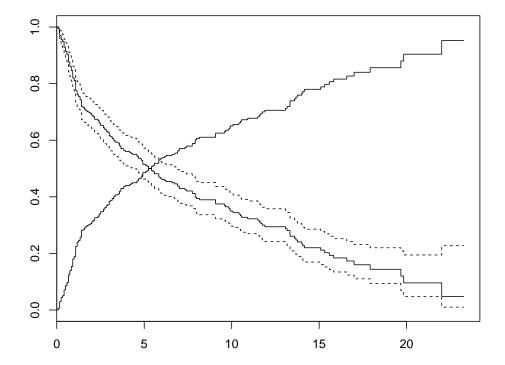
See the structure of this object and apply print() method on it, too. Look at the results; what do you find?

```
> s.all
Call: survfit(formula = suob ~ 1, data = orca)
        events median 0.95LCL 0.95UCL
 338.00 229.00
                  5.42
                          4.33
> str(s.all)
List of 13
           : int 338
 $ n
           : num [1:251] 0.085 0.162 0.167 0.17 0.246 0.249 0.252 0.329 0.334 0.413
 $ time
 $ n.risk : num [1:251] 338 336 334 330 328 327 326 323 322 321 ...
 $ n.event : num [1:251] 2 2 4 2 1 1 3 1 1 1 ...
 $ n.censor : num [1:251] 0 0 0 0 0 0 0 0 0 ...
 $ surv
           : num [1:251] 0.994 0.988 0.976 0.97 0.967 ...
            : chr "right"
  type
 $ std.err : num [1:251] 0.0042 0.00595 0.00847 0.0095 0.00998 ...
 $ lower
           : num [1:251] 0.986 0.977 0.96 0.953 0.949 ...
 $ upper
           : num [1:251] 1 1 0.993 0.989 0.987 ...
 $ conf.type: chr "log"
 $ conf.int : num 0.95
 $ call
           : language survfit(formula = suob ~ 1, data = orca)
```

3. The summary method for a survfit object would return a lengthy life table. However, the plot method with default arguments offers the Kaplan–Meier curve for a conventional illustration of the survival experience in the whole

patient group. Alternatively, instead of graphing survival proportions, one can draw a curve describing their complements: the cumulative mortality proportions. This curve is drawn together with the survival curve as the result of the second command line below.

```
> plot(s.all)
> lines(s.all, fun = "event", mark.time=F, conf.int=F)
```



The effect of option mark.time=F is to omit marking the times when censorings occurred.

#### 2.11.4 Total mortality by stage

Tumour stage is an important prognostic factor in cancer survival studies.

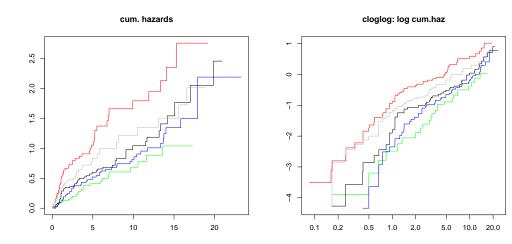
1. Plot separate cumulative mortality curves for the different stage groups marking them with different colours, the order which you may define yourself. Also find the median survival time for each stage.

stage=II	77	51	7.92	4.92	13.34
stage=III	72	51	7.41	3.92	9.90
stage=IV	68	57	2.00	1.08	4.82
stage=unkn	71	45	3.67	2.83	8.17



2. Create now two parallel plots of which the first one describes the cumulative hazards and the second one graphs the log-cumulative hazards against log-time for the different stages. Compare the two presentations with each other and with the one in the previous item.

```
> par(mfrow=c(1,2))
> plot(s.stg, col= col5, fun="cumhaz", main="cum. hazards")
> plot(s.stg, col= col5, fun="cloglog", main = "cloglog: log cum.haz")
```

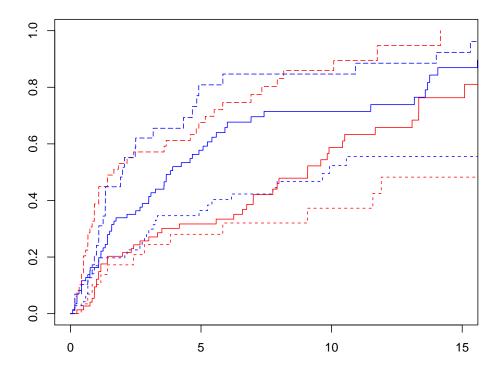


- 3. If the survival times were *exponentially* distributed in a given (sub)population the corresponding cloglog-curve should follow an approximately linear pattern. Could this be the case here in the different stages?
- 4. Also, if the survival distributions of the different subpopulations would obey the *proportional hazards* model, the vertical distance between the cloglog-curves should be approximately constant over the time axis. Do these curves indicate serious deviation from the proportional hazards assumption?
- 5. In the lecture handouts (p. 34, 37) it was observed that the crude contrast between males and females in total mortality appears unclear, but the age-adjustment in the Cox model provided a more expected hazard ratio estimate. We shall examine the confounding by age somewhat closer. First categorize the continuous age variable into, say, three categories by function cut() using suitable breakpoints, like 55 and 75 years, and cross-tabulate sex and age group:

```
> orca$agegr <- cut(orca$age, br=c(0,55,75, 95))</pre>
 stat.table( list( sex, agegr), list( count(), percent(agegr) ),
                margins=T, data = orca )
              -----agegr----
           (0,55] (55,75] (75,95]
                                      Total
 sex
Female
                29
                        74
                                 49
                                        152
             19.1
                      48.7
                               32.2
                                      100.0
                71
Male
                        86
                                 29
                                        186
             38.2
                      46.2
                               15.6
                                      100.0
Total
              100
                       160
                                 78
                                        338
             29.6
                      47.3
                               23.1
                                      100.0
```

Male patients are clearly younger than females in these data. Now, plot Kaplan–Meier curves jointly classified by sex and age.

```
> s.agrx <- survfit(suob ~ agegr + sex, data=orca)
> par(mfrow=c(1,1))
```



In each ageband the mortality curve for males is on a higher level than that for females.

#### 2.11.5 Event-specific cumulative mortality curves

We move on to analysing cumulative mortalities for the two causes of death separately, first overall and then by prognostic factors.

1. Use the survfit-function in survival package with option type="mstate".

```
> cif1 <- survfit( Surv( time, event, type="mstate") ~ 1,</pre>
                   data = orca)
> str(cif1)
List of 18
 $ n
              : int 338
 $ time
              : num [1:251] 0.085 0.162 0.167 0.17 0.246 0.249 0.252 0.329 0.334 0.4
 $ n.risk
              : int [1:251, 1:3] 0 0 0 0 0 0 0 0 0 0 ...
 $ n.event
              : int [1:251, 1:3] 2 2 2 1 1 0 2 1 1 1 ...
              : int [1:251] 0 0 0 0 0 0 0 0 0 0 ...
 $ n.censor
 $ pstate
              : num [1:251, 1:3] 0.00592 0.01183 0.01775 0.02071 0.02367 ...
 $ p0
              : num [1:3(1d)] 0 0 1
  ..- attr(*, "dimnames")=List of 1
  .. ..$ : chr [1:3] "1" "2" ""
            : num [1:3, 1:3, 1:251] 0 0 0.00592 0 0 ...
```

```
$ std.err : num [1:251, 1:3] 0.00417 0.00588 0.00718 0.00775 0.00827 ...
$ sp0 : num [1:3] 0 0 0
$ transitions: 'table' int [1:3, 1:2] 0 0 122 0 0 107
..- attr(*, "dimnames")=List of 2
....$ from: chr [1:3] "1" "2" ""
 ....$ to : chr [1:2] "1" "2"
        : num [1:251, 1:3] 0.00149 0.00447 0.00803 0.00995 0.01193 ...
$ lower
          : num [1:251, 1:3] 0.0236 0.0313 0.0392 0.0431 0.0469 ...
$ upper
$ conf.type : chr "log"
$ conf.int : num 0.95
$ states : chr [1:3] "1" "2" ""
- attr(*, "class")= chr [1:2] "survfitms" "survfit"
```

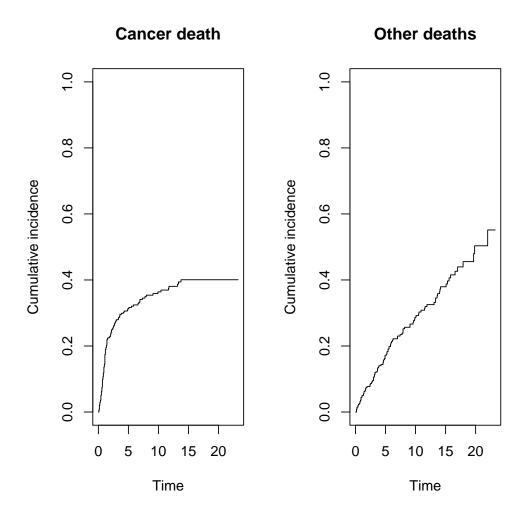
2. One could apply here the plot method of the survfit object to plot the cumulative incidences for each cause. However, we suggest that you use instead a simple function plotCIF() found in the Epi package. The main arguments are

```
data = data frame created by function survfit(),
                                                           (2.1)
event = indicator for the event: values 1 or 2.
                                                           (2.2)
```

Other arguments are like in the ordinary plot() function.

3. Draw two parallel plots describing the overall cumulative incidence curves for both causes of death

```
> par(mfrow=c(1,2))
> plotCIF(cif1, 1, main = "Cancer death")
> plotCIF(cif1, 2, main= "Other deaths")
```

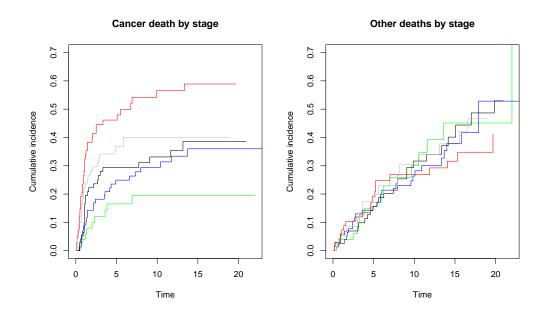


4. Compute the estimated cumulative incidences by stage for both causes of death. Now you have to add variable stage to survfit-function.

See the structure of the resulting object, in which you should observe strata variable containing the stage grouping variable. Plot the pertinent curves in two parallel graphs. Cut the y-axis for a more efficient graphical presentation

```
> col5 <- c("green", "blue", "black", "red", "gray")
 cif2 <- survfit( Surv( time, event, type="mstate") ~ stage,</pre>
                   data = orca)
 str(cif2)
List of 19
              : int [1:5] 50 77 72 68 71
 $ n
              : num [1:307] 0.17 0.498 0.665 0.832 1.166 ...
 $
  time
              : int [1:307, 1:3] 0 0 0 0 0 0 0 0 0 0 ...
              : int [1:307, 1:3] 0 1 1 0 1 1 0 1 1 0 ...
 $ n.event
              : int [1:307] 0 0 0 0 0 0 1 0 0 0 ...
 $ n.censor
 $ pstate
              : num [1:307, 1:3] 0 0.02 0.04 0.04 0.06 ...
              : num [1:5, 1:3] 0 0 0 0 0 0 0 0 0 0 ...
  p0
  ..- attr(*, "dimnames")=List of 2
     ..$ : chr [1:5] "stage=I" "stage=II" "stage=III" "stage=IV" ...
    ..$ : chr [1:3] "1" "2" ""
 $ transitions: 'table' int [1:3, 1:2] 0 0 122 0 0 107
  ..- attr(*, "dimnames")=List of 2
  ....$ from: chr [1:3] "1" "2" ""
```

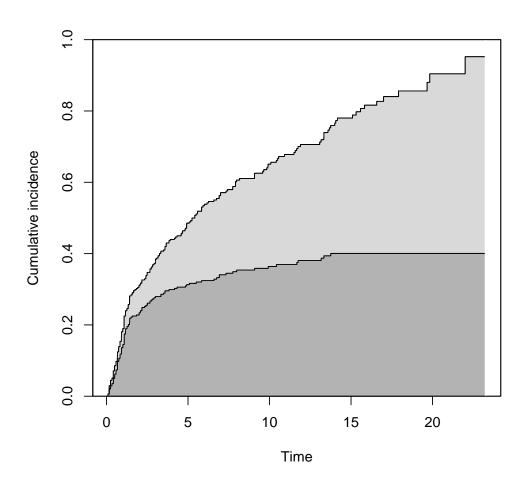
```
: chr [1:2] "1" "2"
  .. ..$ to
              : Named int [1:5] 49 75 62 58 63
  ..- attr(*, "names")= chr [1:5] "stage=I" "stage=II" "stage=III" "stage=IV"
             : num [1:307, 1:3] 0 0.0198 0.0277 0.0277 0.0336 ...
$
  sp0
              : num [1:5, 1:3] 0 0 0 0 0 0 0 0 0 0 ...
$
              : num [1:3, 1:3, 1:307] 0 0 0 0 0 0.02 0 0 -0.02 0 ...
  cumhaz
              : num [1:307, 1:3] NA 0.00287 0.01029 0.01029 0.02003 ...
  lower
              : num [1:307, 1:3] NA 0.139 0.156 0.156 0.18 ...
  upper
             : chr "log"
  conf.type
  conf.int
             : num 0.95
              : chr [1:3] "1" "2" ""
  states
              : chr "mright"
  type
             : language survfit(formula = Surv(time, event, type = "mstate") ~ stage
  attr(*, "class")= chr [1:2] "survfitms" "survfit"
 par(mfrow=c(1,2))
 plotCIF(cif2, 1, main = "Cancer death by stage",
          col = col5, ylim = c(0, 0.7))
> plotCIF(cif2, 2, main= "Other deaths by stage",
          col = col5, ylim = c(0, 0.7))
```



Compare the two plots. What would you conclude about the effect of stage on the two causes of death ?

5. Using another function stackedCIF() in Epi you can put the two cumulative incidence curves in one graph but stacked upon one another such that the lower curve is for the cancer deaths and the upper curve is for total mortality, and the vertical difference between the two curves describes the cumulative mortality from other causes. You can also add some colours for the different zones:

```
> par(mfrow=c(1,1))
> stackedCIF(cif1,colour = c("gray70", "gray85"))
```



### 2.11.6 Regression modelling of overall mortality.

1. Fit the semiparametric proportional hazards regression model, a.k.a. the Cox model, on all deaths including sex, age and stage as covariates. Use function coxph() in package survival. It is often useful to center and scale continuous covariates like age here. The estimated rate ratios and their confidence intervals can also here be displayed by applying ci.lin() on the fitted model object.

```
> options(show.signif.stars = F)
> m1 <- coxph(suob ~ sex + I((age-65)/10) + stage, data= orca)
> summary( m1 )
Call:
coxph(formula = suob \sim sex + I((age - 65)/10) + stage, data = orca)
 n= 338, number of events= 229
                    coef exp(coef) se(coef)
                                                 z Pr(>|z|)
                                    0.14139 2.485 0.012947
sexMale
                 0.35139
                            1.42104
I((age - 65)/10) 0.41603
                                     0.05641 7.375 1.65e-13
                            1.51593
stageII
                 0.03492
                            1.03554
                                     0.24667 0.142 0.887421
stageIII
                 0.34545
                            1.41262
                                    0.24568 1.406 0.159708
```

```
stageIV
                   0.88542
                              2.42399 0.24273 3.648 0.000265
stageunkn
                   0.58441
                              1.79393 0.25125 2.326 0.020016
                   exp(coef) exp(-coef) lower .95 upper .95
                                                          1.875
sexMale
                       1.421 0.7037
                                           1.0771
I((age - 65)/10)
                       1.516
                                  0.6597
                                              1.3573
                                                          1.693

    1.516
    0.6597
    1.3573

    1.036
    0.9657
    0.6386

    1.413
    0.7079
    0.8728

    2.424
    0.4125
    1.5063

stageII
                                                          1.679
stageIII
                                                           2.286
                                 0.4125 1.5063
0.5574 1.0963
                                                           3.901
stageIV
                       1.794
stageunkn
                                                           2.935
Concordance= 0.674 (se = 0.021)
Rsquare= 0.226 (max possible= 0.999)
Likelihood ratio test= 86.76 on 6 df, p=<2e-16
                       = 80.5 on 6 df,
                                             p=3e-15
Wald test
Score (logrank) test = 82.86 on 6 df,
                                              p=9e-16
> round( ci.exp(m1 ), 4 )
                   exp(Est.)
                                2.5% 97.5%
sexMale
                      1.4210 1.0771 1.8748
I((age - 65)/10)
                      1.5159 1.3573 1.6932
                      1.0355 0.6386 1.6793
stageII
                      1.4126 0.8728 2.2864
stageIII
                      2.4240 1.5063 3.9007
stageIV
                      1.7939 1.0963 2.9354
stageunkn
```

Look at the results. What are the main findings?

2. Check whether the data are sufficiently consistent with the assumption of proportional hazards with respect to each of the variables separately as well as globally, using the cox.zph() function.

3. No evidence against proportionality assumption could apparently be found. Moreover, no difference can be observed between stages I and II in the estimates. On the other hand, the group with stage unknown is a complex mixture of patients from various true stages. Therefore, it may be prudent to exclude these subjects from the data and to pool the first two stage groups into one. After that fit a model in the reduced data with the new stage variable.

```
st3III 1.3657 0.9547 1.9536
st3IV 2.3900 1.6841 3.3919
```

4. Plot the predicted cumulative mortality curves by stage, jointly stratified by sex and age, focusing only on 40 and 80 year old patients, respectively, based on the fitted model m2. You need to create a new artificial data frame containing the desired values for the covariates.

```
> newd <- data.frame( sex = c( rep("Male", 6), rep("Female", 6) ),
                     age = rep(c(rep(40, 3), rep(80, 3)), 2),
                     st3 = rep(levels(orca2\$st3), 4))
+
> newd
      sex age st3
    Male 40 I-II
1
2
    Male 40 III
    Male 40
3
               IV
    Male 80 I-II
    Male 80 III
    Male 80
7
  Female 40 I-II
  Female 40 III
8
9 Female 40
10 Female 80 I-II
11 Female 80 III
12 Female 80
               TV
> col3 <- c("green", "black", "red")
> par(mfrow=c(1,2))
 plot( survfit(m2, newdata= subset(newd, sex=="Male" & age==40)),
       col=col3, fun="event", mark.time=F)
> lines( survfit(m2, newdata= subset(newd, sex=="Female" & age==40)),
       col= col3, fun="event", lty = 2, mark.time=F)
> plot( survfit(m2, newdata= subset(newd, sex=="Male" & age==80)),
      ylim = c(0,1), col= col3, fun="event", mark.time=F)
> lines( survfit(m2, newdata= subset(newd, sex=="Female" & age==80)),
        col=col3, fun="event", lty=2, mark.time=F)
```

# 2.11.7 Modelling event-specific hazards and hazards of the subdistribution

1. Fit the Cox model for the cause-specific hazard of cancer deaths with the same covariates as above. In this case only cancer deaths are counted as events and deaths from other causes are included into censorings.

```
> m2haz1 <- coxph( Surv( time, event==1) ~ sex + I((age-65)/10) + st3 , data=orca2 .
> round( ci.exp(m2haz1 ), 4)
                 exp(Est.)
                            2.5% 97.5%
                    1.0171 0.6644 1.5569
sexMale
I((age - 65)/10)
                    1.4261 1.2038 1.6893
st3III
                    1.5140 0.9012 2.5434
                    3.1813 1.9853 5.0978
st3IV
> cox.zph(m2haz1)
                     rho chisq
sexMale
                  0.0651 0.405 0.5246
I((age - 65)/10) 0.2355 6.001 0.0143
```

```
      st3III
      -0.1120 1.174 0.2785

      st3IV
      -0.1858 3.163 0.0753

      GLOBAL
      NA 9.352 0.0529
```

Compare the results with those of model m2. What are the major differences?

2. Fit a similar model for deaths from other causes and compare the results.

```
> m2haz2 <- coxph( Surv( time, event==2) ~ sex + I((age-65)/10) + st3 , data=orca2 .
> round( ci.exp(m2haz2 ), 4)
                 exp(Est.)
                            2.5% 97.5%
sexMale
                    1.8103 1.1528 2.8431
I((age - 65)/10)
                    1.4876 1.2491 1.7715
st3III
                    1.2300 0.7488 2.0206
st3IV
                    1.6407 0.9522 2.8270
> cox.zph(m2haz2)
                      rho
                            chisq
                -0.04954 0.22019 0.639
sexMale
I((age - 65)/10) 0.03484 0.10107 0.751
st3III
                 0.01369 0.01639 0.898
st3IV
                 -0.00411 0.00149 0.969
GLOBAL
                       NA 0.45596 0.978
```

3. Finally, fit the Fine-Gray model for the hazard of the subdistribution for cancer deaths with the same covariates as above. For this you have to first load package cmprsk, containing the necessary function crr(), and attach the data frame.

```
> library(cmprsk)
> attach(orca2)
> m2fg1 <- crr(time, event, cov1 = model.matrix(m2), failcode=1)</pre>
> summary(m2fg1, Exp=T)
Competing Risks Regression
crr(ftime = time, fstatus = event, cov1 = model.matrix(m2), failcode = 1)
                    coef exp(coef) se(coef)
                                                  z p-value
                 -0.0808 0.922
                                    0.2118 -0.381 7.0e-01
sexMale
I((age - 65)/10) 0.2791
                                      0.0918 3.039 2.4e-03
                              1.322
st3III
                  0.3739
                             1.453
                                     0.2588 1.445 1.5e-01
st3IV
                  1.0346
                             2.814
                                      0.2327 4.446 8.8e-06
                 \exp(\text{coef}) \exp(-\text{coef}) = 2.5\% 97.5\%
sexMale
                     0.922
                                1.084 0.609 1.40
I((age - 65)/10)
                     1.322
                                0.756 1.104 1.58
                     1.453
                                0.688 0.875 2.41
st3III
st3IV
                     2.814
                                 0.355 1.783 4.44
Num. cases = 267
Pseudo Log-likelihood = -493
Pseudo likelihood ratio test = 32.1 on 4 df,
```

Compare the results with those of model m2 and m2haz1.

4. Fit a similar model for deaths from other causes and compare the results.

```
> m2fg2 <- crr(time, event, cov1 = model.matrix(m2), failcode=2)
> summary(m2fg2, Exp=T)
```

```
Num. cases = 267
Pseudo Log-likelihood = -438
Pseudo likelihood ratio test = 9.43 on 4 df,
```

#### 2.11.8 Analysis of relative survival

1. Load package popEpi for the estimation of relative survival. Use the (simulated) female Finnish breast cancer patients diagnosed between 1993-2012, called sibr.

```
> library(popEpi)
> head(sibr)
   sex
             bi_date
                            dg_date
                                          ex_date status
                                                                 dg_age
    1 1932-08-20 2009-06-12 2012-12-31 0 76.80996
1:
      1 1950-02-10 L

1 1915-06-11 2002-05-26 2003-01 00

1 1936-02-11 2012-10-12 2012-12-31

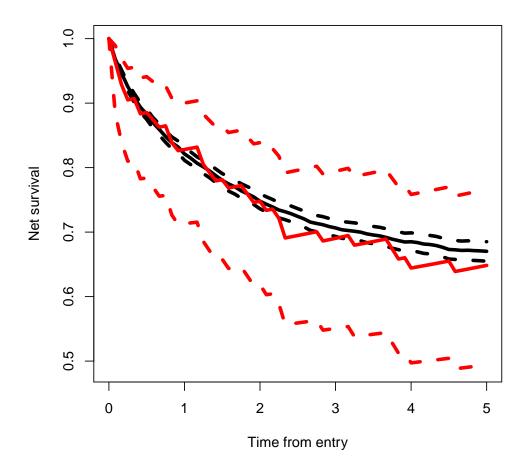
1 1936-02-11 1993-06-21 2012-12-31

1 1931-12-31
      1 1950-02-19 2002-03-08 2012-12-31
                                                          0 52.04658
      1 1950-02-19 2002-03-08 2012-12-31
1 1915-06-11 2002-05-26 2003-01-30
                                                          1 86.95616
                                                          0 76.66667
                                                         0 58.54247
      1 1956-01-09 2002-08-15 2012-12-31
                                                          0 46.59732
```

2. Prepare the data by using lexpand command in the popEpi package, define follow-up time intervals, (calendar time) period that you are interested and where are the population mortality figures. Calculate 5-year observed survival (2008-2012) using period method by Ederer II (default)

```
> ## pretend some are male
> set.seed(1L)
> sire$sex <- rbinom(nrow(sire), 1, 0.01)
> BL <- list(fot = seq(0, 5, 1/12))
> x <- lexpand(sire,
+ birth = bi_date,
+ entry = dg_date,
+ exit = ex_date,
+ status = status,
+ breaks = BL,
+ pophaz = popmort,
+ aggre = list(sex, fot))</pre>
```

3. Calculate 5-year relative survival (2008-2012) using period method by Ederer II (default)



### 2.11.9 Lexis object with multi-state set-up

Before entering to analyses of cause-specific mortality it might be instructive to apply some Lexis tools to illustrate the competing-risks set-up. More detailed explanation of these tools will be given by Bendix in this afternoon.

1. Form a Lexis object from the data frame and print a summary of it. We shall name the main (and only) time axis in this object as stime.

```
NOTE: entry.status has been set to "Alive" for all.
NOTE: entry is assumed to be 0 on the stime timescale.
> summary(orca.lex)
Transitions:
     To
        Alive Oral ca. death Other death Records:
                                                    Events: Risk time:
  Alive
                                     107
                                               338
                                                        229
                                                               1913.67
Transitions:
    To
From
        Persons:
 Alive
              338
```

2. Draw a box diagram of the two-state set-up of competing transitions. Run first the following command line

```
boxes( orca.lex )
```

Now, move the cursor to the point in the graphics window, at which you wish to put the box for "Alive", and click. Next, move the cursor to the point at which you wish to have the box for "Oral ca. death", and click. Finally, do the same with the box for "Other death". If you are not happy with the outcome, run the command line again and repeat the necessary mouse moves and clicks.

#### 2.11.10Poisson regression as an alternative to Cox model

It can be shown that the Cox model with an unspecified form for the baseline hazard  $\lambda_0(t)$  is mathematically equivalent to the following kind of Poisson regression model. Time is treated as a categorical factor with a dense division of the time axis into disjoint intervals or timebands such that only one outcome event occurs in each timeband. The model formula contains this time factor plus the desired explanatory terms.

A sufficient division of time axis is obtained by first setting the break points between adjacent timebands to be those time points at which an outcome event has been observed to occur. Then, the pertinent lexis object is created and after that it will be split according to those breakpoints. Finally, the Poisson regression model is fitted on the splitted lexis object using function glm() with appropriate specifications.

We shall now demonstrate the numerical equivalence of the Cox model m2haz1 for oral cancer mortality that was fitted above, and the corresponding Poisson regression.

1. First we form the necessary lexis object by just taking the relevant subset of the already available orca.lex object. Upon that the three-level stage factor st3 is created as above.

```
> orca2.lex <- subset(orca.lex, stage != "unkn" )</pre>
> orca2.lex$st3 <- Relevel( orca2$stage, list(1:2, 3, 4:5) )</pre>
> levels(orca2.lex$st3) = c("I-II", "III", "IV")
```

0.419

Then, the break points of time axis are taken from the sorted event times, and the lexis object is split by those breakpoints. The timeband factor is defined according to the splitted survival times stored in variable stime.

```
> cuts <- sort(orca2$time[orca2$event==1])</pre>
> orca2.spl <- splitLexis( orca2.lex, br = cuts, time.scale="stime" )</pre>
> orca2.spl$timeband <- as.factor(orca2.spl$stime)</pre>
```

As a result we now have an expanded lexis object in which each subject has several rows; as many rows as there are such timebands during which he/she is still at risk. The outcome status lex.Xst has value 0 in all those timebands, over which the subject stays alive, but assumes the value 1 or 2 at his/her last interval ending at the time of death. – See now the structure of the splitted object.

#### > str(orca2.spl)

```
Classes 'Lexis' and 'data.frame':
                                           12637 obs. of 14 variables:
 $ lex.id : int 2 2 2 2 2 2 3 3 3 3 ...
           : num 0 0.085 0.162 0.252 0.329 0.413 0 0.085 0.162 0.252 ...
  lex.dur: num 0.085 0.077 0.09 0.077 0.084 0.006 0.085 0.077 0.09 0.077
  lex.Cst : Factor w/ 3 levels "Alive", "Oral ca. death", ...: 1 1 1 1 1 1 1 1 1 1 1 ... lex.Xst : Factor w/ 3 levels "Alive", "Oral ca. death", ...: 1 1 1 1 1 2 1 1 1 1 ...
           : Factor w/ 2 levels "Female", "Male": 1 1 1 1 1 2 2 2 2 ...
  age
           : num 83.1 83.1 83.1 83.1 83.1 ...
 $ stage
           : Factor w/ 5 levels "I", "II", "III", ...: 3 3 3 3 3 2 2 2 2 2 ...
 $ time
           : num 0.419 0.419 0.419 0.419 ...
 $ event
          : int 1 1 1 1 1 1 2 2 2 2 ...
           : 'Surv' num [1:12637, 1:2] 0.419
                                                         0.419
                                                                   0.419
 $ suob
                                                  0.419
                                                                            0.419
  ..- attr(*, "dimnames")=List of 2
  ....$ : NULL
  .. ..$ : chr "time" "status"
  ..- attr(*, "type")= chr "right"
 $ agegr
           : Factor w/ 3 levels "(0,55]","(55,75]",...: 3 3 3 3 3 3 1 1 1 1 ...
           : Factor w/ 3 levels "I-II", "III", "IV": 2 2 2 2 2 1 1 1 1 ...
 \$ timeband: Factor w/ 72 levels "0","0.085","0.162",...: 1 2 3 4 5 6 1 2 3 4 ...
 - attr(*, "breaks")=List of 1
  ..$ stime: num 0.085 0.162 0.252 0.329 0.413 0.419 0.496 0.498 0.504 0.58 ...
 - attr(*, "time.scales")= chr "stime"
 - attr(*, "time.since")= chr ""
> orca2.spl[ 1:20, ]
   lex.id stime lex.dur lex.Cst
                                         lex.Xst
                                                    sex
                                                              age stage time
1
        2 0.000
                  0.085
                           Alive
                                           Alive Female 83.08783
                                                                    III 0.419
        2 0.085
                  0.077
                           Alive
                                                                    III 0.419
2
                                           Alive Female 83.08783
3
        2 0.162
                  0.090
                           Alive
                                           Alive Female 83.08783
                                                                    III 0.419
4
        2 0.252
                  0.077
                           Alive
                                           Alive Female 83.08783
                                                                    III 0.419
        2 0.329
5
                  0.084
                          Alive
                                           Alive Female 83.08783
                                                                    III 0.419
        2 0.413
6
                  0.006
                          Alive Oral ca. death Female 83.08783
                                                                    III 0.419
7
        3 0.000
                  0.085
                           Alive
                                           Alive
                                                   Male 52.59008
                                                                     II 7.915
8
        3 0.085
                                                                     II 7.915
                  0.077
                           Alive
                                           Alive
                                                   Male 52.59008
9
        3 0.162
                  0.090
                           Alive
                                           Alive
                                                   Male 52.59008
                                                                     II 7.915
                                                                     II 7.915
10
        3 0.252
                  0.077
                           Alive
                                                   Male 52.59008
                                           Alive
                                                                     II 7.915
        3 0.329
11
                  0.084
                           Alive
                                           Alive
                                                   Male 52.59008
12
        3 0.413
                  0.006
                           Alive
                                                   Male 52.59008
                                                                     II 7.915
                                           Alive
        3 0.419
                                                                     II 7.915
13
                  0.077
                           Alive
                                           Alive
                                                   Male 52.59008
        3 0.496
                                                                     II 7.915
14
                  0.002
                           Alive
                                           Alive
                                                   Male 52.59008
15
        3 0.498
                  0.006
                           Alive
                                           Alive
                                                   Male 52.59008
                                                                     II 7.915
16
        3 0.504
                  0.076
                           Alive
                                                   Male 52.59008
                                                                     II 7.915
                                           Alive
```

```
17
         3 0.580
                   0.003
                            Alive
                                            Alive
                                                     Male 52.59008
                                                                        II 7.915
18
        3 0.583
                   0.003
                            Alive
                                            Alive
                                                     Male 52.59008
                                                                        II 7.915
19
        3 0.586
                   0.003
                            Alive
                                            Alive
                                                     Male 52.59008
                                                                        II 7.915
20
        3 0.589
                   0.076
                                                     Male 52.59008
                                                                        II 7.915
                            Alive
                                            Alive
   event
           suob
                   agegr
                           st3 timeband
       1 0.419
                 (75,95]
                           III
1
2
       1 0.419
                 (75,95]
                                   0.085
                           III
                 (75,95]
3
       1 0.419
                           III
                                   0.162
                 (75,95]
4
       1 0.419
                           III
                                   0.252
                 (75,95]
5
       1 0.419
                           III
                                   0.329
                 (75,95]
6
       1 0.419
                           III
                                   0.413
7
       2 7.915
                  (0.55] I-II
8
       2 7.915
                  (0.55] I-II
                                   0.085
       2 7.915
                  (0,55] I-II
9
                                   0.162
                  (0,55] I-II
10
       2 7.915
                                   0.252
11
       2 7.915
                  (0,55] I-II
                                   0.329
       2 7.915
12
                  (0,55] I-II
                                   0.413
13
       2 7.915
                  (0,55] I-II
                                   0.419
       2 7.915
14
                  (0,55] I-II
                                   0.496
       2 7.915
                  (0,55] I-II
15
                                   0.498
       2 7.915
16
                  (0,55] I-II
                                   0.504
       2 7.915
17
                  (0,55] I-II
                                   0.58
       2 7.915
                  (0,55] I-II
18
                                   0.583
       2 7.915
19
                  (0,55] I-II
                                   0.586
20
       2 7.915
                  (0,55] I-II
                                   0.589
```

2. We are ready to fit the desired Poisson model for oral cancer death as the outcome. The splitted person-years are contained in lex.dur, and the explanatory variables are the same as in model m2haz1. — This fitting may take some time . . .

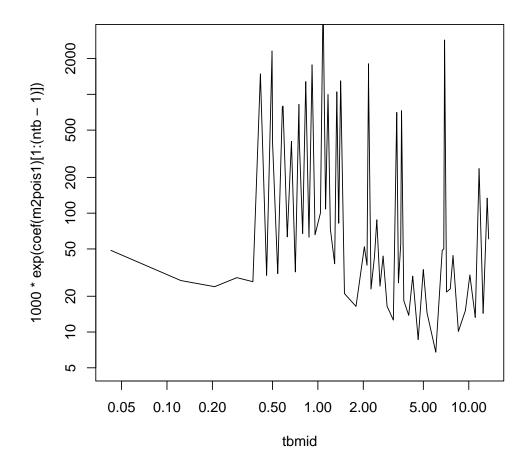
```
> m2pois1 <- glm( 1*(lex.Xst=="Oral ca. death") ~
+     -1 + timeband + sex + I((age-65)/10) + st3,
+     family=poisson, offset = log(lex.dur), data = orca2.spl)</pre>
```

We shall display the estimation results graphically for the baseline hazard (per 1000 person-years) and numerically for the rate ratios associated with the covariates. Before doing that it is useful to count the length ntb of the block occupied by baseline hazard in the whole vector of estimated parameters. However, owing to how the splitting to timebands was done, the last regression coefficient is necessarily zero and better be omitted when displaying the results. Also, as each timeband is quantitatively named according to its leftmost point, it is good to compute the midpoint values tbmid for the timebands

```
> tb <- as.numeric(levels(orca2.spl$timeband)); ntb <- length(tb)
> tbmid <- (tb[-ntb] + tb[-1])/2
                                   # midpoints of the intervals
> round( ci.exp(m2pois1 ), 3)
                 exp(Est.)
                            2.5%
                                  97.5%
                     0.049 0.012
timeband0
                                  0.205
timeband0.085
                     0.027 0.004
                                  0.200
timeband0.162
                     0.024 0.003
                                  0.177
timeband0.252
                     0.029 0.004
                                  0.211
timeband0.329
                     0.027 0.004
                                  0.195
timeband0.413
                     1.486 0.521
                                  4.239
timeband0.419
                     0.030 0.004
                                  0.220
timeband0.496
                     2.317 0.552
```

```
timeband0.498
                     0.390 0.053
                                  2.865
timeband0.504
                     0.031 0.004
                                  0.228
timeband0.58
                     0.787 0.107
                                  5.785
                     0.792 0.108
timeband0.583
                                  5.821
timeband0.586
                     0.797 0.108
                                 5.856
timeband0.589
                     0.063 0.015
                                 0.265
                     0.402 0.055
timeband0.665
                                 2.957
                     0.032 0.004 0.235
timeband0.671
                     0.824 0.112 6.052
timeband0.747
                     0.413 0.056
timeband0.75
                                 3.033
timeband0.756
                     0.067 0.016 0.283
timeband0.83
                     1.281 0.174
                                 9.408
timeband0.832
                     0.063 0.015
                                 0.264
                     1.772 0.423
timeband0.914
                                  7.425
timeband0.917
                     0.066 0.016
                                  0.276
timeband0.999
                     0.100 0.031
                                  0.329
                     6.554 2.874 14.946
timeband1.081
                     0.108 0.033
                                  0.355
timeband1.084
                     0.998 0.136
                                  7.311
timeband1.166
timeband1.169
                     0.074 0.018
                                  0.308
timeband1.251
                     0.038 0.005
                                  0.275
                     1.051 0.144
timeband1.333
                                  7.687
                     0.082 0.020
timeband1.336
                                  0.343
timeband1.413
                     1.300 0.312
                                  5.421
                     1.113 0.152
timeband1.418
                                  8.146
timeband1.421
                     0.021 0.003
                                  0.154
                     0.016 0.004
                                  0.069
timeband1.58
timeband1.999
                     0.052 0.007
                                  0.382
timeband2.067
                     0.036 0.005
                                 0.266
timeband2.166
                     1.811 0.248 13.237
timeband2.168
                     1.216 0.166
                                 8.891
timeband2.171
                     0.023 0.003
                                  0.168
                     0.043 0.006
timeband2.33
                                  0.317
timeband2.415
                     0.088 0.021
                                  0.367
                     0.024 0.003
                                  0.178
timeband2.5
                     0.044 0.006
timeband2.661
                                  0.318
                     0.016 0.002
timeband2.752
                                  0.120
timeband2.998
                     0.013 0.002
                                  0.092
                     0.705 0.097
timeband3.329
                                  5.148
timeband3.335
                     0.026 0.004
                                  0.189
timeband3.502
                     0.055 0.008
timeband3.581
                     0.729 0.100
                                  5.323
timeband3.587
                     0.018 0.003
                                  0.134
timeband3.833
                     0.014 0.002 0.101
timeband4.17
                     0.030 0.004
                                 0.215
timeband4.331
                     0.009 0.001
                                 0.063
                     0.034 0.005 0.245
timeband4.914
                     0.014 0.002 0.105
timeband5.079
timeband5.503
                     0.007 0.001
                                  0.049
timeband6.587
                     0.049 0.007
                                  0.354
                                  0.364
timeband6.749
                     0.050 0.007
                     2.867 0.394 20.860
timeband6.913
                     0.022 0.003
timeband6.916
                                  0.158
timeband7.329
                     0.023 0.003
                                  0.168
                     0.044 0.006
timeband7.748
                                  0.321
timeband7.984
                     0.010 0.001
                                  0.074
                     0.015 0.002
timeband9.084
                                  0.111
timeband9.919
                     0.030 0.004
                                  0.220
timeband10.42
                     0.013 0.002
                                 0.097
```

```
timeband11.671
                      0.237 0.033
                                    1.734
timeband11.748
                      0.014 0.002
                                    0.105
timeband13.166
                      0.134 0.018
timeband13.333
                      0.061 0.008
timeband13.755
                      0.000 0.000
sexMale
                      1.015 0.663
                                    1.554
I((age - 65)/10)
                      1.423 1.201
                                    1.685
st3III
                      1.509 0.898
                                   2.535
st3IV
                      3.178 1.983
                                   5.093
> par(mfrow=c(1,1))
> plot( tbmid, 1000*exp(coef(m2pois1)[1:(ntb-1)]),
              ylim=c(5,3000), log = "xy", type = "l")
```



Compare the regression coefficients and their error margins to those model m2haz1. Do you find any differences? How does the estimated baseline hazard look like?

3. The estimated baseline looks quite ragged when based on 71 separate parameters. A smoothed estimate may be obtained by spline modelling using the tools contained in package splines (see the practical of Saturday 25 May afternoon). With the following code you will be able to fit a reasonable spline model for the baseline hazard and draw the estimated curve (together with a band of the 95% confidence limits about the fitted values). From the same

model you should also obtain quite familiar results for the rate ratios of interest.

```
> library(splines)
> m2pspli <- update(m2pois1, . ~ ns(stime, df = 6, intercept = F) +
          sex + I((age-65)/10) + st3)
> round( ci.exp( m2pspli ), 3)
                                    exp(Est.) 2.5% 97.5%
                                        0.028 0.008 0.101
(Intercept)
ns(stime, df = 6, intercept = F)1
                                        6.505 1.776 23.823
ns(stime, df = 6, intercept = F)2
ns(stime, df = 6, intercept = F)3
                                        2.678 0.560 12.803
                                                     4.187
                                        0.976 0.227
ns(stime, df = 6, intercept = F)4
                                       0.423 0.105 1.699
ns(stime, df = 6, intercept = F)5
                                        1.567 0.082 29.939
ns(stime, df = 6, intercept = F)6
                                        0.434 0.121 1.558
sexMale
                                        1.021 0.667 1.563
I((age - 65)/10)
                                        1.431 1.208 1.696
st3III
                                        1.514 0.901 2.543
st3IV
                                        3.185 1.988 5.104
```

age = 65, st3 = "I-II") > blhaz <- predict(m2pspli, newdata = news, se.fit = T, type = "link")

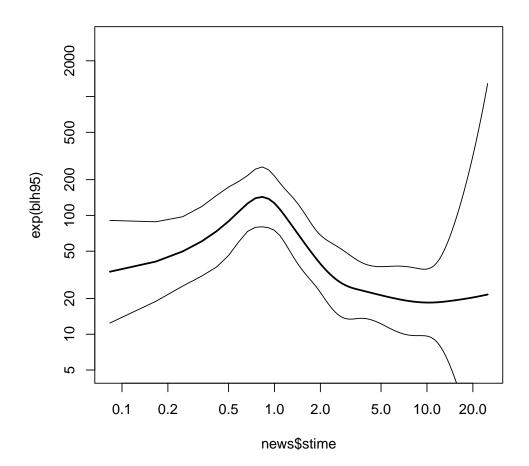
col = rep("black", 3), log = "xy", ylim = c(5,3000))

> blh95 <- cbind(blhaz\$fit, blhaz\$se.fit) %\*% ci.mat()

> par(mfrow=c(1,1))

> news <- data.frame( stime = seq(0,25, length=301), lex.dur = 1000, sex = "Female",

> matplot( news\$stime, exp(blh95), type = "1", lty = c(1,1,1), lwd = c(2,1,1),



### 2.12 Time-splitting, time-scales and SMR

This exercise is about mortaity among Danish Diabetes patients. It is based on the dataset DMlate, a random sample of 10,000 patients from the Danish Diabetes Register (scrambeled dates), all with date of diagnosis after 1994.

1. First, we load the Epi package (and two other packages we will need later) and the dataset, and take a look at it:

```
options( width=90 )
library( Epi )
library( popEpi )
library( mgcv )
data( DMlate )
str( DMlate )
'data.frame':
                     10000 obs. of 7 variables:
$ sex : Factor w/ 2 levels "M", "F": 2 1 2 2 1 2 1 1 2 1 ...
$ dobth: num 1940 1939 1918 1965 1933 ...
$ dodm : num 1999 2003 2005 2009 2009 ...
$ dodth: num NA NA NA NA NA ...
$ dooad: num NA 2007 NA NA NA ...
$ doins: num NA ...
$ dox : num 2010 2010 2010 2010 2010 ...
head( DMlate )
              dobth
                                dodth
                                         dooad doins
      sex
                        dodm
                                                  NA 2009.997
        F 1940.256 1998.917
50185
                                   NA
                                          NA
                                   NA 2007.446
307563
        M 1939.218 2003.309
                                                  NA 2009.997
                                   NA
                                                  NA 2009.997
294104
       F 1918.301 2004.552
                                            NA
336439
       F 1965.225 2009.261
                                   NA
                                            NA
                                                  NA 2009.997
245651
        M 1932.877 2008.653
                                   NA
                                            NA
                                                  NA 2009.997
216824
       F 1927.870 2007.886 2009.923
                                            NA
                                                  NA 2009.923
summary( DMlate )
sex
              dobth
                              dodm
                                            dodth
                                                            dooad
                                                                           doins
M:5185
         Min.
               :1898
                         Min.
                                :1995
                                        Min.
                                               :1995
                                                       Min.
                                                              :1995
                                                                       Min.
                                                                             :1995
F:4815
         1st Qu.:1930
                         1st Qu.:2000
                                        1st Qu.:2002
                                                       1st Qu.:2001
                                                                       1st Qu.:2001
         Median:1941
                         Median:2004
                                        Median:2005
                                                       Median:2004
                                                                       Median:2005
         Mean
                 :1942
                         Mean
                                :2003
                                        Mean
                                               :2005
                                                       Mean
                                                               :2004
                                                                       Mean
                                                                              :2004
         3rd Qu.:1951
                         3rd Qu.:2007
                                        3rd Qu.:2008
                                                        3rd Qu.:2007
                                                                       3rd Qu.:2007
               :2008
                         Max. :2010
                                               :2010
                                                             :2010
         Max.
                                        Max.
                                                       Max.
                                                                       Max.
                                                                              :2010
                                        NA's
                                               :7497
                                                       NA's
                                                                       NA's
                                                               :4503
                                                                              :8209
      dox
Min.
       :1995
1st Qu.:2010
Median:2010
Mean
        :2009
3rd Qu.:2010
        :2010
Max.
```

2. We then set up the dataset as a Lexis object with age, calendar time and duration of diabetes as timescales, and date of death as event.

In the dataset we have a date of exit dox which is either the day of censoring or the date of death:

```
same
dead TRUE <NA>
FALSE 0 7497
TRUE 2503 0
```

So we can set up the Lexis object by specifying the timescales and the exit status via !is.na(dodth):

Note that we made sure the first level of exit.status is "Alive", because the default is to use the first level as entry status when entry.status is not given as argument to Lexis.

The 4 persons are persons that have identical date of diabetes and date of death; they can be found by using keep.dropped=TRUE:

The dropped persons are:

summary( LL )

```
attr( LL, 'dropped' )
      sex
             dobth
                       dodm
                               dodth dooad doins
        M 1917.863 1999.457 1999.457 NA
173047
                                             NA 1999.457
361856
        F 1936.067 1996.984 1996.984
                                       NA
                                             NA 1996.984
245324
        M 1917.877 1999.906 1999.906
                                       NA
                                             NA 1999.906
        F 1919.060 2006.794 2006.794
                                     NA
                                             NA 2006.794
```

We can get an overview of the data by using the **summary** function on the object:

```
Transitions:
    То
      Alive Dead Records:
                         Events: Risk time:
 Alive 7497 2499
                    9996
                            2499
                                  54273.27
                                              9996
head( LL )
                   P dur
                           lex.dur lex.Cst lex.Xst lex.id sex
            Α
                                                            dobth
                                                                     dodm
50185 58.66119 1998.917
                                          Alive 1 F 1940.256 1998.917
                     0 11.0800821
                                  Alive
                                                      M 1939.218 2003.309
307563 64.09035 2003.309
                      0 6.6885695
                                    Alive
                                           Alive
                                                    2
                      0 5.4455852
                                                   3 F 1918.301 2004.552
294104 86.25051 2004.552
                                    Alive
                                          Alive
                                                   4 F 1965.225 2009.261
                      0 0.7364819
336439 44.03559 2009.261
                                    Alive
                                          Alive
                                                   5 M 1932.877 2008.653
245651 75.77550 2008.653 0 1.3442847
                                    Alive
                                          Alive
6 F 1927.870 2007.886
                                   Alive
                                           Dead
```

```
dodth
                 dooad doins
                                dox
                  NA NA 2009.997
50185
         NA
           NA 2007.446
                        NA 2009.997
307563
294104
           NA NA
                        NA 2009.997
           NA
                   NA
336439
                        NA 2009.997
245651
           NA
                   NA
                        NA 2009.997
216824 2009.923
                   NA
                        NA 2009.923
```

3. A crude picture of the mortality by sex can be obtained by the stat.table function:

So not surprising, we see that men have a higher mortality than women, here apparently only some 10%.

4. When we want to assess how mortality depends on age, calendar time and duration or to comapre with population mortality, we would in principle split the follow-up along all three time scales, but in practice it is sufficient to split it along one of the time-scales and then just use the value of each of the time-scales at the left endpoint of the intervals for analysis and for matching with population mortality. Note however that this requires that time-scales are treated as quantitative variables in the modeling.

We note that the total follow-up time was some 54,000 person-years, so if we split the follow-up in 6-month intervals we should get a bit more than 110,000 records. Note that in the popEpi package there is a function with the same functionality, which is faster (particularly for large datasets) and has a somewhat smarter syntax — it returns a data.table:

```
system.time(SL <- splitLexis(LL, breaks=seq(0,125,1/2), time.scale="A"))</pre>
        system elapsed
        0.084
                 2.174
 summary(SL); class(SL)
Transitions:
     To
From
        Alive Dead Records:
                              Events: Risk time: Persons:
  Alive 115974 2499
                    118473
                                 2499 54273.27
                                                      9996
                 "data.frame"
[1] "Lexis"
 system.time( SL <- splitMulti( LL, A=seq(0,125,1/2) ) )</pre>
   user system elapsed
  1.388
        0.084
                1.449
 summary( SL ) ; class( SL )
```

```
Transitions:
     То
         Alive Dead Records:
                               Events: Risk time:
                                                    Persons:
  Alive 115974 2499
                       118473
                                   2499
                                          54273.27
                                                         9996
[1] "Lexis"
                 "data.table" "data.frame"
summary( LL )
Transitions:
    To
       Alive Dead
                   Records:
                              Events: Risk time:
                                                   Persons:
From
                        9996
 Alive 7497 2499
                                  2499
                                         54273.27
                                                       9996
```

We see that the number of records have increased, but the number of persons, events and person-years is still the same as in LL. Thus, the amount of follow-up information is still the same; it is just distributed over more records, and hence allowing more detailed analyses.

#### SMR.

The SMR is the Standardized Mortality Ratio, which is the mortality rate-ratio between the diabetes patients and the general population. In real studies we would subtract the deaths and the person-years among the diabetes patients from those of the general population, but since we do not have access to these, we make the comparison to the general population at large, *i.e.* also including the diabetes patients.

We now want to include the population mortality rates as a fixed variable in the split dataset; for each record in the split dataset we attach the value of the population mortality for the relevant sex, and and calendar time.

This can be achieved in two ways: Either we just use the current split of follow-up time and allocate the population mortality rates for some suitably chosen (mid-)point of the follow-up in each, or we make a second split by date, so that follow-up in the diabetes patients is in the same classification of age and data as the population mortality table.

5. Using the former approach we shall include as an extra variable the population mortality as available from the data set M.dk.

First create the variables in the diabetes dataset that we need for matching with the age and period classification of the population mortality data, that is age, date (and sex) at the midpoint of each of the intervals (or rater at a point 3 months after the left endpoint of the interval — recall we split the follow-up in 6 month intervals).

We need to have variables of the same type when we merge, so we must transform the sex variable in M.dk to a factor, and must for each follow-up interval in the SL data have an age and a period variable that can be used in merging with the population data.

```
str( SL )
Classes 'Lexis', 'data.table' and 'data.frame': 118473 obs. of 14 variables:
$ lex.id : int 1 1 1 1 1 1 1 1 1 1 ...
```

```
: num 58.7 59 59.5 60 60.5 ...
$ P
                1999 1999 2000 2000 2001
         : num
                0 0.339 0.839 1.339 1.839 ...
         : num
  lex.dur: num 0.339 0.5 0.5 0.5 0.5 ...
  lex.Cst: Factor w/ 2 levels "Alive", "Dead": 1 1 1 1 1 1 1 1 1 1 ...
  lex.Xst: Factor w/ 2 levels "Alive", "Dead": 1 1 1 1 1 1 1 1 1 1 ...
         : Factor w/ 2 levels "M", "F": 2 2 2 2 2 2 2 2 2 2 ...
  dobth : num 1940 1940 1940 1940 1940 ...
$ dodm : num 1999 1999 1999 1999 ...
$ dodth : num NA ...
$ dooad : num NA ...
$ doins : num NA ...
         : num 2010 2010 2010 2010 2010 ...
 - attr(*, ".internal.selfref")=<externalptr>
- attr(*, "time.scales")= chr "A" "P" "dur"
- attr(*, "time.since")= chr
                               0.0 0.0 0.0
- attr(*, "breaks")=List of 3
  ..$ A : num 0 0.5 1 1.5 2 2.5 3 3.5 4 4.5 ...
  .. $ P : NULL
 ..$ dur: NULL
SL$Am \leftarrow floor(SL$A+0.25)
SL$Pm <- floor(SL$P+0.25)
data( M.dk )
str( M.dk )
'data.frame':
                    7800 obs. of 6 variables:
$ A : num 0 0 0 0 0 0 0 0 0 ...
$ sex : num
             1 2 1 2 1 2 1 2 1 2 ...
      : num
             1974 1974 1975 1975 1976
      : num
             459 303 435 311 405 258 332 205 312 233 ...
      : num 35963 34383 36099 34652 34965 ...
$ rate: num 12.76 8.81 12.05 8.97 11.58 ...
- attr(*, "Contents") = chr "Number of deaths and risk time in Denmark"
M.dk \leftarrow transform(M.dk, Am = A,
                          Pm = P,
                         sex = factor( sex, labels=c("M","F") ) )
str( M.dk )
'data.frame':
                     7800 obs. of 8 variables:
$ A : num 0000000000...
$ sex : Factor w/ 2 levels "M", "F": 1 2 1 2 1 2 1 2 1 2 ...
             1974 1974 1975 1975 1976 ...
      : num
$ D
      : num
             459 303 435 311 405 258 332 205 312 233 ...
$ Y
      : num
             35963 34383 36099 34652 34965 ...
$ rate: num
             12.76 8.81 12.05 8.97 11.58 ...
             0 0 0 0 0 0 0 0 0 0 ...
     : num
             1974 1974 1975 1975 1976
      : num
We then match the rates from M.dk into SL — sex, Am and Pm are the
common variables, and therefore the match is on these variables:
SLr <- merge( SL, M.dk[,c("sex","Am","Pm","rate")] )</pre>
dim(SL)
[1] 118473
               16
```

This merge only takes rows that have information from both data sets, hence the slightly fewer rows in SLr than in SL — there are a few record in SL with age and period values that do not exist in the population mortality data.

dim( SLr )
[1] 118454

17

6. We compute the expected number of deaths as the person-time multiplied by the corresponding population rate recalling that the rate is given in units of deaths per 1000 PY, whereas lex.dur is in units of 1 PY:

```
SLr$E <- SLr$lex.dur * SLr$rate / 1000
stat.table( sex,
          list( D = sum(lex.Xst=="Dead"),
               Y = sum(lex.dur),
               E = sum(E),
             SMR = ratio(lex.Xst=="Dead",E) ),
          data = SLr.
          margin = TRUE )
       D Y E SMR
    1342.00 27611.40 796.11 1.69
Μ
      1153.00 26654.52 747.77
                             1.54
Total 2495.00 54265.91 1543.88 1.62
stat.table(list(sex, Age = floor(pmax(A,39)/10)*10),
          list( D = sum(lex.Xst=="Dead"),
               Y = sum(lex.dur),
               E = sum(E),
             SMR = ratio(lex.Xst=="Dead",E) ),
           margin = TRUE,
            data = SLr)
     -----Age-----
        30 40 50 60 70 80 90
sex
______
       6.00 32.00 119.00 275.00 486.00 348.00 76.00 1342.00
      2129.67 3034.15 6273.51 7940.22 5842.90 2165.80 225.14 27611.40

    1.94
    9.47
    48.48
    142.38
    275.67
    254.92
    63.26
    796.11

    3.09
    3.38
    2.45
    1.93
    1.76
    1.37
    1.20
    1.69

         5.00 15.00 62.00 157.00 331.00 423.00 160.00 1153.00
F
      2576.33 2742.03 4491.68 6112.30 6383.09 3786.78 562.31 26654.52
         1.24 5.01 22.00 74.00 204.44 318.81 122.26 747.77
         4.02 2.99
                      2.82
                              2.12
                                      1.62 1.33
                                                  1.31
                                                           1.54
        11.00 47.00 181.00 432.00 817.00 771.00 236.00 2495.00
Total
      4706.00 5776.18 10765.19 14052.52 12225.99 5952.59 787.46 54265.91
         3.18 14.48 70.47 216.39 480.11 573.73 185.51 1543.88
                      2.57 2.00 1.70 1.34 1.27 1.62
         3.45
              3.25
```

We see that the SMR is pretty much the same for women and men, but also that there is a steep decrease in SMR by age.

7. We can fit a poisson model with sex as the explanatory variable and log-expected as offset to derive the SMR (and c.i.).

Some of the population mortality rates are 0, so we must exclude those records from the analysis.

```
msmr <- glm( (lex.Xst=="Dead") ~ sex - 1 + offset(log(E)),</pre>
              family = poisson,
```

```
data = subset(SLr,E>0) )
ci.exp( msmr )
    exp(Est.)     2.5%     97.5%
sexM     1.685699     1.597881     1.778344
sexF     1.541922     1.455442     1.633540
```

These are the same SMRs as just computed by stat.table, but now with confidence intervals.

We can assess the ratios of SMRs between men and women by using the ctr.mat argument:

```
round( ci.exp( msmr, ctr.mat=rbind(M=c(1,0),W=c(0,1),'M/F'=c(1,-1)) ), 2 )
    exp(Est.) 2.5% 97.5%
M         1.69 1.60    1.78
W         1.54 1.46    1.63
M/F         1.09 1.01    1.18
```

#### Age-specific mortality

8. We now use this dataset to estimate models with age-specific mortality curves for men and women separately, using splines (the function gam, using s from the mgcv package).

```
r.m \leftarrow gam((lex.Xst=="Dead") \sim s(A,k=20) + offset(log(lex.dur)),
             family = poisson,
               data = subset( SL, sex=="M" ) )
 r.f <- update( r.m, data = subset( SL, sex=="F" ) )</pre>
 gam.check( r.m )
Method: UBRE
               Optimizer: outer newton
full convergence after 3 iterations.
Gradient range [7.812553e-10,7.812553e-10]
(score -0.8040744 & scale 1).
Hessian positive definite, eigenvalue range [1.064907e-05,1.064907e-05].
Model rank = 20 / 20
Basis dimension (k) checking results. Low p-value (k-index<1) may
indicate that k is too low, especially if edf is close to k'.
        k'
             edf k-index p-value
s(A) 19.00 4.66
                    0.95
 gam.check( r.f )
Method: UBRE
              Optimizer: outer newton
full convergence after 1 iteration.
Gradient range [-5.035753e-08,-5.035753e-08]
(score -0.8232311 & scale 1).
Hessian positive definite, eigenvalue range [2.005875e-05,2.005875e-05].
Model rank = 20 / 20
Basis dimension (k) checking results. Low p-value (k-index<1) may
indicate that k is too low, especially if edf is close to k'.
           edf k-index p-value
s(A) 19.0 2.6 0.93
```

Here we are modeling the follow-up (events ((lex.Xst=="Dead")) and person-years (lex.dur)) as a non-linear function of age — represented by the penalized spline function s.

9. From these objects we could get the estimated log-rates by using predict, by supplying a data frame of values for the variables used as predictors in the model. These will be values of age — the ages where we want to see the predicted rates and lex.dur.

The default predict.gam function is a bit clunky as it gives the prediction and the standard errors of these in two different elements of a list, so in Epi there is a wrapper function ci.pred that uses this and computes predicted rates and confidence limits for these, which is usually what is needed.

Note that interms of prediction lex.dur is a covariate too; by setting this to 1000 throughout the data frame nd we get the rates in units of deaths per 1000 PY<sup>1</sup>

10. We can then plot the predicted rates for men and women together using matplot:

An alternative is to use matshade that gives confidence limist as shaded areas

Not surprisingly, the uncertainty on the rates is largest among the youngest where the no. of deths is smallest.

#### Period and duration effects

11. We model the mortality rates among diabetes patients also including current date and duration of diabetes. Note that we for later prediction purposes put the offset in the model formula.

<sup>&</sup>lt;sup>1</sup>Note however this is only the case if the offset is specified in the model formula. If the offset is specified as an argument (offset = log(lex.dur)), then the value of lex.dur in the dataframe will be ignored (equivaent of setting lex.dur to 1 in the newdata argument to ci.pred.)

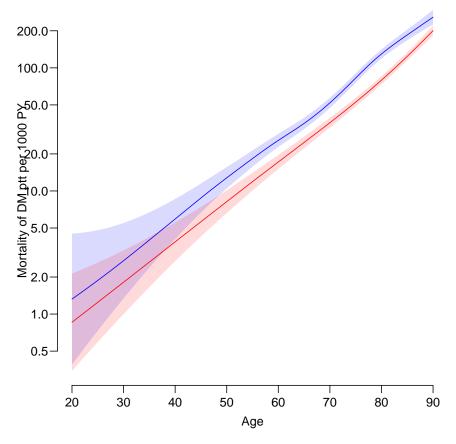


Figure 2.1: Age-specific mortality rates for Danish diabetes patients as estimated from a gam model with only age. Blue: men, red: women.

```
Mcr <- gam( (lex.Xst=="Dead") ~ s(</pre>
                                                                                                                                                A, bs="cr", k=10 ) +
                                                                                                                              s(P, bs="cr", k=10) +
                                                                                                                              s( dur, bs="cr", k=10 ) + offset(log(lex.dur)),
                                                  family = poisson,
                                                          data = subset( SL, sex=="M" ) )
    summary( Mcr )
Family: poisson
Link function: log
Formula:
 (lex.Xst == "Dead") \sim s(A, bs = "cr", k = 10) + s(P, bs = "cr", k = 
              k = 10) + s(dur, bs = "cr", k = 10) + offset(log(lex.dur))
Parametric coefficients:
                                              Estimate Std. Error z value Pr(>|z|)
 (Intercept) -3.54074
                                                                                            0.04938
                                                                                                                                  -71.7
                                                                                                                                                                 <2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Approximate significance of smooth terms:
                                   edf Ref.df Chi.sq
                                                                                                            p-value
s(A)
                                                                                                            < 2e-16 ***
                           3.646 4.518 1013.20
s(P)
                          1.024 1.047
                                                                                    17.58 3.40e-05 ***
s(dur) 7.586 8.384
                                                                                   74.46 1.87e-12 ***
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
R-sq.(adj) = -0.0255 Deviance explained = 9.87%
UBRE = -0.8054 Scale est. = 1
                                     n = 60347
Fcr <- update( Mcr, data = subset( SL, sex=="F" ) )</pre>
summary( Fcr )
Family: poisson
Link function: log
Formula:
(lex.Xst == "Dead") \sim s(A, bs = "cr", k = 10) + s(P, bs = "cr", k = 10) + s(dur, bs = "cr", k = 10) + offset(log(lex.dur))
Parametric coefficients:
           Estimate Std. Error z value Pr(>|z|)
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Approximate significance of smooth terms:
        edf Ref.df Chi.sq p-value
s(A)
      2.668 3.368 988.51 < 2e-16 ***
     1.887 2.370 20.04 0.000123 ***
s(dur) 5.972 6.971 38.95 2.17e-06 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
R-sq.(adj) = -0.0229 Deviance explained = 11.1%
gam.check( Mcr )
Method: UBRE
             Optimizer: outer newton
full convergence after 3 iterations.
Gradient range [-7.482163e-07,2.324787e-07]
(score -0.805401 & scale 1).
Hessian positive definite, eigenvalue range [7.229476e-07,1.904545e-05].
Model rank = 28 / 28
Basis dimension (k) checking results. Low p-value (k-index<1) may
indicate that k is too low, especially if edf is close to k^{\prime}.
        k' edf k-index p-value
      9.00 3.65 0.94 0.920
s(A)
                  0.90
s(P)
     9.00 1.02
                          0.025 *
s(dur) 9.00 7.59
                 0.92 0.375
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
gam.check( Fcr )
Method: UBRE
             Optimizer: outer newton
full convergence after 3 iterations.
Gradient range [-1.401872e-08,1.022359e-08]
(score -0.8240482 & scale 1).
Hessian positive definite, eigenvalue range [1.061413e-05,2.307556e-05].
Model rank = 28 / 28
Basis dimension (k) checking results. Low p-value (k-index<1) may
indicate that k is too low, especially if edf is close to k'.
```

```
k' edf k-index p-value

s(A) 9.00 2.67 0.93 0.650

s(P) 9.00 1.89 0.90 0.035 *

s(dur) 9.00 5.97 0.94 0.855

---

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

For the male rates the edf (effective degrees of freedom) is quite close to the k, but as wee shall see no need to more detailed modeling.

12. We can now plot the estimated effects for men and women:

```
par( mfrow=c(2,3) )
plot( Mcr, ylim=c(-3,3), col="blue" )
plot( Fcr, ylim=c(-3,3), col="red" )
```

13. Not surprisingly, these models fit substantially better than the model with only age as we can see from this comparison:

```
anova( Mcr, r.m, test="Chisq" )
Analysis of Deviance Table
Model 1: (lex.Xst == "Dead") \sim s(A, bs = "cr", k = 10) + s(P, bs = "
k = 10) + s(dur, bs = "cr", k = 10) + offset(log(lex.dur))
Model 2: (lex.Xst == "Dead") \sim s(A, k = 20) + offset(log(lex.dur))
              Resid. Df Resid. Dev
                                                                                                                                                                                      Df Deviance Pr(>Chi)
                                         60332
                                                                                                                11717
                                         60340
                                                                                                                11812 -8.0248 -95.251 < 2.2e-16 ***
 2
 Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
       anova( Fcr, r.f, test="Chisq" )
 Analysis of Deviance Table
Model 1: (lex.Xst == "Dead") \sim s(A, bs = "cr", k = 10) + s(P, bs = "
k = 10) + s(dur, bs = "cr", k = 10) + offset(log(lex.dur))
Model 2: (lex.Xst == "Dead") \sim s(A, k = 20) + offset(log(lex.dur))
              Resid. Df Resid. Dev
                                                                                                                                                                                  Df Deviance Pr(>Chi)
                                        58112
                                                                                                               10204
 1
  2
                                                                                                                 10268 -9.3754 -63.35 4.457e-10 ***
                                         58122
 Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

14. Since the fitted model has three time-scales: current age, current date and current duration of diabetes, so the effects that we see from the plot.gam are not really interpretable; they are (as in any kind of multiple regressions) to be interpreted as "all else equal" which they are not; the three time scales advance simultaneously at the same pace.

The reporting would therefore more naturally be *only* on one time scale, showing the mortality for persons diagnosed in different ages in a given year.

This is most easily done using the ci.pred function with the newdata= argument. So a person diagnosed in age 50 in 1995 will have a mortality measured in cases per 1000 PY as:

```
pts <- seq(0,17,0.5)
nd <- data.frame( A = 50+pts,</pre>
```

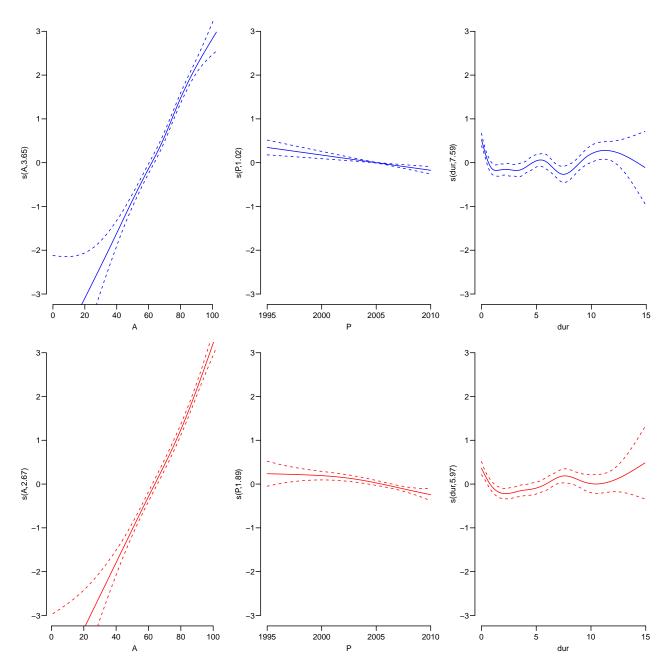


Figure 2.2: Plot of the estimated smooth terms for men (top) and women (bottom). Clearly it seems that the duration effects are somewhat over-modeled.

Note, that we used + offset(log(lex.dur)) as the offset specification in the model, the value of lex.dur in nd will be honoured and prediction be made for the scale chosen, in the model specification; so in this case as events per 1000 PY (since lex.dur is in units of single person-years).

Since there is no duration beyond 18 years in the dataset we only make predictions for 12 years of duration, and do it for persons diagnosed in 1995 and 2005 — the latter is quite dubious too because we are extrapolating calendar time trends way beyond data.

We form matrices of predictions with confidence intervals, that we will plot in the same frame:

15. From figure 2.3 it seems that the duration effect is dramatically over-modeled, so we refit constraining the d.f. to 5 (note that this choice is essentially an arbitray choice) and redo the whole thing again:

```
Mcr <- gam( (lex.Xst=="Dead") ~ s( A, bs="cr", k=10 ) +
                                    P, bs="cr", k=10 ) +
                                 s(dur, bs="cr", k=5) +
                                 offset(log(lex.dur)),
             family = poisson,
               data = subset(SL,sex=="M") )
 Fcr <- update( Mcr,</pre>
               data = subset(SL,sex=="F") )
 gam.check( Mcr )
              Optimizer: outer newton
Method: UBRE
full convergence after 4 iterations.
Gradient range [-2.87389e-07,5.520002e-08]
(score -0.805213 & scale 1).
Hessian positive definite, eigenvalue range [2.83738e-07,1.060921e-05].
Model rank = 23 / 23
Basis dimension (k) checking results. Low p-value (k-index<1) may
indicate that k is too low, especially if edf is close to k'.
        k' edf k-index p-value
s(A)
       9.00 3.70
                    0.85 <2e-16 ***
       9.00 1.01
                    0.87
                           0.035 *
s(dur) 4.00 3.93
                   0.89
                           0.170
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
gam.check( Fcr )
```

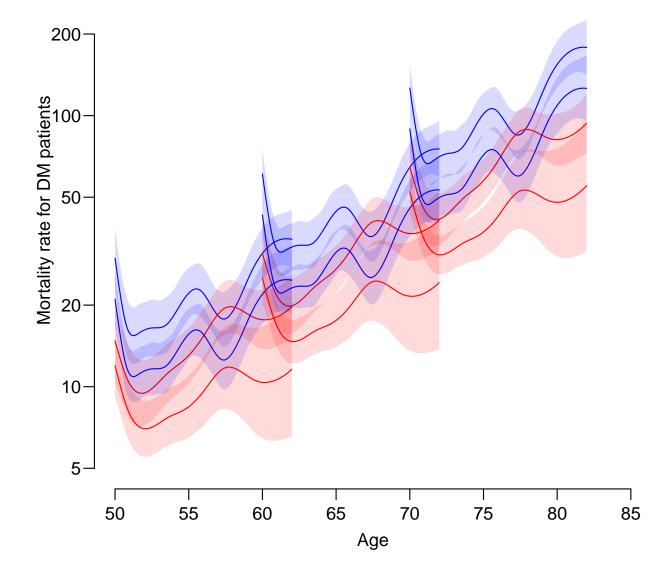


Figure 2.3: Mortality rates for diabetes patients diagnosed 1995 and 2005 in ages 50, 60 and 70; as estimated by penalized splines. Men blue, women red.

```
Method: UBRE Optimizer: outer newton full convergence after 3 iterations.

Gradient range [1.704809e-09,4.79408e-08]
(score -0.8240014 & scale 1).

Hessian positive definite, eigenvalue range [4.823934e-06,1.936723e-05].

Model rank = 23 / 23

Basis dimension (k) checking results. Low p-value (k-index<1) may indicate that k is too low, especially if edf is close to k'.

k' edf k-index p-value
s(A) 9.00 2.65 0.90 <2e-16 ***
```

```
s(P) 9.00 1.92 0.93 0.38

s(dur) 4.00 3.81 0.95 0.78

---

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' '1
```

Thus it seems that k=5 is a bit under modeling the duration effect.

We also add the rate-ratio between men and women using the ci.ratio function:

From figure ?? we see that there is an incraesed mortality in the first few years afer diagnosis (this is a clinical artifact) and little indication that age at diagnosis has any effect. (This can of course be tried explicitly).

Moreover it is pretty clear that the M/W mortality rate ratio is constant across age and duration.

## 2.12.1 SMR modeling

16. We can treat SMR exactly as mortality rates by including the log expected numbers instead of the log person-years as offset, again using separate models for men and women.

We exclude those records where no deaths in the population occur (that is where the rate is 0) — you could say that this correspond to parts of the data where no follow-up on the population mortality scale is available. The rest is essentially just a repeat of the analyses for mortality rates:

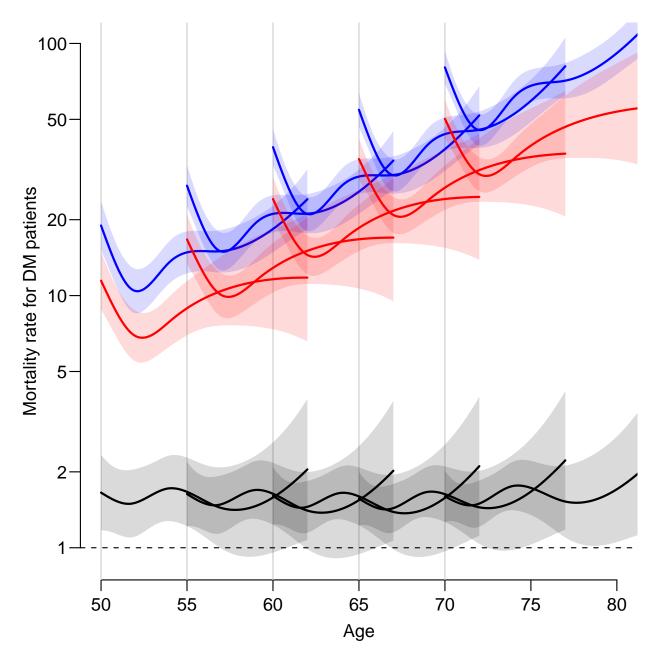


Figure 2.4: Mortality rates for diabetes patients diagnosed 1995 and 2005 in ages 50, 55, 60, 65 and 70; as estimated by penalized splines. Note that we did this for year of diagnosis 2005 alone, but for a longer duration period. Men blue, women red, M/W rate ratio gray.

```
Approximate significance of smooth terms:
                         edf Ref.df Chi.sq p-value
                   1.022 1.044 58.357 2.82e-14 ***
s(A)
s(P) 1.009 1.019 1.972 0.163
s(dur) 3.925 3.996 55.820 3.17e-11 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
R-sq.(adj) = -0.0259 Deviance explained = 0.992%
UBRE = -0.80531 Scale est. = 1
                                                                                                             n = 60333
  summary( Fsmr )
Family: poisson
Link function: log
Formula:
(lex.Xst == "Dead") \sim s(A, bs = "cr", k = 10) + s(P, bs = "cr", k = 
           k = 10) + s(dur, bs = "cr", k = 5)
Parametric coefficients:
                                  Estimate Std. Error z value Pr(>|z|)
(Intercept) 0.75404
                                                               0.05384
                                                                                            14.01 <2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
Approximate significance of smooth terms:
                         edf Ref.df Chi.sq p-value
                1.699 2.149 56.274 3.95e-12 ***
s(A)
s(P)
               1.837 2.306 7.508 0.0375 *
s(dur) 3.818 3.977 35.807 1.57e-06 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
R-sq.(adj) = -0.0228 Deviance explained = 0.947%
UBRE = -0.82414 Scale est. = 1
                                                                                                                n = 58099
  par(mfrow=c(2,3))
  plot(Msmr, ylim=c(-1,2), col="blue")
  plot( Fsmr, ylim=c(-1,2), col="red" )
```

17. We then compute the predicted SMRs from the models for men and women diagnosed in ages 50, 60 and 70 in 1995 and 2005, respectively, and show them in plots side by side. We are going to make this type of plot for other models (well, pairs, for men and women) so we wrap it in a function:

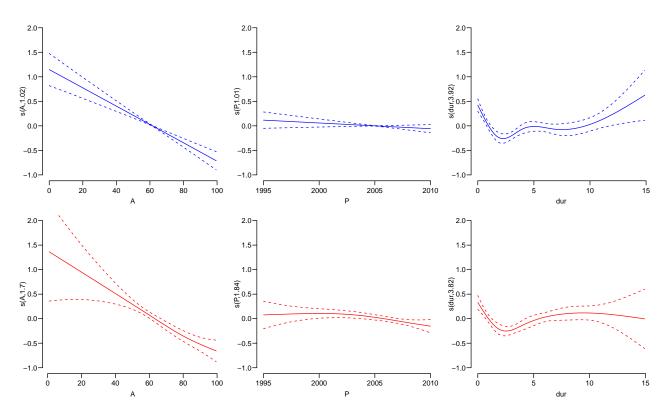


Figure 2.5: Estimated effects of age, calendar time and duration on SMR — top men, bottom women

```
abline( h=1, lty="55" )
```

From figure 2.6 we see that like for mortality there is a clear peak at diagnosis and flattening after approximately 2 years. But also that the duration is possibly over-modeled. Finally there is no indication that the SMR is different for men and women.

18. It would be natural to simplify the model to one with a non-linear effect of duration and linear effects of age at diagnosis and calendar time, and moreover to squeeze the number of d.f. for the non-linear smooth term for duration:

```
Asmr <- gam( (lex.Xst=="Dead")</pre>
                                   sex:I(A-60) +
                                   sex:I(P-2000) +
                                   s(dur, k=5) +
                                   offset(log(E)),
              family = poisson,
                data = SLr)
 summary( Asmr )
Family: poisson
Link function: log
Formula:
(lex.Xst == "Dead") \sim sex + sex:I(A - 60) + sex:I(P - 2000) +
    s(dur, k = 5) + offset(log(E))
```

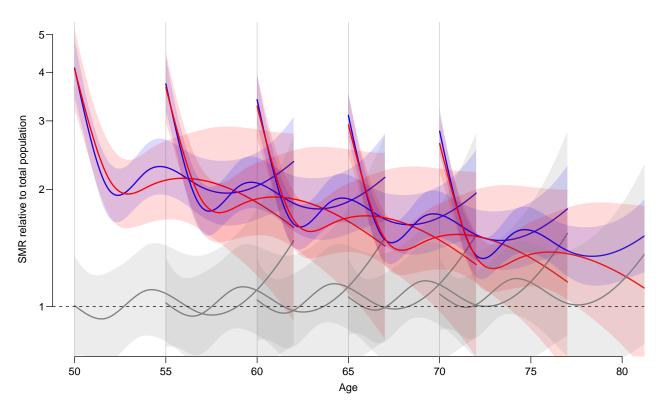


Figure 2.6: Mortality rates for diabetes patients diagnosed 1995 and 2005 in ages 50, 60 and 70; as estimated by penalized splines. Men blue, women red.

```
Parametric coefficients:
                  Estimate Std. Error z value Pr(>|z|)
(Intercept)
                  0.868923
                           0.055576 15.635 < 2e-16 ***
sexF
                  0.035465
                             0.085183
                                      0.416
                                                0.6772
sexM:I(A - 60)
                 -0.018857
                             0.002421
                                      -7.789 6.73e-15 ***
sexF:I(A - 60)
                 -0.019701
                             0.002696
                                      -7.306 2.74e-13 ***
sexM:I(P - 2000) -0.013296
                             0.007936
                                      -1.675
                                                0.0939 .
sexF:I(P - 2000) -0.018563
                             0.008499
                                      -2.184
                                                0.0289 *
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
Approximate significance of smooth terms:
         edf Ref.df Chi.sq p-value
s(dur) 3.856 3.987 60.13 1.57e-12 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
R-sq.(adj) = -0.0242
                       Deviance explained = 0.865%
UBRE = -0.8144 Scale est. = 1
                                      n = 118432
 gam.check( Asmr )
Method: UBRE
               Optimizer: outer newton
full convergence after 4 iterations.
Gradient range [6.36467e-07,6.36467e-07]
(score -0.8143976 & scale 1).
Hessian positive definite, eigenvalue range [3.017067e-06,3.017067e-06].
Model rank = 10 / 10
Basis dimension (k) checking results. Low p-value (k-index<1) may
```

```
indicate that k is too low, especially if edf is close to k'.
```

```
k' edf k-index p-value
s(dur) 4.00 3.86
                    0.9
                          0.045 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
round( (ci.exp(Asmr, subset="sex")-1)*100, 1)
                exp(Est.) 2.5% 97.5%
                      3.6 -12.3 22.4
sexF
sexM:I(A - 60)
                     -1.9 -2.3
                                -1.4
sexF:I(A - 60)
                     -2.0 -2.5 -1.4
                                 0.2
sexM:I(P - 2000)
                     -1.3 -2.8
sexF:I(P - 2000)
                     -1.8 -3.5
                                -0.2
```

Thus the decrease in SMR per year of age is about 2% / year for both sexes and 1.3% per calendar year for men, but 1.8% per year for women.

The estimate of sex indicates that the SMR for 60 year old women in 2000 at duration 0 of DM is about 3.6% larger than that of men, but nowhere near significantly so.

19. We can use the previous code to show the predicted mortality under this model.

We see that there is absolutely no indication of difference between men and women, but also that the estimated effect of duraion is not exactly credible.

20. If we deem the curves non-credible, we may resort to a brutal parametric assumption without any penalization of curvature involved. If we choose a natural spline for the duration with knots at 0,1,3,6 years we get a model with 3 parameters, try:

```
dim( Ns(SLr$dur, knots=c(0,1,4,8) ) )
[1] 118432 3
```

Now fit the same model as above using this:

```
SMRglm \leftarrow glm((lex.Xst="Dead") \sim I(A-60) + I(P-2000) + Ns(dur, knots=c(0,1,4,8)) + offset(log(E)), family = poisson, \\ data = SLr)
```

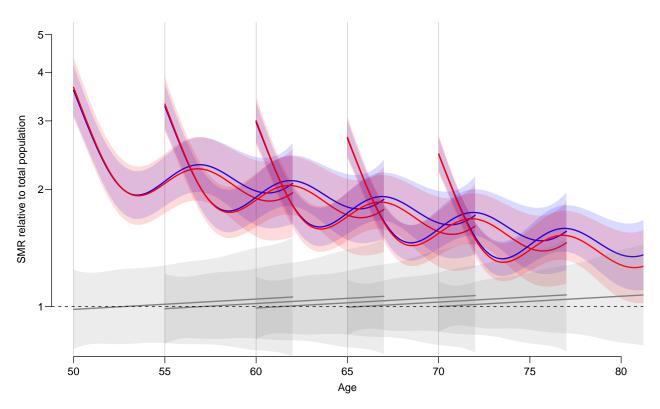


Figure 2.7: Mortality rates for diabetes patients diagnosed 1995 and 2005 in ages 50, 60 and 70; as estimated by penalized splines. Men blue, women red.

Then we can plot again:

Form figure 2.8 it appears that the SMR drops by a factor 2 during the first 2 years, increases a bit and after that decreases by age. But the general pattern is that after som 5 years the SMR no longer depend on the age at diagnosis — but the evidence for this is pretty thin.

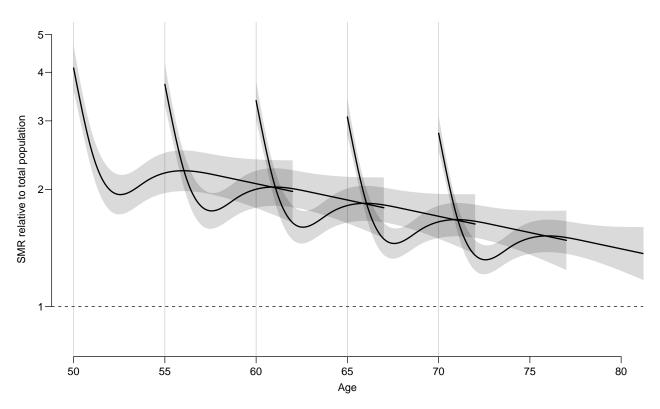


Figure 2.8: Mortality rates for diabetes patients diagnosed 1995 and 2005 in ages 50, 60 and 70; as estimated by penalized splines, no difference between men and women assumed

*IARC*, 2018 2.13 Causal inference **223** 

#### 2.13 Causal inference

# 2.13.1 Proper adjustment for confounding in regression models

The first exercise of this session will ask you to simulate some data according to pre-specified causal structure (don't take the particular example too seriously) and see how you should adjust the analysis to obtain correct estimates of the causal effects.

Suppose one is interested in the effect of beer-drinking on body weight. Let's assume that in addition to the potential effect of beer on weight, the following is true in reality:

- Men drink more beer than women
- Men have higher body weight than women
- People with higher body weight tend to have higher blood pressure
- Beer-drinking increases blood pressure

The task is to simulate a dataset in accordance with this model, and subsequently analyse it to see, whether the results would allow us to conclude the true association structure.

- 1. Sketch a causal graph (not necessarily with R) to see, how should one generate the data
- 2. Suppose the actual effect sizes are following:
  - The probability of beer-drinking is 0.2 for females and 0.7 for males
  - Men weigh on average 10kg more than women
  - One kg difference in body weight corresponds in average to 0.5mmHg difference in (systolic) blood pressures
  - Beer-drinking increases blood pressure by 10mmHg in average.
  - Beer-drinking has **no** effect on body weight

The R commands to generate the data are:

- 3. Now fit the following models for body weight as dependent variable and beer-drinking as independent variable. Look, what is the estimated effect size:
  - (a) Unadjusted (just simple linear regression)
  - (b) Adjusted for sex
  - (c) Adjusted for sex and blood pressure

224 2.13 Causal inference SPE: Solutions

```
> library( Epi )
> m1a<-lm(weight~beer, data=bdat)
> m2a<-lm(weight~beer+sex, data=bdat)
> m3a<-lm(weight~beer+sex+bp, data=bdat)
> ci.lin(m1a)
> ci.lin(m2a)
> ci.lin(m3a)
```

- 4. What would be the conclusions on the effect of beer on weight, based on the three models? Do they agree? Which (if any) of the models gives an unbiased estimate of the actual causal effect of interest?
- 5. How can the answer be seen from the graph?
- 6. Now change the data-generation algorithm so, that in fact beer-drinking does increase the body weight by 2kg. Look, what are the conclusions in the above models now. Thus the data is generated as before, but the weight variable is computed as:

```
> bdat$weight <- 60 + 10*bdat$sex + 2*bdat$beer + rnorm(1000,0,7)

> bdat$bp <- 110 +0.5*bdat$weight + 10*bdat$beer+ rnorm(1000,0,10) #
> m1b<-lm(weight~beer,data=bdat)
> m2b<-lm(weight~beer+sex,data=bdat)
> m3b<-lm(weight~beer+sex+bp,data=bdat)
> ci.lin(m1b)
> ci.lin(m2b) # the correct model
> ci.lin(m3b)
```

7. Suppose one is interested in the effect of beer-drinking on blood pressure instead, and is fitting a) an unadjusted model for blood pressure, with beer as an only covariate; b) a model with beer, weight and sex as covariates. Would either a) or b) give an unbiased estimate for the effect? (You may double-check whether the simulated data is consistent with your answer).

```
> m1bp<-lm(bp~beer,data=bdat)
> m2bp<-lm(bp~beer+weight+sex,data=bdat)
> m3b<-lm(weight~beer+sex+bp,data=bdat)
> ci.lin(m1bp)
> ci.lin(m2bp) # the correct model
```

# 2.13.2 Instrumental variables estimation, Mendelian randomization and assumptions

In the lecture slides it was shown that in a model for blood glucose level (associated with the risk of diabetes), both BMI and FTO genotype were significant. Seeing such result in a real dataset may misleadingly be interpreted as an evidence of a direct effect of FTO genotype on glucose. Conduct a simulation study to verify that one may see a significant genotype effect on outcome in such model if in fact the assumptions for Instrumental Variables estimation (Mendelian Randomization) are valid – genotype has a direct effect on the exposure only, whereas exposure-outcome association is confounded.

*IARC*, 2018 2.13 Causal inference **225** 

1. Start by generating the genotype variable as Binomial(2,p), with p=0.2:

```
> n <- 10000
> mrdat <- data.frame(G = rbinom(n,2,0.2))
> table(mrdat$G)
```

2. Also generate the confounder variable U

```
> mrdat$U <- rnorm(n)</pre>
```

3. Generate a continuous (normally distributed) exposure variable BMI so that it depends on G and U. Check with linear regression, whether there is enough power to get significant parameter estimates. For instance:

```
> mrdat$BMI <- with(mrdat, 25 + 0.7*G + 2*U + rnorm(n) )</pre>
```

4. Finally generate Y ("Blood glucose level") so that it depends on BMI and U (but not on G).

```
> mrdat$Y <- with(mrdat, 3 + 0.1*BMI - 1.5*U + rnorm(n,0,0.5) )
```

5. Verify, that simple regression model for Y, with BMI as a covariate, results in a biased estimate of the causal effect (parameter estimate is different from what was generated)

```
> mxy<-lm(Y ~ BMI, data=mrdat)
> ci.lin(mxy)
```

How different is the estimate from 0.1?

6. Estimate a regression model for Y with two covariates, G and BMI. Do you see a significant effect of G? Could you explain analytically, why one may see a significant parameter estimate for G there?

```
> mxyg<-lm(Y ~ G + BMI, data=mrdat)
> ci.lin(mxyg)
```

7. Find an IV (instrumental variables) estimate, using G as an instrument, by following the algorithm in the lecture notes (use two linear models and find a ratio of the parameter estimates). Does the estimate get closer to the generated effect size?

```
> mgx<-lm(BMI ~ G, data=mrdat)
> ci.lin(mgx) # check the instrument effect
> bgx<-mgx$coef[2] # save the 2nd coefficient (coef of G)
> mgy<-lm(Y ~ G, data=mrdat)
> ci.lin(mgy)
> bgy<-mgy$coef[2]
> causeff <- bgy/bgx
> causeff # closer to 0.1?
```

8. A proper simulation study would require the analysis to be run several times, to see the extent of variability in the parameter estimates. A simple way to do it here would be using a for-loop. Modify the code as follows (exactly the same commands as executed so far, adding a few lines of code to the beginning and to the end):

**226** 2.13 Causal inference SPE: Solutions

```
> n <- 10000
> # initializing simulations:
> # 30 simulations (change it, if you want more):
> nsim<-30
> mr<-rep(NA,nsim)</pre>
                    # empty vector for the outcome parameters
> for (i in 1:nsim) { # start the loop
+ ### Exactly the same commands as before:
+ mrdat <- data.frame(G = rbinom(n,2,0.2))
+ mrdat$U <- rnorm(n)
+ mrdat\$BMI \leftarrow with(mrdat, 25 + 0.7*G + 2*U + rnorm(n))
+ mrdat\$Y \leftarrow with(mrdat, 3 + 0.1*BMI - 1.5*U + rnorm(n, 0, 0.5))
+ mgx<-lm(BMI ~ G, data=mrdat)
+ bgx<-mgx$coef[2]
+ mgy<-lm(Y ~ G, data=mrdat)
+ bgy<-mgy$coef[2]
+ # Save the i'th parameter estimate:
+ mr[i]<-bgy/bgx
      # end the loop
```

Now look at the distribution of the parameter estimate:

```
> summary(mr)
```

9. (optional) Change the code of simulations so that the assumptions are violated: add a weak direct effect of the genotype G to the equation that generates Y:

```
> mrdat\$Y \leftarrow with(mrdat, 3 + 0.1*BMI - 1.5*U + 0.05*G + rnorm(n,0,0.5))
```

Repeat the simulation study to see, what is the bias in the average estimated causal effect of BMI on Y.

10. (optional) Using library sem and function tsls, obtain a two-stage least squares estimate for the causal effect. Do you get the same estimate as before?

```
> library(sem)
> summary(tsls(Y ~ BMI, ~G, data=mrdat))
```

#### Why are simulation exercises useful for causal inference?

If we simulate the data, we know the data-generating mechanism and the "true" causal effects. So this is a way to check, whether an analysis approach will lead to estimates that correspond to what is generated. One could expect to see similar phenomena in real data analysis, if the data-generation mechanism is similar to what was used in simulations.

# 2.14 Nested case-control study and case-cohort study:

## Risk factors of coronary heart disease

In this exercise we shall apply both the nested case-control (NCC) design and the case-cohort (CC) design in sampling control subjects from a defined cohort or closed study population. The case group comprises those cohort members who die from coronary heart disease (CHD) during a > 20 years follow-up of the cohort. The risk factors of interest are cigarette smoking, systolic blood pressure, and total cholesterol level.

Our study population is an occupational cohort comprising 1501 men working in blue-collar jobs in one Nordic country. Eligible subjects had no history of coronary heart disease when recruited to the study in the early 1990s. Smoking habits and many other items were inquired at baseline by a questionnaire, and blood pressure was measured by a research nurse, the values being written down on the questionnaire. Serum samples were also taken from the cohort members at the same time and were stored in a freezer. For some reason, the data in the questionnaires were not entered to any computer file, but the questionnaires were kept in a safe storehouse for further purposes. Also, no biochemical analyses were initially performed for the sera collected from the participants. However, dates of birth and dates of entry to the study were recorded in an electronic file.

In 2010 the study was suddenly reactivated by those investigators of the original team who were still alive then. As the first step mortality follow-up of the cohort members was executed by record linkage to the national population register, from which the dates of death and emigration were obtained. Another linkage was performed with the national register of causes of death in order to get the deaths from coronary heard disease identified. As a result a data file occoh.txt was completed containing the following variables:

id = identification number,
birth = date of birth,
entry = date of recruitment and baseline measurements,
exit = date of exit from mortality follow-up,
death = indicator for vital status at the end of follow-up,
= 1, if dead from any cause, and = 0, if alive,
chdeath = indicator for death from coronary heart disease,
= 1, if "yes", and 0, if "no".

This exercise is divided into five main parts:

- (1) Description of the study base or the follow-up experience of the whole cohort, identification of the cases and illustrating the risk sets.
- (2) Nested case-control study within the cohort: (i) selection of controls by risk set or time-matched sampling using function ccwc() in package Epi, (ii) collection of exposure data for cases and controls from the pertinent data

- base of the whole cohort to the case-control data set using function merge(), and (iii) analysis of case-control data using function clogit() in package survival(),
- (3) Case-cohort study within the cohort: (i) selection of a subcohort by simple random sampling from the cohort, (ii) fitting the Cox model to the data by weighted partial likelihood using function coxph() in package survival() with appropriate weighting and correction of estimated covariance matrix for the model coefficients; also using function cch() in package survival() for the same task.
- (4) Comparison of results from all previous analyses, also with those from a full cohort design.
- (5) Further tasks and homework.

# 2.14.1 Reading the cohort data, illustrating the study base and risk sets

11. Load the packages Epi and survival. Read in the cohort data file and name the resulting data frame as oc. See its structure and print the univariate summaries.

```
> library(Epi)
> library(survival)
> url <- "http://bendixcarstensen.com/SPE/data"</pre>
> oc <- read.table( paste(url, "occoh.txt", sep = "/"), header=TRUE)
> str(oc)
'data.frame':
                   1501 obs. of 6 variables:
$ id : int 1 2 3 4 5 6 7 8 9 10 ...
 $ birth : Factor w/ 1349 levels "1929-08-01", "1929-12-23",..: 811 230 537 566 266 3
 $ entry : Factor w/ 302 levels "1990-08-14","1990-08-15",..: 1 1 1 1 1 2 2 2 2 2.
         : Factor w/ 290 levels "1992-02-25", "1992-04-06", ...: 290 290 290 290 203 2
$ death : int 0 0 0 0 1 1 1 1 0 0 ...
$ chdeath: int 0 0 0 0 0 0 0 1 0 0 ...
> summary(oc)
      id
                     birth
                                       entrv
                                                         exit
               1931-02-19:
Min.
      :
          1
                                1990-08-18: 12
                                                  2009-12-31:1205
               1931-08-24:
1st Qu.: 376
                            3
                                1991-04-10: 12
                                                  2000-01-23:
Median: 751
               1933-02-28: 3
                                1991-04-24: 11
                                                  2000-10-04:
Mean : 751
               1939-04-25: 3
                                1991-12-18: 11
                                                  2001-10-13:
3rd Qu.:1126
               1941-07-01: 3
                                1990-11-07: 10
                                                  2008-02-09:
               1943-04-16: 3
                                1991-03-30: 10
                                                  2008-03-23:
                                                               2
Max. :1501
                                (Other) :1435
                                                  (Other) : 286
               (Other) :1483
                   chdeath
    death
Min. :0.0000 Min. :0.00000
 1st Qu.:0.0000
               1st Qu.:0.00000
Median :0.0000
                Median :0.00000
Mean :0.1972
                 Mean :0.07995
3rd Qu.:0.0000
                 3rd Qu.:0.00000
Max. :1.0000
                 Max. :1.00000
```

12. It is convenient to change all the dates into fractional calendar years

```
> oc$ybirth <- cal.yr(oc$birth)
> oc$yentry <- cal.yr(oc$entry)
> oc$yexit <- cal.yr(oc$exit)</pre>
```

We shall also compute the age at entry and at exit, respectively, as age will be the main time scale in our analyses.

```
> oc$agentry <- oc$yentry - oc$ybirth
> oc$agexit <- oc$yexit - oc$ybirth</pre>
```

13. As the next step we shall create a lexis object from the data frame along the calendar period and age axes, and as the outcome event we specify the coronary death.

```
> oc.lex <- Lexis( entry = list( per = yentry,
                                age = yentry - ybirth ),
+
                   exit = list( per = yexit),
            exit.status = chdeath,
                     id = id, data = oc)
NOTE: entry.status has been set to 0 for all.
> str(oc.lex)
Classes 'Lexis' and 'data.frame':
                                       1501 obs. of 17 variables:
        : 'cal.yr' num 1991 1991 1991 1991 ...
         : 'cal.yr' num 47.5 56.1 51.4 51.1 55.5 ...
 $ lex.dur: 'cal.yr' num 19.4 19.4 19.4 19.4 15.6 ...
 $ lex.Cst: num 0 0 0 0 0 0 0 0 0 0 ...
 $ lex.Xst: int 0 0 0 0 0 0 0 1 0 0 ...
 $ lex.id : int 1 2 3 4 5 6 7 8 9 10 ...
         : int 1 2 3 4 5 6 7 8 9 10 ...
 $ birth : Factor w/ 1349 levels "1929-08-01", "1929-12-23",..: 811 230 537 566 266 3
 $ death : int 0000111100...
 $ chdeath: int 0 0 0 0 0 0 0 1 0 0 ...
  ybirth: 'cal.yr' num 1943 1935 1939 1940 1935 ...
  yentry : 'cal.yr' num
                        1991 1991 1991 1991 ...
 $ yexit : 'cal.yr' num 2010 2010 2010 2010 2006 ...
 $ agentry: 'cal.yr' num 47.5 56.1 51.4 51.1 55.5 ...
 $ agexit : 'cal.yr' num 66.9 75.5 70.8 70.5 71.1 ...
- attr(*, "time.scales")= chr "per" "age"

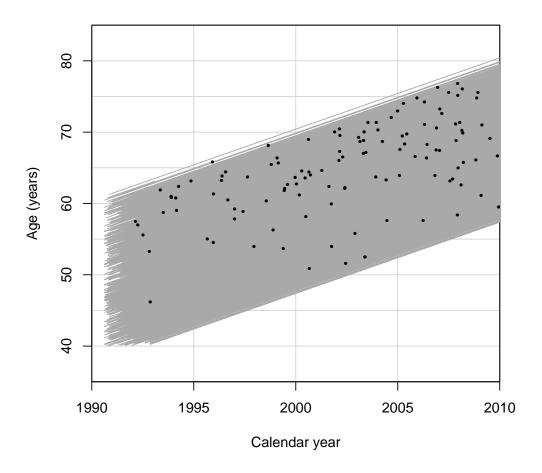
- attr(*, "time.since")= chr "" ""

- attr(*, "breaks")=List of 2
  .. $ per: NULL
  ..$ age: NULL
> summary(oc.lex)
Transitions:
    To
From 0 1 Records:
                       Events: Risk time: Persons:
  0 1381 120
                  1501
                           120
                                 25280.91
                                               1501
```

14. At this stage it is informative to examine a graphical presentation of the follow-up lines and outcome cases in a conventional Lexis diagram. To rationalize your work we have created a separate source file plots-caco-ex.R to do the graphics for this tas as well as for some forthcoming ones. The source source file is found in the same folder where the data sets are. – Load the source file and have a look at the content of the first function in it

Function plot1() makes the graph required here. No arguments are needed when calling the function

```
> plot1()
```



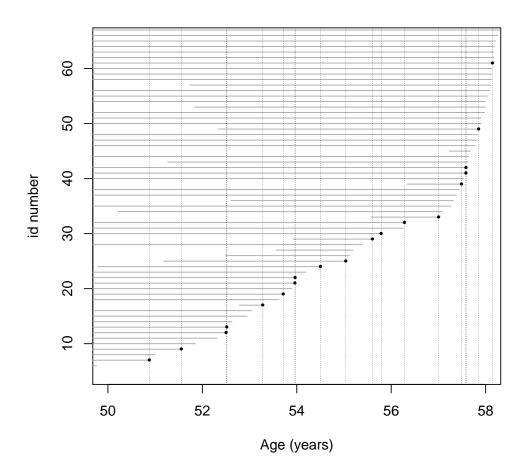
15. As age is here the main time axis, we shall illustrate the *study base* or the follow-up lines and outcome events along the age scale, being ordered by age at exit. Function plot2() in the same source file does the work. Vertical lines at those ages when new coronary deaths occur are drawn to identify the pertinent *risk sets*. For that purpose it is useful first to sort the data frame and the lexis object jointly by age at exit & age at entry, and to give a new ID number according to that order.

```
> oc.ord <- cbind(ID = 1:1501, oc[ order( oc$agexit, oc$agentry), ] )
> oc.lexord <- Lexis( entry = list( age = agentry ),</pre>
                          exit = list( age = agexit),
                  exit.status = chdeath,
                            id = ID, data = oc.ord)
NOTE: entry.status has been set to 0 for all.
> plot2
function ()
    plot(oc.lexord, time.scale = "age", xlim = c(40, 80), xlab = "Age (years)")
    points(oc.lexord, time.scale = "age", pch = c(NA, 16)[oc.lexord$lex.Xst +
         1], cex = 0.5)
    with(subset(oc.lexord, lex.Xst == 1), abline(v = agexit,
         lty = 3, lwd = 0.5)
> plot2()
```



Using function plot3() in the same source file we now zoom the graphical illustration of the risk sets into event times occurring between 50 to 58 years.

```
> plot3
function ()
{
```



## 2.14.2 Nested case-control study

We shall now employ the strategy of *risk-set sampling* or *time-matched* sampling of controls, *i.e.* we are conducting a *nested case-control study* within the cohort.

16. The risk sets are defined according to the age at diagnosis of the case. Further matching is applied for age at entry by 1-year agebands. For this purpose we first generate a categorical variable agen2 for age at entry

```
> oc.lex$agen2 <- cut(oc.lex$agentry, br = seq(40, 62, 1) )</pre>
```

Matched sampling from risk sets may be carried out using function ccwc() found in the Epi package. Its main arguments are the times of entry and

exit which specify the time at risk along the main time scale (here age), and the outcome variable to be given in the fail argument. The number of controls per case is set to be two, and the additional matching factor is given. – After setting the RNG seed (with your own number), make a call of this function and see the structure of the resulting data frame cactrl containing the cases and the chosen individual controls.

```
> set.seed(9863157)
> cactrl <-
    ccwc(entry=agentry, exit=agexit, fail=chdeath,
         controls = 2, match= agen2,
         include = list(id, agentry),
         data=oc.lex, silent=FALSE)
Sampling risk sets: ......
> str(cactrl)
'data.frame':
                   360 obs. of 7 variables:
$ Set
        : num 1 1 1 2 2 2 3 3 3 4 ...
        : num 8 1155 614 95 204 ...
$ Time : num 63.9 63.9 63.9 66.7 66.7 ...
$ Fail : num 1001001001...
$ agen2 : Factor w/ 22 levels "(40,41]","(41,42]",..: 8 8 8 8 8 8 8 8 8 8 ...
$ id : int 8 1155 614 95 204 292 115 351 526 504 ...
$ agentry: num 47.7 47 47.4 47.5 47.6 ...
```

Check the meaning of the four first columns of the case-control data frame from the help page of function ccwc().

17. Now we shall start collecting data on the risk factors for the cases and their matched controls, including determination of the total cholesterol levels from the frozen sera! The storehouse of the risk factor measurements for the whole cohort is file occoh-Xdata.txt. It contains values of the following variables.

18. In the next step we collect the values of the risk factors for our cases and controls by merging the case-control data frame and the storehouse file. In this operation we use the id variable in both files as the key to link each individual case and control with his own data on risk factors.

```
'data.frame': 360 obs. of 10 variables:
$ id : int 2 4 8 13 15 37 41 42 43 47 ...
$ Set : num 16 93 1 25 50 5 5 9 18 96 ...
$ Map : num 2 4 8 13 15 37 41 42 43 47 ...
$ Time : num 59 63.7 63.9 70.2 60.8 ...
$ Fail : num 0 0 1 0 0 0 1 1 1 0 ...
$ agen2 : Factor w/ 22 levels "(40,41]","(41,42]",..: 17 12 8 15 19 1 1 17 15 21 .
$ agentry: num 56.1 51.1 47.7 54.9 59 ...
$ smok : int 3 1 2 2 2 3 4 2 3 1 ...
$ tchol : num 6.55 5.93 7.43 5.28 6.03 5.15 6.09 5.41 5.72 6.22 ...
$ sbp : int 128 102 154 153 147 116 125 156 128 154 ...
```

19. We shall treat smoking as categorical and total cholesterol and systolic blood pressure as quantitative risk factors, but the values of the latter will be divided by 10 to get more interpretable effect estimates.

Convert the smoking variable into a factor.

```
> oc.ncc$smok <- factor(oc.ncc$smok,
+ labels = c("never", "ex", "1-14/d", ">14/d"))
```

20. It is useful to start the analysis of case-control data by simple tabulations by the categorized risk factors. Crude estimates of the rate ratios associated with them, in which matching is ignored, can be obtained as instructed in Janne's lecture on Poisson and logistic models on Saturday 23 May. We shall focus on smoking

```
> stat.table( index = list( smok, Fail ),
         contents = list( count(), percent(smok) ),
          margins = T, data = oc.ncc )
 _____
       -----Fail-----
            0 1 Total
smok
never 89 31
                         120
         37.1 25.8
                        33.3
                  19
           44 19 63
18.3 15.8 17.5
 1-14/d
            73
                   42
                         115
           30.4
                 35.0
                        31.9
>14/d
            34
                  28
                         62
           14.2
                 23.3
                        17.2
                         360
Total
           240
                 120
          100.0
                 100.0
                      100.0
> smok.crncc <- glm( Fail ~ smok, family=binomial, data = oc.ncc)
> round(ci.exp(smok.crncc), 3)
          exp(Est.) 2.5% 97.5%
(Intercept) 0.348 0.231 0.524
             1.240 0.631 2.437
smokex
smok1-14/d
smok>14/d
             1.652 0.946 2.885
             2.364 1.239 4.511
```

21. A proper analysis takes into account matching that was employed in the selection of controls for each case from the pertinent risk set further restricted to subjects who were about the same age at entry as the case was. Also, adjustment for the other risk factors is desirable. In this analysis function clogit() in survival package is utilized. It is in fact a wrapper of function coxph().

```
> m.clogit <- clogit( Fail ~ smok + I(sbp/10) + tchol +
        strata(Set), data = oc.ncc )
> summary(m.clogit)
Call:
coxph(formula = Surv(rep(1, 360L), Fail) ~ smok + I(sbp/10) +
    tchol + strata(Set), data = oc.ncc, method = "exact")
 n= 360, number of events= 120
             coef exp(coef) se(coef)
                                         z Pr(>|z|)
smokex
          0.06792
                   1.07028 0.34415 0.197 0.84355
smok1-14/d 0.47116
                    1.60185 0.30430 1.548 0.12154
                    2.52584 0.33378 2.776 0.00550 **
smok>14/d 0.92657
I(sbp/10) 0.15898
                    1.17231 0.05544 2.868 0.00413 **
                   1.41921 0.11182 3.131 0.00174 **
tchol
          0.35010
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
          exp(coef) exp(-coef) lower .95 upper .95
smokex
              1.070
                        0.9343
                                  0.5452
                                             2.101
smok1-14/d
              1.602
                        0.6243
                                  0.8823
                                             2.908
smok>14/d
              2.526
                        0.3959
                                  1.3131
                                             4.859
                        0.8530
I(sbp/10)
              1.172
                                  1.0516
                                             1.307
tchol
              1.419
                        0.7046
                                  1.1399
                                             1.767
Rsquare= 0.069 (max possible= 0.519)
Likelihood ratio test= 25.78
                             on 5 df,
                    = 22.03
                                        p = 5e - 04
Wald test
                             on 5 df,
Score (logrank) test = 24.34
                             on 5 df,
                                        p = 2e - 04
> round(ci.exp(m.clogit), 3)
          exp(Est.) 2.5% 97.5%
              1.070 0.545 2.101
smokex
smok1-14/d
              1.602 0.882 2.908
smok>14/d
              2.526 1.313 4.859
I(sbp/10)
              1.172 1.052 1.307
              1.419 1.140 1.767
tchol
```

Compare these with the crude estimates obtained above.

## 2.14.3 Case-cohort study

Now we start applying the second major outcome-selective sampling strategy for collecting exposure data from a big study population

22. The subcohort is selected as a simple random sample (n = 260) from the whole cohort. The id-numbers of the individuals that are selected will be stored in vector subcids, and subcind is an indicator for inclusion to the subcohort.

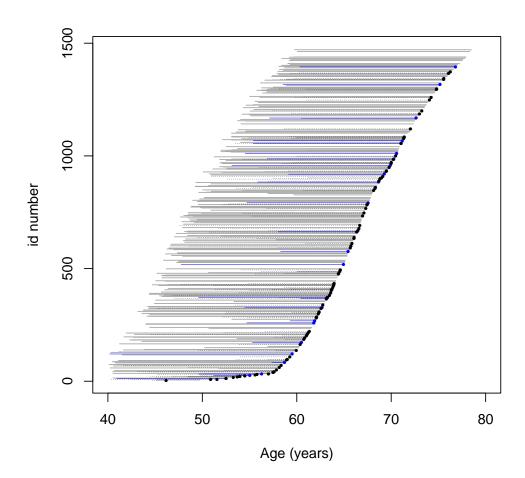
```
> N <- 1501; n <- 260
> set.seed(1579863)
> subcids <- sample(N, n )
> oc.lex$subcind <- 1*(oc.lex$id %in% subcids)</pre>
```

23. We form the data frame oc.cc to be used in the subsequent analysis selecting the union of the subcohort members and the case group from the data frame of the full cohort. After that we collect the data of the risk factors from the data storehouse for the subjects in the case-cohort data

```
> oc.cc <- subset( oc.lex, subcind==1 | chdeath ==1)</pre>
> oc.cc <- merge( oc.cc, ocX[, c("id", "smok", "tchol", "sbp")],
    by = "id")
> str(oc.cc)
Classes 'Lexis' and 'data.frame':
                                          355 obs. of 22 variables:
        : int 6 8 18 27 28 37 40 41 42 43 ...
         : num 1991 1991 1991 1991 ...
        : num 54.4 47.7 50.1 49.3 58.4 ...
$ lex.dur: num 16.8 16.2 19.4 19.4 19.4 ...
$ lex.Cst: num 0 0 0 0 0 0 0 0 0 0 ...
$ lex.Xst: int 0 1 0 0 0 0 0 1 1 1 ...
$ lex.id : int 6 8 18 27 28 37 40 41 42 43 ...
$ birth : Factor w/ 1349 levels "1929-08-01", "1929-12-23",...: 336 790 639 680 101
$ entry : Factor w/ 302 levels "1990-08-14","1990-08-15",..: 1 2 3 4 4 6 6 6 6 6 .
$ exit : Factor w/ 290 levels "1992-02-25","1992-04-06",..: 229 218 290 290 290
$ death : int 1 1 0 0 0 0 1 1 1 1 ...
$ chdeath: int 0 1 0 0 0 0 0 1 1 1 ...
$ ybirth : num 1936 1943 1941 1941 1932 ...
$ yentry : num 1991 1991 1991 1991 ...
$ yexit : num 2007 2007 2010 2010 2010 ...
$ agentry: num 54.4 47.7 50.1 49.3 58.4 ...
$ agexit : num 71.3 63.9 69.5 68.7 77.8 ...
$ agen2 : Factor w/ 22 levels "(40,41]","(41,42]",..: 15 8 11 10 19 1 6 1 17 15 ...
$ subcind: num 1 0 1 1 1 1 1 1 1 0 ...
$ smok : int 2 2 1 4 1 3 4 4 2 3 ...
$ tchol : num 5.9 7.43 3.34 8.31 4.56 5.15 5.88 6.09 5.41 5.72 ...
        : int 119 154 130 140 230 116 141 125 156 128 ...
 - attr(*, "breaks")=List of 2
 ..$ per: NULL
 ..$ age: NULL
- attr(*, "time.scales")= chr "per" "age"
- attr(*, "time.since")= chr "" ""
```

24. Function plot4() in the same source file creates a graphical illustration of the lifelines contained in the case-cohort data. Lines for the subcohort non-cases are grey without bullet at exit, those for subcohort cases are blue with blue bullet at exit, and for cases outside the subcohort the lines are black and dotted with black bullets at exit.

```
time.scale = "age", pch = 16, col = "blue", cex = 0.5)
lines(subset(oc.lexord, chdeath == 1 & !(id %in% subcids)),
    time.scale = "age", lty = 3, lwd = 0.5, col = "black")
points(subset(oc.lexord, chdeath == 1 & !(id %in% subcids)),
    time.scale = "age", pch = 16, col = "black", cex = 0.5)
}
> plot4()
```



25. Define the categorical smoking variable again.

```
> oc.cc$smok <- factor(oc.cc$smok,
+ labels = c("never", "ex", "1-14/d", ">14/d"))
```

A crude estimate of the hazard ratio for the various smoking categories k vs. non-smokers (k = 1) can be obtained by tabulating cases  $(D_k)$  and person-years  $(y_k)$  in the subcohort by smoking and then computing the relevant exposure odds ratio for each category:

$$HR_k^{\text{crude}} = \frac{D_k/D_1}{y_k/y_1}$$

```
> sm.cc <- stat.table( index = smok,
+ contents = list( Cases = sum(lex.Xst), Pyrs = sum(lex.dur) ),
+ margins = T, data = oc.cc)
> print(sm.cc, digits = c(sum=0, ratio=1))
```

26. To estimate jointly the rate ratios associated with the categorized risk factors we now fit the pertinent Cox model applying the method of weighted partial likelihood as presented by Ling & Ying (1993) and Barlow (1994). The weights for all cases and non-cases in the subcohort are first computed and added to the data frame.

Next, the Cox model is fitted by the method of weighted partial likelihood using coxph(), such that the robust covariance matrix will be used as the source of standard errors for the coefficients.

```
> oc.cc$surob <- with(oc.cc, Surv(agentry, agexit, chdeath) )</pre>
> cc.we <- coxph( surob \sim smok + I(sbp/10) + tchol, robust = TRUE,
        weight = w, data = oc.cc)
> summary(cc.we)
coxph(formula = surob ~ smok + I(sbp/10) + tchol, data = oc.cc,
    weights = w, robust = TRUE)
 n= 355, number of events= 120
              coef exp(coef) se(coef) robust se z Pr(>|z|)
         -0.08862 0.91519 0.29229 0.35196 -0.252 0.80120
smokex
smok1-14/d 0.52294 1.68697 0.23852 0.30705 1.703 0.08855 .
smok>14/d 0.95799 2.60644 0.26625 0.34746 2.757 0.00583 **
I(sbp/10) 0.11754 1.12472 0.04025 0.05615 2.093 0.03632 *
tchol
        0.31095 1.36471 0.07488 0.09890 3.144 0.00167 **
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
          exp(coef) exp(-coef) lower .95 upper .95
smokex
             0.9152
                       1.0927
                               0.4591
                                            1.824
smok1-14/d
             1.6870
                        0.5928
                                  0.9242
                                             3.079
smok>14/d 2.6064
I(sbp/10) 1.1247
tchol 1.3647
                        0.3837
                                  1.3191
                                             5.150
                     0.8891
0.7328
                                1.0075
1.1242
                                             1.256
                                            1.657
```

```
Concordance= 0.673 (se = 0.029)
Rsquare= 0.1 (max possible= 0.988)
Likelihood ratio test= 37.28 on 5 df,
                                       p = 5e - 07
                                       p=0.001
Wald test = 19.86 on 5 df,
Score (logrank) test = 38.89 on 5 df,
                                       p=2e-07,
                                                  Robust = 19.31 p=0.002
  (Note: the likelihood ratio and score tests assume independence of
     observations within a cluster, the Wald and robust score tests do not).
> round( ci.exp(cc.we), 3)
          exp(Est.) 2.5% 97.5%
              0.915 0.459 1.824
smokex
              1.687 0.924 3.079
smok1-14/d
              2.606 1.319 5.150
smok>14/d
I(sbp/10)
              1.125 1.008 1.256
tchol
              1.365 1.124 1.657
```

The covariance matrix for the coefficients may also be computed by the dfbeta-method. After that a comparison is made between standard errors from the naive, robust and dfbeta covariance matrix, respectively. You will see that the naive SEs are essentially smaller than those obtained by the robust and the dfbeta method, respectively.

27. The same analysis can also be done using function cch() in package survival with method = "LinYing" as follows:

```
> cch.LY <- cch( surob ~ smok + I(sbp/10) + tchol, stratum=NULL,
    subcoh = ~subcind, id = ~id, cohort.size = N, data = oc.cc,
     method ="LinYing" )
> summary(cch.LY)
Case-cohort analysis, x $method, LinYing
with subcohort of 260 from cohort of 1501
Call: cch(formula = surob ~ smok + I(sbp/10) + tchol, data = oc.cc,
   subcoh = ~subcind, id = ~id, stratum = NULL, cohort.size = N,
   method = "LinYing")
Coefficients:
            Coef
                   HR (95% CI)
          -0.089 0.915 0.459 1.825 0.801
smokex
smok1-14/d 0.523 1.687 0.934 3.047 0.083
smok>14/d 0.958 2.607 1.326 5.123 0.005
I(sbp/10) 0.118 1.125 1.017 1.244 0.022
          0.311 1.365 1.121 1.661 0.002
tchol
```

28. The summary() method for the cch() object does not print the standard errors for the coefficients. The following comparison demonstrates numerically that the method of Lin & Ying is the same as weighted partial likelihood coupled with dfbeta covariance matrix.

```
> cbind( coef( cc.we), coef(cch.LY) )
                 [,1]
smokex -0.08862081 -0.0888895
smok1-14/d 0.52293602 0.5229370
smok>14/d 0.95798562 0.9580133
I(sbp/10) 0.11753848 0.1175287
          0.31094520 0.3109491
tchol
> round( cbind( sqrt(diag(cc.we$naive.var)), sqrt(diag(cc.we$var)),
     sqrt(diag(covdfb.we)), sqrt(diag(cch.LY$var)) ), 3)
           [,1] [,2] [,3] [,4]
          0.292 0.352 0.353 0.352
smokex
smok1-14/d 0.239 0.307 0.302 0.302
smok>14/d 0.266 0.347 0.345 0.345
I(sbp/10) 0.040 0.056 0.051 0.051
tchol 0.075 0.099 0.100 0.100
```

#### 2.14.4 Full cohort analysis and comparisons

Finally, suppose the investigators could afford to collect the data of risk factors from the storehouse for the whole cohort.

29. Let us form the data frame corresponding to the full cohort design and convert again smoking to be categorical.

```
> oc.full <- merge( oc.lex, ocX[, c("id", "smok", "tchol", "sbp")],
+ by.x = "id", by.y = "id")
> oc.full$smok <- factor(oc.full$smok,
+ labels = c("never", "ex", "1-14/d", ">14/d"))
```

Juts for comparison with the corresponding analysis in case-cohort data perform a similar crude estimation of hazard ratios associated with smoking.

```
> sm.coh <- stat.table( index = smok,
+ contents = list( Cases = sum(lex.Xst), Pyrs = sum(lex.dur) ),
        margins = T, data = oc.full)
> print(sm.coh, digits = c(sum=0, ratio=1))
_____
        Cases Pyrs
never
           31 10363
          19
42
                  4879
1-14/d
                  6246
            28
>14/d
                  3793
           120 25281
> HRcoh <- (sm.coh[ 1, -5]/sm.coh[ 1, 1])/(sm.coh[ 2, -5]/sm.coh[2, 1])
> round(HRcoh, 3)
```

```
ex 1-14/d > 14/d
1.000 1.302 2.248
                   2.468
```

30. Fit now the Cox model to the full cohort, and there is no need to employ extra tricks upon the ordinary coxph() fit.

```
> cox.coh <- coxph( Surv(agentry, agexit, chdeath) ~
        smok + I(sbp/10) + tchol, data = oc.full)
> summary(cox.coh)
coxph(formula = Surv(agentry, agexit, chdeath) ~ smok + I(sbp/10) +
   tchol, data = oc.full)
 n= 1501, number of events= 120
            coef exp(coef) se(coef)
                                    z Pr(>|z|)
         smokex
smok1-14/d 0.72567 2.06612 0.23704 3.061 0.002203 **
smok>14/d 0.95054 2.58711 0.26198 3.628 0.000285 ***
I(sbp/10) 0.14372 1.15456 0.04096 3.509 0.000450 ***
         tchol
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
         exp(coef) exp(-coef) lower .95 upper .95
smokex
             1.116
                     0.8962
                             0.629
smok1-14/d
             2.066
                      0.4840
                               1.298
                                         3.288
smok>14/d
             2.587
                      0.3865
                               1.548
                                         4.323
I(sbp/10)
                      0.8661
                               1.065
             1.155
                                         1.251
             1.304
tchol
                      0.7671
                              1.135
                                        1.498
Concordance= 0.681 (se = 0.029)
Rsquare= 0.027 (max possible= 0.653)
Likelihood ratio test= 41.16 on 5 df,
                                    p = 9e - 08
Wald test
                  = 42.05 on 5 df,
                                    p = 6e - 08
Score (logrank) test = 43.29 on 5 df,
                                    p = 3e - 08
```

31. Lastly, a comparison of the point estimates and standard errors between the different designs, including variants of analysis for the case-cohort design, can be performed.

```
> betas <- round(cbind( coef(cox.coh),
      coef(m.clogit),
      coef(cc.we), coef(cch.LY) ), 3)
> colnames(betas) <- c("coh", "ncc", "cc.we", "cch.LY")</pre>
> betas
           coh ncc cc.we cch.LY
         0.110 0.068 -0.089 -0.089
smokex
smok1-14/d 0.726 0.471 0.523 0.523
smok>14/d 0.951 0.927 0.958 0.958
I(sbp/10) 0.144 0.159 0.118 0.118
tchol
          0.265 0.350 0.311 0.311
> SEs <- round(cbind( sqrt(diag(cox.coh$var)),
     sqrt(diag(m.clogit$var)), sqrt(diag(cc.we$naive.var)),
     sqrt(diag(cc.we$var)), sqrt(diag(covdfb.we)),
sqrt(diag(cch.LY$var)) ), 3)
> SEs
```

```
ncc ccwe-nai ccwe-rob ccwe-dfb cch-LY
smokex
           0.292 0.344
                          0.292
                                  0.352
                                            0.353
                                                   0.352
smok1-14/d 0.237 0.304
                          0.239
                                   0.307
                                            0.302
                                                   0.302
smok>14/d 0.262 0.334
                                            0.345
                          0.266
                                   0.347
                                                   0.345
I(sbp/10) 0.041 0.055
                          0.040
                                   0.056
                                            0.051
                                                   0.051
tchol
           0.071 0.112
                          0.075
                                   0.099
                                            0.100
                                                   0.100
```

You will notice that the point estimates of the coefficients obtained from the full cohort, nested case-control, and case-cohort analyses, respectively, are somewhat variable.

However, the standard errors across the NCC and different proper CC analyses are relatively similar. Those from a naive covariance matrix of a CC analysis, though, are practically equal to the SEs from the full cohort analysis, reflecting the fact that the naive analysis implicitly assumes there being as much information available as there is with full cohort data.

#### 2.14.5 Further exercises and homework

- 32. If you have time, you could run both the NCC study and CC study again but now with a larger control group or subcohort; for example 4 controls per case in NCC and n=520 as the subcohort size in CC. Remember resetting the seed first. Pay attention in the results to how much closer will be the point estimates and the proper SEs to those obtained from the full cohort design.
- 33. Instead of simple linear terms for sbp and tchol you could try to fit spline models to describe their effects.
- 34. A popular alternative to weighted partial likelihood in the analysis of case-cohort data is the pseudo-likelihood method (Prentice 1986), which is based on "late entry" to follow-up of the case subjects not belonging to the subcohort. A longer way of applying this approach, which you could try at home after the course, would first require manipulation of the oc.cc data frame, as outlined on slide 34. Then coxph() would be called like in model object cc.we above but now with weights = 1. Similar corrections on the covariance matrix are needed, too. However, a shorter way is provided by function cch() which you can apply directly to the case-cohort data oc.cc as before but now with method = "Prentice". Try this and compare the results with those obtained by weighted partial likelihood in models cc.we and cch.LY.
- 35. Yet another computational solution for maximizing weighted partial likelihood is provided by a combination of functions twophase() and svycoxph() of the survey package. The approach is illustrated with an example in a vignette "Two-phase designs in epidemiology" by Thomas Lumley (see
  - http://cran.r-project.org/web/packages/survey/vignettes/epi.pdf, p. 4-7). You can try this at home and check that you would obtain similar results as with models cc.we and cch.LY.

#### Time-dependent variables and multiple 2.15states

#### 2.15.1The renal failure dataset

1. The dataset is in Stata-format, so we read the dataset using read.dta from the foreign package (which is part of the standard R-distribution):

```
library( Epi )
library( foreign )
clear()
renal <- read.dta( "http://BendixCarstensen.com/SPE/data/renal.dta" )
# renal <- read.dta( "./data/renal.dta" )</pre>
renal$sex <- factor( renal$sex, labels=c("M","F") )</pre>
head( renal )
 id sex
                                 dor
              dob
                        doe
      M 1967.944 1996.013
                                  NA 1997.094
1 17
       F 1959.306 1989.535 1989.814 1996.136
3 27
      F 1962.014 1987.846
                                                   3
                                  NA 1993.239
      M 1950.747 1995.243 1995.717 2003.993
                                                   0
      F 1961.296 1987.884 1996.650 2003.955
                                                   0
      F 1952.374 1983.419
                                  NA 1991.484
```

2. We use the Lexis function to declare the data as survival data with age, calendar time and time since entry into the study as timescales. Note that any coding of event > 0 will be labeled "ESRD", i.e. renal death (death of kidney (transplant or dialysis), or person).

Note that you must make sure that the "alive" state (here NRA) is the first, as Lexis assumes that everyone starts in this state (unless of course entry.status is specified):

```
Lr <- Lexis( entry = list( per = doe,</pre>
                            age = doe-dob,
                            tfi = 0),
               exit = list( per = dox ),
        exit.status = factor( event>0, labels=c("NRA", "ESRD") ),
               data = renal )
NOTE: entry.status has been set to "NRA" for all.
 str( Lr )
Classes 'Lexis' and 'data.frame':
                                         125 obs. of 14 variables:
        : num 1996 1990 1988 1995 1988 ...
 $ age
          : num 28.1 30.2 25.8 44.5 26.6 ...
         : num 0000000000...
 $ lex.dur: num 1.08 6.6 5.39 8.75 16.07 ...
 $ lex.Cst: Factor w/ 2 levels "NRA", "ESRD": 1 1 1 1 1 1 1 1 1 1 ...
 $ lex.Xst: Factor w/ 2 levels "NRA", "ESRD": 2 2 2 1 1 2 2 1 2 1 ...
 $ lex.id : int 1 2 3 4 5 6 7 8 9 10 ...
 $ id
         : num 17 26 27 33 42 46 47 55 62 64 ...
         : Factor w/ 2 levels "M", "F": 1 2 2 1 2 2 1 1 2 1 ...
 $ sex
         : num 1968 1959 1962 1951 1961 ...
 $ dob
 $ doe
                1996 1990 1988 1995 1988 ...
         : num
 $ dor
         : num
                NA 1990 NA 1996 1997 ...
                1997 1996 1993 2004 2004
          : num
 $ event : num 2 1 3 0 0 2 1 0 2 0 ...
 - attr(*, "time.scales")= chr "per" "age" "tfi"
```

```
- attr(*, "time.since")= chr "" "" ""
- attr(*, "breaks")=List of 3
...$ per: NULL
...$ age: NULL
...$ tfi: NULL
summary( Lr )
Transitions:
    To
From NRA ESRD Records: Events: Risk time: Persons:
    NRA 48 77 125 77 1084.67 125
```

3. We can visualize the follow-up in a Lexis-diagram, using the plot method for Lexis objects.

The result is the left hand plot in figure 2.9, and we see a person entering at a negative age, clearly because he is born way out in the future.

4. So we correct the data and make the correct plot, as seen in the right hand plot in figure 2.9:

```
Lr <- transform(Lr, dob = ifelse(dob>2000, dob-100, dob),
                     age = ifelse( dob>2000, age+100, age ) )
subset( Lr, id==586 )
       per
                 age tfi lex.dur lex.Cst lex.Xst lex.id id sex
                                                                      dob
                                                                               doe do
88 1989.343 61.18857
                    0 3.495893
                                     NRA
                                            ESRD
                                                     88 586
                                                              M 1928.155 1989.343
       dox event
88 1992.839
plot( Lr, col="black", lwd=3 )
```

5. We can produce a slightly more fancy Lexis diagram. Note that we have a x-axis of 40 years, and a y-axis of 80 years, so when specifying the output file adjust the total width of the plot so that the use mai mai to specify the margins of the plot leaves a plotting area twice as high as wide. The mai argument to par gives the margins in inches, so the total size of the horizontal and vertical margins is 1 inch, to which we add 80/5 in the height, and 40/5 in the horizontal direction, each giving exactly 5 years per inch in physical size.

6. We now do a Cox-regression analysis with the variables sex and age at entry into the study, using time since entry to the study as time scale.

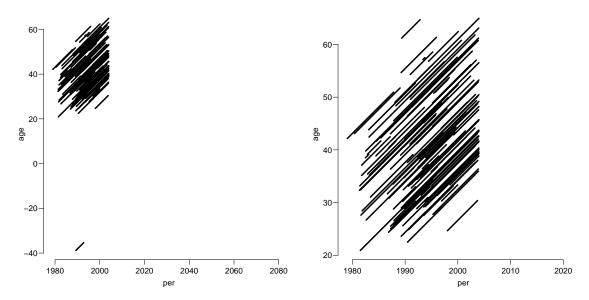


Figure 2.9: Default Lexis diagram before and after correction of the obvious data outlier.

```
library( survival )
 mc <- coxph( Surv( lex.dur, lex.Xst=="ESRD" ) ~</pre>
              I(age/10) + sex, data=Lr)
 summary( mc )
Call:
coxph(formula = Surv(lex.dur, lex.Xst == "ESRD") ~ I(age/10) +
    sex, data = Lr)
  n= 125, number of events= 77
             coef exp(coef) se(coef)
                                            z Pr(>|z|)
                      1.7357
                               0.1402 3.932 8.43e-05 ***
I(age/10)
           0.5514
                               0.2727 -0.666
          -0.1817
                      0.8338
sexF
                                                 0.505
                0 '*** 0.001 '** 0.01 '* 0.05 '. ' 0.1 ' ' 1
Signif. codes:
          exp(coef) exp(-coef) lower .95 upper .95
             1.7357
                                   1.3186
                                               2.285
I(age/10)
                         0.5761
             0.8338
                         1.1993
                                   0.4886
                                               1.423
sexF
Concordance= 0.612 (se = 0.036)
Rsquare= 0.121 (max possible= 0.994)
                                           p = 3e - 04
Likelihood ratio test= 16.07
                              on 2 df,
                              on 2 df,
Wald test
                      = 16.38
                                           p = 3e - 04
Score (logrank) test = 16.77
                               on 2 df,
```

The hazard ratio between males and females is 1.19 (0.70–2.04) (the inverse of the c.i. for female vs male) and between two persons who differ 10 years in age at entry it is 1.74 (1.32–2.29).

7. The main focus of the paper was to assess whether the occurrence of remission (return to a lower level of albumin excretion, an indication of kidney recovery) influences mortality.

"Remission" is a time-dependent variable which is initially 0, but takes the value 1 when remission occurs. This is accomplished using the cutLexis



Figure 2.10: The more fancy version of the Lexis diagram for the renal data.

function on the Lexis object, where we introduce a remission state "Rem". We declare the "NRA" state as a precursor state, i.e. a state that is *less* severe than "Rem" in the sense that a person who see a remission will stay in the "Rem" state unless he goes to the "ESRD" state. The statement to do this is:

```
Lc <- cutLexis( Lr, cut = Lr$dor, # where to cut follow up</pre>
               timescale = "per", # what timescale are we referring to
             new.state = "Rem", # name of the new state
split.state = TRUE, # different states sepending on previous
        precursor.states = "NRA" ) # which states are less severe
 summary( Lc )
Transitions:
     To
From NRA Rem ESRD ESRD(Rem) Records: Events: Risk time: Persons:
              69 0 122 98
0 8 32 8
69 8 154 106
                                         98 824.77
  NRA 24 29
      0 24
                                                      259.90
                                                                    32
  Rem
  Sum 24 53
                                                     1084.67
                                                                    125
```

Note that we have two different ESRD states depending on whether the person was in remission or not at the time of ESRD.

To illustrate how the cutting of follow-up has worked we can list the records for select persons before and after the split:

```
subset( Lr, lex.id %in% c(2:4,21))[,c(1:9,12)]
                 age tfi
                            lex.dur lex.Cst lex.Xst lex.id
                                                             id sex
                                                                          dor
   1989.535 30.22895
                       0 6.60061602
                                         NRA
                                                ESRD
                                                          2
                                                             26
                                                                  F 1989,814
   1987.846 25.83196
                       0 5.39322382
                                         NRA
                                                ESRD
                                                          3
                                                             27
                                                                  F
                                                                           NA
  1995.243 44.49589
                       0 8.74982888
                                         NRA
                                                 NRA
                                                          4 33
                                                                  M 1995.717
21 1992.952 32.35626
                       0 0.07905544
                                                                  F
                                         NRA
                                                 NRA
                                                         21 152
                                                                           NA
 subset( Lc, lex.id %in% c(2:4,21))[,c(1:9,12)]
                  age
                            tfi
                                   lex.dur lex.Cst
                                                      lex.Xst lex.id
                                                                       id sex
         per
                                                                                   dor
2
    1989.535 30.22895 0.0000000 0.27891855
                                                NRA
                                                                   2
                                                                       26
                                                                            F 1989.814
                                                          R.em
127 1989.814 30.50787 0.2789185 6.32169747
                                                                    2
                                                                       26
                                                                            F 1989.814
                                                Rem ESRD(Rem)
    1987.846 25.83196 0.0000000 5.39322382
                                                                   3
                                                                      27
                                                                            F
                                                NRA
                                                         ESRD
                                                                                    NA
                                                                   4 33
                                                                            M 1995.717
    1995.243 44.49589 0.0000000 0.47330595
                                                NRA
                                                          Rem
129 1995.717 44.96920 0.4733060 8.27652293
                                                                   4
                                                                      33
                                                                            M 1995.717
                                                Rem
                                                          Rem
   1992.952 32.35626 0.0000000 0.07905544
                                                NRA
                                                          NRA
                                                                   21 152
                                                                            F
                                                                                    NA
```

8. We can show how the states are connected and the number of transitions between them by using boxes. This is an interactive command that requires you to click in the graph window

Alternatively you can let R try to place the boxes for you, and even compute rates (in this case in units of events per 100 PY):

9. We can make a Lexis diagram where different coloring is used for different segments of the follow-up. The plot.Lexis function draws a line for each record in the dataset, so we can just index the coloring by lex.Cst and lex.Xst as appropriate — indexing by a factor corresponds to indexing by the *index number* of the factor levels, so you must be know which order the factor levels are in.

10. We now make Cox-regression of mortality (i.e. endpoint "ESRD") with sex, age at entry and remission as explanatory variables, using time since entry as timescale.

We include lex.Cst as time-dependent variable, and indicate that each record represents follow-up from tfi to tfi+lex.dur.

```
( EP <- levels(Lc)[3:4] )
[1] "ESRD" "ESRD(Rem)"
```

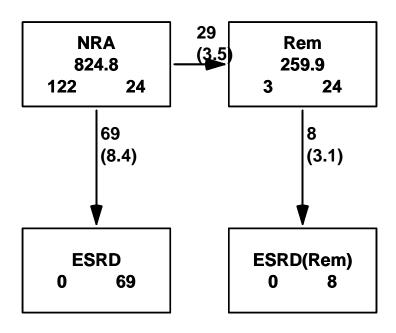


Figure 2.11: States and transitions between them.

The numbers in each box are the person-years and the number of persons starting (left) and ending (right) their follow-up in each state; the numbers on the arrows are the number of transitions and the overall transition rates (in per 100 PY, by the scale.R=100).

```
m1 <- coxph( Surv( tfi,</pre>
                                       # from
                  tfi+lex.dur,
                                       # to
                  lex.Xst %in% EP ) ~ # event
             sex + I((doe-dob-50)/10) + # fixed covariates
             (lex.Cst=="Rem"),
                                      # time-dependent variable
             data = Lc )
summary( m1 )
Call:
coxph(formula = Surv(tfi, tfi + lex.dur, lex.Xst %in% EP) ~ sex +
   I((doe - dob - 50)/10) + (lex.Cst == "Rem"), data = Lc)
 n= 154, number of events= 77
                         coef exp(coef) se(coef)
                                                    z Pr(>|z|)
sexF
                     -0.05534
                              0.94616 0.27500 -0.201 0.840517
I((doe - dob - 50)/10) 0.52190
                               1.68522 0.13655 3.822 0.000132 ***
lex.Cst == "Rem"TRUE -1.26241
                               Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
                     exp(coef) exp(-coef) lower .95 upper .95
sexF
                        0.9462 1.0569 0.5519 1.6220
```

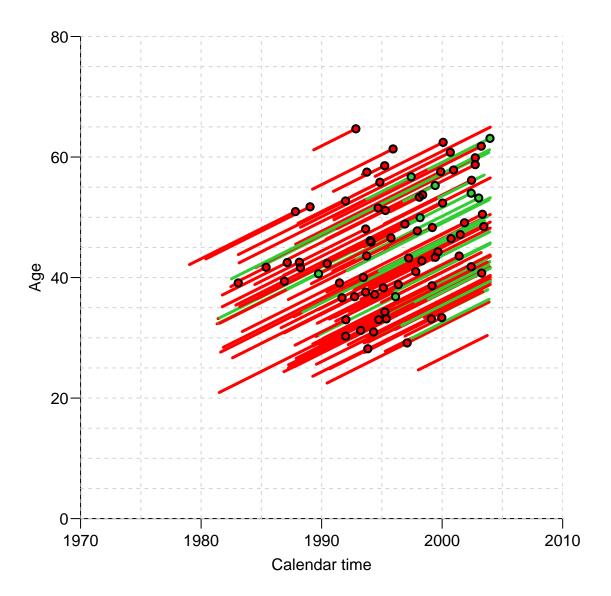


Figure 2.12: Lexis diagram for the split data, where time after remission is shown in green.

```
1.6852
I((doe - dob - 50)/10)
                                                           2.2024
                                      0.5934
                                                 1.2895
lex.Cst == "Rem"TRUE
                           0.2830
                                      3.5339
                                                0.1331
                                                           0.6016
Concordance= 0.664 (se = 0.036)
Rsquare= 0.179 (max possible= 0.984)
Likelihood ratio test= 30.31
                              on 3 df,
                     = 27.07
                               on 3 df,
                                          p = 6e - 06
Score (logrank) test = 29.41
                               on 3 df,
                                          p = 2e - 06
```

We see that the rate of ESRD is less than a third among those who obtain remission — 0.28 (0.13–0.60), showing that we can be pretty sure that the rate is at least halved.

11. The assumption in this model about the two rates of remission is that they are proportional as functions of time since remission. This could be tested quickly with the cox.zph function:

... which shows no sign of interaction between remission state and time since entry to the study. Possibly because of the limited amount of data.

#### 2.15.2 Splitting the follow-up time

12. We split the follow-up time every month after entry, and verify that the number of events and risk time is the same as before and after the split:

```
sLc <- splitLexis( Lc, "tfi", breaks=seq(0,30,1/12) )</pre>
 summary( Lc, scale=100 )
Transitions:
     To
From NRA Rem ESRD ESRD(Rem) Records: Events: Risk time:
  NR.A
          29
                69
                            0
                                  122
                                              98
                                                        8.25
  R.em
           24
                 0
                            8
                                    32
                                               8
                                                        2.60
                                                                    32
  Sum
      24
          53
                69
                            8
                                    154
                                             106
                                                       10.85
                                                                    125
 summary(sLc, scale=100 )
Transitions:
     To
      NR.A
            Rem ESRD ESRD(Rem) Records:
                                           Events: Risk time:
From
                                                                Persons:
 NRA 9854
             29
                  69
                        0
                                     9952
                                                 98
                                                          8.25
                                                                      122
         0 3139
                                     3147
                                                                      32
                   0
                              8
                                                 8
                                                          2.60
 R.em
  Sum 9854 3168
                              8
                                    13099
                                                106
                                                                      125
                  69
                                                         10.85
```

Thus both the cutting and splitting preserves the number of ESRD events and the person-years. The cut added the "Rem" events, but these were preserved by the splitting.

13. Now we fit the Poisson-model corresponding to the Cox-model we fitted previously. The function ns() produces a model matrix corresponding to a piece-wise cubic function, modeling the baseline hazard explicitly (think of the ns terms as the baseline hazard that is not visible in the Cox-model)

```
library( splines )
 mp <- glm(lex.Xst \%in\% EP \sim Ns(tfi, knots=c(0,2,5,10)) +
            sex + I((doe-dob-40)/10) + I(lex.Cst=="Rem"),
            offset = log(lex.dur),
            family = poisson,
              data = sLc )
 ci.exp( mp )
                                                                 97.5%
                                    exp(Est.)
                                                     2.5%
(Intercept)
                                   0.01664432 0.003956765
                                                            0.07001509
Ns(tfi, knots = c(0, 2, 5, 10))1 5.18917654 1.949220473
                                                           13.81452410
Ns(tfi, knots = c(0, 2, 5, 10))2 34.20004192 1.764901998 662.72397483
Ns(tfi, knots = c(0, 2, 5, 10))3 4.43318269 2.179992749
                                                            9.01521750
                                  0.91751162 0.536258807
                                                            1.56981584
I((doe - dob - 40)/10)
                                  1.70082390 1.300814311
                                                            2.22383927
I(lex.Cst == "Rem")TRUE
                                  0.27927558 0.131397003
                                                            0.59358165
```

We see that the effects are pretty much the same as from the Cox-model.

14. We may instead use the gam function from the mgcv package:

```
library( mgcv )
mx <- gam( (lex.Xst %in% EP) ~ s( tfi, k=10 ) +
            sex + I((doe-dob-40)/10) + I(lex.Cst=="Rem") +
            offset(log(lex.dur)),
            family = poisson,
              data = sLc)
ci.exp( mp, subset=c("Cst", "doe", "sex") )
                                       2.5%
                        exp(Est.)
                                                 97.5%
I(lex.Cst == "Rem")TRUE 0.2792756 0.1313970 0.5935816
I((doe - dob - 40)/10) 1.7008239 1.3008143 2.2238393
                        0.9175116 0.5362588 1.5698158
 ci.exp( mx, subset=c("Cst", "doe", "sex") )
                        exp(Est.)
                                       2.5%
I(lex.Cst == "Rem")TRUE 0.2784664 0.1309448 0.5921846
I((doe - dob - 40)/10) 1.6992068 1.2995225 2.2218191
sexF
                        0.9309991 0.5435510 1.5946240
```

We see that there is virtually no difference between the two approaches in terms of the regression parameters.

15. We extract the regression parameters from the models using ci.exp and compare with the estimates from the Cox-model:

```
ci.exp( mx, subset=c("sex","dob","Cst"), pval=TRUE )
                        exp(Est.)
                                       2.5%
sexF
                        0.9309991 0.5435510 1.5946240 0.7945537031
I((doe - dob - 40)/10)
                        1.6992068 1.2995225 2.2218191 0.0001066911
I(lex.Cst == "Rem")TRUE 0.2784664 0.1309448 0.5921846 0.0008970954
 ci.exp( m1 )
                       exp(Est.)
                                      2.5%
                                               97.5%
sexF
                       0.9461646 0.5519334 1.621985
I((doe - dob - 50)/10) 1.6852196 1.2895097 2.202360
lex.Cst == "Rem"TRUE
                       0.2829710 0.1330996 0.601599
 round( ci.exp( mp, subset=c("sex","dob","Cst") ) / ci.exp( m1 ), 3 )
                        exp(Est.) 2.5% 97.5%
sexF
                            0.970 0.972 0.968
I((doe - dob - 40)/10)
                            1.009 1.009 1.010
I(lex.Cst == "Rem")TRUE
                            0.987 0.987 0.987
```

Thus we see that it has an absolute minimal influence on the regression parameters to impose the assumption of smoothly varying rates or not.

16. The model has the same assumptions as the Cox-model about proportionality of rates, but there is an additional assumption that the hazard is a smooth function of time since entry. It seems to be a sensible assumption (well, restriction) to put on the rates that they vary smoothly by time. No such restriction is made in the Cox model. The gam model optimizes the shape of the smoother by general cross-validation:

```
plot( mx )
```

17. However, termplot does not give you the *absolute* level of the underlying rates because it bypasses the intercept. If we want this we can predict the rates as a function of the covariates:

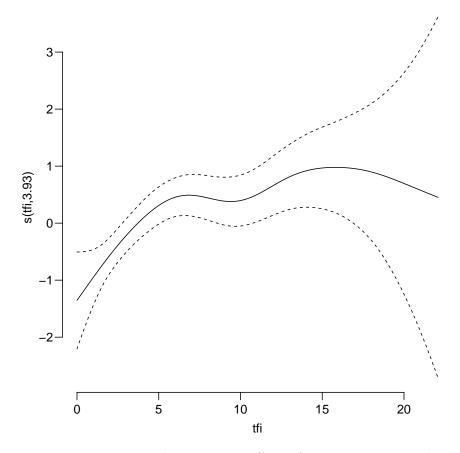


Figure 2.13: Estimated non-linear effect of tfi as estimated by gam.

```
nd \leftarrow data.frame(tfi = seq(0,20,.1),
                sex = "M",
                doe = 1990,
                dob = 1940,
            lex.Cst = "NRA";
            lex.dur = 100)
str( nd )
'data.frame':
                 201 obs. of 6 variables:
        : num 0 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9 ...
 tfi
        : Factor w/ 1 level "M": 1 1 1 1 1 1 1 1 1 1 ...
 sex
              doe
              : num
$ lex.Cst: Factor w/ 1 level "NRA": 1 1 1 1 1 1 1 1 1 1 1 ...
$ lex.dur: num 100 100 100 100 100 100 100 100 100 ...
matshade( nd$tfi, cbind( ci.pred( mp, newdata=nd );
                      ci.pred( mx, newdata=nd ) ), plot=TRUE,
         type="1",
                 lwd=3:4, col=c("black", "forestgreen"),
         log="y", xlab="Time since entry (years)",
                 ylab="ESRD rate (per 100 PY) for 50 year man" )
```

18. Apart from the baseline timescale, time since NRA, the time since remission might be of interest in describing the mortality rate. However this is only relevant for persons who actually have a remission, but there is only 28 persons in this group and 8 events — this can be read of the plot with the

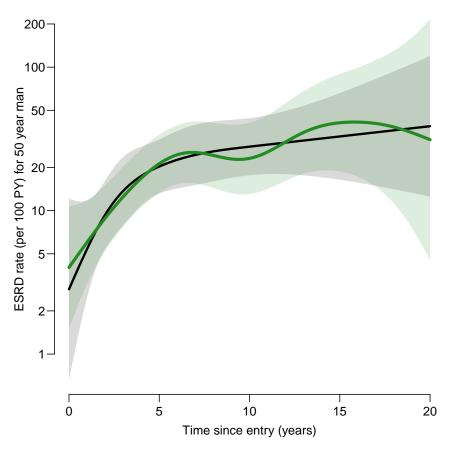


Figure 2.14: Rates of ESRD by time since NRA for a man aged 50 at start of NRA. The green line is the curve fitted by gam, the black the one fitted by an ordinary glm using Ns with knots at 0, 2, 5 and 10 years.

little boxes, figure 2.11.

The variable we want to have in the model is current date (per) minus date of remission (dor): per-dor), but *only* positive values of it. This can be fixed by using pmax(), but we must also deal with all those who have missing values, so construct a variable which is 0 for persons in "NRA" and time since remission for persons in "Rem":

```
sLc <- transform( sLc, tfr = pmax( (per-dor)/10, 0, na.rm=TRUE ) )</pre>
```

19. We can now expand the model with this variable:

```
mPx <- gam( lex.Xst %in% EP ~ s( tfi, k=10 ) +
                    factor(sex) + I((doe-dob-40)/10) +
                    I(lex.Cst=="Rem") + tfr +
                    offset(log(lex.dur/100)),
             family = poisson,
               data = sLc )
round( ci.exp( mPx ), 3 )
                        exp(Est.) 2.5%
                                             97.5%
(Intercept)
                            9.173 6.919
                                            12.162
factor(sex)F
                            0.927 0.539
                                             1.592
I((doe - dob - 40)/10)
                            1.701 1.301
                                             2.224
```

```
I(lex.Cst == "Rem")TRUE
                             0.302 0.093
                                              0.981
                             0.884 0.212
                                              3.693
s(tfi).1
                              2.403 0.569
                                             10.149
s(tfi).2
                             7.876 0.121
                                            511.580
                                              1.784
s(tfi).3
                             0.491 0.135
s(tfi).4
                             0.623 0.052
                                              7.524
                                              5.867
s(tfi).5
                              1.551 0.410
s(tfi).6
                             0.450 0.054
                                              3.762
s(tfi).7
                             1.829 0.477
                                              7.016
s(tfi).8
                            12.544 0.009 17964.281
s(tfi).9
                              1.881 0.278
                                             12.746
```

We see that the rate of ESRD decreases about 12% per year in remission, but not significantly so — in fact we cannot exclude large effects of time since remission in either direction, at least 3 fold in either direction is perfectly compatible with data. There is no information on this question in the data.

#### 2.15.3 Prediction in a multistate model

If we want to make proper statements about the survival and disease probabilities we must know not only how the occurrence of remission influences the rate of death/ESRD, but we must also model the occurrence rate of remission itself.

20. The rates of ESRD were modelled by a Poisson model with effects of age and time since NRA — in the models mp and mx. But if we want to model whole process we must also model the remission rates transition from "NRA" to "Rem", but the number of events is rather small (see figure 2.11), so we restrict covariates in this model to only time since NRA and sex. Note that only the records that relate to the "NRA" state can be used:

```
mr <- gam( lex. Xst=="Rem" ~ s( tfi, k=10 ) + sex,
            offset = log(lex.dur),
            family = poisson,
              data = subset( sLc, lex.Cst=="NRA" ) )
 ci.exp( mr, pval=TRUE )
             exp(Est.)
                            2.5%
                                       97.5%
(Intercept) 0.02466228 0.0148675 0.04090991 1.255532e-46
            2.60593044 1.2549319 5.41134814 1.019750e-02
sexF
s(tfi).1
            1.00280757 0.9164889 1.09725609 9.513196e-01
s(tfi).2
            0.99788151 0.8528556 1.16756868 9.788845e-01
s(tfi).3
            0.99899866 0.9390756 1.06274547 9.746765e-01
            0.99893713 0.9142049 1.09152270 9.812395e-01
s(tfi).4
            0.99911474 0.9418672 1.05984177 9.765307e-01
s(tfi).5
s(tfi).6
            0.99897084 0.9255211 1.07824963 9.789171e-01
s(tfi).7
            1.00094972 0.9438566 1.06149638 9.747279e-01
s(tfi).8
            0.99688411 0.7535273 1.31883465 9.825635e-01
            0.94804631 0.6368367 1.41133790 7.927002e-01
s(tfi).9
```

We see that there is a clear effect of sex; women have a remission rate 2.6 times higher than for men, both when using glm and ns and gam with s.

21. In order to use the function simLexis we must have as input to this the initial status of the persons whose life-course we shall simulate, and the transition rates in suitable form:

• Suppose we want predictions for men aged 50 at NRA. The input is in the form of a Lexis object (where lex.dur and lex.Xst will be ignored). Note that in order to carry over the time.scales and the time.since attributes, we construct the input object using subset to select columns, and NULL to select rows (see the example in the help file for simLexis):

```
inL <- subset( sLc, select=1:11 )[NULL,]</pre>
str(inL)
Classes 'Lexis' and 'data.frame':
                                           0 obs. of 11 variables:
 $ lex.id : int
$ per
         : num
$ age
          : num
$ tfi
         : num
$ lex.dur: num
$ lex.Cst: Factor w/ 4 levels "NRA", "Rem", "ESRD",...
$ lex.Xst: Factor w/ 4 levels "NRA", "Rem", "ESRD",...
$ sex
          : Factor w/ 2 levels "M", "F":
$ dob
         : num
$ doe
          : num
- attr(*, "time.scales")= chr "per" "age" "tfi"
- attr(*, "time.since")= chr "" "" "" - attr(*, "breaks")=List of 3
  .. $ per: NULL
 ..$ age: NULL
  ..$ tfi: num 0 0.0833 0.1667 0.25 0.3333 ...
 timeScales(inL)
[1] "per" "age" "tfi"
 inL[1,"lex.id"] <- 1
inL[1,"per"] <- 2000
inL[1, "age"] <- 50
inL[1,"tfi"] <- 0
 inL[1,"lex.Cst"] <- "NRA"
 inL[1,"lex.Xst"] <- NA</pre>
 inL[1,"lex.dur"] <- NA</pre>
inL[1,"sex"] <- "M"
inL[1,"doe"] <- 2000
inL[1,"dob"] <- 1950
 inL <- rbind( inL, inL )</pre>
inL[2, "sex"] <- "F"
inL
 lex.id per age tfi lex.dur lex.Cst lex.Xst id sex dob doe
      1 2000 50 0
                       NA NRA <NA> NA M 1950 2000
       1 2000 50
                   0
                            NA
                                   NRA
                                          <NA> NA F 1950 2000
str( inL )
Classes 'Lexis' and 'data.frame':
                                          2 obs. of 11 variables:
$ lex.id : num 1 1
$ per
        : num 2000 2000
$ age
         : num 50 50
$ tfi
         : num 0 0
$ lex.dur: num NA NA
$ lex.Cst: Factor w/ 4 levels "NRA", "Rem", "ESRD", ...: 1 1
$ lex.Xst: Factor w/ 4 levels "NRA", "Rem", "ESRD",..: NA NA
         : num NA NA
          : Factor w/ 2 levels "M", "F": 1 2
$ sex
$ dob
          : num 1950 1950
         : num 2000 2000
- attr(*, "breaks")=List of 3
  .. $ per: NULL
```

```
..$ age: NULL
..$ tfi: num 0 0.0833 0.1667 0.25 0.3333 ...
- attr(*, "time.scales")= chr "per" "age" "tfi"
- attr(*, "time.since")= chr "" "" ""
```

• The other input for the simulation is the transitions, which is a list with an element for each transient state (that is "NRA" and "Rem"), each of which is again a list with names equal to the states that can be reached from the transient state. The content of the list will be glm objects, in this case the models we just fitted, describing the transition rates:

22. Now generate the life course of 5,000 persons (of each sex), and look at the summary. The system.time command is just to tell you how long it took, you may want to start with 100 just to see how long that takes.

```
system.time( sM <- simLexis( Tr, inL, N=5000 ) )</pre>
         system elapsed
 48.568
         0.268 48.846
 # save( sM, file="sM.Rda"
 # load( file="sM.Rda" )
 summary( sM, by="sex" )
$M
Transitions:
     To
From NRA Rem ESRD ESRD(Rem)
                                Records:
                                          Events: Risk time:
  NRA
        3 2547 2450
                         0
                                    5000
                                             4997
                                                    20043.50
                                                                   5000
        0 624
                          1923
                                    2547
                                             1923
                                                    25666.68
                                                                   2547
  R.em
                0
        3 3171 2450
  Sum
                         1923
                                    7547
                                             6920
                                                    45710.19
                                                                   5000
$F
Transitions:
     To
From NRA Rem ESRD ESRD(Rem)
                                Records:
                                          Events: Risk time:
                                                               Persons:
  NRA
        0 3956 1044
                           0
                                    5000
                                             5000
                                                    11738.61
                                                                   5000
  Rem
        0 1009
                          2947
                                    3956
                                             2947
                                                     43766.08
                                                                   3956
        0 4965 1044
                          2947
                                    8956
                                             7947
                                                    55504.69
                                                                   5000
  Sum
```

The many ESRD-events in the resulting data set is attributable to the fact that we simulate for a very long follow-up time.

23. Now we want to count how many persons are present in each state at each time for the first 10 years after entry (which is at age 50). This can be done by using nState:

```
nStm <- nState( subset(sM,sex=="M"), at=seq(0,10,0.1), from=50, time.scale="age" )</pre>
nStf <- nState( subset(sM,sex="F"), at=seq(0,10,0.1), from=50, time.scale="age" )
head( nStf )
      State
             Rem ESRD ESRD(Rem)
when
        NRA
       5000
             0
                   0
                              0
 50.1 4809
             173
                   18
                              0
 50.2 4625 339
                   35
```

```
50.3 4456 494 49 1
50.4 4302 630 66 2
50.5 4147 763 87 3
```

We see that we get a count of persons in each state at time points 0,0.1,0.2,... years after 50 on the age time scale.

24. Once we have the counts of persons in each state at the designated time points, we compute the cumulative fraction over the states, arranged in order given by perm:

```
ppm \leftarrow pState(nStm, perm=c(2,1,3,4))
ppf <- pState( nStf, perm=c(2,1,3,4) )</pre>
head( ppf )
     State
when
          Rem
                 NRA ESRD ESRD(Rem)
 50
      0.0000 1.0000 1.0000
 50.1 0.0346 0.9964 1.0000
 50.2 0.0678 0.9928 0.9998
                                     1
 50.3 0.0988 0.9900 0.9998
                                     1
 50.4 0.1260 0.9864 0.9996
                                     1
 50.5 0.1526 0.9820 0.9994
 tail( ppf )
      State
                NRA
                       ESRD ESRD(Rem)
when
          Rem
 59.5 0.5374 0.5482 0.7512
 59.6 0.5364 0.5466 0.7498
 59.7 0.5346 0.5442 0.7476
                                     1
 59.8 0.5318 0.5406 0.7444
                                     1
 59.9 0.5278 0.5362 0.7404
                                     1
      0.5252 0.5334 0.7376
                                     1
```

25. Then we plot the cumulative probabilities using the plot method for pState objects:

```
plot( ppf )
```

26. Now try to improve the plot so that it is easier to read, and easier to compare men and women:

We see that the probability that a 50-year old man with NRA sees a remission from NRA during the next 10 years is about 25% whereas the same

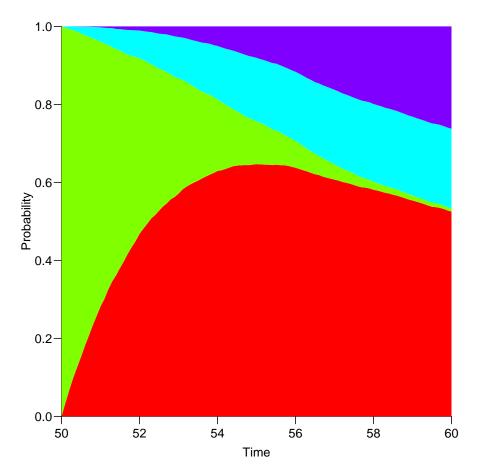


Figure 2.15: The default plot for a pState object, bottom to top: Alive remission, alive no remission, dead no remission, dead remission.

for a woman is about 50%. Also it is apparent that no new remissions occur after about 5 years since NRA — mainly because only persons with remission are alive after 5 years.

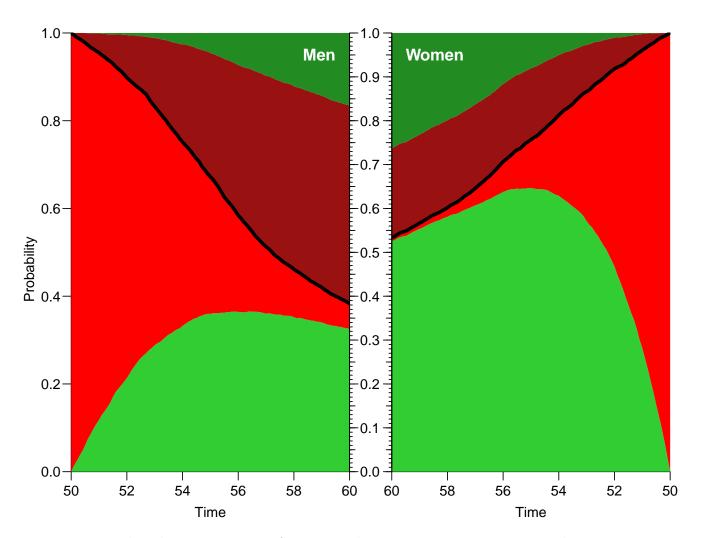


Figure 2.16: Predicted state occupancy for men and women entering at age 50. The green areas are remission, the red without remission; the black line is the survival curve.