

# CS1632, LECTURE 2: TESTING THEORY AND TERMINOLOGY

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Key (  ) concept to the  
course

Expected behavior vs observed behavior

# Expected behavior vs observed behavior

You need to know what “should” happen under some circumstances, then check to see if that behavior actually occurred.

For example, assume I have a function `foo`, which accepts an integer, `a`, and returns a float. What should happen if I send in the value `a = 42`?

This is a simple idea, but it’s the “Fundamental Theorem of Testing” (although note that we may violate it later...)

# Example

Assume foo is supposed to return the square root of the passed in value a.

When I send in the value  $a = 42$ , then I expect to be returned the value 6.48074069841.

When I send in the value  $a = 9$ , then I expect to be returned the value 3.

When I send in the value  $a = -1$ , then I expect....

# THE IMPOSSIBILITY OF EXHAUSTIVE TESTING

- Let's say we want to ensure that our square root method will never fail, no matter what we send in. Assume we are using a standard Java int (signed 32-bit integer)
- How many values do we have to test?

4,294,967,296

# What if there are a 1000 method calls?

- Assume each method call accepts one 32-bit int argument
- Remember that methods in a Java-like language can have side-effects (in other words, they are not pure functions)
  - Can access / modify global variables, global data structures
  - Means a method call is affected by all previous method calls

$$4,294,967,296 \wedge 1000$$



# THAT'S EQUAL TO...

91171950785279002509723338967578745479915846704161093266316858586590561893971899669618585741969928523387207745761469132800197981751886314439367551781375622355182494132784122242065904571923125296267977156632231162513245  
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67443834386341569639844449666759577829376

## TEST CASES!

# What if the argument is an object reference?

- That object could be a list data structure, a tree, a graph, ...
- How many shapes can a tree take?

Would testing all the combinations of arguments guarantee that there are no problems?

# LOL NOPE

- Compiler issues
- Parallel programming issues
- Non-functional issues (performance, usability, etc.)
- Floating-point issues
- Integration issues
- Systems-level issues
- Ambiguous or misunderstood requirements

# LOL NOPE

- Compiler issues

- Your source code does not run on the computer, the compiled binary does
- Depending on compiler and compile options, many different binaries can be produced! Besides the binary you used for testing.
- What if the compiler has a bug? (Rare)
- What if the compiler *exposes* a bug in your program? (More frequent)

```
int add_up_to (int count) {  
    int sum, i; /* some C compilers will init sum to 0, some will not */  
    for(i = 0; i <= count; i++) sum = sum + i;  
    return sum;  
}
```

- Big problem for C/C++, less of a problem for Java since all bytecode is run on JVM (In above example, Java Virtual Machine always initializes all variables to 0)

# LOL NOPE

- Compiler issues
- Parallel programming issues
  - If there is a data race, the result of your program is undefined
    - Doesn't matter whether you are using C/C++ or Java
    - Worst part: for many data races, result is correct 99% of time, masking the bug
  - Even with no data race, the result of your program is often nondeterministic (Depending upon the respective speed of each thread)
    - To thoroughly test, you have to vary the speed of each thread, even for same input

# LOL NOPE

- Compiler issues
- Parallel programming issues
- Non-functional issues (performance, usability, etc.)
- Floating-point issues
- Integration issues
- Systems-level issues
- Ambiguous or misunderstood requirements

# Testing = ART + SCIENCE

- There are techniques for testing which can reduce the number of tests necessary for sufficient test coverage.
- Defining what “sufficient test coverage” means is subjective.
- We must rely on domain knowledge to decide.



# Equivalence class partitioning

- We can partition the testing parameters into “equivalence classes”
  - Equivalence class = a natural grouping of values with similar behavior
- For example, in our square root method:
  - Negative numbers (input) -> Imaginary numbers (output)
  - 0 -> 0
  - Positive numbers -> Positive numbers

# Equivalence classes are strictly partitioned

- For any given input value, it must belong to one and ONLY one equivalence class (strictly partitioned)
- If there are values that belong to multiple equivalence classes, you probably need another equivalence class
- Example:
  - Right handed people -> writes with right hand
  - Left handed people -> writes with left hand
  - Jane can write with both hands. Which equivalence class does she belong to?*
  - Solution: add “Ambidextrous people -> writes with both hands”

# Multiple partitionings

- Assume in the previous square root method, if the result contains a decimal point (e.g.  $1.3$  or  $2.23i$ ), it prints in **red**, otherwise in black.
- Now we have two partitionings:
  - The positive / 0 / negative partitioning on the previous slide
  - The decimal / non-decimal partitioning on this slide:
    - Number contains decimal -> output printed in **red**
    - Number does not contain decimal -> output printed in black
- Therefore, a value now belongs to two equivalence classes, but in different partitionings (e.g. value  $1.3$  belongs to “positive” and “decimal” classes)
- A set of values can be partitioned in limitless ways

# Values do not have to be numeric

- On Twitter, if you follow somebody, you see all of their tweets, unless they are writing directly to somebody you do not follow.
- Equivalence classes:
  - You do not follow person A -> DO NOT see the tweet
  - You do follow person A, they are not writing directly to somebody -> see the tweet
  - You do follow person A, they are writing directly to person B, whom you also follow -> see the tweet
  - You do follow person A, they are writing directly to person B, whom do you not follow -> DO NOT see tweet

# Values do not have to be numeric

- Suppose Twitter only allows alphanumeric [A-Za-z0-9] characters, and tweets must contain at least one character. Tweets that contain any invalid characters are not posted.
- Equivalence classes (NV = number of valid characters, NI = number of invalid characters):
  - $(NV \geq 1, NI == 0)$  -> Post the tweet
  - $(NV == 0, NI == 0)$  -> DO NOT post the tweet
  - $(NI \geq 1)$  -> DO NOT post the tweet (note NV is irrelevant here)

# Test Each Equivalence Class

- Pick at least one value from each equivalence class
- This will ensure you capture behavior from each “class” of possible behavior
- Will find a good percentage of defects without exhaustive testing!
- We reduced the problem something a human can do! Woo-hoo!
- How to pick the input? Well, that is part of the art.
  - However, there are some good guidelines!

# Interior and boundary values

- Theory: Problems are more prevalent on the boundaries of equivalence classes than in the middle.

# Why?

- Suppose expected behavior is:
  - Method shall take citizenship and age as arguments
  - Method shall determine whether a person can be US president according to a set of rules
  - Rule 1: Person must be a US citizen to be US president
  - Rule 2: Person must be 35 years or older to be US president

- Suppose implementation is:

```
boolean canBePresident(int age, boolean citizen) {  
    return age > 35 && citizen;  
}
```

- Is observed behavior the same as expected behavior?



# Equivalence class partitioning

CANNOT\_BE\_PRESIDENT =  
[...19,20,21,22,23,24,25,26,27,28,29,30,31,32,33,34]

CAN\_BE\_PRESIDENT =  
[35,36,37,38,39,40,41,42,43,44,45,46,47,48,49,50...]

# Try to test both boundary and interior values

CANNOT\_BE\_PRESIDENT =  
[...19,20,21,22,23,24,25,26,27,28,29,30,31,32,33,**34**]

CAN\_BE\_PRESIDENT =  
[**35**,36,37,38,39,40,41,42,43,44,45,46,47,48,49,50...]

- At the boundary values (shown in **red**)
- In fact, there is a bug at: `age > 35`

# Try to test both boundary and interior values

CANNOT\_BE\_PRESIDENT =  
[...19,20,21,22,23,24,25,26,27,28,29,30,31,32,33,34]

CAN\_BE\_PRESIDENT =  
[35,36,37,38,39,40,41,42,43,44,45,46,47,48,49,50...]

- Testing interior values is also important to see behavior in interior

# Try to test both boundary and interior values

CANNOT\_BE\_PRESIDENT =  
[...19,20,21,22,23,24,25,26,27,28,29,30,31,32,33,34]

CAN\_BE\_PRESIDENT =  
[35,36,37,38,39,40,41,42,43,44,45,46,47,48,49,50...]

- Are we done?

# “Hidden” (IMPLICIT) boundary values

- The boundary values we have gone over already are explicit – that is, they are defined by the requirements of the problem itself.
- Some boundaries are implicit – they are generated from the domain, architecture, hardware, or other elements:
  - MAXINT, MININT
  - Maximum precision of a floating point value
  - Allocation limitation (memory, hard drive space, network bandwidth, etc.)
  - Physical world boundaries (weight can't be negative, Y2K won't happen, etc.)
    - Side note: Y2K did happen and anti-gravity may yet happen

# Add implicit boundary values

CANNOT\_BE\_PRESIDENT =

[**MININT**, ..., -1, **0**, 1, ... 19, 20, **21**, 22, 23, 24, 25, 26, 27, 28, 29, **30**, 31, 32, 33, **34**]

CAN\_BE\_PRESIDENT =

[**35**, 36, 37, 38, **39**, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, **50**, ..., **MAXINT**]

- **MININT**, **MAXINT**: hardware boundaries
- **0**: physical world boundaries (age cannot be negative)

# Base, edge, and corner cases

- **Base case** – An element in an equivalence class that is not around a boundary (interior value), OR an expected use case.
- **Edge case** – An element in an equivalence class that is next to a boundary (boundary value), OR an unexpected use case.
- **Corner case (or pathological case)** – A case which can only occur outside of normal operating parameters, or a combination of multiple edge cases.

# Black-, white, and grey-box testing

- **Black-box testing:**

- Testing with no knowledge of the interior structure or code of the application
- Tests are performed from the user's perspective, looking at the system as a whole

- **White-box testing:**

- Testing with explicit knowledge of the interior structure and codebase
- Tests are performed at the code-level (e.g. testing individual methods or classes)

- **Grey-box testing:**

- Testing with some knowledge of the interior structure and codebase
- Knowledge may come from partial inspection of code or a design document
- Tests are performed from the user's perspective, but informed by tester's knowledge



# Black-box testing examples

- Accessing a website, using a browser, to look for flaws
- Running a script against an API endpoint
- Checking to see that changing fonts in a word processor works

# White-box testing examples

- Testing that a function returns the correct result
- Testing that instantiating an object creates a valid object
- Checking that there are no unused variables in a method
- Checking that exceptions are properly caught and handled

# Grey-box testing examples

- *Reviewing code* and noticing that bubble sort is used. Then write a *user-facing test* involving a large input size.
- *Reviewing code* in a web app and noticing user input is not properly sanitized of code. Then write a *user-facing test* which attempts SQL code injection or cross site scripting.
- *Reading a design document* and noticing a critical network connection through which a lot of data passes through. Then write a *user-facing test* that stresses that network connection.

# Static vs dynamic testing

- Dynamic testing = code is executed (at least the part that is exercised in that test run)
- Static testing = code is not executed

# Dynamic testing

- If you're thinking about testing, probably what you are thinking about.
  - Code is executed under certain circumstances  
(e.g. input values, environment variables, compiler, OS, runtime library, etc.)
  - **Observed results** are then compared with **expected results**
- Much more commonly used in industry
- The majority of the class will be about dynamic testing

# Static testing

- Code is reviewed by a person or testing tool, without being executed
- Examples:
  - Code walkthroughs and reviews
  - Source Code Analysis
    - Linting
    - Model checking
    - Complexity analysis
    - Code coverage
    - Finite state analysis
    - ... COMPILING!