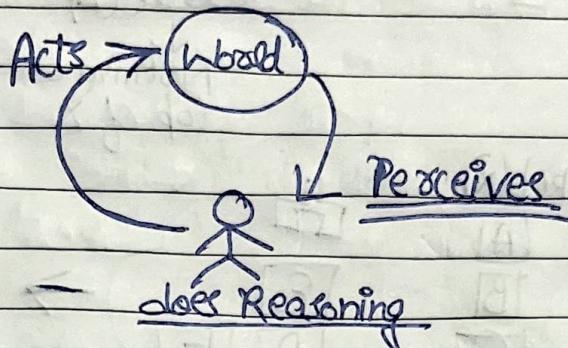


Planning

⇒ The reasoning side of acting is planning.



In planning problem, we will have

⇒ Domain Description
 Action Specification
 Goal States description

↔ Planning Domain description language (PDDL)

⇒ Planner will be domain independent.

$$\text{PDDL I-O} \rightleftharpoons \begin{matrix} \text{STRIPS} \\ \text{Planners} \end{matrix} \quad \begin{matrix} \text{domain} \\ \text{language} \end{matrix}$$

(for describing planning domain)

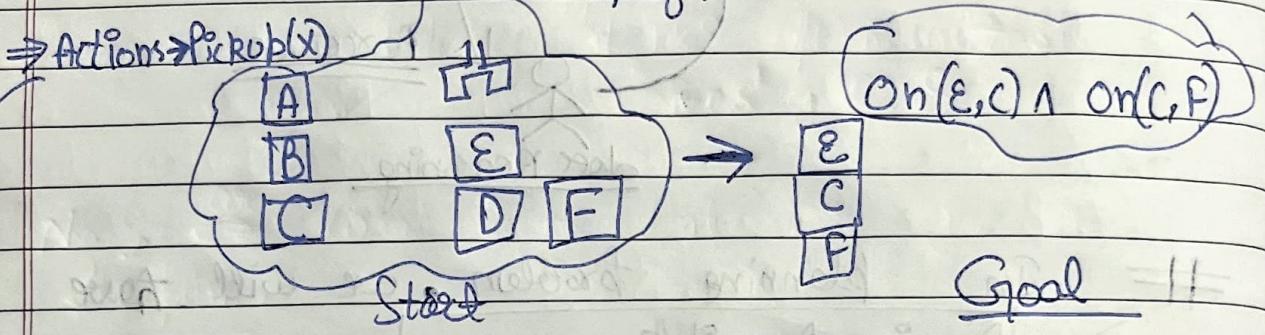
Assumptions:-

- ① Space is finite
- ② Fully observable. → Agent can sense the entire world.
↓
Agent is only one making changes in the world.
- ③ Static
- ④ Deterministic → Whatever actions agent does they will happen in real world.
- ⑤ Simple goals.
- ⑥ Plan → Sequence of actions
- ⑦ Instantaneous actions. (No time)

⇒ Let's see how Box world is described in STRIPS :-

⇒ Domain Predicates → $\text{On}(x,y)$, $\text{OnTable}(x)$, $\text{Holding}(x)$, $\text{clear}(x)$, $\text{AtEmpty}(AE)$

\downarrow
Nothing on top of X
 \downarrow
X on table



⇒ Using predicates we can describe the states like $\text{On}(A,B)$, $\text{On}(B,C)$, $\text{OnTable}(C)$... $\text{clear}(A)$ etc.

⇒ Actions → For describing actions :-

⇒ what is true for action to be applicable?

⇒ What will become true after action is applied.

In STRIPS → for Action $\Rightarrow \text{pickup}(x)$

Here, F
could be
picked

- ① Precondition $\Rightarrow \text{OnTable}(x)$, $\text{clear}(x)$, AE
- ② Add : $\text{Holding}(x)$
- ③ Delete : $\text{OnTable}(x)$, AE

⇒ Preconditions satisfied

② PutDown(x)

Precondition : $\text{Holding}(x)$

Add : $\text{OnTable}(x)$, AE

Delete : $\text{Holding}(x)$

uses \Rightarrow likes(Steve, easy course)
^ - Finance course

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- ③ Unstack(x, y) : Unstack x from y
④ Unstack(y, x) : Stack x on y

In modern for action or we use,

- ① pre(a)
② effects⁺(a) } effects
③ effects⁻(a) }

Planning problem \rightarrow Domain description $\rightarrow D$
 \uparrow
operators $\rightarrow O$
Start $\rightarrow S$
Goal $\rightarrow G$

\rightarrow Described by (O, D, S)
 \rightarrow Described by (O, D, S, G)

S
 $+G$ is set of predicates

\Rightarrow Action (a) is applicable if $Precond(a) \subseteq S$
When ~~a~~ a is applied we Progress to S'
 $S' \leftarrow (S \setminus \text{effects}^-(a)) \cup \text{effects}^+(a)$

A plan $\pi = (a_1, a_2, \dots, a_n)$ [seq. of actions]

GoalTest $\circledcirc S$ then S is Goal state.

Set of pred. describing the goal

Having a God test & somebody gives me a plan π
 ⇒ How to validate that plan π is correct i.e. it solves the problem?
 ↳ Write a small program that will progress over the state i.e. it applies all action in seq. & sees if the result is correct i.e. $g \subseteq S$

Now, we want algos that will give us the plan.

Stack(x, y)

Pre :- Holding(x), clear(y)
 effects⁺ : On(x, y), AE, clear(x)
 effects⁻ : Holding(x), clear(y)

UnStack(x, y)

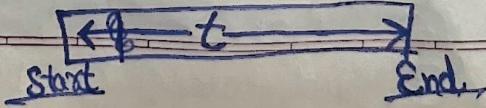
Pre :- ~~On(x, y)~~, AE, clear(x)
 effects⁺ : Holding(x), clear(y)
 effects⁻ : On(x, y), AE, clear(x)

Richer Domains Actions :-

⇒ Conditional effects →

effects which come into force only if certain condⁿ are true. (if)

⇒ Durative actions (Time taken into account)
 represented by intervals



Here, we have Start Preconditions + End Precondition
 & Effects
 & overall condⁿ
 & Effects

⇒ Metric Values → keep track of values throughout the duration

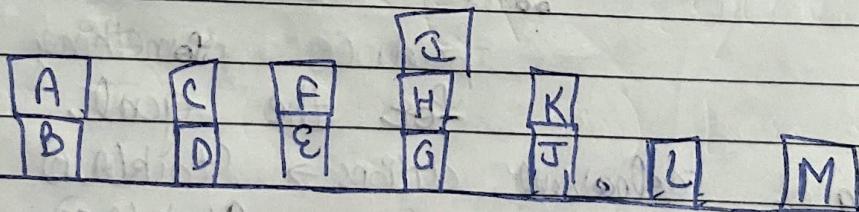
These are not considered in our case

We will focus on STRIPS PDDL domain only

Action a is applicable if $pre(a)$ is a
 $c \in S$ in state S .
 → $progress(S, a) \quad S' \leftarrow (S - effect^-(a)) \cup effect^+(a)$
~~goal g~~
 ⇒ State S satisfies a goal g if
 $g \subseteq S$

Planning problem → (Start S , goal g , actions)

Start State :-



Goal State →



FSSP → does ⇒ Forward State Space Search

↳ moveGen on goal would generate all the possible actions =
 Unstack A, -C, F, -I, -K or Pickup L, -M

Say, K is Pickup & S' updated to's
 again moveGen on S' & so on

Problem → Large branching factor
 ↳ route force X

① do Heuristic Search (Not in Syllabus)
 (We want domain independent heuristics)

② do Backward Search

BSSP → does

⇒ Backward State Space Search

Relevant actions →

a is relevant for goal q iff
 $\text{effect}^+(a) \cap q \neq \emptyset$
 $\text{+ effect}^-(a) \cap q = \emptyset$

∴ we want those actions that
 produce something relevant
 for the goal.

e.g. relevant actions → Stack(A, B)
 Stack(B, D)

∴ here BSSS is focused on goal
 ∴ small branching factor

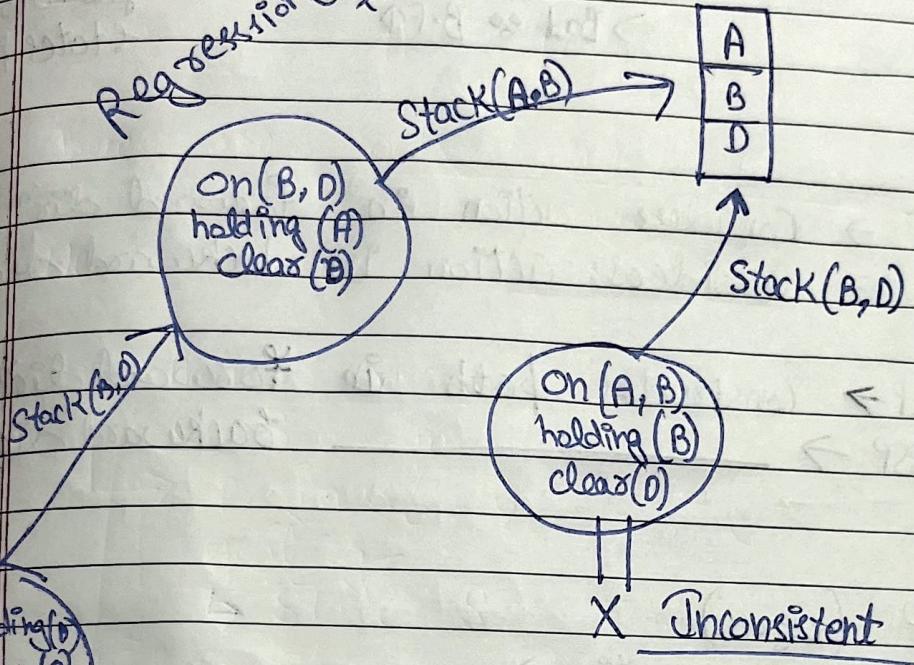
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not sound (what we get is
not state)

egress (g, a)

$$g' \leftarrow (g - \text{effects}(a)) \cup \text{pre}(a)$$

Regression (going back
from goal)



Disadvantage \Rightarrow what we get are not states essentially.

\Rightarrow terminates when

$g''' \subseteq \text{Start}$

Check for Valid Plan :-

$\Pi, (S, g, \text{action})$

begin with start state

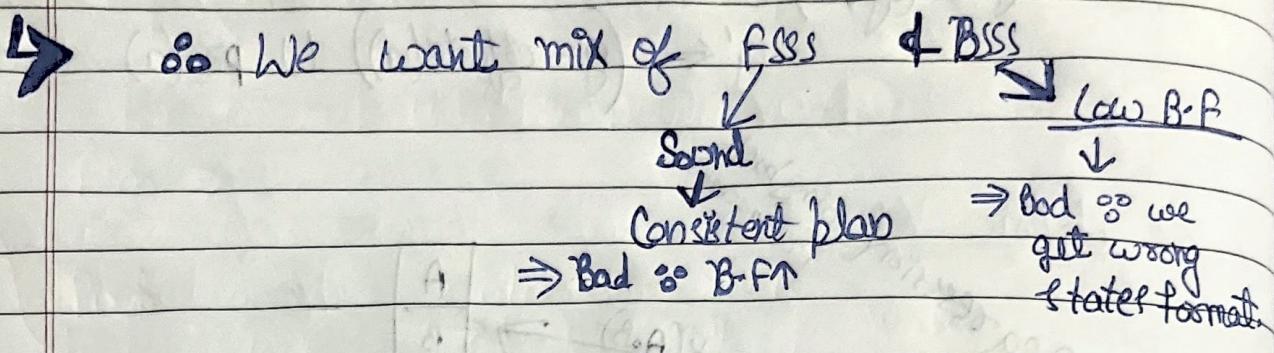
keep progressing with actions

& see the state reached in goal or not

Check for Consistency & Prune States :-

Deletes the inconsistent node path.

(State Top)



→ In FSSP → Consider action in forward dirn
 BSSP → Consider action in backward dirn

→ In FSSP → Constructs path in forward dirn
 In BSSP → _____ backward dirn.

→ In BSSP + (regress)

→ relevant action ⇒

$$\begin{aligned} \text{effects}^+(a) \cap g &\neq \emptyset \\ \text{effects}^-(a) \cap g &= \emptyset \end{aligned}$$

→ Regression

$$g' \leftarrow [g - \text{effects}^-(a)] \cup \text{postcond}(a)$$

In FSSP (progress)

$$S' \leftarrow (S - \text{effects}^-(a)) \cup \text{effects}^+(a)$$

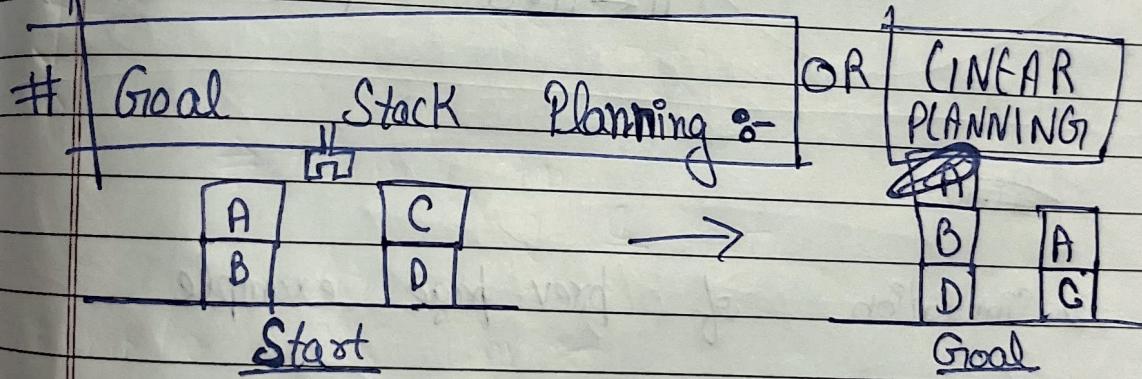
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⇒ In Construction of plan in forward dirⁿ, we will always end up with states. ✓

⇒ But, in backward SSP form end + what we get might not be a state, hence we do validity check. ✗

⇒ In FSSP by considering actions in forward dirⁿ ⇒ B.F↑
 But, in BSSP by considering actions in backward dirⁿ B.F↓

• We want construction in forward dirⁿ ($S \rightarrow G$) & actions in backward dirⁿ. (Goal oriented)



$$\text{goal} = \text{on}(A, B)$$

$$\wedge \text{on}(B, D)$$

$$\wedge \text{clear}(A)$$

Algo →
 Push goal (\$) onto Stack
 Pop Stack
 If precond :
 if true
 do nothing
 else
 Push relevant action onto Stack

(Cond is already true)

Else (not predicate means action)

Algo \Rightarrow

Push goals onto Stack
 If predicate
 If true (predicate cond already true)
 do nothing
 else
 Push relevant action onto stack
 Push precond(a) onto stack
 Push each predicate of precond(a)

Socializing the goals

\vdash Else (Action)

Add action to plan $\Pi \leftarrow \Pi \cdot a$ ($\cdot \rightarrow$ concatenate)

\Rightarrow Simulation of prev page example

Initial Sub Goals \Rightarrow

- OnAB \downarrow onBD
- onBD
- onAB

onAB popped out
↳ predicate

& true in given \Rightarrow do nothing

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On BD → predicate
 not true for given state
 so we push an action which will
 make this true

On BD → action → Stack BD
 ↗ pushed

precond → holding(B) [h(B)]
 ^ clear(D) [c(D)]
 Also h(B)
 c(D)

Current Stack →

② On AB \wedge on BD → Stack BD
 h(B) \wedge c(D)

h(B)
 c(D)

\Rightarrow Pop \Rightarrow c(D) ↗ Not true

so push an action to make
 this true.

③ Unstack(C)

④ Precond → on CD \wedge AE \wedge clear C

AE
 on CD
 c(C)

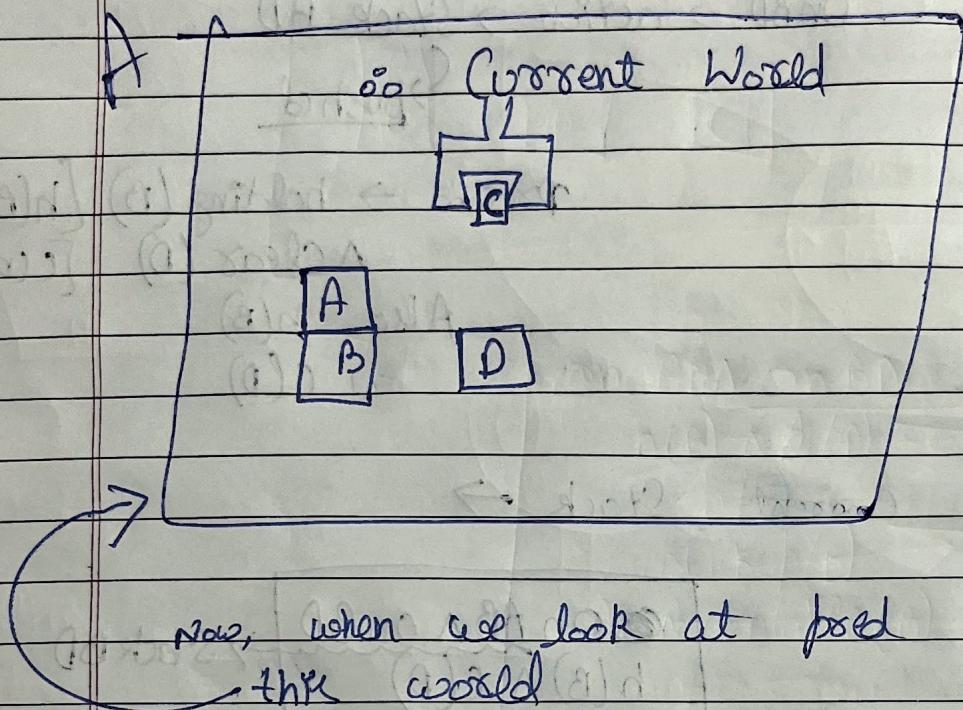
Pop C(C) → True → Pred

Pop on(D) → True → Pred

Pop AE → True

Pop $\text{on}(D) \wedge A \in \text{clear}(C)$ \rightarrow ~~Action~~ Pred \Rightarrow True

Pop $\text{Unstack}(C)$ \rightarrow Action ①
 \therefore Add this to plan



Now, $\text{pop} \Rightarrow h(B)$

Not true

\therefore Insert relevant action

Here we have a choice

To make holding B true
 make an action $\text{Unstack}(x, B)$ or
 $\text{pickup}(B)$

Say we choose Pickup(B) [By looking at State]

Pickup(B)

$A \in \text{OnTable}(B) \wedge \text{clear}(B)$

$A \in$

on(B)

C(B)

Pop C(B)

∴ Another action → Not true

Unstack(A, B)

$\text{on}(A, B) \wedge A \in \text{clear}(A)$

$\ominus A \in$

on(A, B)

clear(A)

clear(A)

on(A, B)

→ true → popped out

$A \in$

→ not true.

Another action

PutDown(c)

h(c)

②

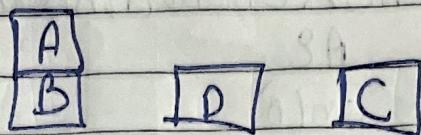
③

Pop h(c) → true

Do action PutDown(c)

~~Stack Content~~

$B \Rightarrow$ world becomes



Stack \Rightarrow

on A B \wedge on B D

~~h(B) \wedge h(C(A))~~

~~h(B)~~

Pickup(B)

~~A \in onTable(B) \wedge clear(B)~~

A \Rightarrow

~~on(B)~~

~~Unstack(A, B)~~

~~on(A, B) \wedge A \in on(C(A))~~

A \Rightarrow

~~on(A, B)~~

~~C(A)~~

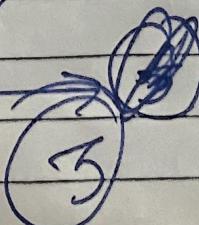
Putdown(C)

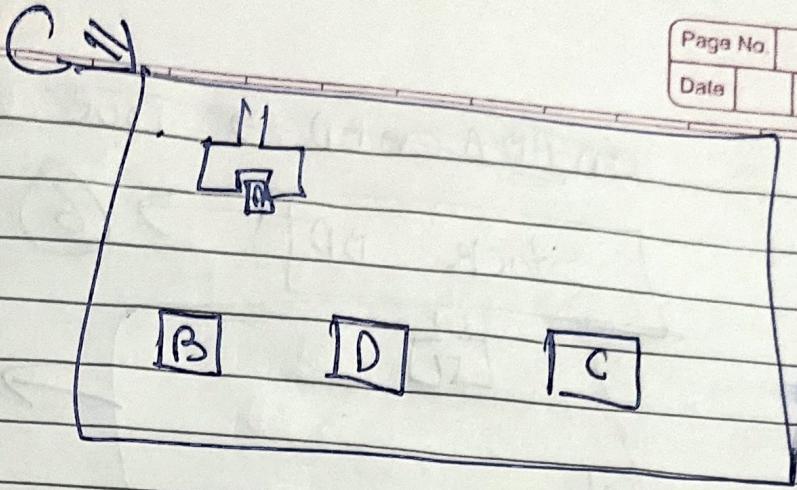
C \Rightarrow

Pop, on(A, B) \wedge A \in on(C(A)) \rightarrow TRUE

Pop Unstack(A, B)

4 ACTION





$\text{On}(B) \rightarrow \text{True}$

(4)

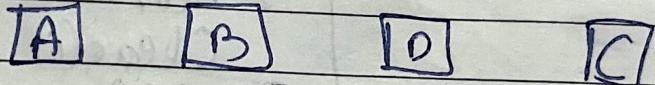
$\text{At} \rightarrow \text{Not true}$

$\boxed{\text{Putdown}(A)}$

$\xrightarrow{h(A)}$

executed

$D \Rightarrow$

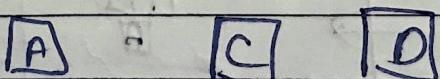


$\text{At} \wedge \text{Ontable}(B) \wedge \text{Clear}(B) \rightarrow \text{True}$

(5)

$\boxed{\text{Pickup}(B) \rightarrow \text{Action}}$

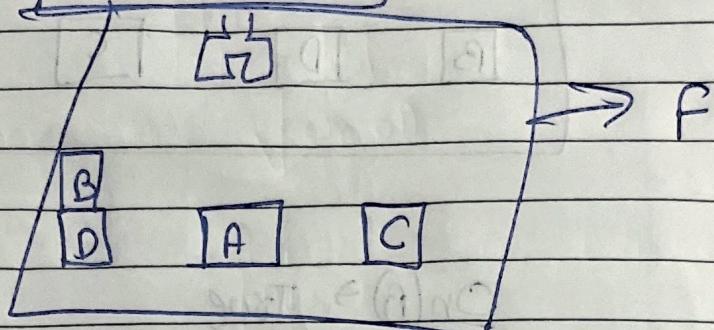
$E \Rightarrow$



$h(B) \wedge c(D) \rightarrow \text{True}$

~~On AB \wedge On BD \rightarrow true~~

Stack BD \rightarrow 6



\Rightarrow ~~On AB \wedge On BD~~

\rightarrow Not true

\therefore Add action

Stack

Stack AC

$h(A) \wedge \text{clear}(C)$

$\text{Clear}(C)$

$h(A) \Rightarrow$

$h(A) \rightarrow$ Not true

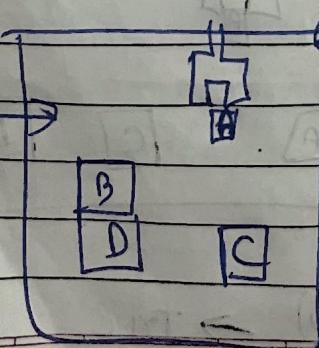
~~Pickup(A) \rightarrow~~ 7

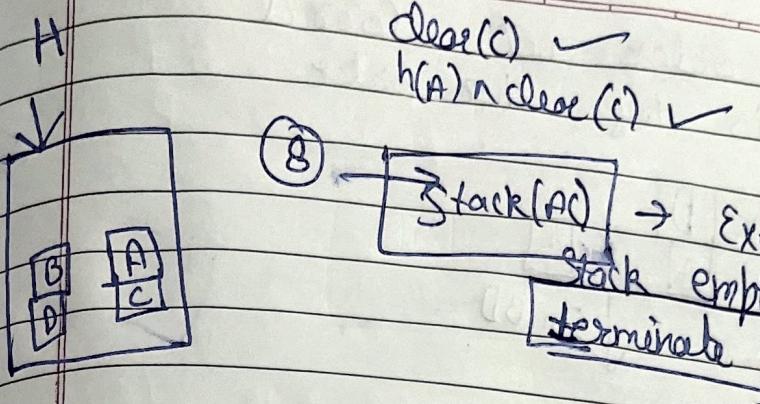
~~A \in Action(A) \rightarrow True~~

~~A \in \rightarrow True~~

~~clear(A) \rightarrow True~~

G1 \rightarrow





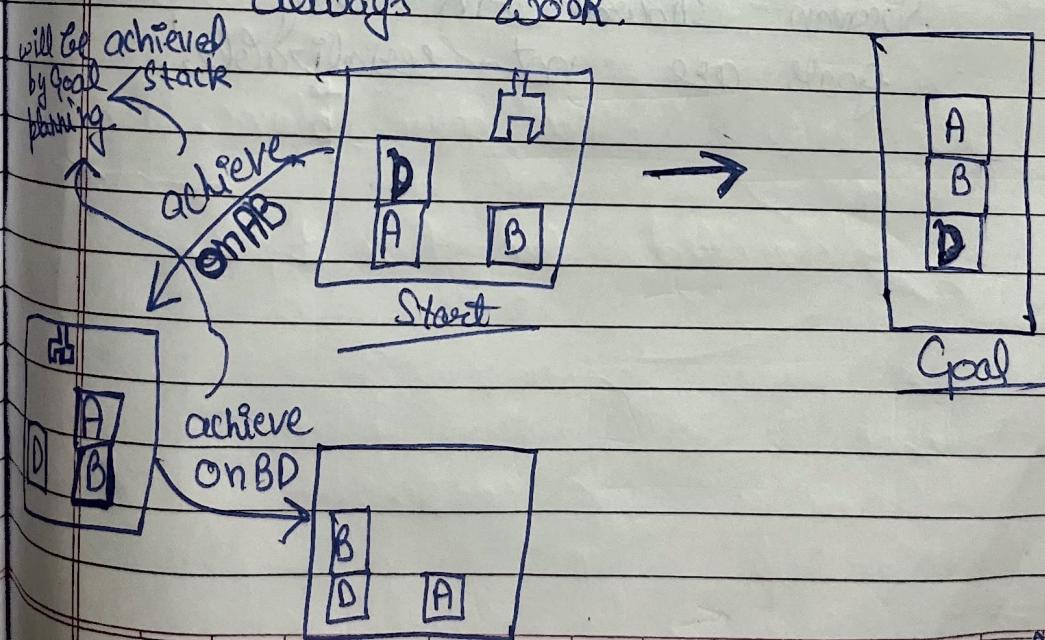
Plans considered in backward fashion
 (Construction of Plan) But action taken in forward

→ Ordering how to perform action is important here

→ Here, we are ~~reality~~ serializing the Goals, hence known as Linear planning.

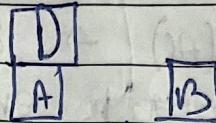
SUSSMAN's Anomaly

→ It shows that Goal stack will not always work.

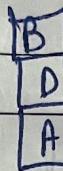


∴ We achieved ^{how on BD & on AB} but Not Goals state

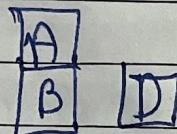
so This order not correct
let's try other order



↓ on BD



↓ on AB



↓
Goal not achieved

We can do extra work but
Algo wrong here



Sosman showed in many problems
goals are not serializable.

Non LINEAR PLANNING (Partial Order Planning)

- ↳ Least Commitment planning
(Very less commitments)
(we will add only limited stuff to plan)
- ↳ Plan Space Planning
 - ↳ Partially specified \Rightarrow Refinement Step Plan
- ↳ Partial Plan is denoted as a 4 tuple $\langle A, \mathcal{L}, C, B \rangle$ (all are set)
- ↳ $A \rightarrow$ Actions part of plan
- ↳ $\mathcal{L} \rightarrow$ Ordering relation which specifies order of actions.
- ↳ $C \rightarrow$ Causal links
- ↳ $B \rightarrow$ Binding constraints
- \Rightarrow Say Current action = stack(A, x)
then we can put constraints
 - $x = A$
 - $x \neq B$
 - $x \in \{B, C\}$

Causal Link is a triple where $\langle a, P, b \rangle$

$\langle a, p, b \rangle$ means

a produces predicate P
+ b consumes predicate P

a, bare actions

example \rightarrow

$\langle \text{Unstack}(A, y), \text{holding}(A) , \text{potDown}(A) \rangle$

$\Rightarrow \text{PE effect}(a)$
 $+ \text{PE second}(b)$

\Rightarrow In GalStack planning, we commit to solve one subgoal first and then the second subgoal.

But in partial plan limited commitments.

\Rightarrow we are not working in space of states anymore, we will start with some initial plan and we will apply refinement step to get new plans.

Search space contains only plans. (Partial plans)

\hookrightarrow described by four tuple.

What we want to do

- \hookrightarrow look at a partial plan
- \hookrightarrow choose a refinement step
- \hookrightarrow come up with new partial plan

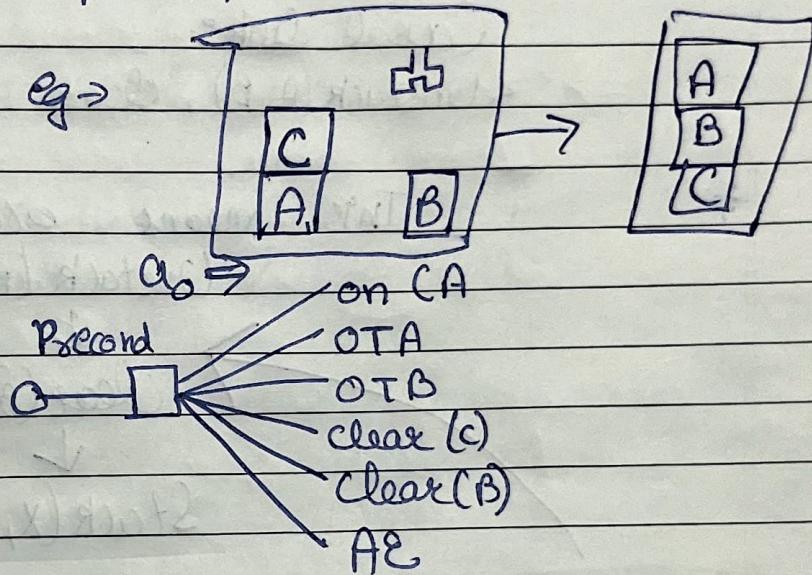
When to terminate :-

Initial plan - Π_0 has two actions & one ordering constraint.

$\langle (a_0, a_0), a_0 \leq a_0, (), () \rangle$

$a_0 \rightarrow$ no preconditions
effects = {start}

nil $\xrightarrow{a_0}$ Start It simple produces start state



$a_0 \rightarrow$ no effects

precond \rightarrow

on AB

()

on BC

Π_0 can be seen to stand for set of plans in which a_0 is first action & a_0 is last

Now, the goal is to make connections b/w actions

↳ We want to add causal links such that they are not disturbed later on.

Problem :-

Say we want for an action

Causal link :-

$\langle \text{Unstack}(A, B), \text{clear } B, \text{Stack}(X, B) \rangle$

This means ordering

$\text{Unstack}(A, B)$

\rightarrow

\downarrow

$\text{clear } B$

\downarrow

$\text{Stack}(X, B)$

Order is there but not contiguous. Other actions could happen b/w them.

Say b/w them another action $\text{Stack}(Y, Y)$ comes

$$+ Y = B$$

Then $\text{Stack}(Y, Y)$ is ~~that~~.

∴ Causal link will be disrupted by this action.

⇒ Planning process should consider this into account & do something about it.

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⇒ TWFAK was one of the first NC Planning algo.

↳ There they use the term Clobbering / DEClobbering which modern algoe don't use.

⇒ Clobbering means I am Clobbering the causal link. If it clobbers it then another action will DEClobber it. (causal link)
Hence causal links are not disrupted.

⇒ Ordering links should be consistent. (No cycle)

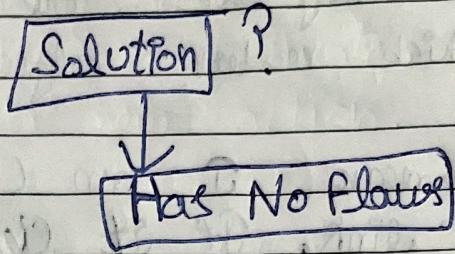
Refinement steps are of 4 types
 ↳ Add. action to A
 ↳ Add ordering link to B
 ↳ Add causal link to C
 ↳ Add a constraint
 ⇒ We could choose any one at a time.

~~Imp~~
 ⇒ we will start with initial partial plan π₀ then we start to fill in
 ↳ How to fill in?
 ↳ We have series of refinement steps.

When to terminate? Solution
 ↳ State Space perspective
 ↳ Complete B
 ↳ Topological sort of $\Pi \rightarrow \Pi'$
 ↳ Progress from start state + applicable action.

Many topological sort possible so ignore.

Other ways



⇒ We want to look at partial plan & want to say whether solution or not

⇒ Implicitly we are doing the prev. page thing only.

i.e., if this were a ca^n then any consistent ordering of action will be valid.

But, here we say this by looking at partial plan only.

Has no flaws :-

→ Open goals → (If No causal links)
There is no action which produces the subgoal. then flaw

② Threat → No threat should be there

i.e. an action threatens the causal link,
(shown in prev. pages).

→ An action G threatens the causal link
(a, p, b)

if C produces not of P ①
 & happen after a & before b.
 ② ③

To resolve ^{the last} one of 3 shouldn't happen.

⇒ Partial plan is a solution plan if it has no flaws.

High lvl algo \Rightarrow

- ① Start with initial plan
- ② Keep refining it
- ③ Do ② till no flaws.

Algo \Rightarrow

PSP(Π_0)

$\Pi \leftarrow \Pi_0$

while Π has a flaw

Choose a flaw f

let $R(f)$ be set of resolvers for

f if $R(f) = \emptyset$ then

return FAIL

else

choose $\pi \in R(f)$

$\Pi \leftarrow \text{Apply } (\pi, \Pi)$

(flaw resolved)

Return Π

⇒ PSP should be able to solve Sussman's anomaly.

⇒ How to address open goal flaw :-

↳ 2 ways :-

- (1) Existing action in the plan can supply a predicate.
- (2) Add a new action.

How to resolve a threat :-

~~3 cases~~ → ① Separation → Add ^{binding} Constraint

② Demotion

If A is a threat to $\langle A_1, P, A_2 \rangle$
then Add ~~Capital~~ ~~constraint~~
ordering $(A_2 < A)$
 $(A_2 \text{ happens before } A)$

③ Promotion

Add $(A_1 < A)$ to ordering set
 $(A_1 \text{ happens before } A)$

⇒ We have 5 resolvers :-

(2+3)

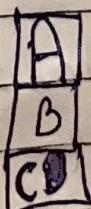
For open goal ⇒ 2 resolvers

↳ Existing Action ~~old~~

↳ New Action

For threat :-

* Sussman's Anomaly



① threatened by
②

\hookrightarrow ordering
link

\Rightarrow ③ + ④ Connected

Action(s)

```

graph TD
    A[Unstack CA] --> B[Put down - Pick up B]
    B --> C[Stack BC]
    C --> D[Stack AB]
    E[In this we can] --> F[Unstack A]
  
```

From this we can
make a linear plan
(Using topological sort)

