

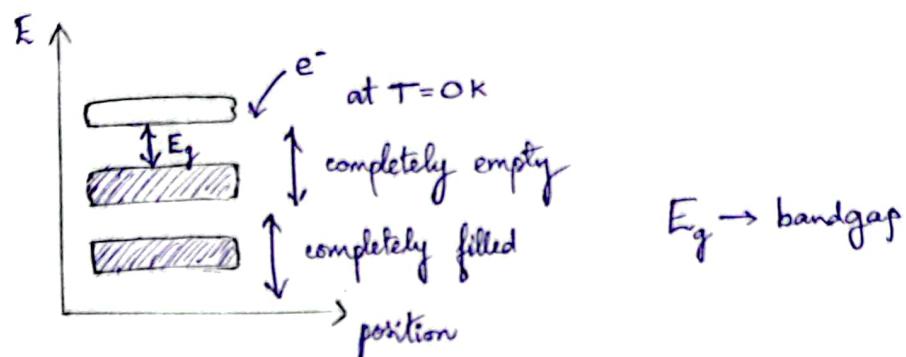
Diamond cubic structure (DC):-

Obtained by two FCC lattices interpenetrating body-diagonally.

Eg: Silicon (same FCC), GaAs (Different FCC), GaN → HCP

Basis:- Unit of a lattice

09/01/2023



Semiconductor $\rightarrow E_g$ is small

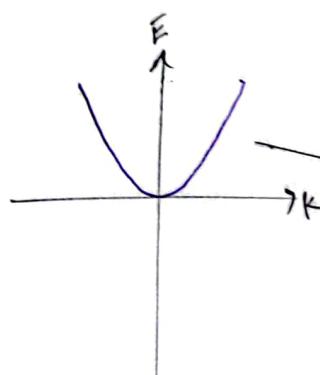
Insulator $\rightarrow E_g$ is large $\rightarrow E_g > 4\text{ eV}$

Metal \rightarrow Partially filled band at 0K

of free e^-

$$p = mv \\ F = \frac{1}{2}mv^2 = \frac{p^2}{2m}$$

$$p = \hbar k \rightarrow h/2\pi \\ k = \frac{2\pi}{\lambda} \rightarrow \text{De-Broglie wavelength}$$



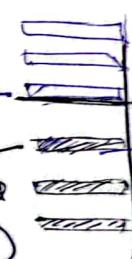
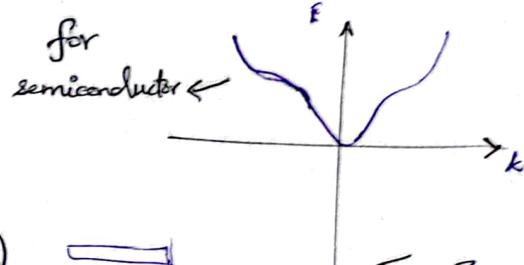
$$= \frac{\hbar^2 k^2}{2m}$$

$\rightarrow E-k$ relation
of a free e^-

(Dispersion relation)

lowest empty band
(Conduction band)

highest filled band
(Valence band)



$$F = -f(k) \quad (\text{for min})$$

$$E = E_0 + \frac{\partial E}{\partial k} k + \frac{1}{2} \frac{\partial^2 E}{\partial k^2} \cdot k^2 \approx E_0 + \frac{1}{2} \frac{\partial^2 E}{\partial k^2} \cdot k^2$$

(that focuses the plot for semiconductor e⁻)

reference energy

$$\Rightarrow \frac{\hbar^2 k^2}{2m} = E_0 + \left(\frac{k^2}{2} \cdot \frac{\partial^2 E}{\partial k^2} \right)$$

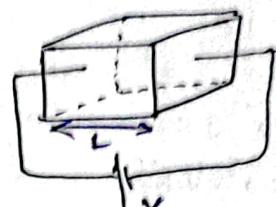
L.v. imp!

$$m^* = k^2 \left(\frac{\partial^2 E}{\partial k^2} \right)^{-1}$$

$$|\epsilon| = V/L$$

$$\Rightarrow F = -q\epsilon$$

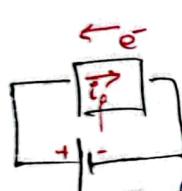
$$= -q(\frac{V}{L}) = m^* \frac{dv}{dt} \rightarrow \text{velocity}$$



15/01/2023

Concept of holes

$$T = 0K$$



e⁻'s moving in conduction band (E_C)

$$(I_n)$$

$$n = 0$$

$$e^-$$

$$E_C$$

$$p = 0$$

$$e^+$$

$$E_V$$

$$e^+$$

$$\text{"holes" moving in valence band}$$

$$(E_V)$$

$$T = 10K$$

$$e^{i\omega - \epsilon}$$

$$E_C$$

$$e^{-\epsilon}$$

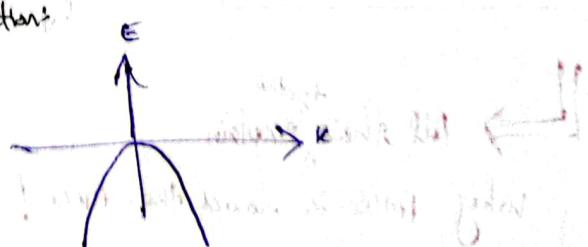
$$E_V$$

$$\text{No. of } e^+ \approx 10^{22} \text{ cm}^{-3}$$

e⁻ in a semiconductor: E-k relation

$$-qE = m_e^* \frac{dv}{dt}$$

(E₀ = 0 as e⁻ is in free band)



Now,

I'll be creating a virtual particle called "hole" :

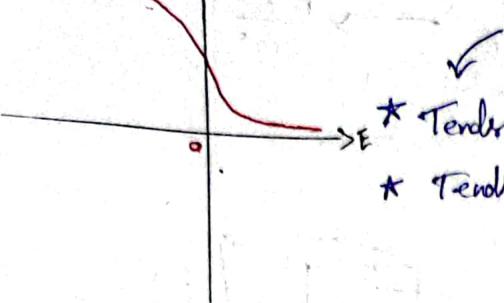
$$qE = (-m_e^*) \frac{dv}{dt}$$

$$qE = m_h^* \frac{dv}{dt}$$

Entropy

Fermi-Dirac eqn:

$$f(E) = \frac{1}{1 + e^{(E-E_F)/k_B T}}$$



$$k_B = 1.38 \times 10^{-23} \text{ J K}^{-1}$$

$$= 8.6 \times 10^{-5} \text{ eV K}^{-1}$$

Tells us the density \leftarrow for an e^-

of e^-s in any particular energy level.

NOTE: Probability of occurrence of a hole = $[1 - f(E)]$

16/01/2024

Density of States (DOS)

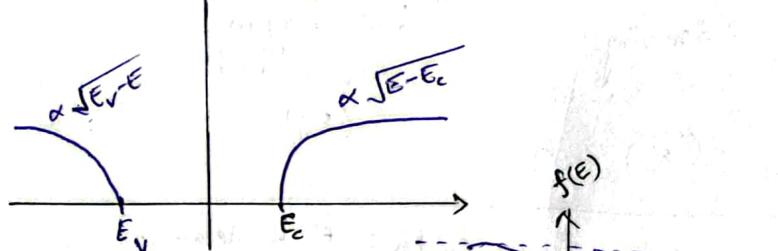
$N_c(E) \rightarrow$ Unit: per unit energy per unit vol.
($\text{eV}^{-1} \text{cm}^3$)

Number of states $N = \int_{E_c}^{E_c + \Delta E} N_c(E) dE$ for $\Delta E > 0$

Also, note that right @ $E = E_c$, $N = 0$.

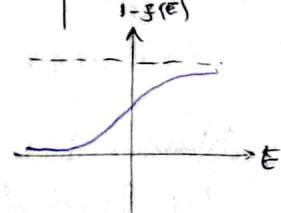
$$N_c = \left[\frac{1}{2\pi^2} \left(\frac{2m_e^* e}{\hbar^2} \right)^{3/2} \right] \sqrt{E - E_c}$$

$$N_v = \left[\frac{1}{2\pi^2} \left(\frac{2m_h^* e}{\hbar^2} \right)^{3/2} \right] \sqrt{E_v - E}$$



All these together explain why PMOS is slower than NMOS!

So... no. of e^-s in conduction band 'n' = $\int_{E_c}^{E_c + \Delta E} f(E) \cdot N_c(E) dE$ per unit volume



no. of holes in valence band 'p' = $\int_{E_v - \Delta E}^{E_v} [1 - f(E)] \cdot N_v(E) dE$ per unit volume

$\therefore n \propto \sqrt{SE}$ and $p \propto S E$:

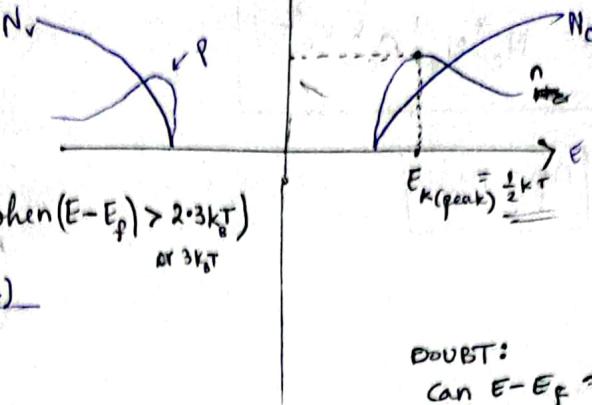
$$\langle E_k \rangle = \frac{3}{2} kT$$

NOTE:

If $E \gg E_F$,

Boltzmann Approximation: (when $(E - E_F) > 2-3kT$)

$$f(E) = \frac{1}{1 + e^{(E-E_F)/kT}} \approx e^{-\frac{(E-E_F)}{kT}}$$



DOUBT:
Can $E - E_F = E_F$?

Another approximation:

$$n = \int_{E_c}^{E_c+\infty} f(E) N_c(E) dE$$

NOTE: @ room temp,
 $k_B T = 0.026 \text{ eV}$

Approximation is valid as $f(E)$ decays quite fast and has already decayed a lot. \therefore negligible effects.

NOTE:

Requirement:

$$E_c - E_F \gg k_B T$$

$$\therefore n = \int_{E_c}^{\infty} f(E) N_c(E) dE = N_c^* e^{-\frac{(E_c - E_F)}{k_B T}}$$

"analytically
integrable"

N_c^* → Effective DOS (just a prefactor of exponential)

$\because e^-$ has
2 spins

$$@ T = 300 \text{ K}, \quad k_B T = 26 \text{ meV}$$

$$@ T = 600 \text{ K}, \quad k_B T = 52 \text{ meV}$$

$$\therefore n = N_c^* e^{-\frac{(E_c - E_F)}{k_B T}}$$

$$P = N_v^* e^{-\frac{(E_F - E_V)}{k_B T}}$$

18/01/2023

Ideal semiconductor $\Rightarrow n_i = p_i$

(intrinsic semiconductor) $\therefore n_i \cdot p_i = ?$

$$n_i^2 = N_c^* N_v^* e^{-\frac{(E_c - E_V)}{k_B T}}$$

$$n_i = \sqrt{N_c^* N_v^*} e^{\left(\frac{-E_V}{2k_B T}\right)}$$

$\Rightarrow n = p$

The most driving force for semiconductor

What if $n_i \neq p_i$?

If $n \neq p$ [Extrinsic Semiconductor] (created by doping)

Then $np = N_c^* N_v^* e^{\left(\frac{-E_g}{k_B T}\right)}$

$$np = n_i^2$$

It says that whether semiconductor intrinsic or extrinsic,
 $n \cdot p = \text{CONSTANT}$ same value

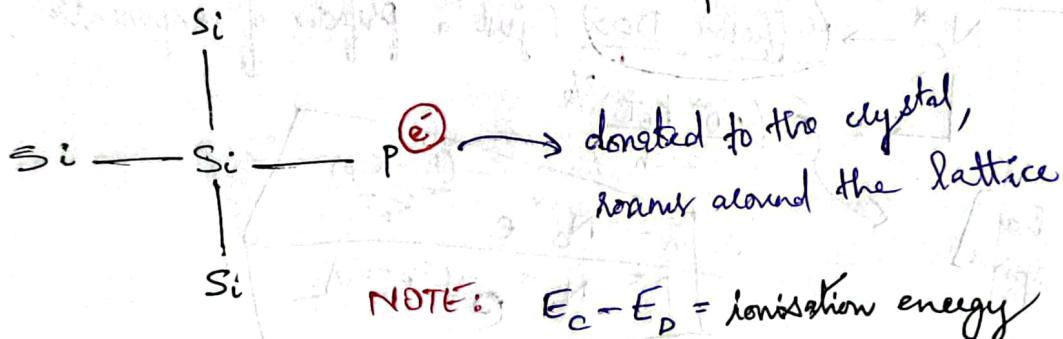
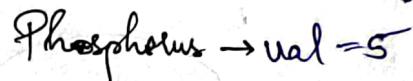
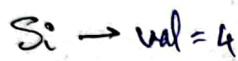
23/1/2024



$$\text{Si} \rightarrow \text{Ni} \approx 11 \times 10^{10} \text{ cm}^{-3}, E_g = 1.1 \text{ eV}$$

Extrinsic \rightarrow n-type (e) (donor level) (N_p = donor density)
 \rightarrow p-type (e^-) (h) (acceptor level) (N_A = acceptor density)

Give introduced something (doping) that gave rise to new energy level (E_D)



Requirements for doping:

- * Val (new atom) $>$ Val (old atom)
- * Donor must be shallow donor ($E_C - E_D$ must be less than $k_B T$)

Donor conc $\sim 10^{19} \text{ cm}^{-3}$, whereas host atoms $\sim 10^{24} \text{ cm}^{-3}$.

\therefore 1 donor atom among 10^5 host atoms, \therefore they do not bond.

$\Rightarrow \therefore$ they can't form a band, just a discrete line defect of energy level E_D .

Charge Neutrality

Intrinsic $\rightarrow n_i = p_i$

Intrinsic $\rightarrow n + N_A = p + N_D$

In addition,

\therefore law of mass action holds, $np = n_i^2$

$$n_i = 10^{10} \text{ cm}^{-3}$$

$$N_D = 10^{18} \text{ cm}^{-3}$$

$$N_A = 10^{17} \text{ cm}^{-3}$$

Note: If $(N_D - N_A) \gg n_i$ \Leftrightarrow predominantly doped by donors

$$n \approx (N_D - N_A)$$

[Similarly, if $(N_A - N_D) \gg n_i$]

$$\Rightarrow p \approx (N_A - N_D)$$

$$p = \frac{n_i^2}{n}$$

$$n \approx (N_D - N_A)$$

$$\Rightarrow p_F / 10^{17} \text{ cm}^{-3}$$

$$\therefore p = \frac{10^{20}}{9 \times 10^{17}} = \frac{1}{9} \times 10^3 \text{ cm}^{-3}$$

Here,

$$n = N_c e^{-\frac{(E_C - E_F)}{k_B T}}$$

$$p = N_v e^{-\frac{(E_F - E_V)}{k_B T}}$$

$n \gg p$

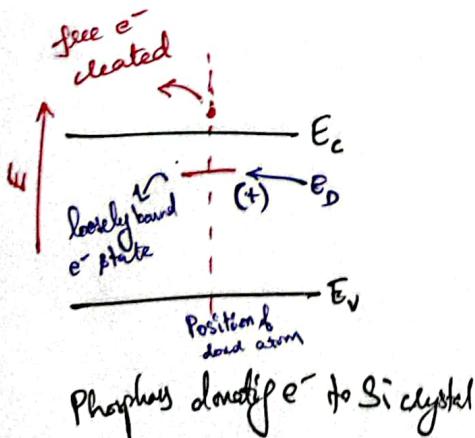
$E_F - E_C$ is large

$E_V - E_F$ is small
(very very small)

Conclusion

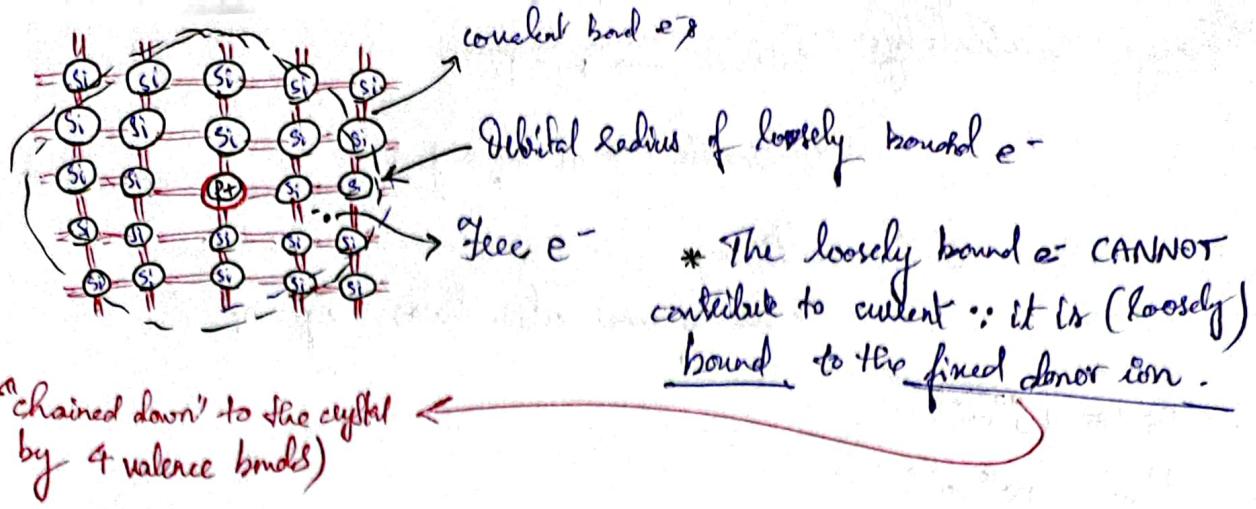
of Fermi-level being close to $E_C \Leftrightarrow n\text{-type}$

$E_V \Leftrightarrow p\text{-type}$



* The lowest energy (ground) state of an e^- associated with the donor atom exists only near that donor atom, so the donor state of energy (E_D) does not exist throughout the crystal.

* Donor state is close to conduct. band edge -



25/01/2024

Summary

$$n = N_c' e^{-\frac{(E_c - E_F)}{k_B T}}$$

$$p = N_v' e^{-\frac{(E_F - E_V)}{k_B T}}$$

$$f(E) = \frac{1}{1 + e^{(E - E_F)/k_B T}} \\ \approx e^{-\frac{(E - E_F)}{k_B T}}$$

$$n = \int_{E_c}^{\infty} f(E) N_c(E) dE$$

$$= N_c' e^{-\frac{(E_c - E_F)}{k_B T}}$$

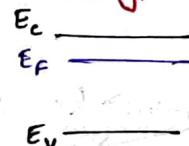
$$\text{Intrinsic: } n_i = p_i = \sqrt{N_c N_v} e^{-\frac{(E_g)}{k_B T}}$$

$$\text{Extrinsic: } n_p = n_i^2 \\ \text{AND } n_n = p + N_D^+$$

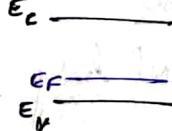
$$\text{If } N_D \gg n_i \Rightarrow n \approx (N_D + N_A)$$

$$N_c = [] \sqrt{E - E_c} \quad \text{if } E \geq E_c$$

n-type



p-type



Avg. energy of e^- : $\langle E \rangle = \frac{\int E n(E) dE}{n}$

total no.
of e^-

$$= \boxed{\frac{3}{2} k_B T}$$

\rightarrow In a quantum well: $-\frac{3}{2} k_B T$

\rightarrow In nanoelectronics: $-\frac{1}{2} k_B T$

\rightarrow If a quantum dot: $-V_{bias}$

Si.

$$E_g = 1.1 \text{ eV}$$

$$N_c' = 10^{22} \text{ cm}^{-3}$$

$$N_V' = 2 \times 10^{22} \text{ cm}^{-3}$$

$$\Rightarrow n_i = \sqrt{N_c' N_V'} e^{-\frac{E_g}{2k_B T}}$$

$$= 10^{22} \cdot \sqrt{2} e^{-\frac{1.1}{2 \times 0.026}}$$

$$= 9.19425 \times 10^{12} \text{ cm}^{-3}$$

Q. Where is the position of Fermi level?

Sol. $\because n = N_c' e^{\frac{(E_F - E_C)}{k_B T}} \therefore E_F - E_C = k_B T \ln \left(\frac{n}{N_c'} \right) = 0.026 \ln \left(\frac{9.19 \times 10^{12}}{10^{22}} \right)$

$$= -0.5 \text{ eV}$$

NOTE: If the density of electrons and holes were equal ($N_c' = N_V'$)
then don't you expect Fermi level to be right in the middle?

So, intrinsic $\Rightarrow n_i = p_i \Rightarrow e^{-\frac{(E_C - E_F)}{k_B T}} = e^{-\frac{(E_F - E_V)}{k_B T}} \Rightarrow E_C - E_{F_{\text{intrinsic}}} = E_{F_{\text{intrinsic}}} - E_V$

Proved :) $\Rightarrow E_F = \frac{E_C + E_V}{2}$

Qn. $E_g = 1.1 \text{ eV}$ $N_c' = 10^{22} \text{ cm}^{-3}$ $N_V' = 2 \times 10^{22} \text{ cm}^{-3} \therefore n_i = 9.19 \times 10^{12} \text{ cm}^{-3}$

Doping: $N_D = 10^{17}$ $N_A = 0$ then, $E_F = ??$

Sol. $n = N_D - N_A = 10^{17}$. Now, $n = N_c' e^{-\frac{(E_C - E_F)}{k_B T}}$
($\because \gg n_i$) $\Rightarrow E_F - E_C = k_B T \ln \left(\frac{n}{N_c'} \right)$
 $= 0.026 \ln \left(10^{17}/10^{22} \right)$
 $= -0.29$

Conclusion: As you see, doping the SC with more e^- (by N_D) results in moving of E_{Fermi} closer to E_C .

Q. In previous Qn, what if $N_D = 10^{22} \text{ cm}^{-3}$? **Q**

(Shikha's eyes XD)

Sol.

$$E_F - E_C = k_B T \ln \left(\frac{n}{N_c} \right)$$

$$= 0.026 \ln \left(\frac{10^{22}}{10^{22}} \right) = 0 \Rightarrow E_F = E_C$$

Is it?



What went wrong?

Boltzmann!

$$|E_C - E_F| \gg k_B T$$

?

$\rightarrow 28 \text{ meV}$

o failed!

* If my e⁻ density is much smaller than the effective density of states... then Boltzmann approx holds.

* If Auditorium is filling close complete... don't use Boltzmann instead use integration approach. $\rightarrow N_c \sim T^{3/2}$

!! * Effective density of states is a fn of temp; DOS is NOT!

(In the classroom, if Pizza is distributed, strength of class goes above normal, the no. of chairs don't)

Explanation using physics and not mere eqns: If $T \uparrow \Rightarrow E_F \downarrow \Rightarrow (E_C - E_F) \uparrow$

(comes down to the middle)

* No. of carriers \uparrow when $T \uparrow$

which may overpower the doping level...

$\therefore E_F \downarrow$ and at extreme temp, E_F converges to E_{F_i} (because both e⁻ and holes are **M**) and hence $n_i \approx p_i$ (for very large T) and E_F comes down to mid-point.

NOTE: E_F moves and moves but never crosses midline.

29/01/2024

Transport

$$\epsilon = -\nabla V$$

$$= -\frac{\partial V}{\partial x} = -\frac{[V(x=L) - V(x=0)]}{L} = +\frac{V}{L}$$

$$V = IR = I \frac{\rho L}{A} = \vec{J} \rho l = \frac{I l}{\sigma} \Rightarrow J = \frac{\sigma V}{l}$$

Mobility unit: $\frac{\text{cm}^2}{\text{Vs}} \quad (= \frac{V}{E})$

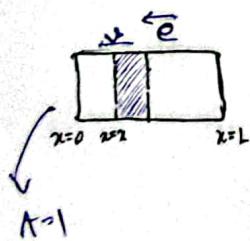
$$\Rightarrow \vec{J} = \sigma \vec{E} \rightarrow \text{Ohm's law!}$$

NOTE: Kirchhoff's law \rightarrow based on charge conservation!

Whatever comes in, goes out ✓

* No "accumulation" of charge carriers
 $\uparrow \downarrow$

$$\vec{J} = \sigma \vec{E} = \text{const.} \checkmark$$



$$J = \left(\frac{dQ}{dt} \right) \text{ per unit area} \rightarrow \text{drift velocity}$$

$$= nqAv$$

$$= nq\mu E$$

$$\boxed{J = \sigma E}$$

$$\propto E$$

$$\Rightarrow v = \mu E$$

mobility

NOTE:

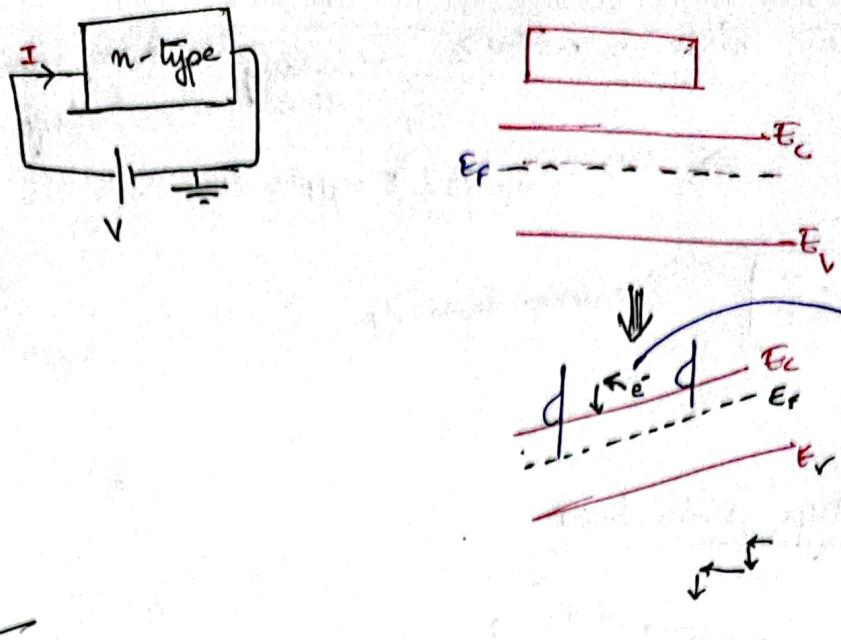
Metal has very low mobility!

$\approx 0.02 \frac{\text{cm}^2}{\text{Vs}} \Rightarrow \therefore \text{NOT used in high-speed devices}$

Semiconductors $\approx 500 \frac{\text{cm}^2}{\text{Vs}}$

Graphene $\approx 10^4 \frac{\text{cm}^2}{\text{Vs}}$

holds for metals as well as semiconductors



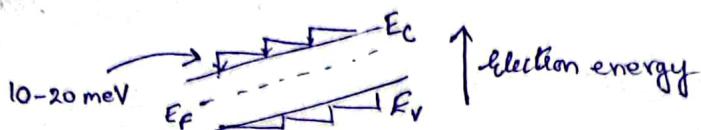
$$\text{Force} = qE = m^* \left(\frac{dv}{dt} \right) = m^* \frac{\langle v \rangle}{\tau} \rightarrow \begin{array}{l} \text{Scattering time} \\ \Rightarrow \text{avg velocity} \\ = v_{\text{shift}} \end{array}$$

$$\Rightarrow \langle v \rangle = v_{\text{shift}} = \left(\frac{q/2}{m^*} \right) E = \mu E$$

$$\Rightarrow \boxed{\mu = \frac{q/2}{m^*} = \frac{v}{E}} \rightarrow \text{microscopic definition of } \mu$$

31/01/2024

p-type semiconductor

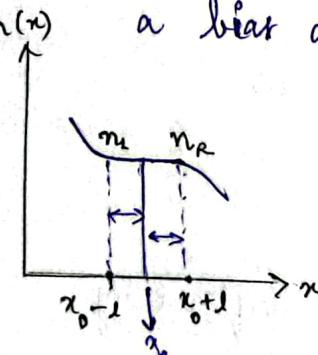


Holes act like balloons in the diagram for e⁻ energy.

$$\therefore J_p = qP\mu_p E \quad ; \quad J_n = qn\mu_n E$$

$$\therefore J = J_p + J_n = qE(P\mu_p + n\mu_n) = \sigma E$$

Diffusion: Movement of carriers without application of a bias due to concentration gradient.



\therefore Probability of carrier to be on the right $\rightarrow n_R l / 2$
left $\rightarrow n_L l / 2$

e⁻/carrier
(in Brownian motion)

\therefore flux of carriers across x_0 from left to right

$$= \frac{n_R l - n_L l}{2\tau}$$

2τ → "time taken for carrier to travel a length l, not the mean scattering time!"

$$\therefore F = \frac{(n_1 - n_2)l}{2\pi} = -\left(\frac{l^2}{2\pi}\right) \frac{\partial n}{\partial x} = -D \frac{\partial n}{\partial x}$$

D = Diffusion constant

$J_{n,\text{diff}}$ = Diffusion Current for electrons

$$\therefore J_{n,\text{diff}} = -qF = qD_n \frac{\partial n}{\partial x}$$

Similarly, $J_{p,\text{diff}} = qF = -qD_p \frac{\partial n}{\partial x}$

$$J_n = qn\mu_n E + qD_n \frac{\partial n}{\partial x}$$

⇒ Total current density

$$J_p = qP\mu_p E - qD_p \frac{\partial n}{\partial x}$$

$$J = J_n + J_p$$

Einstein's relation :

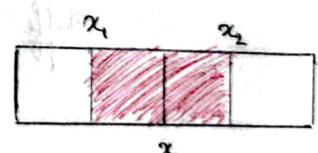
$$\boxed{D = \frac{K_B T}{\mu g}}$$

(only valid with Boltzmann approx)

* $E_C - E_F > 2k_B T \rightarrow$ Non-degenerate Semiconductor. Boltzmann ✓

⇒ Non-equilibrium condition

"Steady state has NOT been reached yet"



$$\therefore F(x_2) - F(x_1) = -\frac{\partial (n \Delta x)}{\partial E}$$

n = e⁻ density in Δx region

$$\therefore J_n = -qF$$

$$\Rightarrow J(x_2) - J(x_1) = q \frac{dn}{dt} \cdot \Delta x$$

$$\therefore \frac{\partial J}{\partial x} = q \frac{\partial n}{\partial t}$$

$$\text{Now, } J_n = qn\mu_n E + qD_n \frac{\partial n}{\partial x}$$

$$\therefore \frac{\partial J_n}{\partial x} = q\mu_n \left(n \frac{\partial E}{\partial x} + E \frac{\partial n}{\partial x} \right) + qD_n \frac{\partial^2 n}{\partial x^2} = \gamma \frac{\partial n}{\partial t}$$

$$\Rightarrow \mu_n \left(n \frac{\partial E}{\partial x} + E \frac{\partial n}{\partial x} \right) + D_n \frac{\partial^2 n}{\partial x^2} = \frac{\partial n}{\partial t}$$

What if no bias is applied?

$$E = 0 \Rightarrow D_n \frac{\partial^2 n}{\partial x^2} = \frac{\partial n}{\partial t}$$

$n = n_0 + \Delta n$

eq. condition

of Fick's 2nd law
of diffusion

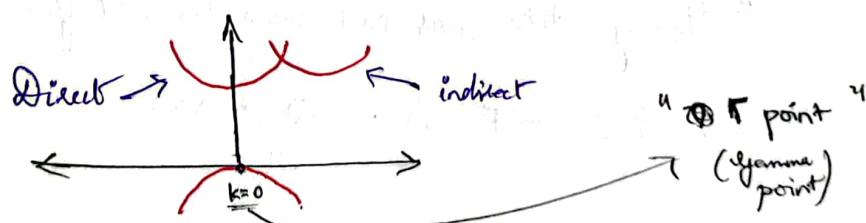
$$\therefore D_n \frac{\partial^2 (\Delta n)}{\partial x^2} = \frac{\partial (\Delta n)}{\partial t}$$

* Direct Bandgap Semiconductor:

Valence band maxima and conduction band minima occur at same k . (GaN, GaAs)

* Indirect Bandgap Semiconductor:

Valence band maxima and conduction band minima are different k . (Si, Ge)



A semiconductor is illuminated uniformly by light

\downarrow
 e^- -hole pair is produced.



? uniformly distributed

$$\therefore \frac{\partial n}{\partial n} = 0$$

$$\Rightarrow \frac{\partial^2 n}{\partial n^2} = 0 \Rightarrow \frac{\partial n}{\partial t} = 0$$

$$\Rightarrow \Delta n = \text{const}$$

p-type (EHP)

Optical generation

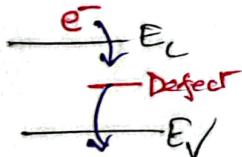
$$E = h\nu$$

If $h\nu > E_g$, e^- moves to the conduction band, creating an EHP.

Thermal generation: EHP generated due to thermal energy supplied.

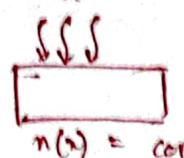
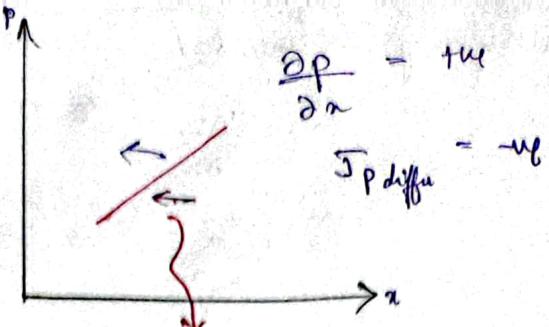
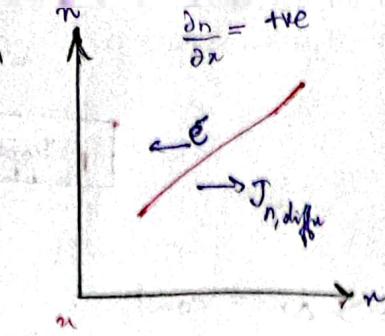
Direct recombination: e^- in conduction band directly jumps down to the valence band.

Indirect recombination: There may be defects in the lattice structure which can provide additional energy levels for e^- to come into.



$$\frac{\partial n}{\partial t} = D_n \frac{\partial^2 n}{\partial x^2} + G - R$$

01/01/2024



$$n(x) = n_0 + \Delta x$$

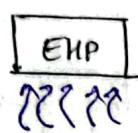
$$\frac{\partial n}{\partial x} = \frac{\partial \Delta n}{\partial x}$$

(current is now in the -ve edge direction)

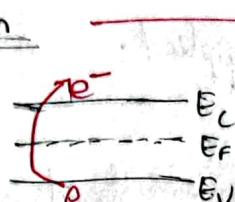
Excess carrier dynamics:

$$\frac{\partial \Delta n}{\partial t} = D \frac{\partial^2 (\Delta n)}{\partial x^2}$$

Optical generation



Light



measured

air

GOP in cm^{-3}/s

(generation optical)

* Thermal generation - G_{th} in cm^{-3}/s [n_i (intrinsic generated)]

Recombinations

Direct
recombination

[Band-to-band (B2B)
recombination]

Defect-assisted
recombination

[Shockley Read Hall]
(SRH)

$$P(t) = (1 - e^{-t/\tau_m})$$

[Poisson distribution]

* Recombination $R = \Delta n / \tau_m$ ← average

Defect
recombination

τ_m = Recombination lifetime

So in this case, our continuity eqn becomes -

$$\frac{\partial \Delta n}{\partial t} = D \frac{\partial^2 (\Delta n)}{\partial x^2} + GOP - \frac{\Delta n}{\tau_n}$$

* NOTE: Again, if uniformly illuminated, Δn is same everywhere.

Thus concn gradient $\frac{\partial (\Delta n)}{\partial x} = 0 \rightarrow \frac{\partial^2 (\Delta n)}{\partial x^2} = 0$

$$\text{So, } \frac{\partial \Delta n}{\partial t} = GOP - \frac{\Delta n}{\tau_n}$$

$$\Rightarrow \Delta n(t) = GOP \cdot \tau_n (1 - e^{-t/\tau_n})$$

$$\Delta n(t=0) = 0$$

$$\Delta n(t=\infty) = GOP \cdot \tau_n$$

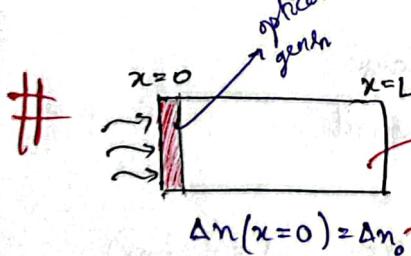
(like charging of a $-HT$!)

$$\text{at } t = \infty, \frac{\partial \Delta n}{\partial t} = 0$$

* whatever has to happen, has happened. That's how we find **Steady state light?**

$$\therefore \Delta n(t=\infty) = GOP \cdot \tau_n$$

generation = recombination



GOP acts here as I'm shining light only from left.
excess e⁻ density per unit time (GOP) @ x=0

$$\Delta n(x,t) \rightarrow \Delta n(x,\infty) \equiv \Delta n(x) ?$$

(Note)
(Interest)

↓
excess e⁻ density profile
at steady state

$$\frac{\partial \Delta n}{\partial t} = 0$$

$$D_n \frac{\partial^2 \Delta n}{\partial x^2} + GOP = \frac{\Delta n}{\tau_n}$$

$$\Rightarrow \Delta n(x) = Ae^{-\frac{x}{\sqrt{D_n \tau_n}}} + Be^{\frac{x}{\sqrt{D_n \tau_n}}}$$

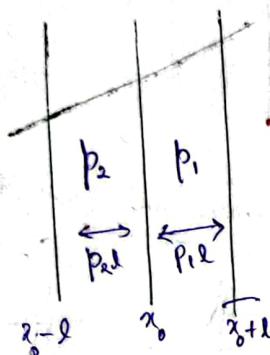
$$\Delta n(x) = Ae^{\frac{-x}{\sqrt{D_n z_n}}} + Be^{\frac{x}{\sqrt{D_n z_n}}}$$

Excess carriers cannot glow as you go deeper ($\uparrow x$) in the semiconductor

$$= Ae^{\frac{-x}{\sqrt{D_n z_n}}} = Ae^{-x/L_n}$$

$$\sqrt{D_n z_n} = L_n = \text{diffusion length}$$

02/02/2024



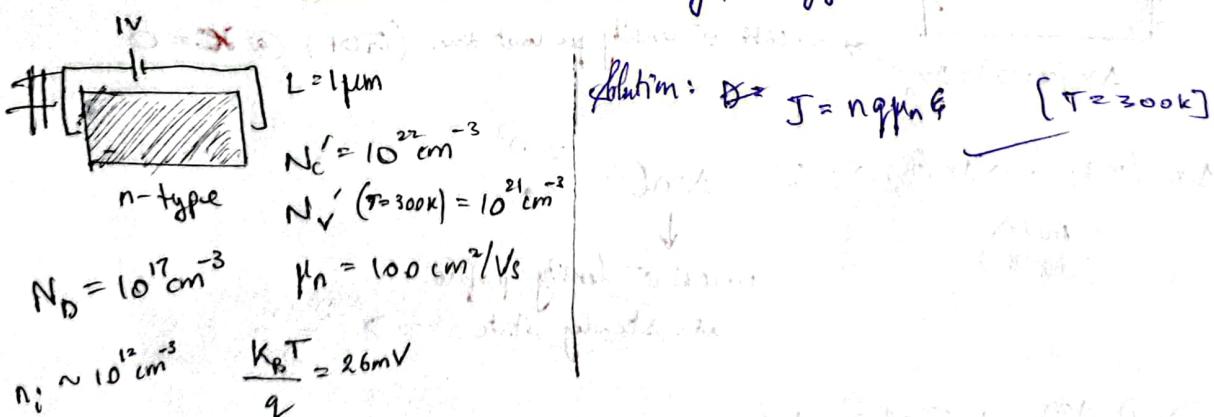
$$p_i = p_2 + \frac{\partial p}{\partial x} \Delta x \quad [\text{Taylor expansion}]$$

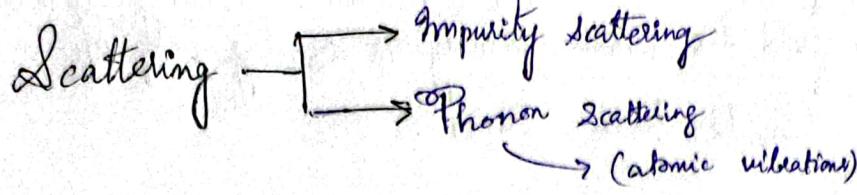
$$\text{Total } e^- \text{ moving towards right} = \frac{p_2 l - p_1 l}{2}$$

Monte Carlo Algorithm: Studying the microscopic level

NOTE: * Photon momentum is small, energy is large

* Phonon momentum is large, energy is small





$$\mu_I = \frac{q\tau_I^*}{m^*} \quad \mu_P = \frac{q\tau_P^*}{m^*}$$

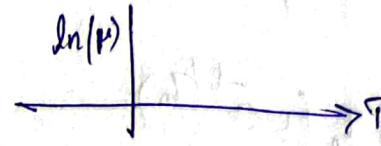
$$\frac{1}{\tau_{\text{eff}}} = \frac{1}{\tau_I} + \frac{1}{\tau_P} \quad [\text{Mottissen's rule}]$$

and $\frac{1}{\tau_{\text{eff}}} = \frac{1}{\tau_I} + \frac{1}{\tau_P^*}$

Temperature dependency of μ

$$\mu_P \sim T^{-3/2}$$

$$\mu_S \sim T^{3/2}$$

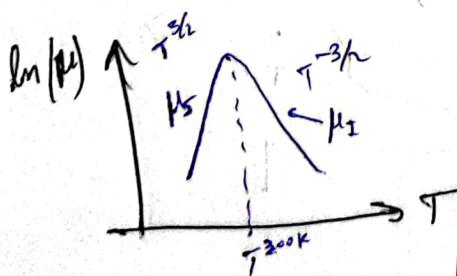


At low T , $\mu_P \rightarrow \mu_S$ negligible
 $\mu_S \rightarrow \mu_S$ dominates

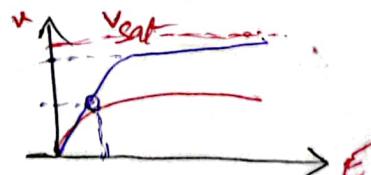
At high T , $\mu_P \rightarrow \mu_P$ dominates
 $\mu_P \rightarrow \mu_I$ negligible

$T \uparrow \Rightarrow e^-$ intrinsic motion fast

Interaction time with fixed charge is less → less scattering → mole mobility ↑



$$v_{\text{el}} = \mu \times E$$



$$\mu = \frac{\mu_0}{1 + \left(\frac{E}{E_0}\right)} \rightarrow \text{low-field mobility}$$

E_c is that electric field for which velocity is exactly half of what it ideally should have been.

$$\text{at } E = E_c, \quad v = \frac{\mu_0}{1 + \frac{E}{E_c}} \cdot E_c = \frac{\mu_0}{2} E_c$$

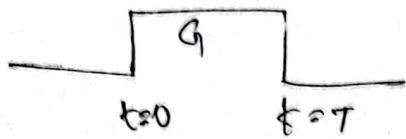
whereas

$$\text{ideal: } v = \mu_0 E_c$$

#

SSSS
P-type

$$\Delta n(t) = ?$$



NOTE:

Recombination rate $R = \beta n p$
 $\zeta = 1/2$

$$\therefore \tau_n \propto \frac{1}{\beta N_A} \quad (\text{for a p-type})$$

$$\Delta n(t) = G \tau_n (1 - e^{-t/\tau_n})$$

$$\frac{\partial \Delta n}{\partial t} = D_n \frac{\partial^2 \Delta n}{\partial x^2} + G - \frac{\Delta n}{\tau_n}$$

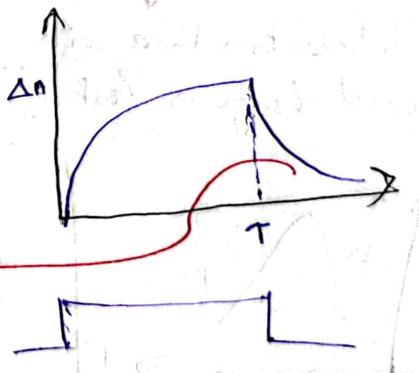
$t > T$

$$= -\Delta n / \tau_n$$

$$\Rightarrow \Delta n = \Delta n(t=T) e^{-t/\tau_n}$$

Poisson distribution

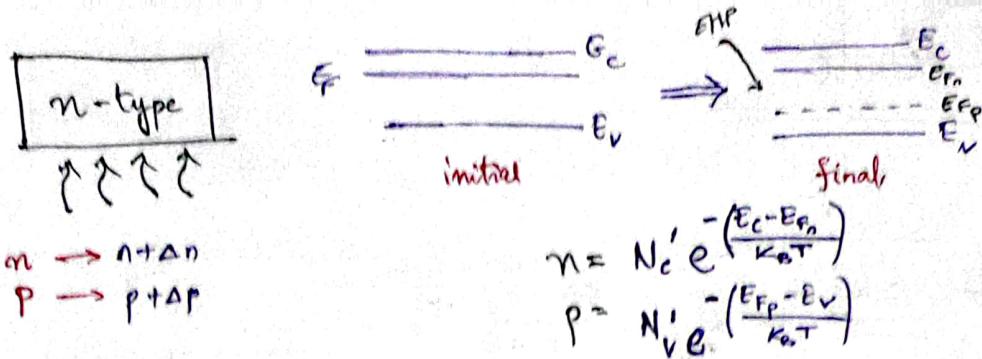
$$\therefore \Delta n(t=T) = G \tau_n (1 - e^{-T/\tau_n})$$



We want this to decay faster,

$$\therefore \text{reduce } \tau_n$$

05/02/2024



$$n = N_C e^{-\frac{(E_C - E_{F_n})}{k_B T}}$$
$$p = N_V e^{-\frac{(E_{F_p} - E_V)}{k_B T}}$$

I can keep using these Quasi-Fermi levels for non-eqm conditions.

[NOTE: This is assumed purely for ease of analysis]

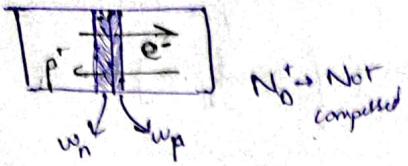
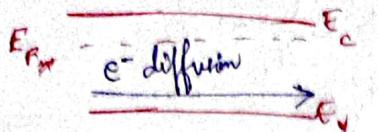
* Dielectric relaxation time $\sim ps$

$N(E)dE$:- Number of electronic states per unit volume with an energy between E and $E+dE$ in the conduction band!

$$E - E_C = \text{electron kinetic energy} = \frac{p_x^2}{2m_x} + \frac{p_y^2}{2m_y} + \frac{p_z^2}{2m_z}$$

Diode

n-type



$$N_D^+ \cdot w_n = N_A^- \cdot w_p$$

$$\frac{dE_F}{dx} = 0$$

p-type



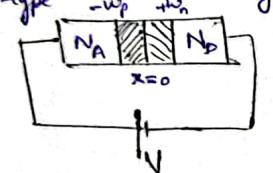
Steps:
Gradient of charge carriers

\downarrow
 e^- / hole diffuse

\downarrow
create internal E field

\downarrow
 e^- / hole now drift

06/02/2024 PN Junction diode



$$\text{At eqm, } V=0, J=J_p + J_n$$

$$J_p = 0 \quad J_n = 0$$

$$\text{Also, } E_F = \text{CONSTANT at eqm} \left(\frac{dE_F}{dx} = 0 \right)$$

$$N_A^- W_p = N_D^+ W_n$$

$$J_n = q \mu_n n E + q D_n \frac{\partial n}{\partial x} \quad \frac{D}{\mu} = \frac{k_B T}{q}$$

$$= q \mu_n \left(n E + \frac{k_B T}{q} \frac{\partial n}{\partial x} \right) \quad n = N_c' e^{-\frac{(E_c - E_F)}{k_B T}}$$

$$\frac{\partial n}{\partial x} = \frac{N_c'}{k_B T} e^{-\frac{(E_c - E_F)}{k_B T}} \left[\frac{\partial E_F}{\partial x} - \frac{\partial E_c}{\partial x} \right]$$

? (how?)

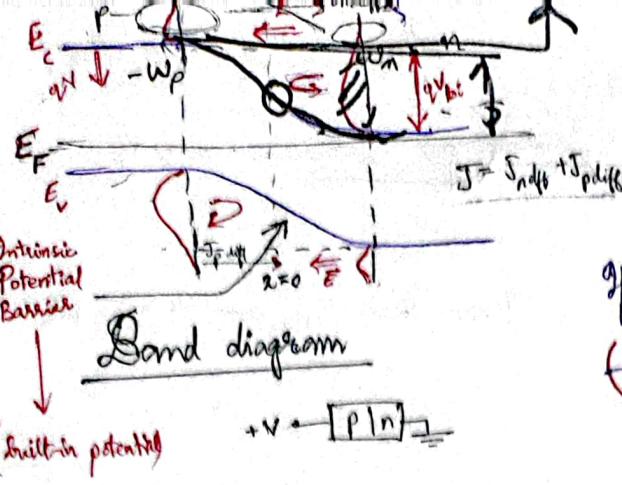
$$J_n = \mu_n n \left(\frac{\partial E_F}{\partial x} \right)$$

$$\Rightarrow \frac{\partial n}{\partial x} = \frac{n}{k_B T} \left(\frac{\partial E_F}{\partial x} - q E \right)$$

Effective electric field

$$\Sigma E = \frac{1}{q} \left(\frac{\partial E_F}{\partial x} \right)$$

\therefore At eqm $\frac{\partial E_F}{\partial x} = 0$, Fermi level lines up at the eqm



Forward bias

$$|W_n| + |W_p| = \text{depletion width}$$

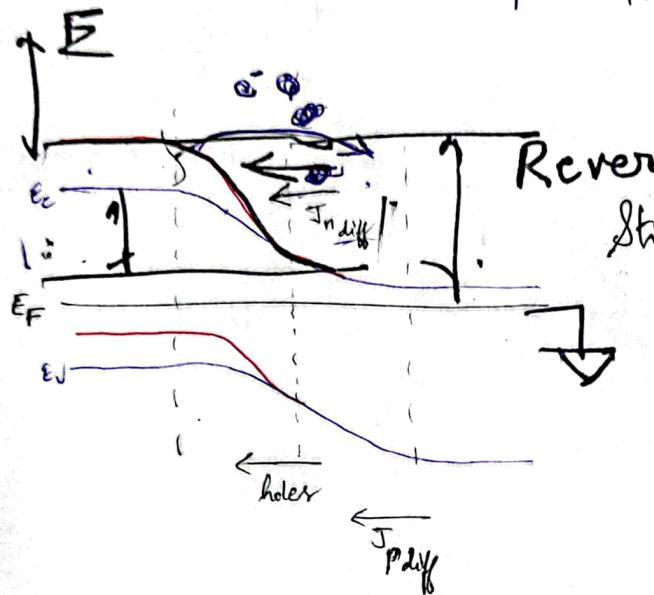
If V apply a bias of V , then energy (built-in potential) reduces to $q(V_{bi} - V)$.

What if V apply -ve bias at P-side? [Reverse bias]

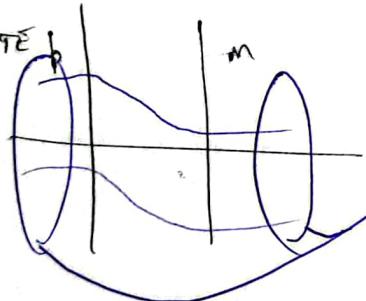


Now the levels are pulled up!

→ Barrier has increased for the n-side, but it has helped e^- in p-side.



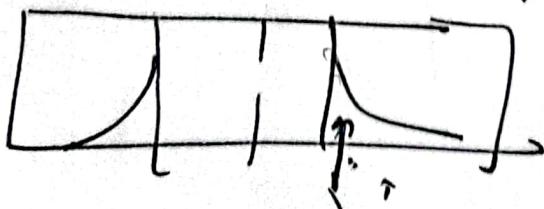
NOTE:



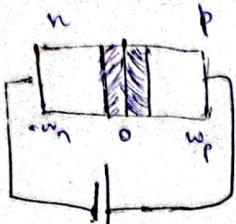
ASSUMPTIONS

- 1] Quasi-neutral region (far away from interface)
Here $E = 0$.
- 2] Abrupt junction
- 3] Boltzmann approximation is valid
- 4] Low-level injection

P. \leftarrow \rightarrow n (e^-)

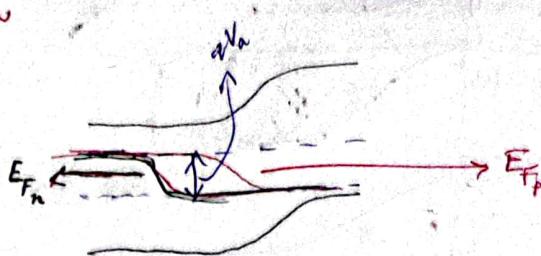
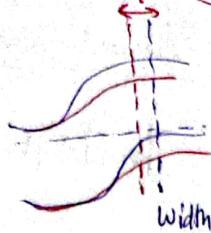


08/02/2024



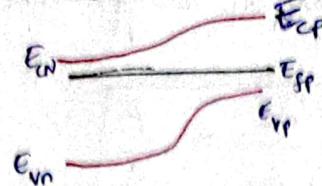
I apply a V_a forward bias...

$$W = W_n + W_p \downarrow$$



Forward bias: E_{F_p} comes down by qV_a .

13/02/2024

P-N JunctionAt $T = 0 \text{ K}$, $V_A = 0$

$$n = N_c e^{-\frac{(E_{Fn} - E_{Fn})}{k_B T}}$$

$$p = N_v' e^{-\left(\frac{E_{FP} - E_{Vp}}{k_B T}\right)}$$

$$= N_p$$

$$E_{Fn} - E_{Fn} = k_B T \ln \left(\frac{N_c'}{N_0} \right)$$

$$E_{FP} - E_{Vp} = k_B T \ln \left(\frac{N_v'}{N_A} \right)$$

~~(How?)~~ $V_{bi} = \frac{k_B T}{q} \ln \left(\frac{N_A N_D}{n_i^2} \right) \quad V_{bi} = E_g - (E_{Fn} + E_{FP} - E_{Vp})$

$$qV_{bi} = E_g - k_B T \left(\ln \left(\frac{N_c'}{N_0} \right) + \ln \left(\frac{N_v'}{N_A} \right) \right) = E_g - k_B T \ln \left(\frac{N_c' N_v'}{N_0 N_A} \right)$$

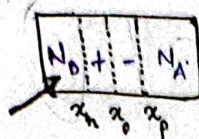
$$\text{using } n_i = \sqrt{N_c' N_v'} e^{-\frac{E_g}{2k_B T}}$$

$$= E_g - k_B T \ln \left(\frac{n_i^2}{N_A N_0} e^{\frac{E_g}{k_B T}} \right)$$

$$= E_g - k_B T \ln \left(\frac{n_i^2}{N_A N_0} \right) - k_B f \cdot \frac{E_g}{k_B T}$$

$$\Rightarrow V_{bi} = \frac{k_B T}{q} \ln \left(\frac{N_A N_D}{n_i^2} \right)$$

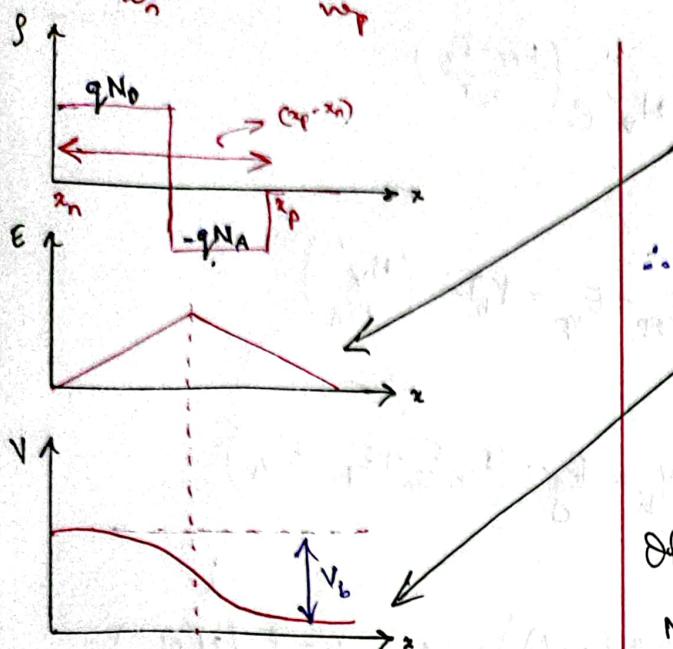
Gauss' law in Differential form:



$$N_D(x_0 - x) = N_A(x_p - x_0)$$

$\underbrace{w_n}_{\omega_n}$ $\underbrace{w_p}_{\omega_p}$

$$\frac{\partial E}{\partial x} = \frac{\rho}{\epsilon_0}$$



Band diagram
= -qV

$$E_i = \frac{q N_D}{\epsilon_0} (x - x_0)$$

$$\therefore V(x) = \frac{-q N_D}{\epsilon_0} (x^2 - x_0^2)$$

$$W = W_n + W_p = \left(\frac{2 E V_{bi}}{q} \left(\frac{1}{N_A} + \frac{1}{N_D} \right) \right)^{1/2}$$

$\Rightarrow W \propto V^{1/2}$

Okay, consider a doping case like ...

$N_D^+ \gg N_A^-$ * Holes moving from p to n
(p → heavily doped)

$w_n \ll w_p$ * Depletion region always penetrates into the lower doped region

$$n_{no} = N_c e^{-\left(\frac{E_{cn} - E_{Fn}}{k_B T}\right)}$$

$$n_{po} = \left(N_c e^{-\left(\frac{E_{cp} - E_{Fp}}{k_B T}\right)} \right)$$

$$\therefore n_{po} = N_c e^{-\left(\frac{E_{cn} - E_{Fp}}{k_B T}\right)} \cdot e^{\left(\frac{qV_{bi}}{k_B T}\right)}$$

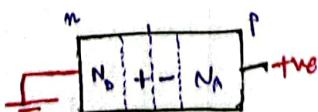
$$= [e^{E_{cn}/k_B T} \times e^{-E_{cn}/k_B T}] \times e^{E_{cp}/k_B T} \times e^{-E_{Fp}/k_B T}$$

at eqm, $E_{Fp} = E_{cp} = E_{Fn}$

$$\Rightarrow n_{po} = \left(n_{no} \right) e^{-\left(\frac{|qV_{bi}|}{k_B T}\right)}$$

$\frac{n}{n_{no}}$

minority carrier on p-side majority carrier on n-side



* We found out the minority carrier concentration because we want to look into diffusion.

Now, what happens if we apply a forward bias?

If $V_a > 0$, \Rightarrow

$$V_{bi} \rightarrow V_{bi} - V_a$$

[splitting in Fermi-level = V_a]

$$\uparrow q(V_{bi} - V_a)$$

$$P_n = P_{p0} e^{\left(\frac{-q(V_{bi} - V_a)}{k_B T}\right)}$$

$$P_p = P_{p0} e^{\left(\frac{-q(V_{bi} - V_a)}{k_B T}\right)}$$

$$n_p = n_{p0} e^{\left(\frac{-q(V_{bi} - V_a)}{k_B T}\right)}$$

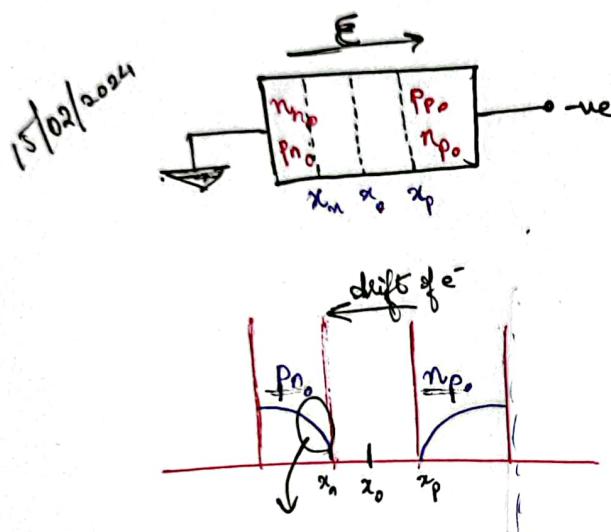
$$\Delta n_p (\alpha = x_p) = n_p - n_{p0} e^{\left(\frac{-q(V_{bi} - V_a)}{k_B T}\right)}$$

excess carriers
that have come
due to bias

at bias

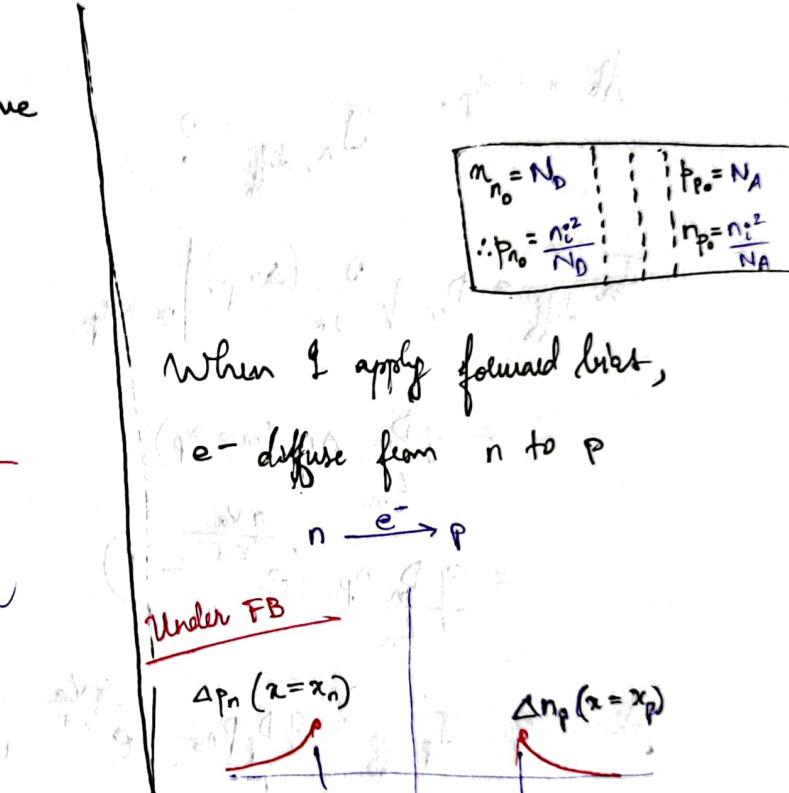
at eqm

$$= n_{p0} e^{\left(\frac{-q(V_{bi})}{k_B T}\right)} - n_{p0}$$



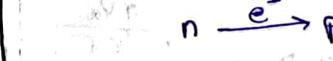
$$\nabla \cdot \vec{J} = -\frac{\partial P}{\partial x}$$

$\therefore J \rightarrow \text{continuous}$



When I apply forward bias,

e- diffuse from n to p



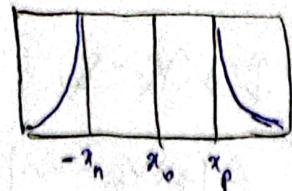
Under FB

$$\Delta n_p (\alpha = x_n)$$

$$\Delta n_p (\alpha = x_p)$$

$$\Delta n_p \sim e^{-(x-x_p)/L_n}$$

17/02/2024



$$\frac{\partial^2 \Delta n}{\partial x^2} = \frac{\Delta n_p}{L_n^2}$$

$$\Rightarrow \Delta n = A e^{-x/L_n} + B e^{x/L_n}$$

decaying \downarrow at $x=0$ to $x=L$

$$= A e^{-x/L_n} = \Delta n_p(x=0) e^{-x/L_n}$$

$$\Delta n_p(x > x_p) = \Delta n_p|_{x=x_p} e^{-x_p/L_n}$$

$$\frac{\partial \Delta n_p}{\partial t} = D_n \frac{\partial^2 (\Delta n_p)}{\partial x^2} - \frac{\Delta n_p}{2n}$$

At steady state, $\frac{\partial}{\partial t} (\Delta n_p) = 0$

$$- (x - x_p)/L_n$$

$$\therefore \Delta n_p = \Delta n_p(x=x_p) e^{- (x - x_p)/L_n}$$

$$; L_n = \sqrt{D_n T_n}$$

in quasi-neutral region

At $x = x_p$, $J_{n, \text{diff}} = ?$

$$J_{n, \text{diff}} = D_n \sqrt{\frac{\partial (\Delta n_p)}{\partial x}} \Big|_{x=x_p}$$

$$= \frac{q D_n}{L_n} \Delta n_p(x=x_p)$$

$$= \frac{q D_n n_{p0}}{L_n} \left(e^{\frac{qV_a}{kT}} - 1 \right)$$

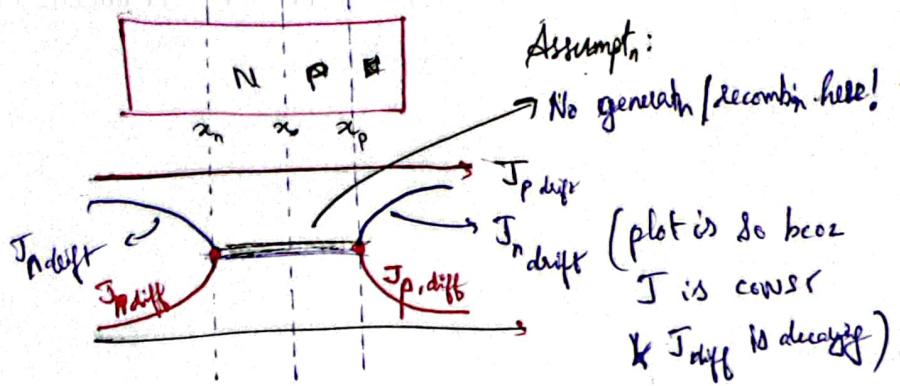
Similarly, $J_{p, \text{diff}} = \frac{q D_p P_{n0}}{L_p} \left(e^{\frac{-qV_a}{kT}} - 1 \right)$

$$\therefore J = q \left(\frac{D_n n_{p0}}{L_n} + \frac{D_p P_{n0}}{L_p} \right) \left(e^{\frac{qV_a}{kT}} - 1 \right)$$

$$\boxed{J = J_0 \left(e^{\frac{qV_a}{kT}} - 1 \right)}$$



Shockley diode eqn.



J_{diff} need not be symmetric to

$J_{n,\text{diff}}$; depends on parameters