

2) Given

$$P(C) = 0.01 \text{ (Having cancer)}$$

$$P(B) = P(C)^c \text{ (Benign tumor - not cancer)}$$

$$= 1 - P(C) = 1 - 0.01 = 0.99$$

$$P(C/CT) = 0.8 \text{ (cancerous tumor detected)}$$

$$P(NC/B) = 0.9 \text{ (Benign tumor detection not cancer)}$$

$$\therefore P(C/B) = 0.1$$

Using Bayes rule

$$~~P(CT/C) = \frac{P(C/CT)P(C)}{P(C/CT)P(C) + P(C/B)P(B)}~~ \quad P(CT/C) = \frac{P(C/CT)P(C)}{P(C)}$$

$$\Rightarrow P(CT/C) = \frac{P(C/CT)P(C)}{P(C/CT)P(C) + P(C/B)P(B)}$$

$$= \frac{0.8 \times 0.01}{[0.8 \times 0.01] + [0.1 \times 0.99]}$$

$$= \frac{0.008}{0.008 + 0.099} = 0.0747$$

$$\approx 0.075$$

Hence, the probability of patient having cancer if test is positive is 0.075

$$P(CT/C) = 0.075 = 7.5\% \quad (OR)$$

$$P(CT/C) = 0.0747$$