Cryptography and Network Security Chapter 7

Fifth Edition

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Random Numbers

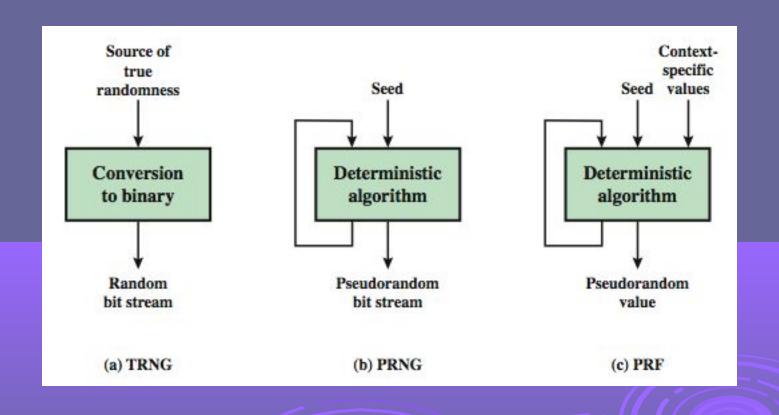
- many uses of random numbers in cryptography
 - nonces in authentication protocols to prevent replay
 - session keys
 - public key generation
 - keystream for a one-time pad
- in all cases its critical that these values be
 - statistically random, uniform distribution, independent
 - unpredictability of future values from previous values
- true random numbers provide this
- care needed with generated random numbers

Pseudorandom Number Generators (PRNGs)

- often use deterministic algorithmic techniques to create "random numbers"
 - although are not truly random
 - can pass many tests of "randomness"
- known as "pseudorandom numbers"
- created by "Pseudorandom Number Generators (PRNGs)"

Reference: R. Hegadi and A. P. Patil, "A Statistical Analysis on In-Built Pseudo Random Number Generators Using NIST Test Suite," 2020 5th International Conference on Computing, Communication and Security (ICCCS), Patna, India, 2020, pp. 1-6, doi: 10.1109/ICCCS49678.2020.9276849.

Random & Pseudorandom Number Generators



PRNG Requirements

- randomness
 - uniformity, scalability, consistency
- unpredictability
 - forward & backward unpredictability
 - use same tests to check
- characteristics of the seed
 - secure
 - if known adversary can determine output
 - so must be random or pseudorandom number

PRNG Requirements

Randomness

- Uniformity at any point in the generation of the PRN sequence, the occurrence of a zero or a one is equally likely (i.e., p = 0.5)
- Scalability any test for randomness applicable to a sequence can also be applied to any random subsequence (it should pass)
- Consistency the characteristics of the PRN sequence of the PRNG must not depend on the seed used

Linear Congruential RN Generator

common iterative technique using:

$$X_{n+1} = (aX_n + c) \mod m$$

- given suitable values of parameters can produce a long random-like sequence
- suitable criteria to have are:
 - function generates a full-period
 - generated sequence should appear random
 - efficient implementation with 32-bit arithmetic
- note that an attacker can reconstruct sequence given a small number of values have possibilities for making this harder

Blum Blum Shub RN Generator

- based on public key algorithms
- use least significant bit from iterative equation:
 - $\bullet \quad \mathbf{x}_{i} = \mathbf{x}_{i-1}^{2} \mod \mathbf{n}$
 - where n=p.q, and primes p, q
- unpredictable, passes next-bit test
- security rests on difficulty of factoring N
- is unpredictable given any run of bits
- slow, since very large numbers must be used
- too slow for cipher use, good for key generation

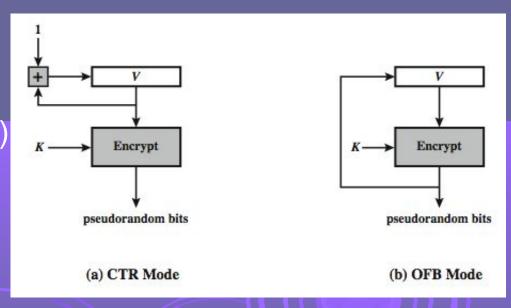
Using Block Ciphers as PRNGs

- for cryptographic applications, can use a block cipher to generate random numbers
- often for creating session keys from master key
- CTR (Counter mode)

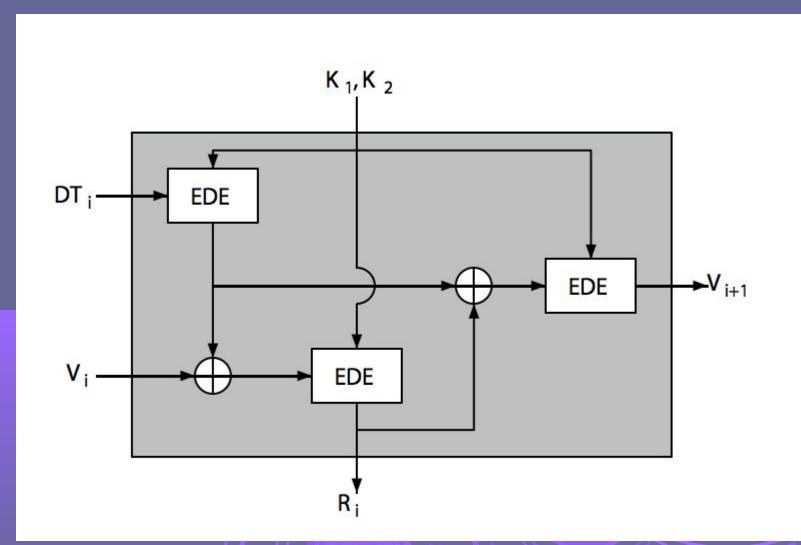
$$X_i = E_K[V_i]$$

OFB(o/p feedback mode)

$$X_{\underline{i}} = \mathbb{E}_{K}[X_{\underline{i}-1}]$$



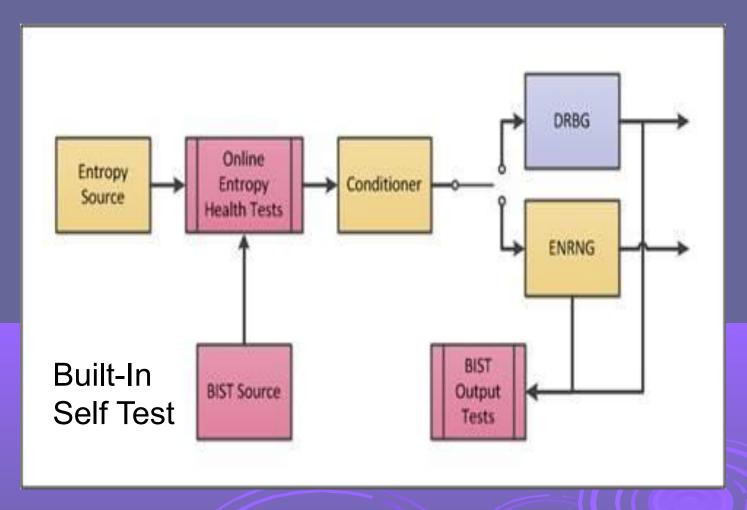
ANSI X9.17 PRG



Natural Random Noise

- best source is natural randomness in real world
- find a regular but random event and monitor
- do generally need special h/w to do this
 - eg. radiation counters, radio noise, audio noise, thermal noise in diodes, leaky capacitors, mercury discharge tubes etc
- starting to see such h/w in new CPUs
 - Intel Ivy Bridge, Via Padlock
- problems of bias or uneven distribution in signal
 - have to compensate for this when sample, often by passing bits through a hash function
 - best to only use a few noisiest bits from each sample
 - RFC4086 recommends using multiple sources + hash

Intel Ivy Bridge TRNG



Health tests are basic, ad hoc, but detect RNG failure Output zero with carry zero on failure (can't read a 0)

Trustworthiness of TRNGs

- Design appears to be very sound
- Possible back doors
 - Snowden leaks show NSA coerced hardware and software manufacturers to introduce back doors
 - Intel and Via hardware considered suspect
- Approach by FreeBSD
 - Use hardware PRNG as a source
 - Pass through Yarrow PRNG algorithm when producing cryptographically significant random numbers

See: https://www.schneier.com/paper-varrow.pdf

Published Sources

- a few published collections of random numbers
- Rand Co, in 1955, published 1 million numbers
 - generated using an electronic roulette wheel
 - has been used in some cipher designs of Khafre
- earlier Tippett in 1927 published a collection
- issues are that:
 - these are limited
 - too well-known for most uses

Summary

- pseudorandom number generation
- stream ciphers
- true random numbers

