



5. A/B Testing for Website Conversion Rate Optimization

Dataset

<u>Group</u>	<u>Converted</u>	<u>Count</u>
A	0	4695
	1	305
B	0	4607
	1	393

Group	Converted	COUNTA of Use
 A	0	4695
	1	305
A Total		5000
 B	0	4607
	1	393
B Total		5000
Grand Total		10000

Converted	COUNTA of Use
0	9302
1	698
Grand Total	10000

Group	COUNTA of Use
A	5000
B	5000
Grand Total	10000

Group (A) (Control):

- no. of users: $n_A = 5000$
- no. of conversions: $x_A = 305$

Group (B) (Treatment):

- no. of users: $n_B = 5000$
- no. of conversions: $x_B = 393$

sample conversion rates:

$$- p_A = \frac{x_A}{n_A} = \frac{305}{5000} = 0.0610 = 6.10\%$$

$$- p_B = \frac{x_B}{n_B} = \frac{393}{5000} = 0.0786 = 7.86\%$$

Compute (SE) for each proportion:

$$SE(p) = \sqrt{\frac{p(1-p)}{n}}$$

$$SE_A = 0.003386$$

$$SE_B = 0.003806$$

Construct the 95% Confidence Intervals:

A 95% confidence interval for a proportion is given by:

$$\hat{p} \pm Z_{\alpha/2} \times SE(\hat{p})$$

$$\text{for } 95\% \text{ CI, } Z_{\alpha=0.5/2} = Z_{0.25} = 1.96$$

Group A:

• Lower Bound:

$$\begin{aligned} L_A &= p_A - 1.96 \times SE_A = 0.0610 - (1.96 \times 0.003386) \\ &= 0.0610 - 0.006635 \\ &= \underline{0.05437} \end{aligned}$$

Upper Bound:

$$U_A = p_A + 1.96 \times SE_A = \underline{0.06764}$$

- 95% CI for Group A is $(0.0544, 0.0676)$
or $(5.44\%, 6.76\%)$.

Group B:

Lower Bound:

$$L_B = p_B - 1.96 \times SE_B = 0.0786 - 1.96 \times 0.003806 \\ = \underline{\underline{0.07114}}$$

Upper Bound:

$$U_B = p_B + 1.96 \times SE_B = \underline{\underline{0.08606}}$$

- 95% CI for Group B is $(0.0711, 0.0861)$
or $(7.11\%, 8.61\%)$

Interpretation

(A) Conversion rate is 6.10% with a 95% CI of approx.
 $(5.44\%, 6.76\%)$

(B) T.R. is 7.86% with a 95% CI $(7.11\%, 8.61\%)$

The treatment group shows a higher conversion rate than the control group and C.I. suggest that the difference might be statistically significant.

Define Hypothesis -

• Null Hypothesis (H_0):

The conversion rates are equal between the two groups.

$$H_0 : p_A = p_B$$

• Alternative hypothesis (H_1):

The conversion rates differ b/w the two groups:

$$H_1 : p_A \neq p_B$$

* Data and sample proportions -

Under null hypothesis, we assume common rate

$$\hat{p} = \frac{x_A + x_B}{n_A + n_B} = \frac{698}{10000} = 0.0698$$

• Compute the (SE)

$$SE = \sqrt{\hat{p}(1-\hat{p}) \cdot \left(\frac{1}{n_A} + \frac{1}{n_B} \right)}$$

$$S.E. = \sqrt{0.00002596} \approx 0.00510$$

• Z-statistic

$$Z = \frac{\hat{p}_B - \hat{p}_A}{SE} = \frac{0.0786 - 0.0610}{0.00510} = \frac{0.0176}{0.00510} = \underline{\underline{3.45}}$$

• Determine the p-value -

- $Z = 3.45$, one-tailed prob. is very small (around 0.0007)

- for two-tailed test:

$$\begin{aligned} p\text{-value} &= 2 \times P(Z > 3.45) \\ &= 2 \times 0.0003 \\ &= 0.0006 \end{aligned}$$

$p\text{-value} < 0.05$, reject H_0 .

Interpretation -

- The two-proportion Z-test \Rightarrow Z statistic value of 3.45 with p-value of 0.0006.
- this provides strong evidence against the null hypothesis, indicating that new checkout page has significantly higher conversion rate than the existing page.

Potential risks of Type I (false positive) and Type II (false negative) errors.

Type I (False Positive):

- Rejecting the null hypothesis when it is actually true.
- Concluding that the new checkout page (treatment) improves conversion rates when, in reality, there is no difference.

• could lead to implementing a change that doesn't truly benefit the company.

• Failing to reject the null hypothesis when the alternative hypothesis is actually true.

• Concluding that there is no difference between the checkout pages when new page does in fact improve conversion rate.

• this would mean missing an opportunity to increase conversions