

# Analog Circuits(EE3300) Simulation Exercise 1

### EE19BTECH11041, Srijith Reddy Pakala

Department of Electrical Engineering
IIT Hyderabad

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#### 1 Problem statement

1. MOS transistors in nano-scale CMOS processes don't quite follow quadratic I-V characteristics we studied in the class. Their exact models (BSIM, PSP) contain hundredsof parameters, and it is almost impossible to use these models for hand calculations. In this exercise, we will try to extract a simple quadratic model for MOS transistors from the available BSIM4 model.

Download model files and corresponding LTspice files from the class website.

Determine the following for NMOS (L=65nm, W=1um) and PMOS (L=65nm, W=1um) transistors from the given model files:

(Given supply voltage,  $V_{dd}=1.1$  V. Use  $V_{ds}=V_{ds0}=V_{dd}/2$ , when not specified.)

- .  $V_{gs0}$ : $V_{gs}$  value in the middle of the quadratic region of  $I_{ds}$   $V_{gs}$  curve. Use derivative function available in waveform viewer.
- .  $g_{m0}$ : $g_m$  at  $V_{gs0}$ .
- .  $V_T$ : x-axis intercept of tangent at  $V_{gs0}$  in  $g_m$   $V_{gs}$  curve.
- .  $\beta = \mu C_{ox}$ : Using above extracted values and assuming quadratic behaviour.
- .  $g_{ds0}$ : $g_{ds}$  at  $V_{gs0}$ .
- .  $\lambda$ : Channel-length modulation parameter.  $(V_{gs}=V_{gs0})$ .

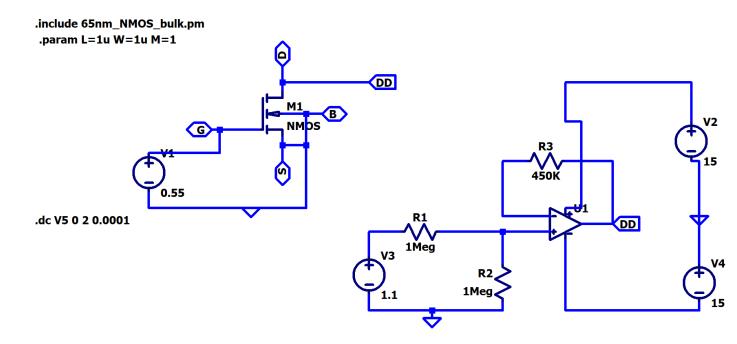


What is the range of  $V_{gs}$  for which error in estimated  $g_m$  is less than 50 %?

2. Repeat the above exercise for longer channel length devices. NMOS (L=1um, W=1um)and PMOS (L=1um, W=1um).

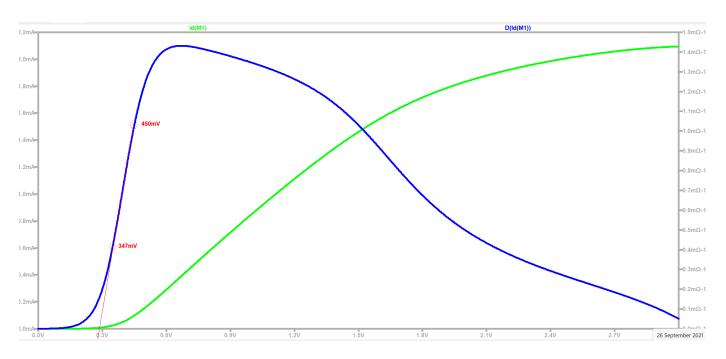
#### Question 1

#### Schematic of NMOS



Circuit schematic





From the graph we can see that the derivative is linear for  $V_{gs}$  in range of 347mV and 450mV.

$$V_{gs0} = \frac{347mV + 450mV}{2} = 388mV \tag{1}$$

$$g_{m0} = g_m|_{V_{gs0}} = 714\mu\Omega^{-1} \tag{2}$$

From the extension of tangent to x-axis we get

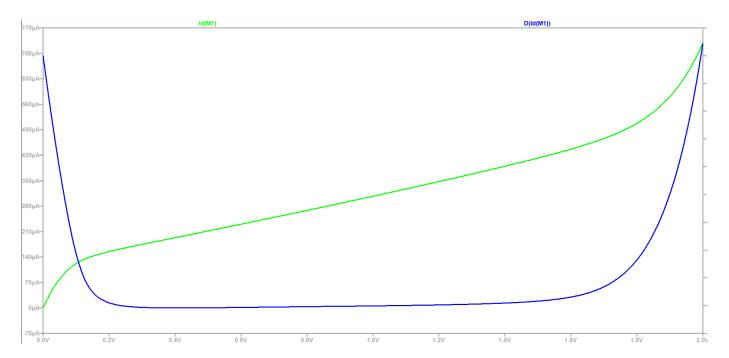
$$V_T = 288mV (3)$$

$$\frac{\beta W(V_{gs0} - V_T)}{L} = g_{m0} \tag{4}$$

$$\beta = 569~\mu$$



### $I_{ds}$ Vs $V_{ds}$ and $g_{ds}$ Vs $V_{ds}$ Curves



from the graph  $g_{ds0}\ : g_{ds}$  at  $V_{gs0}$  and  $V_{ds}=0.55 \mathrm{V}.$ 

$$g_{ds0} = 185\mu\Omega^{-1} \tag{5}$$

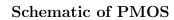
From the below equation we can calculate  $\lambda$ .

$$I_{ds}\lambda = g_{ds} \tag{6}$$

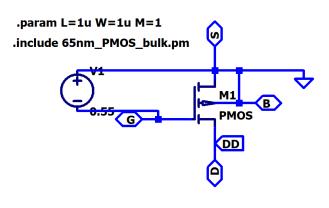
 $\lambda = 0.87.$ 

Now to find range of  $V_{gs}$  with less than 50 % Error we need to find values in range of  $(g_m/2,3g_m/2)$ .

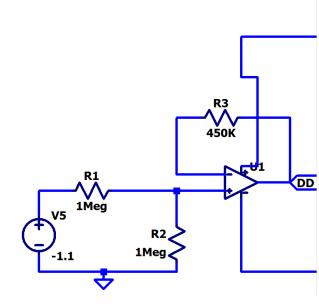
 $V_{gs} \text{ range} = (337 \text{mV}, 458 \text{mV})$ 





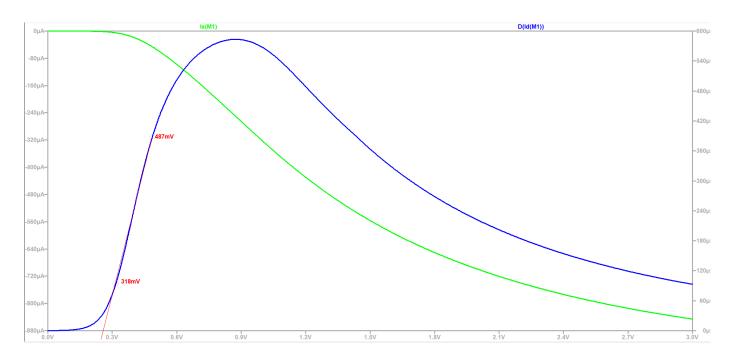


.dc V1 0 2 0.001



Circuit schematic





From the graph we can see that the derivative is linear for  $V_{gs}$  in range of -318mV and -487mV.

$$V_{gs0} = \frac{-318mV - 487mV}{2} = -395mV \tag{7}$$

$$g_{m0} = g_m|_{V_{gs0}} = -232\mu\Omega^{-1} \tag{8}$$

From the extension of tangent to x-axis we get

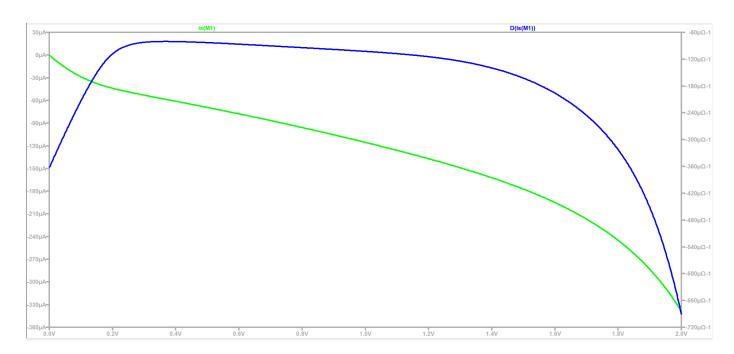
$$V_T = -280mV (9)$$

$$\frac{\beta W(V_{gs0} - V_T)}{L} = g_{m0} \tag{10}$$



 $\beta=184.8\mu$ 

### $I_{ds}$ Vs $V_{ds}$ and $g_{ds}$ Vs $V_{ds}$ Curves



from the graph  $g_{ds0}\ : g_{ds}$  at  $V_{gs0}$  and  $V_{ds}=0.55 \mathrm{V}.$ 

$$g_{ds0} = -84.99\mu\Omega^{-1} \tag{11}$$

From the below equation we can calculate  $\lambda$ .

$$I_{ds}\lambda = g_{ds} \tag{12}$$

 $\lambda = 1.14.$ 

Now to find range of  $V_{gs}$  with less than 50 % Error we need to find values in range of  $(g_m/2,3g_m/2)$ .

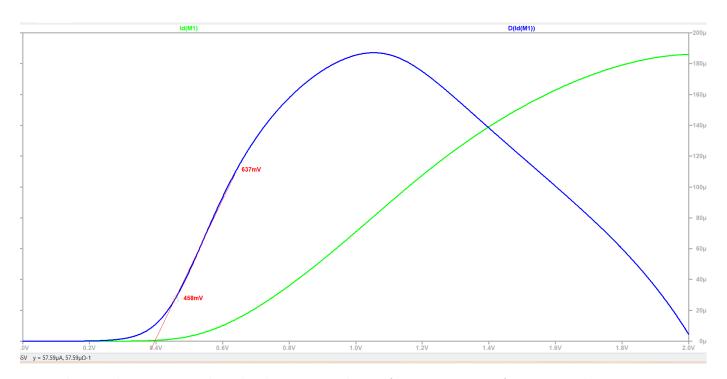
 $V_{gs} \text{ range} = (-332 \text{mV}, -460 \text{mV})$ 

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#### Long channeled NMOS

### $I_{ds}$ Vs $V_{gs}$ and $g_m$ Vs $V_{gs}$ Curves



From the graph we can see that the derivative is linear for  $V_{gs}$  in range of 458mV and 637mV.

$$V_{gs0} = \frac{458mV + 637mV}{2} = 550mV \tag{13}$$

$$g_{m0} = g_m|_{V_{gs0}} = 69.35\mu\Omega^{-1} \tag{14}$$

From the extension of tangent to x-axis we get

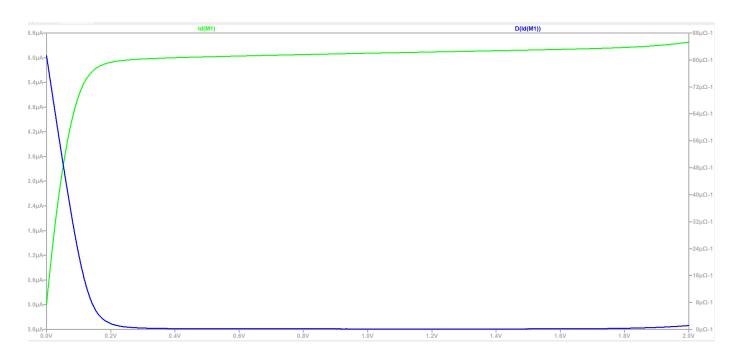
$$V_T = 400mV \tag{15}$$

$$\frac{\beta W(V_{gs0} - V_T)}{L} = g_{m0} \tag{16}$$



 $\beta = 541 \,\mu$ 

### $I_{ds}$ Vs $V_{ds}$ and $g_{ds}$ Vs $V_{ds}$ Curves



from the graph  $g_{ds0}\,:g_{ds}$  at  $V_{gs0}$  and  $V_{ds}=0.55\mathrm{V}.$ 

$$g_{ds0} = 191n\Omega^{-1} (17)$$

From the below equation we can calculate  $\lambda$ .

$$I_{ds}\lambda = g_{ds} \tag{18}$$

 $\lambda=0.0316.$ 

Now to find range of  $V_{gs}$  with less than 50 % Error we need to find values in range of  $(g_m/2,3g_m/2)$ .

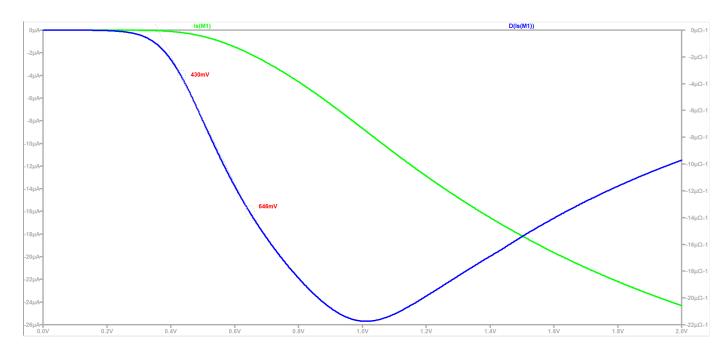
 $V_{gs} \text{ range} = (475 \text{mV}, 626 \text{mV})$ 

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#### Long channeled PMOS

### $I_{ds}$ Vs $V_{gs}$ and $g_m$ Vs $V_{gs}$ Curves



From the graph we can see that the derivative is linear for  $V_{gs}$  in range of -430mV and -646mV.

$$V_{gs0} = \frac{-430mV - 646mV}{2} = -538mV \tag{19}$$

$$g_{m0} = g_m|_{V_{gs0}} = -8.68\mu\Omega^{-1} \tag{20}$$

From the extension of tangent to x-axis we get

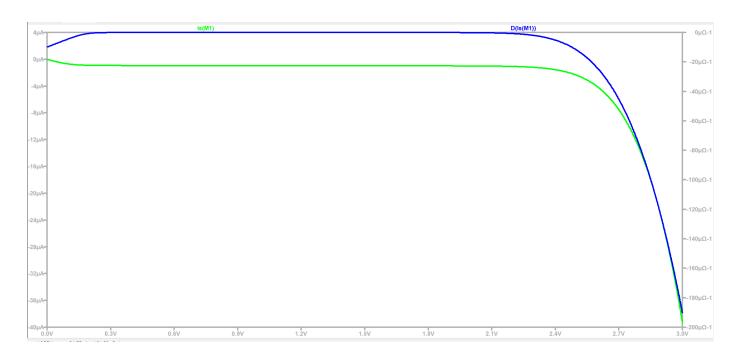
$$V_T = -350mV (21)$$

$$\frac{\beta W(V_{gs0} - V_T)}{L} = g_{m0} \tag{22}$$



 $\beta = 491\mu$ 

## $I_{ds}$ Vs $V_{ds}$ and $g_{ds}$ Vs $V_{ds}$ Curves



from the graph  $g_{ds0}\,:g_{ds}$  at  $V_{gs0}$  and  $V_{ds}=0.55\mathrm{V}.$ 

$$g_{ds0} = -30n\Omega^{-1} (23)$$

From the below equation we can calculate  $\lambda$ .

$$I_{ds}\lambda = g_{ds} \tag{24}$$

 $\lambda=0.0315.$ 

Now to find range of  $V_{gs}$  with less than 50 % Error we need to find values in range of  $(g_m/2,3g_m/2)$ .

 $V_{gs} \; \mathrm{range} = (\text{-}452 \mathrm{mV}, \text{-}633 \mathrm{mV})$ 

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