

# Analog Lab (EE2401)

## Experiment 1 : Inverter characteristics

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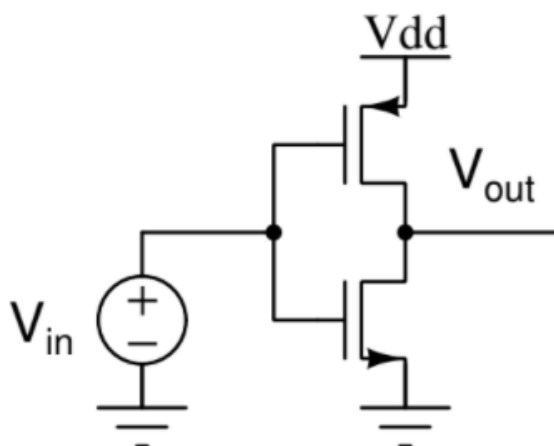
### 1 Aim

our aim here is to understand how an inverter works and understand it's characteristics.

#### Inverter

An inverter does the functions of Not gate i.e. it negates the input.

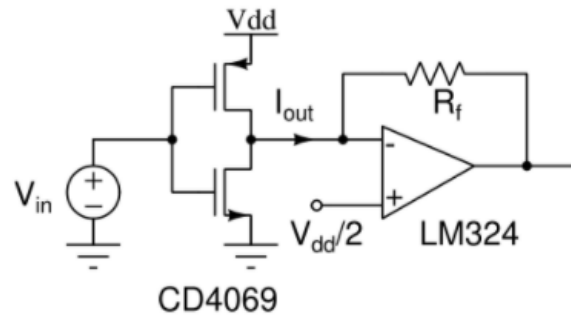
#### CMOS inverter



Inverter using NMOS and PMOS

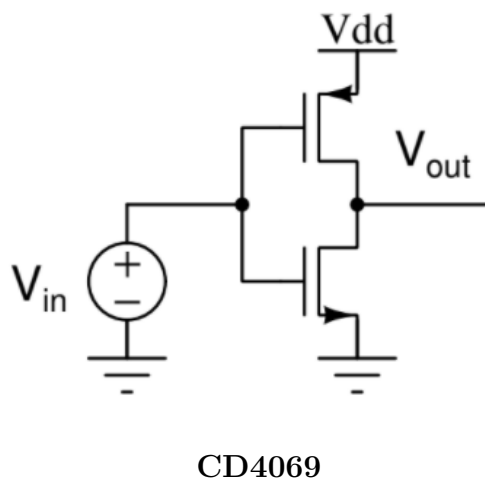
## 2 Problem statement)

1. Determine large-signal  $I_{out}$  vs  $V_{in}$  of a CMOS inverter using the circuit below:

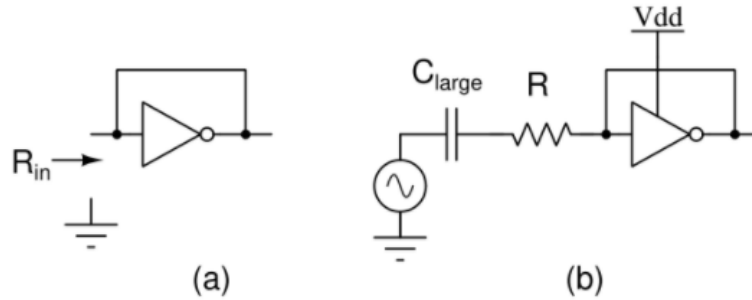


**Figure 1:** Setup to find  $I_{out}$  without using an ammeter.

- . • Sweep  $V_{in}$  from 0V to  $V_{DD}$  (6V).
  - . • What is the self-bias voltage ( $V_B$ ) of the inverter?
  - . • Find the transconductance at  $V_B$ .
  - . • Choose appropriate supply voltages for the opamp.
2. Determine large-signal  $V_{out}$  vs  $V_{in}$  of a CMOS inverter using the circuit below:



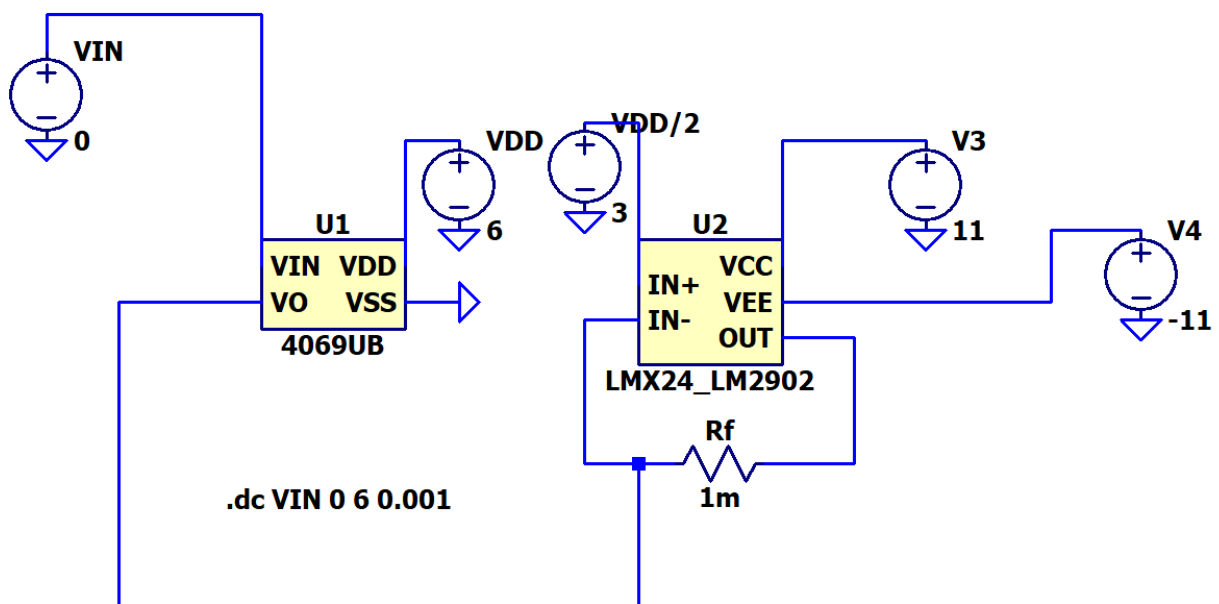
Find small-signal resistance of the self-biased inverter using the circuit shown below for  $V_{DD} = 5V, 6V$  and  $9V$ :



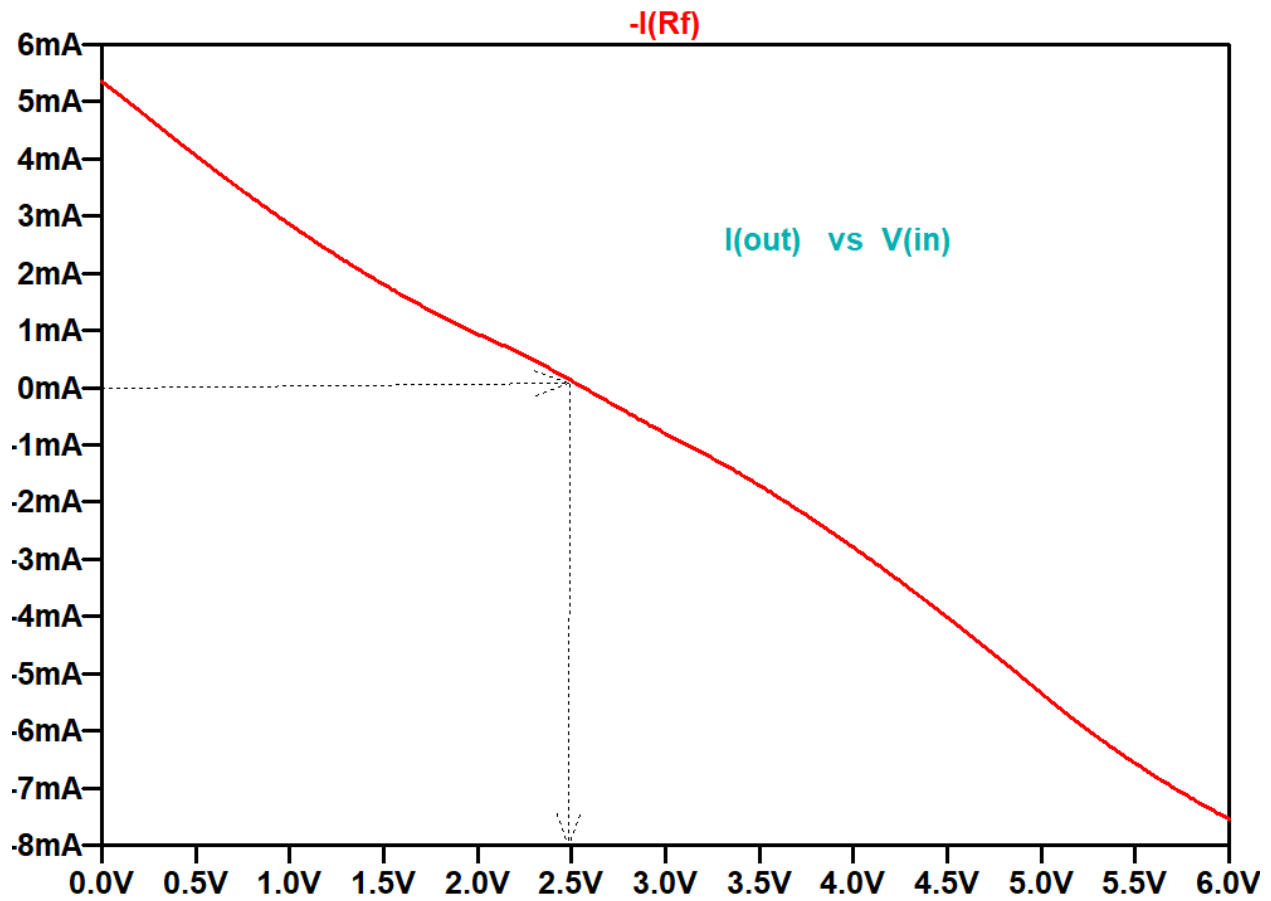
3. Using the data from above two experiments, estimate small-signal  $g_m$  and  $r_o$  of the transconductor. Also find out  $V_T$  and  $\beta$  of the NMOS and PMOS of inverter.

### 3 Results and observations

#### Question 1



## Output plot



Plot: I(out) Vs V(in)

### Self-Bias Voltage :

- Now as we can see  $I_{out} = 0$  A at  $V_{in} = 2.56$  V i.e. let's say it's point A and let's say that the self-bias voltage is  $V_B$ .
- Since we already know that at self-bias the only self-biased inverter circuit has pmos and nmos in saturation region.

$$I_{out} = \beta_p(6 - V_B - |V_{Tp}|)^2 - \beta_n(V_B - |V_{Tn}|)^2 = 0 \quad (1)$$

- Now let's see how the current equations are and what region pmos and nmos are in at point A.

### NMOS

$$V_{gs} = 2.56, V_{ds} = 3 \quad (2)$$

$$V_{ds} \geq V_{gs} - V_{Tn} \quad (3)$$

NMOS is in saturation region.

### PMOS

$$V_{sg} = 3.44, V_{ds} = 3 \quad (4)$$

- $V_{sd} \geq V_{sg} - |V_{Tp}|$  if  $|V_{Tp}| > 0.44V$  (saturation region).
- $V_{sd} \leq V_{sg} - |V_{Tp}|$  if  $|V_{Tp}| < 0.44V$  (linear region)

• Therefore if  $|V_{Tp}|$  is greater than 0.44 V, then both PMOS and NMOS are in saturated region at point A and by comparing current equations we can say  $V_B = 2.56$  V.(self-bias voltage)

• We will verify whether  $|V_{Tp}|$  is greater than 0.44 V at last while doing calculations, if it is not then we will correct the self bias voltage accordingly.

• For now let's assume  $|V_{Tp}|$  is greater than 0.44 V and proceed with  $V_B = 2.56$  V.

### Transconductance at $V_B$

$$Transconductance = \left. \frac{\partial I_{out}}{\partial V_{in}} \right|_{V_{in}=V_B} \quad (5)$$

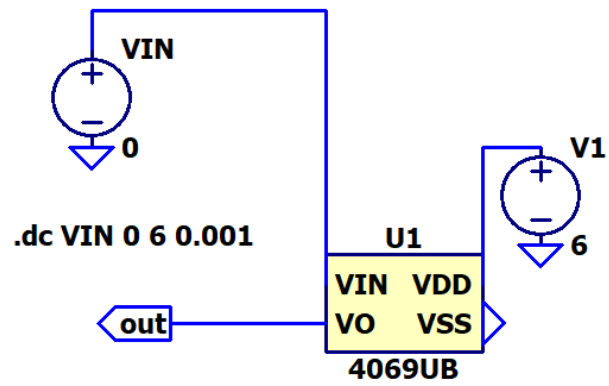
• From the above equation we can clearly say that Transconductance is the slope of  $I_{out}$  Vs  $V_{in}$  at self bias voltage.

$$Transconductance = \left. \frac{\partial I_{out}}{\partial V_{in}} \right|_{V_{in}=2.56V} \quad (6)$$

• Transconductance at  $V_B$  is  $0.00187 \Omega^{-1}$ .

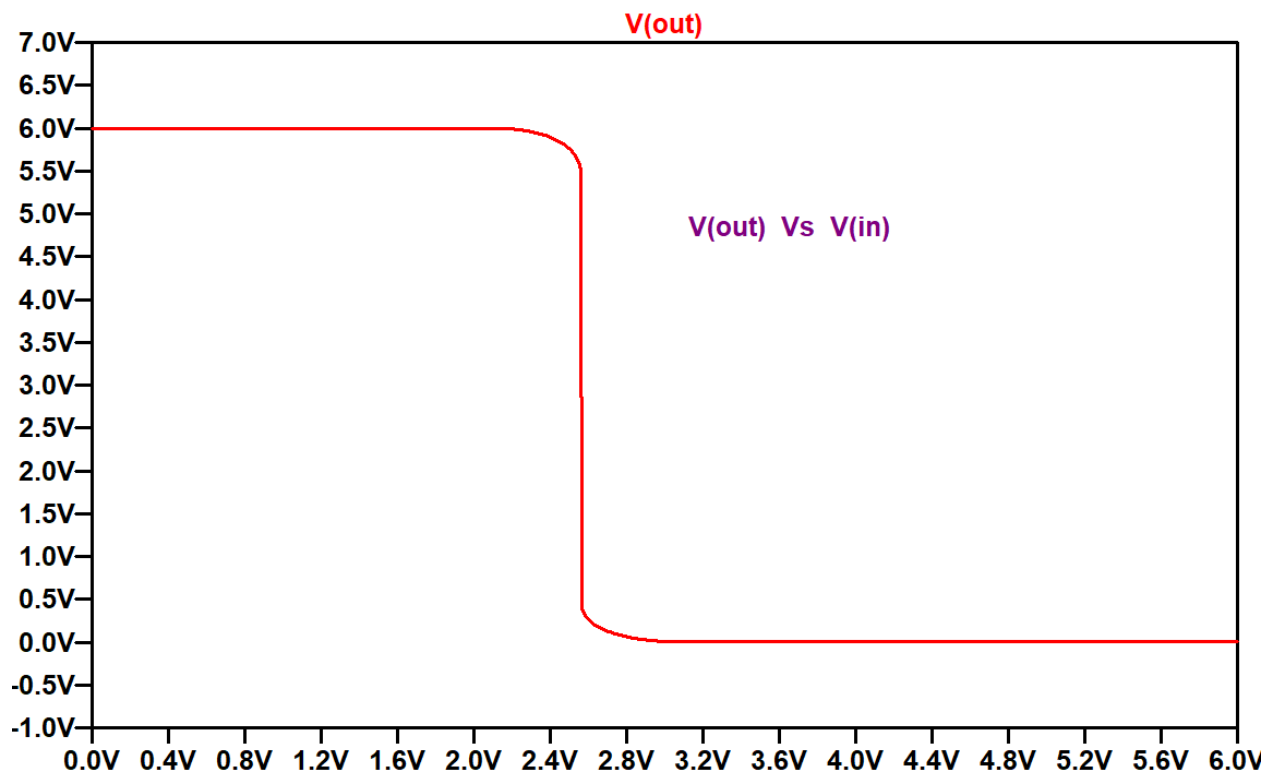
P.T.O

## Question 2



**Inverter**

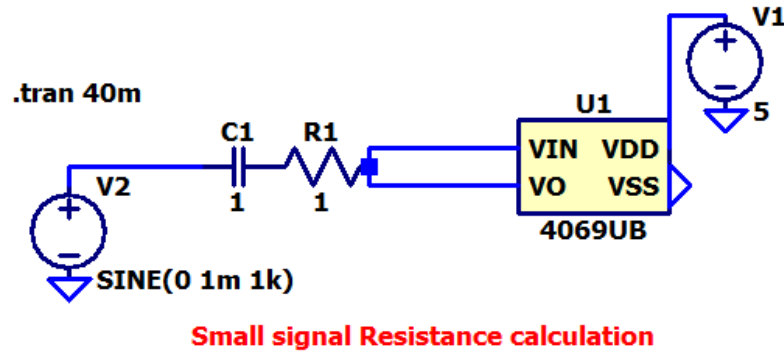
Output plot



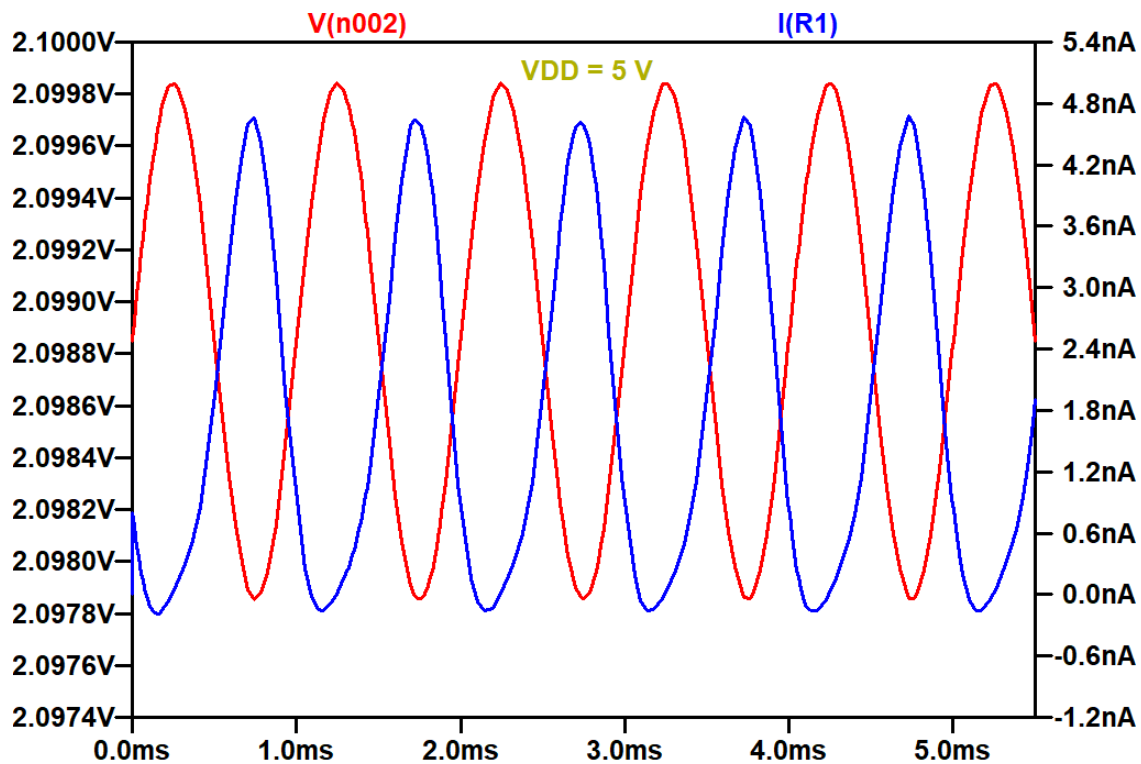
Plot:  $V(out)$  Vs  $V(in)$

- As we can clearly see that the output stays at 6V until  $V_{in}$  is 2.1 V and then starts to decrease slowly in parabolic way until around  $V_{in}$  is 2.56 V and then decreases suddenly with almost  $\infty$  slope around same  $V_B$  and starts to slow down and then becomes 0 V after  $V_{in}$  is 3.1 V.

Question 2(a)



Output plot at  $V_{DD} = 5V$



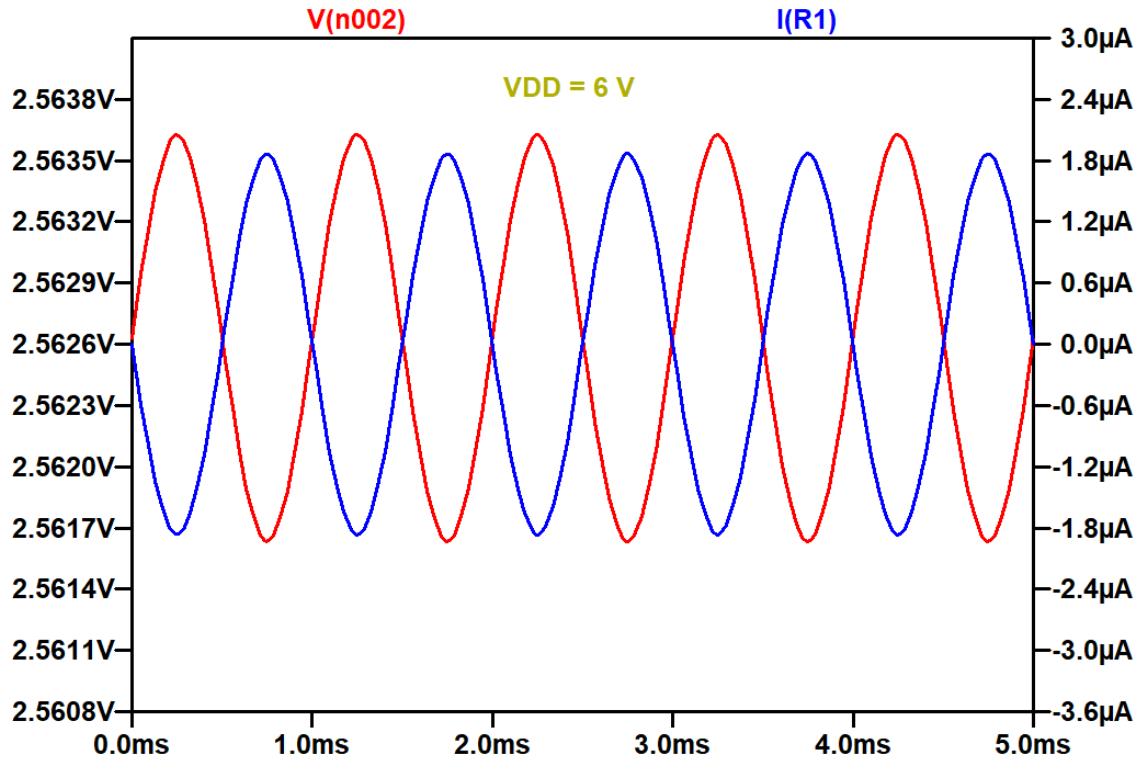
Plot:  $V(o)$ ,  $I(R1)$  Vs time(ms)

Calculating small signal resistance at  $V_{DD} = 5V$

$$\Delta I = 4.5585862 \text{ nA}, \Delta V = 1.9616359 \text{ mV}. \quad (7)$$

$$\text{Small signal resistance}(R_{in}) = \frac{\Delta V}{\Delta I} = 430316.72 \text{ } \Omega \approx 430.3K\Omega \quad (8)$$

Output plot at  $V_{DD} = 6V$



Plot:  $V(o)$ ,  $I(R1)$  Vs time(ms)

Calculating small signal resistance at  $V_{DD} = 6V$

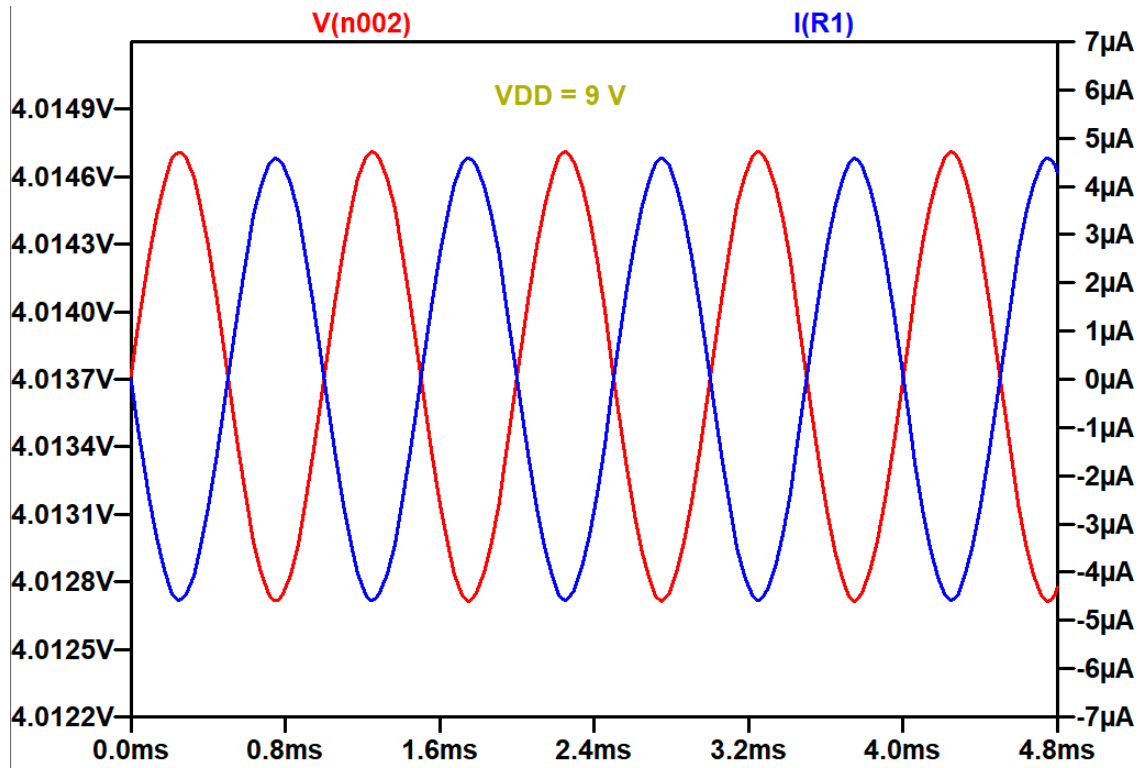
- Similar from the above case but now we have used  $R1 = 1m$ .

$$\Delta I = 3.7244534 \text{ } \mu A, \Delta V = 1.9905448 \text{ mV} \quad (9)$$

$$\text{Small signal resistance}(R_{in}) = \frac{\Delta V}{\Delta I} = 534.45 \text{ } \Omega \quad (10)$$



Output plot at  $V_{DD} = 9V$



Plot:  $V(o)$ ,  $I(R1)$  Vs time(ms)

Calculating small signal resistance at  $V_{DD} = 9V$

- Similar from the above case.

$$\Delta I = 9.1278399 \mu A, \Delta V = 1.9863906 mV \quad (11)$$

$$\text{Small signal resistance}(R_{in}) = \frac{\Delta V}{\Delta I} = 217.61 \Omega \quad (12)$$

- The large differences in small signal resistance when  $V_{DD}=5V$  and  $V_{DD}=6,9V$  can be accounted to the fact that Self bias at  $V_{DD}=5V$  is less than  $V_{Tn}$  i.e. the NMOS and PMOS are not in saturation.

P.T.O

### Question 3

#### Finding $g_m$ , $r_o$ and $V_T$ , $\beta$ of NMOS and PMOS

- From  $V_{out}$  Vs  $V_{in}$  plot, we can say that  $V_{Tn} = 2.1$  V, Since  $V_{out}$  is 6V until 2.1V, i.e. Nmos is in cutoff region when  $0 < V_{in} < V_{Tn}$ .
- Similarly  $6 - |V_{Tp}| = 3.1$  ,i.e.  $V_{Tp} = -2.9$ V because  $V_{out}$  is 0V when  $V_{in}$  is from 3.1V to 6V, i.e. Pmos is in cutoff region when  $6 - |V_{Tp}| < V_{in} < 6$  and therefore our assumption from earlier for finding self-bias is correct and  $V_B = 2.562$  V
- Now to find  $\beta_p$ ,  $\beta_n$ ,  $\lambda_p$  and  $\lambda_n$ , we need to 4 equations which we can extract from 4 data points of the  $I_{out}$  Vs  $V_{in}$  and  $V_{out}$  Vs  $V_{in}$  plots.
- Let's do two cases and compare first when we assume no early effect in mosfets.

#### No early effect

- Assume  $\lambda_p, \lambda_n \approx 0$ .

#### Data point A ( $V_{in} = 0$ V)

From  $I_{out}$  Vs  $V_{in}$ , we get  $I_{out} = 5.3520189$  mA, Since NMOS is in cutoff region and PMOS is in linear region.

$$I_{out} = \beta_p \left( V_{SG} - |V_{Tp}| - \frac{V_{SD}}{2} \right) V_{SD} = 5.3520189 \text{ mA.} \quad (13)$$

- By substituting all values we obtain  $\beta_p = 0.001115$  A/V<sup>2</sup>.

#### Data point B ( $V_{in} = 6$ V)

From  $I_{out}$  Vs  $V_{in}$ ,  $I_{out} = -7.5530359$ mA, Since NMOS is in linear region and PMOS is in cutoff region.

$$I_{out} = -\beta_n \left( V_{GS} - |V_{Tn}| - \frac{V_{DS}}{2} \right) V_{DS} = -7.5530359 \text{ mA.} \quad (14)$$

- By substituting all values we obtain  $\beta_n = 0.00104903276$  A/V<sup>2</sup>.
- Now we take into account the early effect and see how it affects our parameters.

**With early effect**

**Data point A ( $V_{in} = 0V$ )**

- From  $I_{out}$  Vs  $V_{in}$ , we get  $I_{out} = 5.3520189 \text{ mA}$ ,

$$I_{out} = \beta_p \left( V_{SG} - |V_{Tp}| - \frac{V_{SD}}{2} \right) V_{SD} (1 + \lambda_p V_{SD}) = 5.3520189 \text{ mA}. \quad (15)$$

- By substituting all the values we get.

$$I_{out} = 4.8\beta_p(1 + 3\lambda_p) = 5.3520189 \text{ mA}. \quad (16)$$

**Data point B ( $V_{in} = 6V$ )**

- From  $I_{out}$  Vs  $V_{in}$ , we get  $I_{out} = -7.5530359 \text{ mA}$ ,

$$I_{out} = -\beta_n \left( V_{GS} - |V_{Tn}| - \frac{V_{DS}}{2} \right) V_{DS} (1 + \lambda_n V_{DS}) = -7.5530359 \text{ mA}. \quad (17)$$

- By substituting all the values we get.

$$I_{out} = 7.2\beta_n(1 + 3\lambda_n) = 7.5530359 \text{ mA}. \quad (18)$$

**Data point C ( $V_{in} = 2.42V$ )**

- From  $V_{out}$  Vs  $V_{in}$ , we get  $V_{out} = 5.8718 \text{ V}$ . and NMOS is in Saturation region and PMOS is in linear region. Using  $I_p = I_n$ .

$$\beta_p \left( V_{SG} - |V_{Tp}| - \frac{V_{SD}}{2} \right) V_{SD} (1 + \lambda_p V_{SD}) = \frac{\beta_n}{2} \left( V_{GS} - |V_{Tn}| \right)^2 (1 + \lambda_n V_{DS}). \quad (19)$$

- By substituting all the values we get,

$$0.07896\beta_p(1 + 0.1282\lambda_p) = 0.0512\beta_n(1 + 5.8718\lambda_n). \quad (20)$$

### Data point D ( $V_{in} = 2.70V$ )

- From  $V_{out}$  Vs  $V_{in}$ , we get  $V_{out} = 124.74$  mV. and NMOS is in linear region and PMOS is in saturation region. Using  $I_p = I_n$ .

$$\beta_n \left( V_{GS} - |V_{Tn}| - \frac{V_{DS}}{2} \right) V_{DS} (1 + \lambda_n V_{DS}) = \frac{\beta_p}{2} \left( V_{SG} - |V_{Tp}| \right)^2 (1 + \lambda_p V_{SD}). \quad (21)$$

- By substituting all the values we get,

$$0.0007476\beta_n(1 + 0.0012474\lambda_n) = 0.08\beta_p(1 + 5.9987526\lambda_p). \quad (22)$$

- Now solving all the 4 equations (16),(18),(20),(22) we get

$$\begin{aligned} \beta_p &= 0.00224347, \\ \beta_n &= -0.00139172, \\ \lambda_p &= -0.167667, \\ \lambda_n &= -0.584588. \end{aligned}$$

- As we can see the results obtained doesn't match with expectations and from the netlist data sheet we can see that  $\lambda_n$  and  $\lambda_p$  is given as 1.87m.

- Therefore let's use  $\beta_p$  and  $\beta_n$  obtained from case 1 without early effect and  $\lambda_n$  and  $\lambda_p$  from datasheet to find  $g_m$ ,  $r_o$ .

**$g_m$  and  $r_o$  at self-bias**

$$g_m = g_{mn} + g_{mp} = \beta_n(V_{GS} - V_{Tn}) + \beta_p(V_{SG} - |V_{Tp}|) = 0.0010845A/V. \quad (23)$$

$$r_o = (r_{no}/r_{po}) = \frac{1}{(\lambda_p + \lambda_n)I_{DS}} = 2409168.86\Omega \approx 2.409M\Omega \quad (24)$$

## 4 Unusual behaviour comments

- The small signal resistance of the self-biased inverter at  $V_{DD} = 5V$  is quite high which can be because  $V(\text{self-bias}) < |V_{Tp}|$ .
- We have seen the unusual values of parameters obtained when early effect is taken into consideration.
- We can also see that  $r_o$  value is quite high.

Thank  
you