

COSI 167A

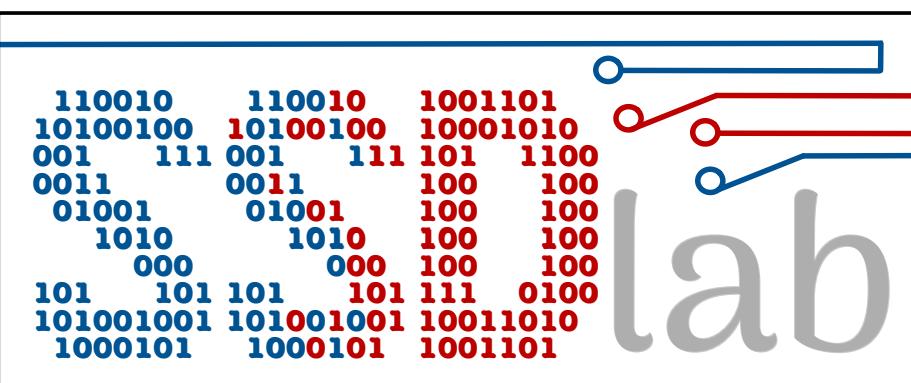
Advanced Data Systems

Class 7

Class Projects

Prof. Subhadeep Sarkar

<https://ssd-brandeis.github.io/COSI-167A/>



Class logistics

and administrivia

The third technical question is now available on the class website
(due before the class on **Tue, Sep 24**).

Project 1 is due in **~12 hours**.

First guest lecture: next Tuesday (**Sep 24**).

Register for paper presentation! (<https://shorturl.at/4P0IT>)

Paper presentation

and discussion

Register for paper presentation! (<https://shorturl.at/4POIT>)

Brandeis

HOME

SCHEDULE

PROJECTS

PRESENTATION

RESOURCES

POLICIES

Advanced Data Systems
COSI 167A

SYLLABUS

GRADESCOPE

MOODLE

Paper presentation

and discussion

Register for paper presentation! <https://shorturl.at/4POIT>

HOME

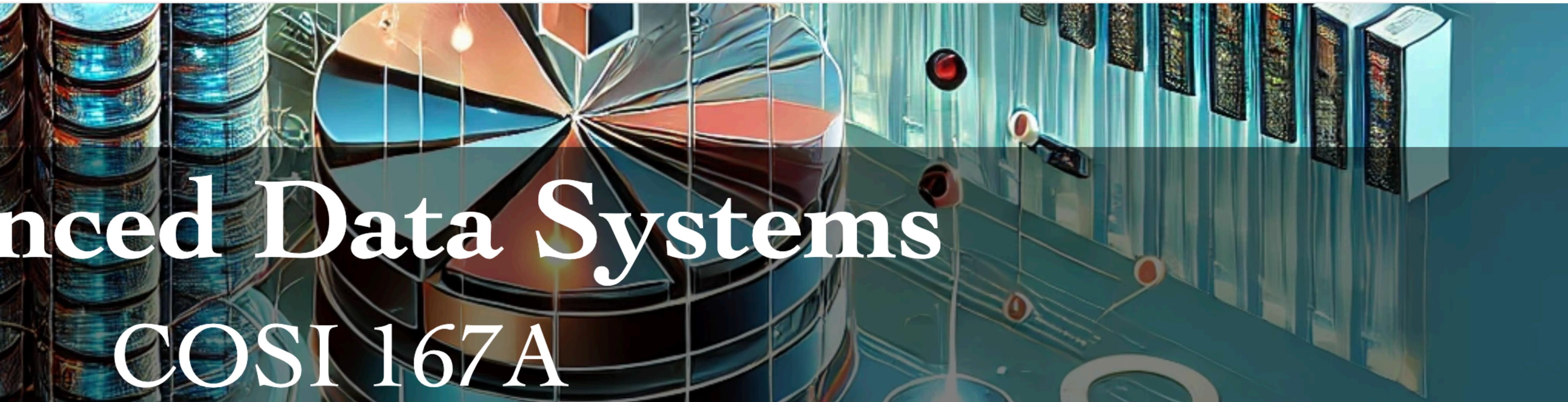
SCHEDULE

PROJECTS

PRESENTATION

RESOURCES

POLICIES



nced Data Systems

COSI 167A

Paper presentation

and discussion

Register for paper presentation! (<https://shorturl.at/4POIT>)

2 students will be responsible for presenting the paper
learn the art of technical presentation, think as: **visualizing a review**

prepare slides **at least a week before** your presentation
get your **slides reviewed** by me twice before your final presentation

Pro tip: Start **EARLY!**

Today in COSI 167A

What's on the cards?

Cost analysis

Class projects!

Cost analysis

Counting all I/Os

Ingestion cost

expected #I/Os performed to write a single entry to **disk**

note: if an entry is written **multiple times**, **count all I/Os**

Query cost

expected #I/Os performed to perform a single query

compare costs with and without **auxiliary (helper) data structures**

P : pages in buffer
 B : entries/page
 L : #levels
 T : size ratio

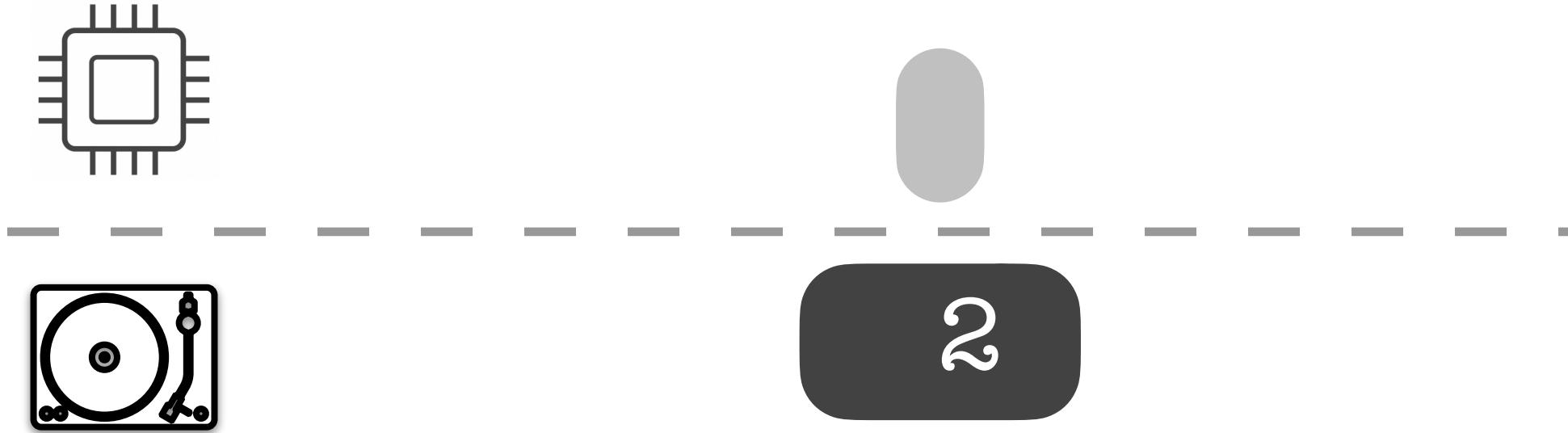


P : pages in buffer
 B : entries/page
 L : #levels
 T : size ratio
 N : #entries in tree

Ingestion cost

Inserts and updates

leveled LSM-tree



in general, #times an entry is written to a level = \mathbf{T}

happens for all \mathbf{L} levels on disk

Total #times an entry is written in the tree = $\mathbf{L} \cdot \mathbf{T}$

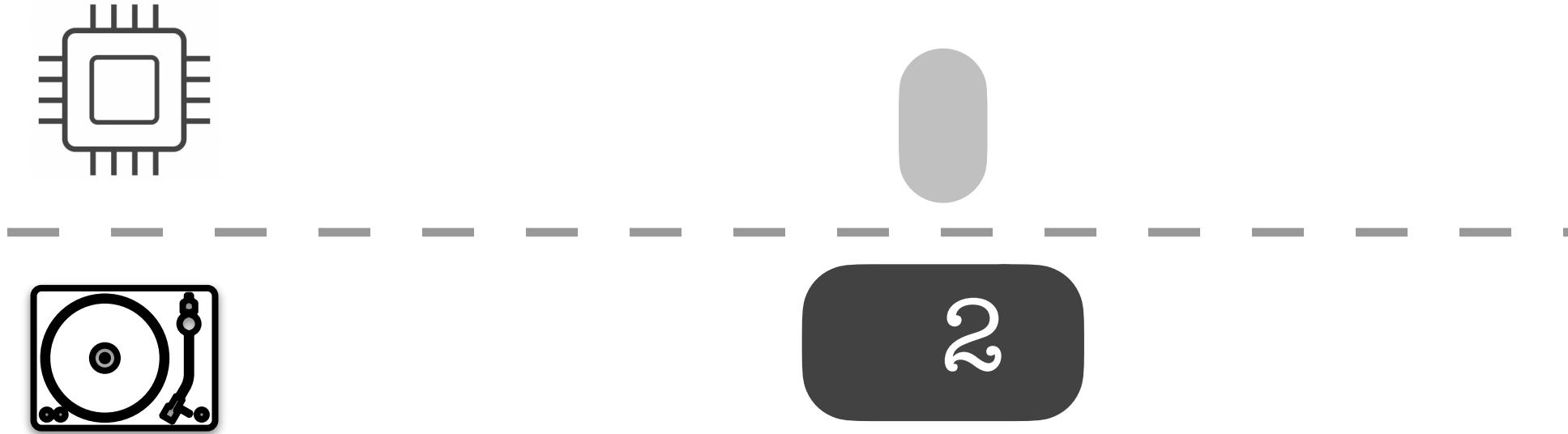
B entries are written to disk per I/O

P : pages in buffer
 B : entries/page
 L : #levels
 T : size ratio
 N : #entries in tree

Ingestion cost

Inserts and updates

leveled LSM-tree



in general, #times an entry is written to a level = \mathbf{T}

happens for all \mathbf{L} levels on disk

Total #times an entry is written in the tree = $\mathbf{L} \cdot \mathbf{T}$

B entries are written to disk per I/O

Average number of I/Os to write a single entry = $\mathbf{L} \cdot \mathbf{T} / \mathbf{B}$

Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost | range lookup cost |
|------------------|--------------------|-------------------|-------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | | |
| Tiered LSM-tree | | | |
| B+-tree | | | |
| Sorted array | | | |
| Log | | | |

Cost analysis

Counting all I/Os

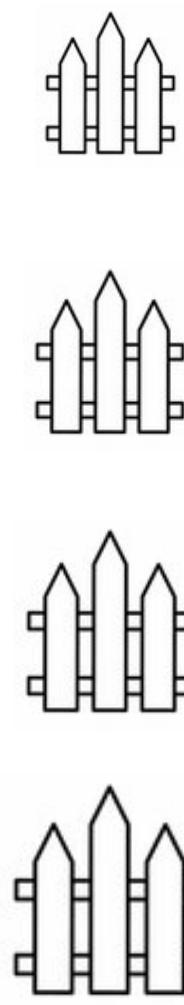
| data structure | ingestion cost | point lookup cost | range lookup cost |
|-------------------------|--------------------|-------------------|-------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | | |
| Tiered LSM-tree | $O(L / B)$ | | |
| B+-tree | | | |
| Sorted array | | | |
| Log | | | |

Point lookup cost

Looking for a specific key



leveled LSM-tree



**fence
pointers**

(page-wise zone map)

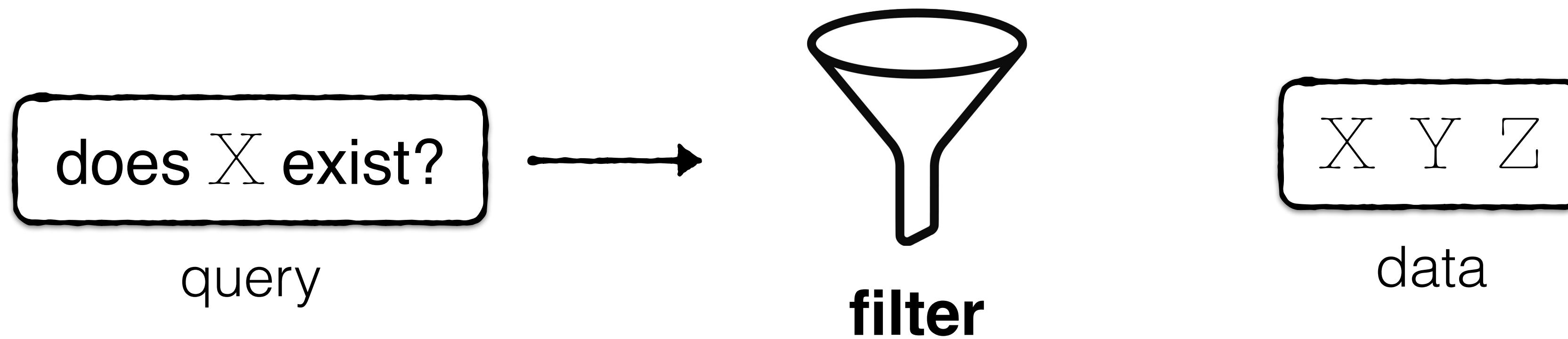


filter

What is a **filter**?

Answers membership queries

answers
membership queries



**no false
negatives**



**false positives with
tunable probability**

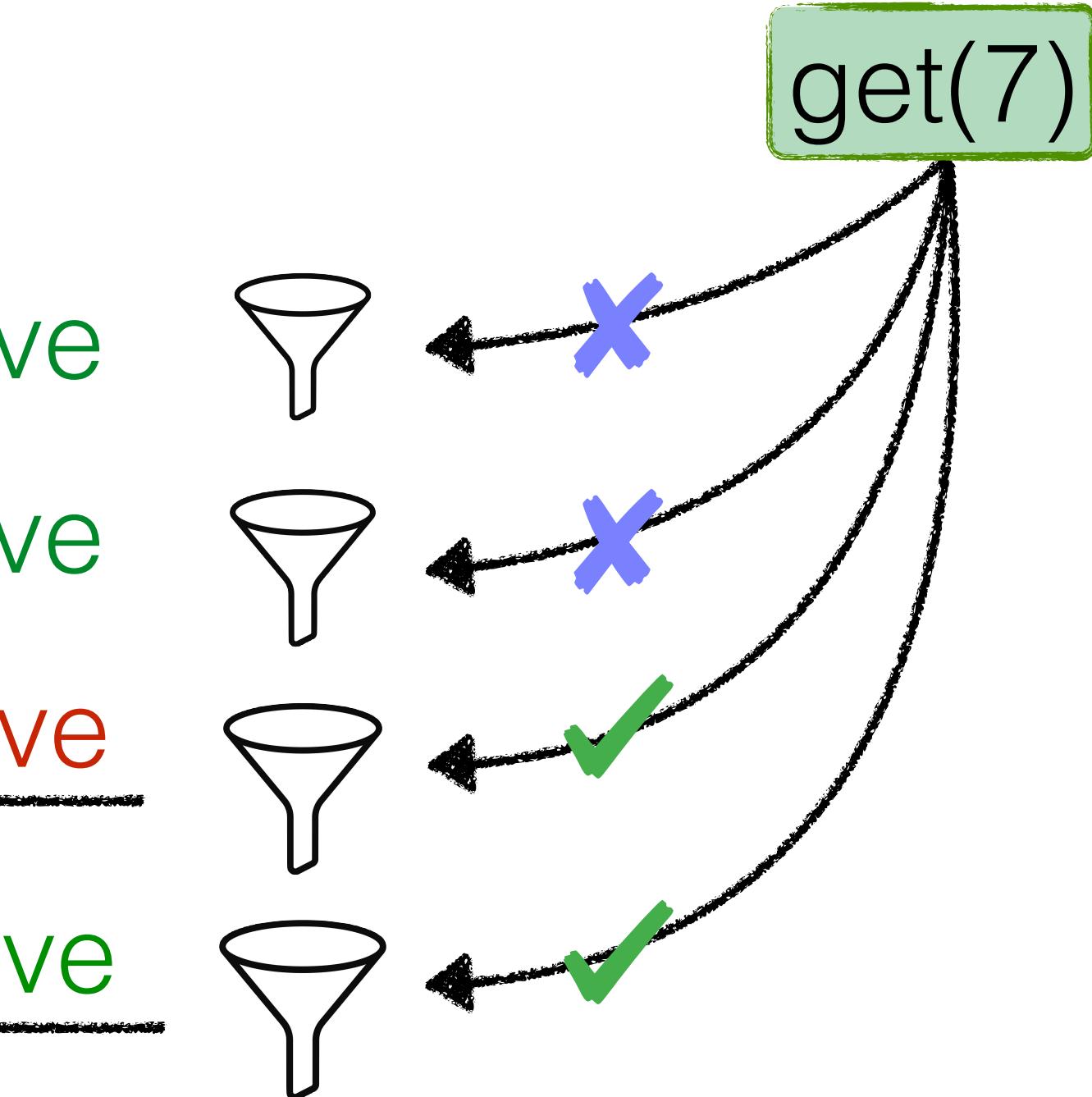
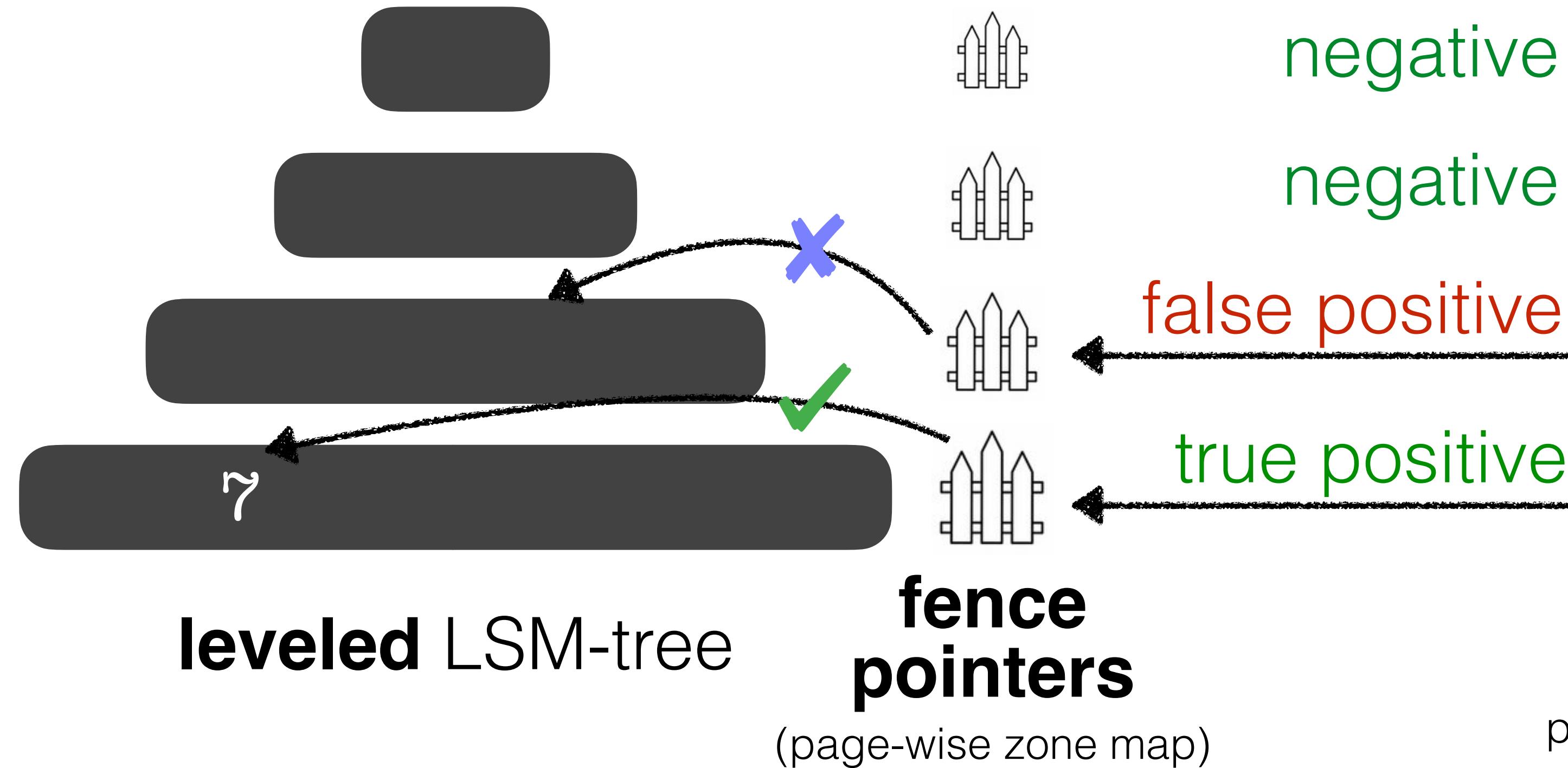


P : pages in buffer
 B : entries/page
 L : #levels
 T : size ratio
 N : #entries in tree

Point lookup cost

Looking for a specific key

ϕ = false positive rate of the filter



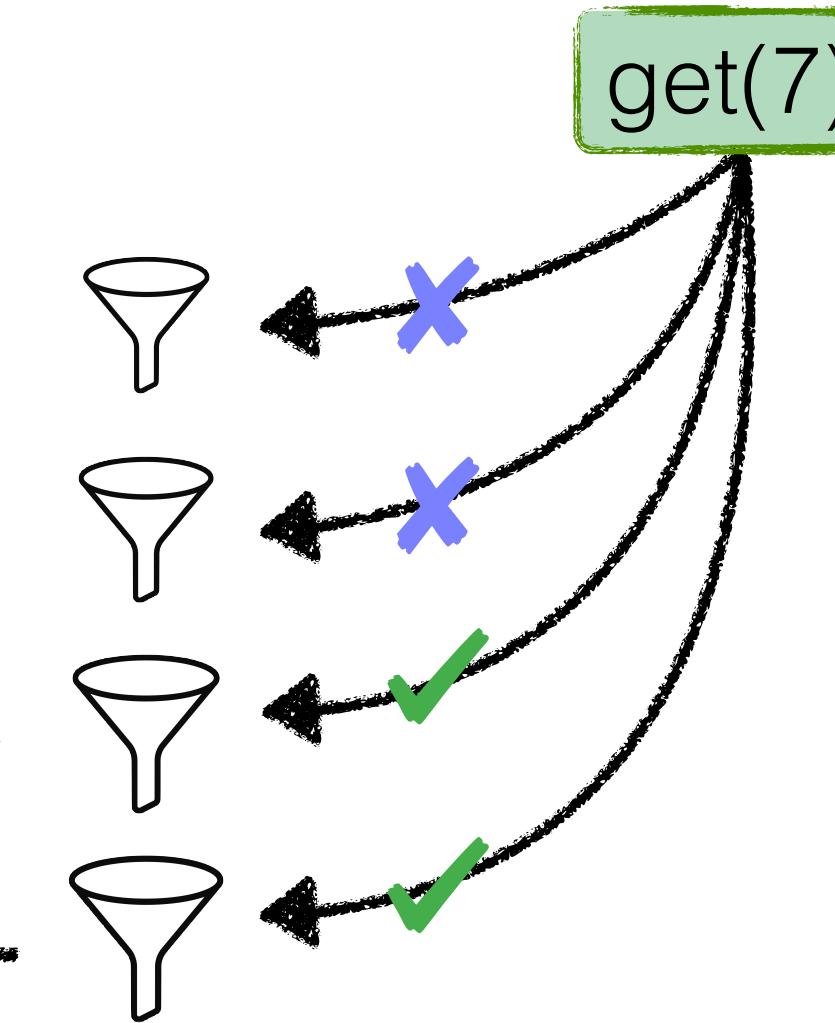
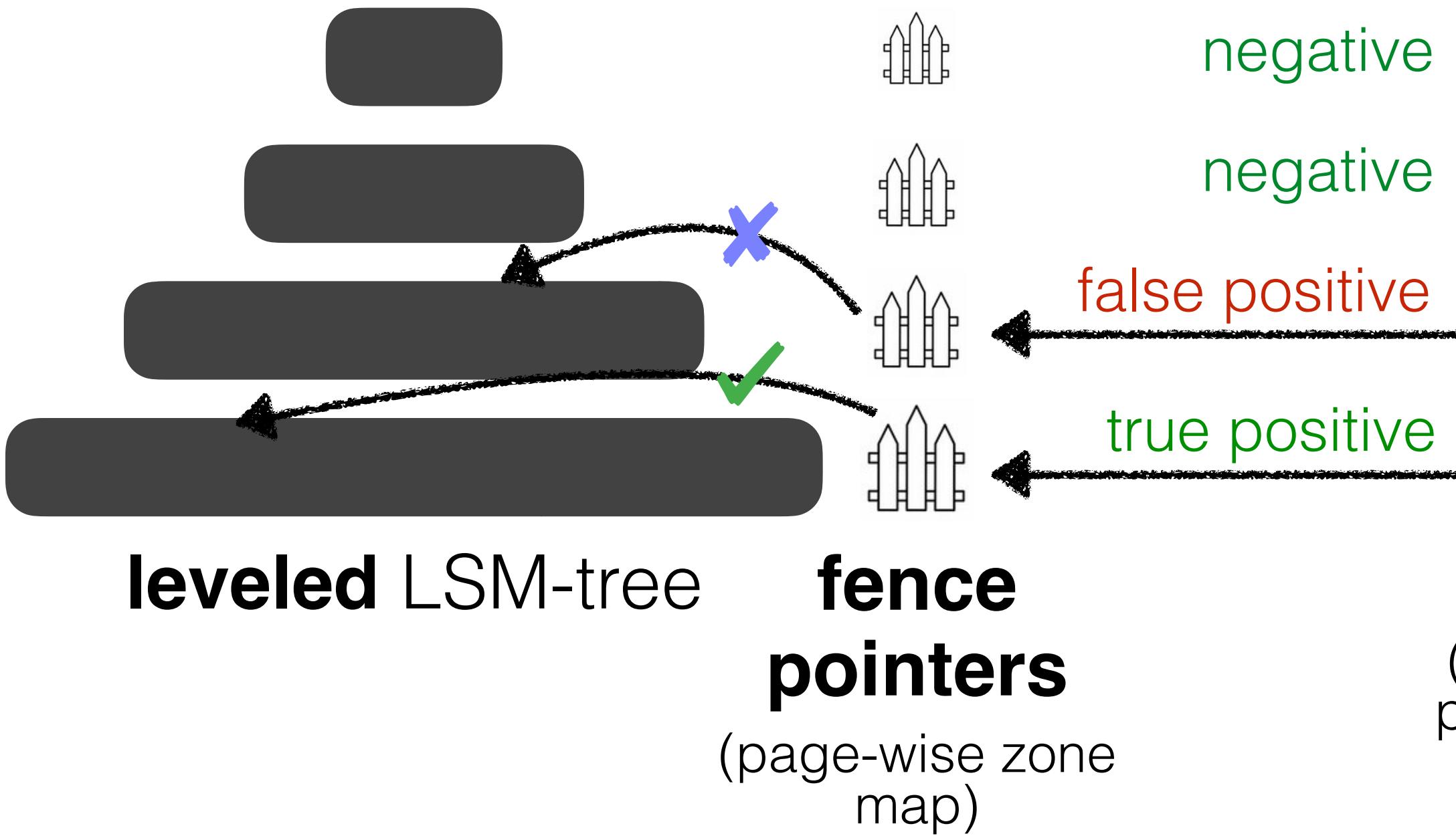
filter
(one filter per sorted run)

P : pages in buffer
 B : entries/page
 L : #levels
 T : size ratio
 N : #entries in tree

Point lookup cost

Looking for a specific key

ϕ = false positive rate of the filter



1 I/O for the sorted run (level) containing the data

+

1 I/O with probability ϕ for all other sorted runs

1 sorted runs per level

Cost of non-empty point lookup

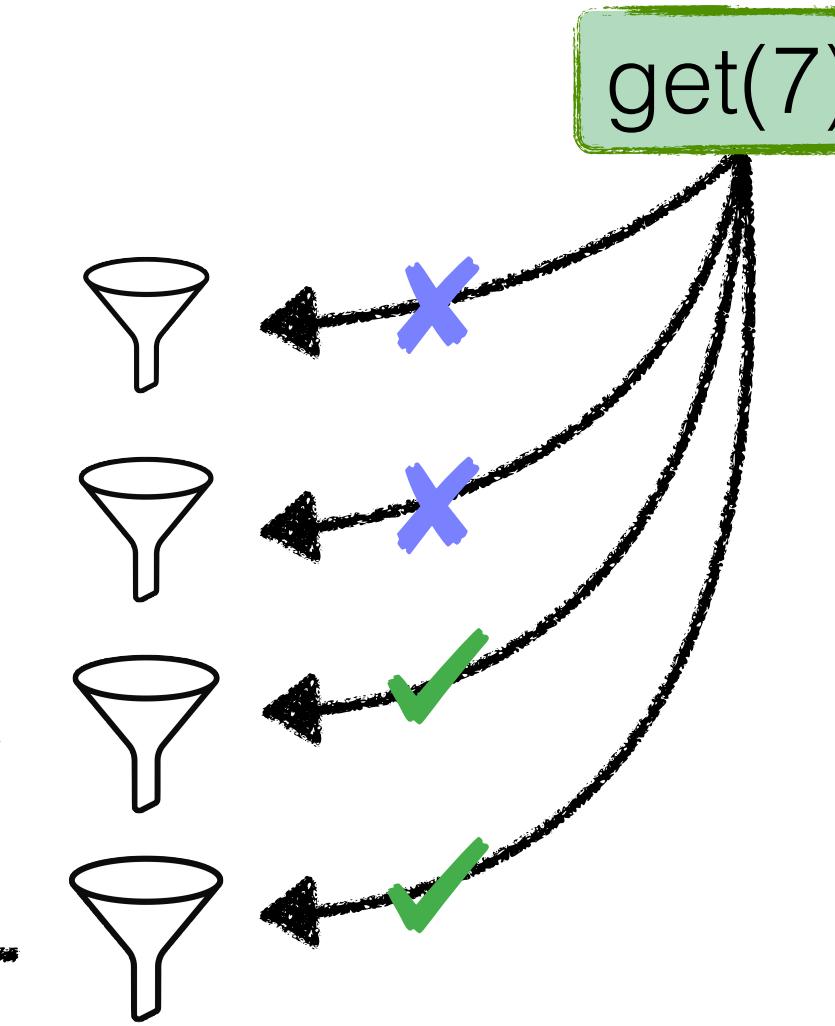
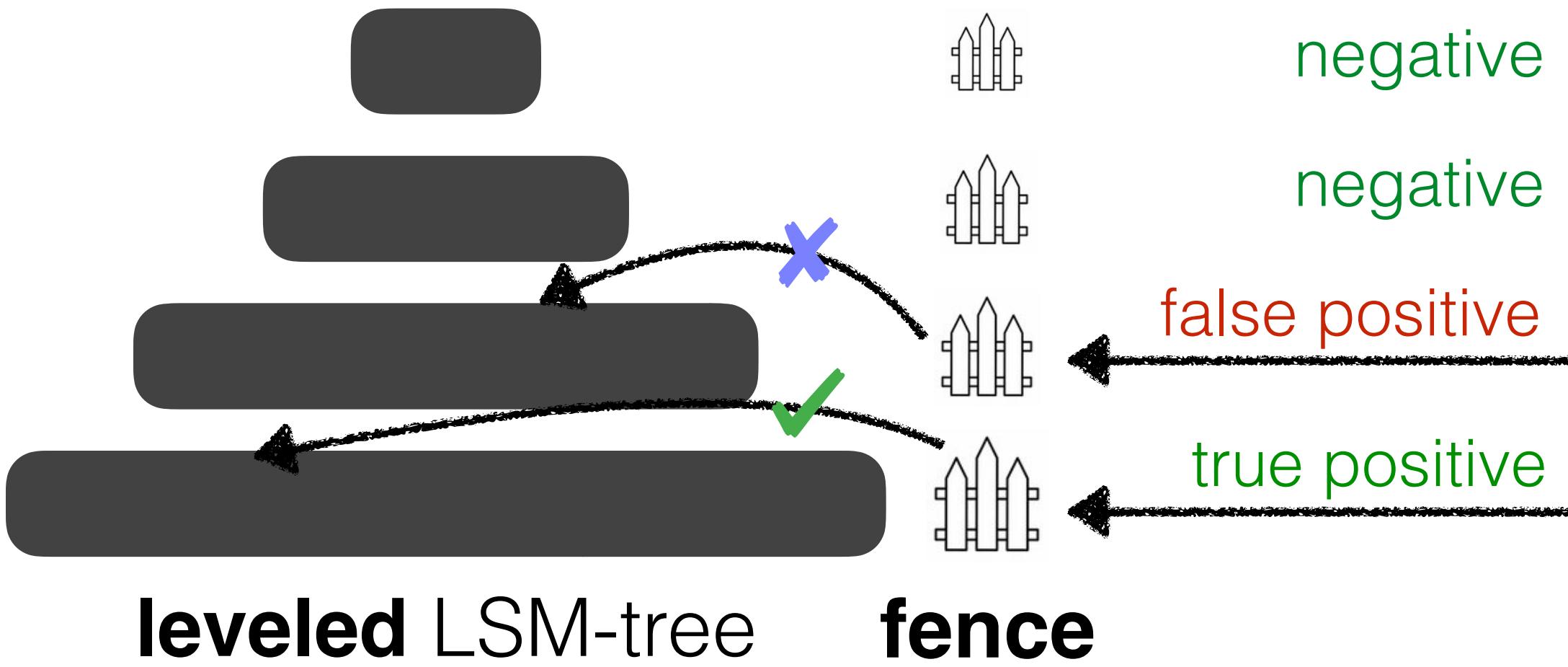
$$= 1 + \phi \cdot (L-1)$$

P : pages in buffer
 B : entries/page
 L : #levels
 T : size ratio
 N : #entries in tree

Point lookup cost

Looking for a specific key

ϕ = false positive rate of the filter



1 I/O for the sorted run (level)
containing the data

+

1 I/O with probability ϕ for
all other sorted runs

1 sorted runs per level

filter
(one filter
per sorted
run)

Cost of non-empty point lookup

$$= 1 + \phi \cdot (L-1)$$

Cost of empty point lookup = $\phi \cdot L$

Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost* | range lookup cost |
|------------------|--------------------|-----------------------|-------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)$ | |
| Tiered LSM-tree | $O(L / B)$ | | |
| B+-tree | | | |
| Sorted array | | | |
| Log | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “1 +” to get cost of empty lookups)

Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost* | range lookup cost |
|------------------|--------------------|-------------------------------|-------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)$ | |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)$ | |
| B+-tree | | | |
| Sorted array | | | |
| Log | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “1 +” to get cost of empty lookups)

Cost analysis

Counting all I/Os

$\phi = 0.008$ with 10 BPK

| data structure | ingestion cost | point lookup cost* | range lookup cost |
|------------------|--------------------|-------------------------------|-------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)$ | |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)$ | |
| B+-tree | | | |
| Sorted array | | | |
| Log | | | |

Monkey takes this **another step further!**

Cost analysis

Counting all I/Os

$\phi = 0.008$ with 10 BPK

| data structure | ingestion cost | point lookup cost* | range lookup cost |
|------------------|--------------------|---------------------------------|-------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | |
| B+-tree | | | |
| Sorted array | | | |
| Log | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)



Brandeis
UNIVERSITY



Monkey shaves off the “L” factor from the cost

Range lookup cost

Looking for keys in a range

P : pages in buffer

B : entries/page

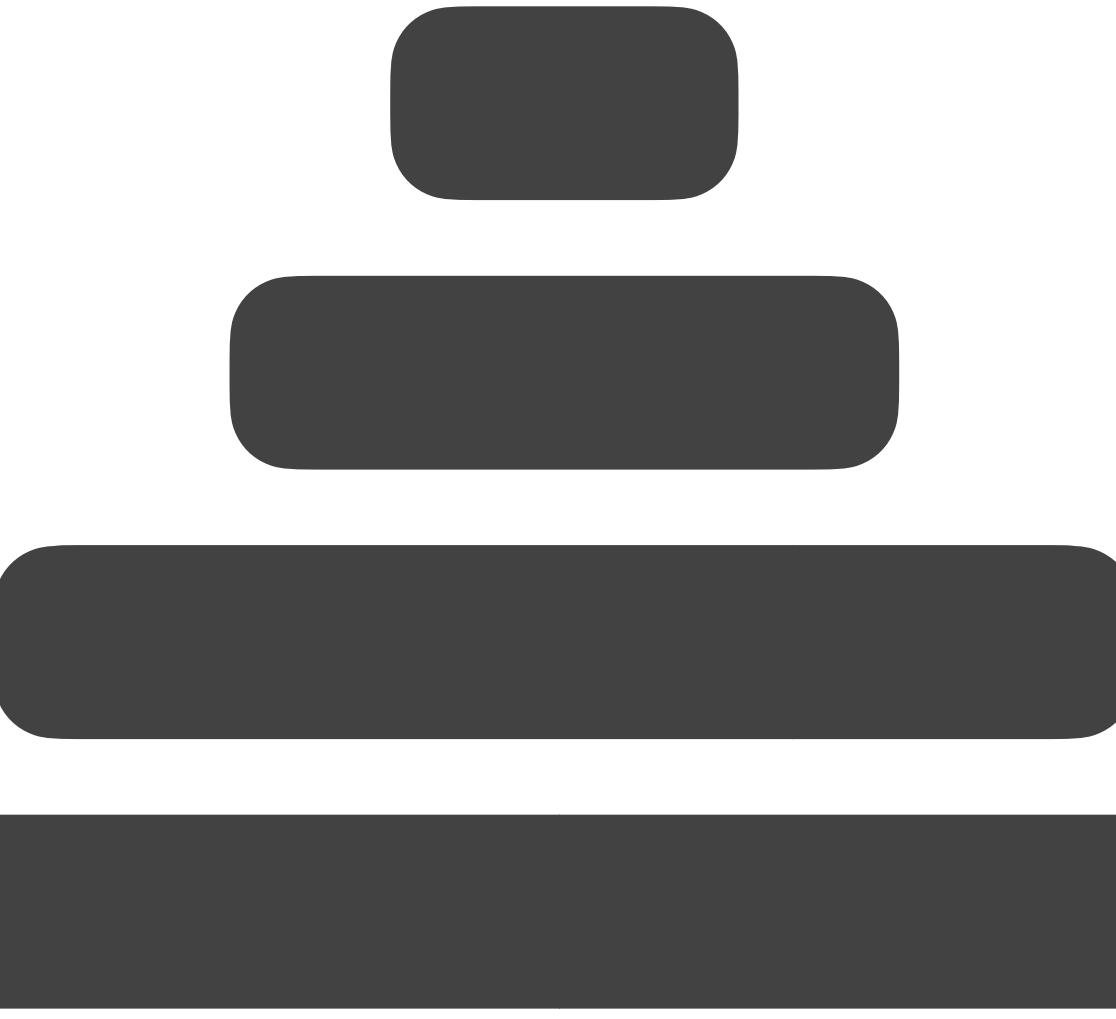
L : #levels

T : size ratio

N : #entries in tree

Range lookup cost

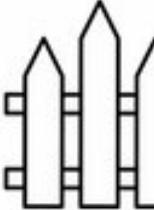
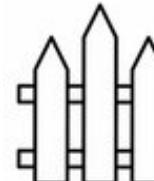
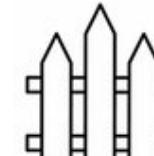
Looking for keys in a range



leveled LSM-tree

**fence
pointers**

(page-wise zone map)

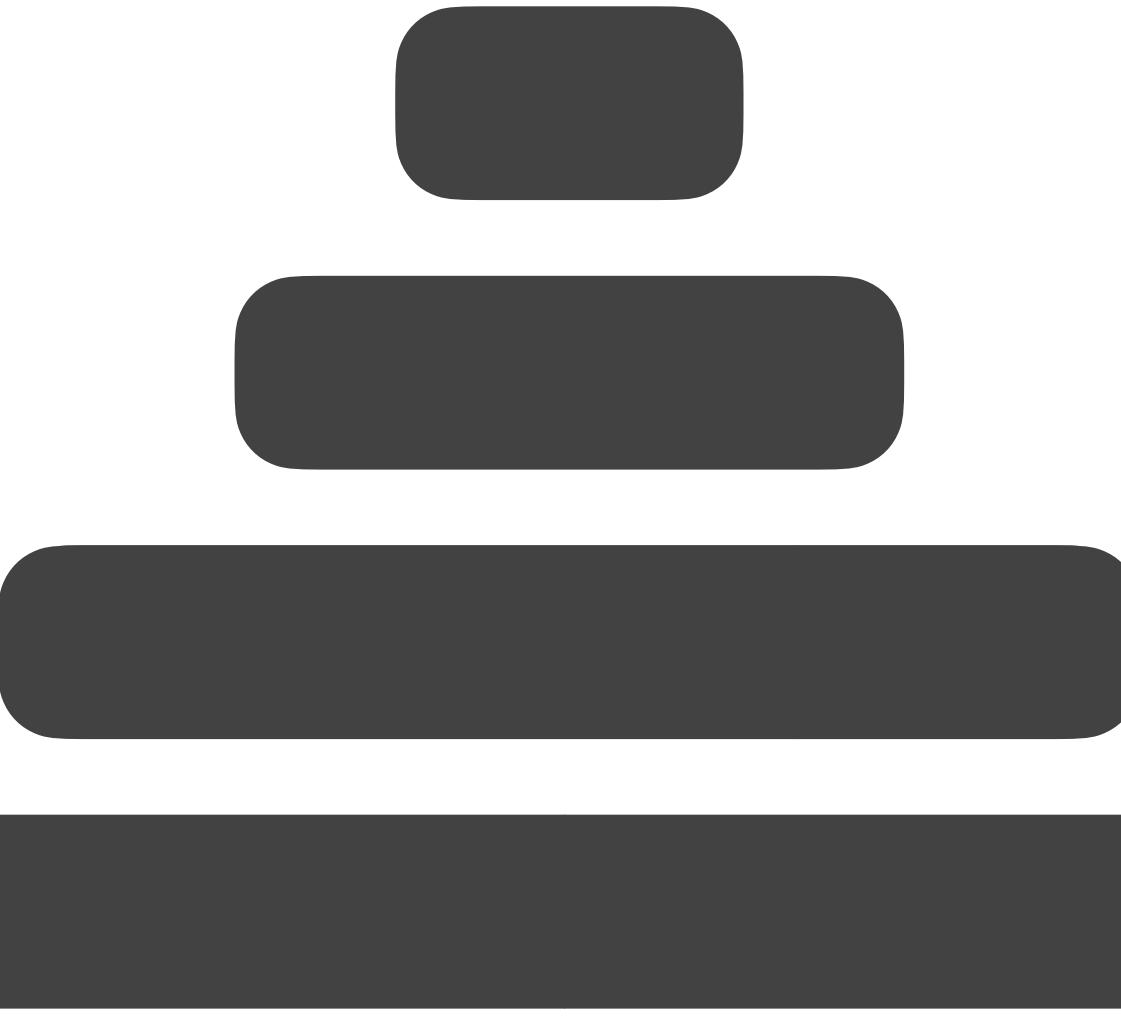


filter

P : pages in buffer
 B : entries/page
 L : #levels
 T : size ratio
 N : #entries in tree

Range lookup cost

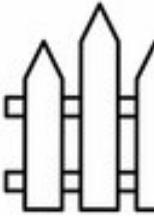
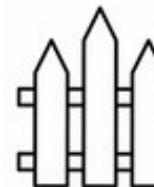
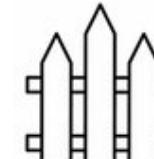
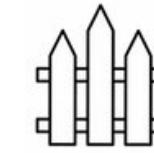
Looking for keys in a range



leveled LSM-tree

**fence
pointers**

(page-wise zone map)



filter

P : pages in buffer

B : entries/page

L : #levels

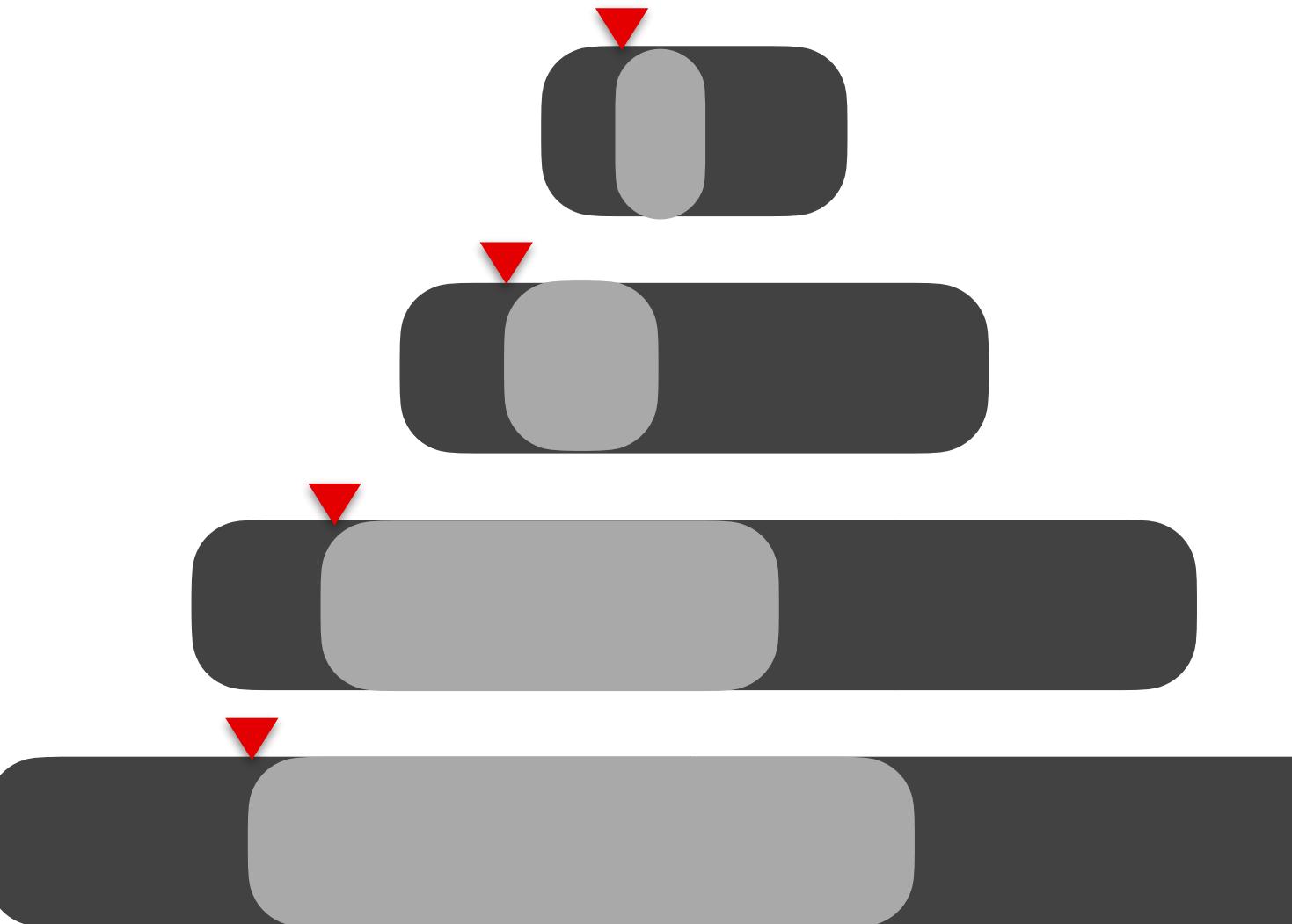
T : size ratio

N : #entries in tree

Range lookup cost

Looking for keys in a range

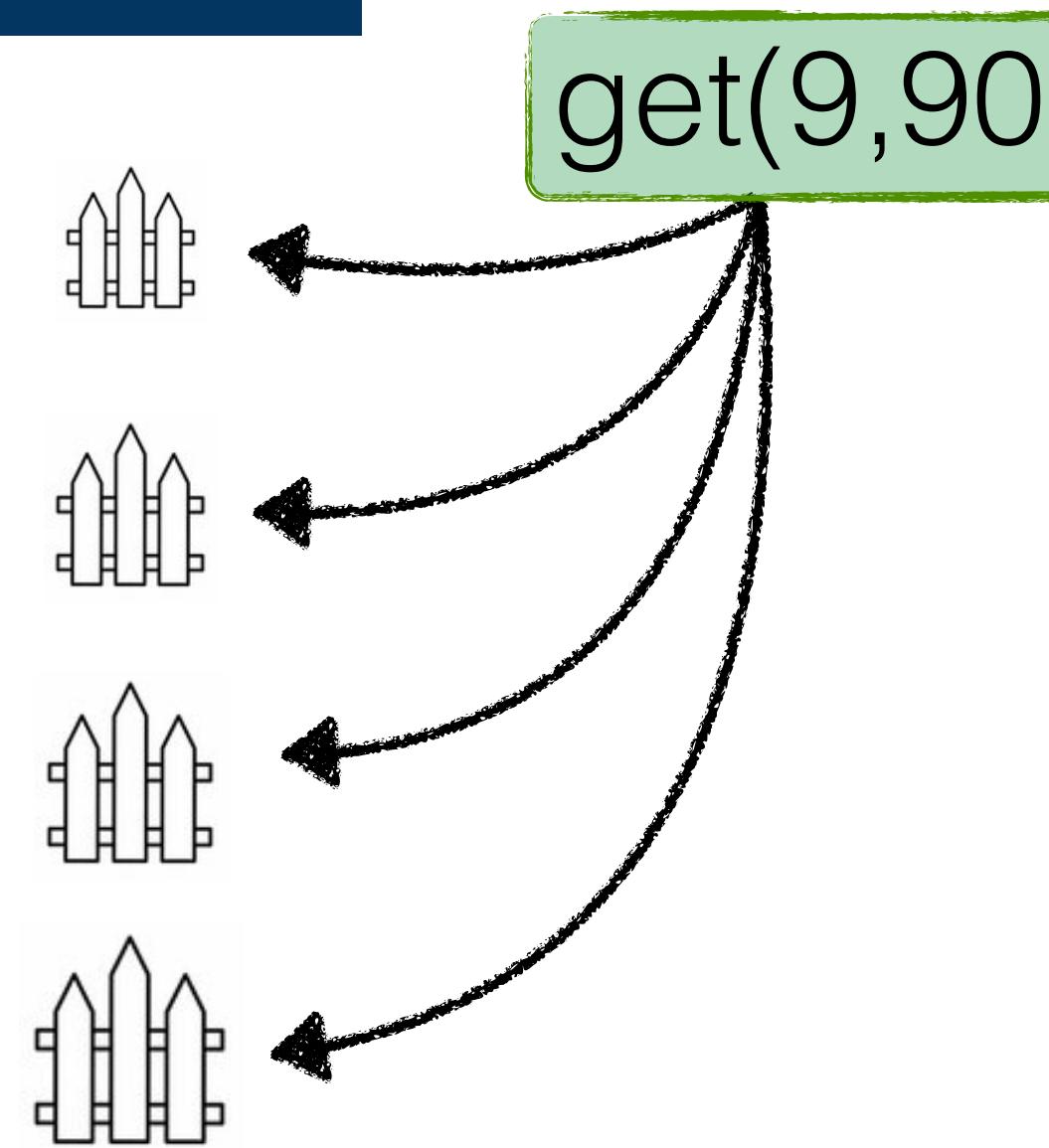
s = **selectivity** of the range query



leveled LSM-tree

**fence
pointers**

(page-wise zone map)



Brandeis
UNIVERSITY

P : pages in buffer

B : entries/page

L : #levels

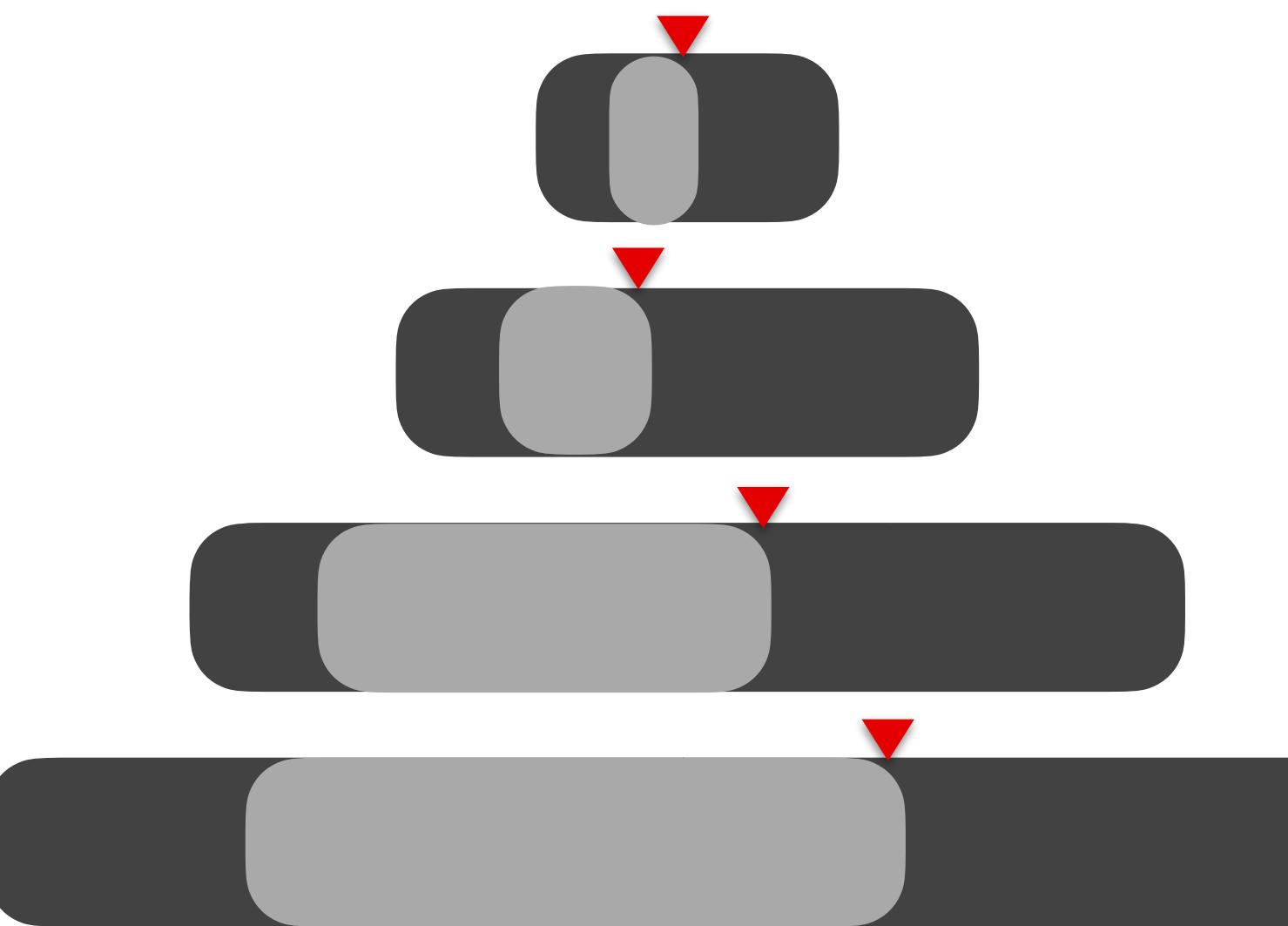
T : size ratio

N : #entries in tree

Range lookup cost

Looking for keys in a range

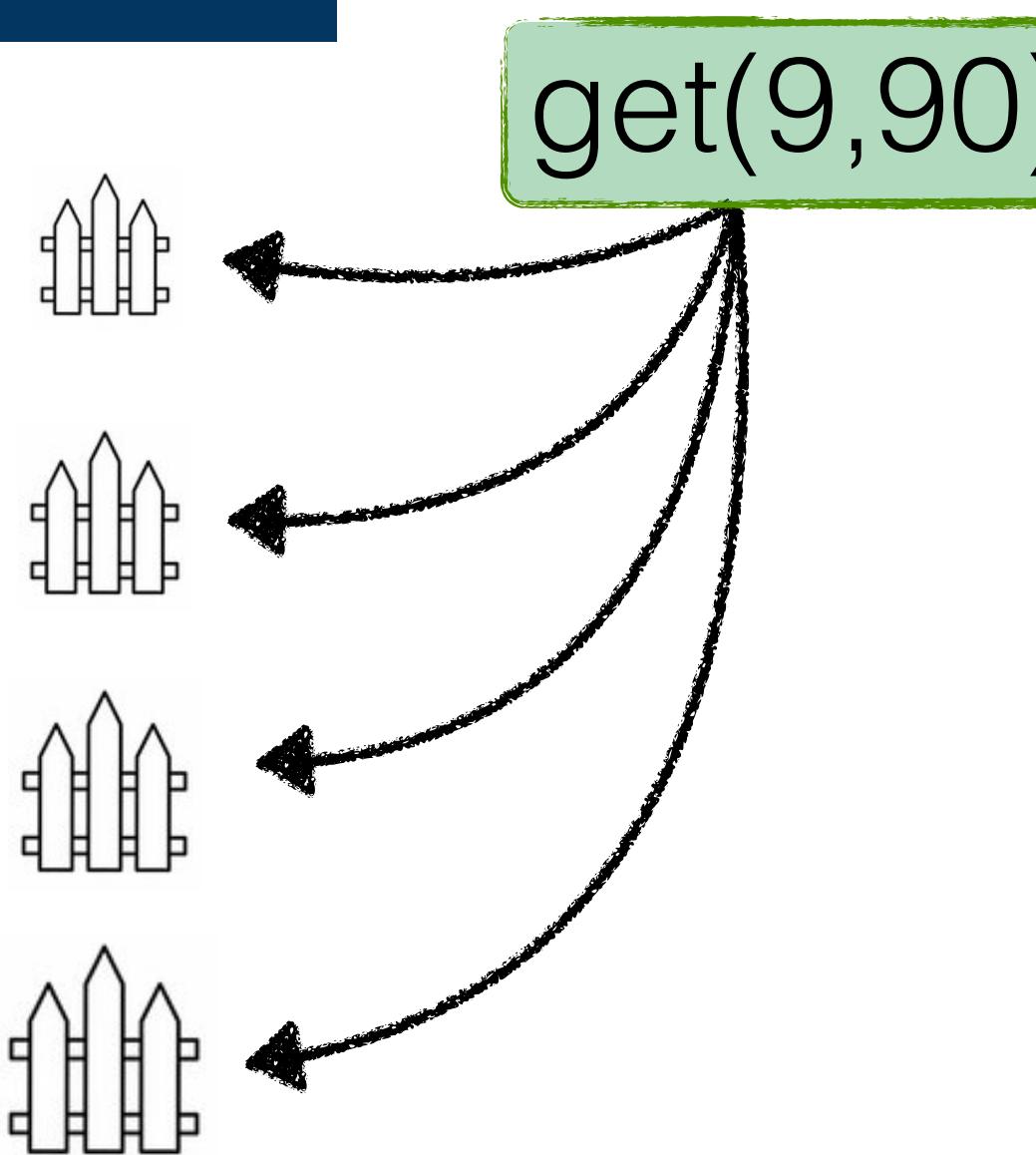
$s = \text{selectivity}$ of the range query



leveled LSM-tree

**fence
pointers**

(page-wise zone map)



total entries in tree = N

#entries per page = B

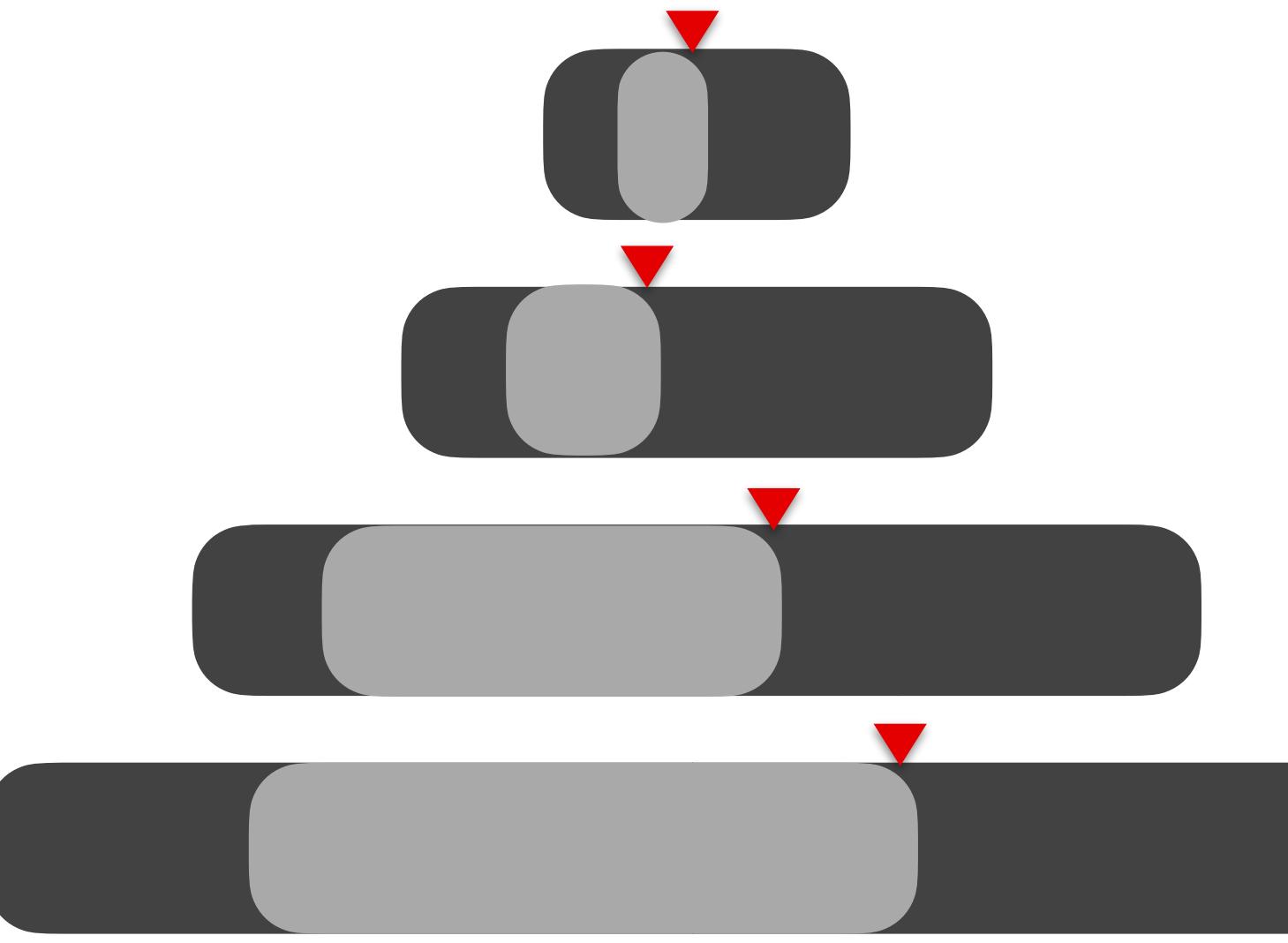
#pages in tree = N/B

P : pages in buffer
 B : entries/page
 L : #levels
 T : size ratio
 N : #entries in tree

Range lookup cost

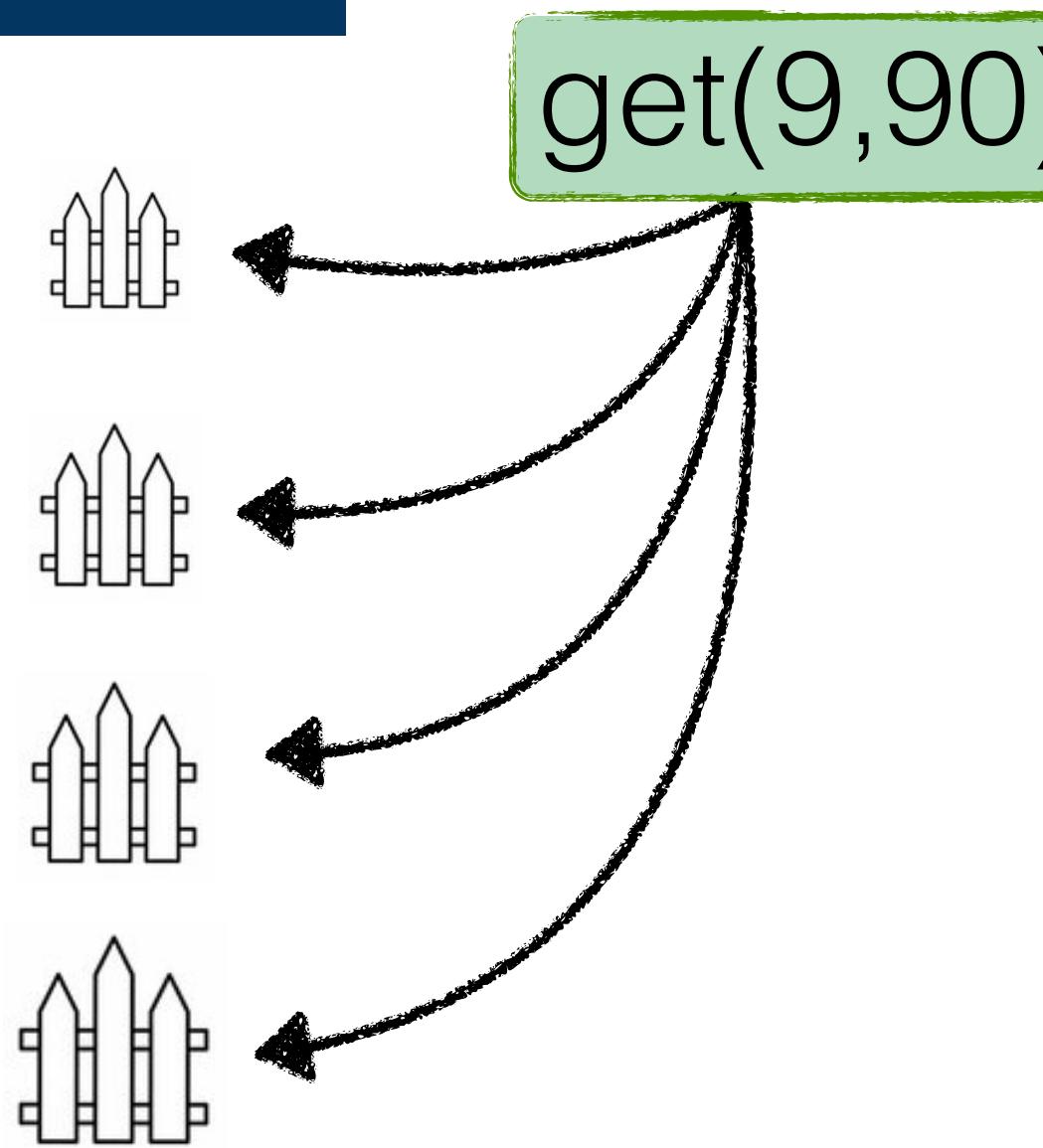
Looking for keys in a range

$s = \text{selectivity}$ of the range query



**fence
pointers**

(page-wise zone map)



total entries in tree = N

#entries per page = B

#pages in tree = N/B

Cost of range lookup = $s \cdot N/B$

What about the **range query cost** in a **tiered LSM-tree**?

same cost for
leveled & tiered LSM

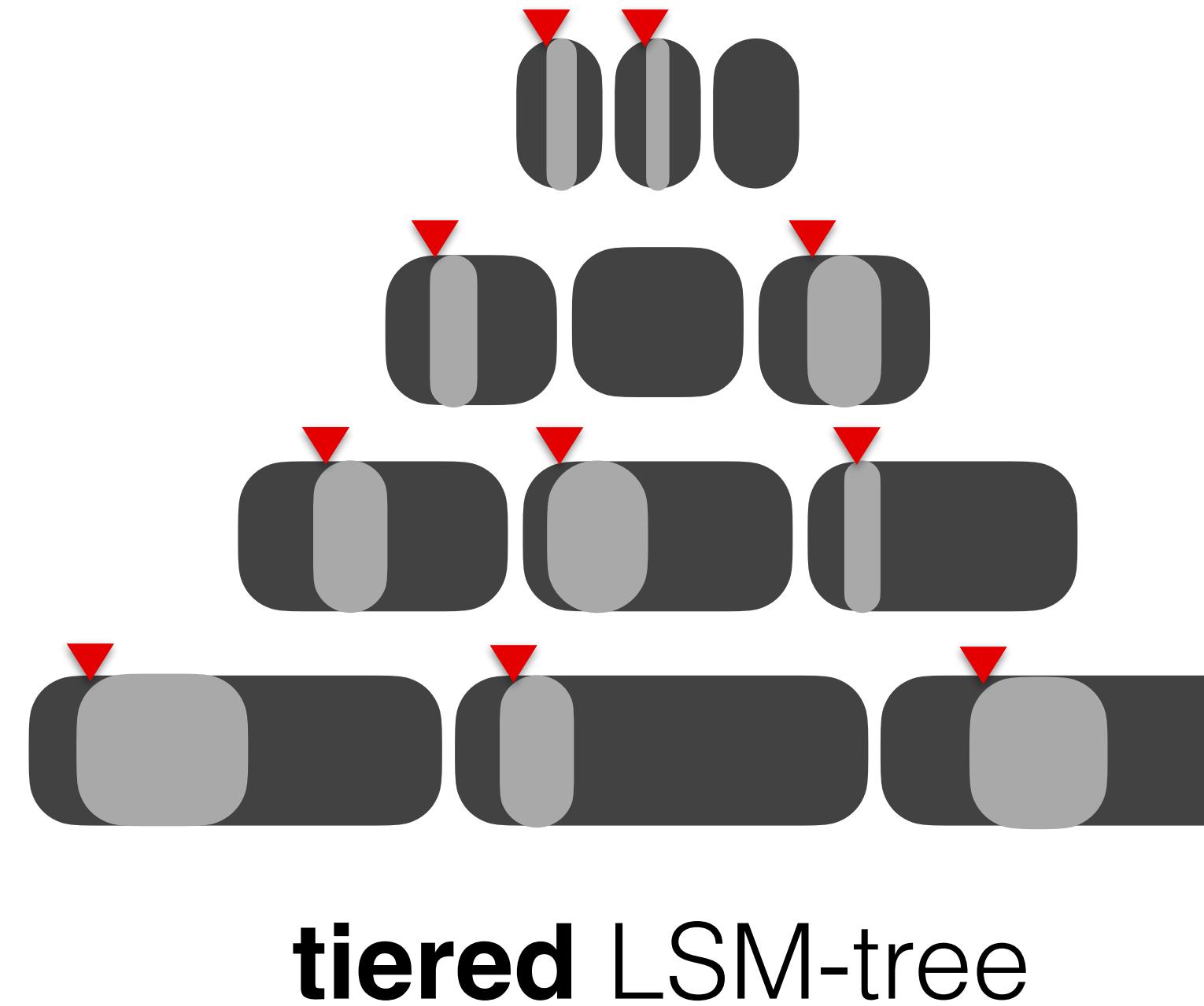


P : pages in buffer
 B : entries/page
 L : #levels
 T : size ratio
 N : #entries in tree

Range lookup cost

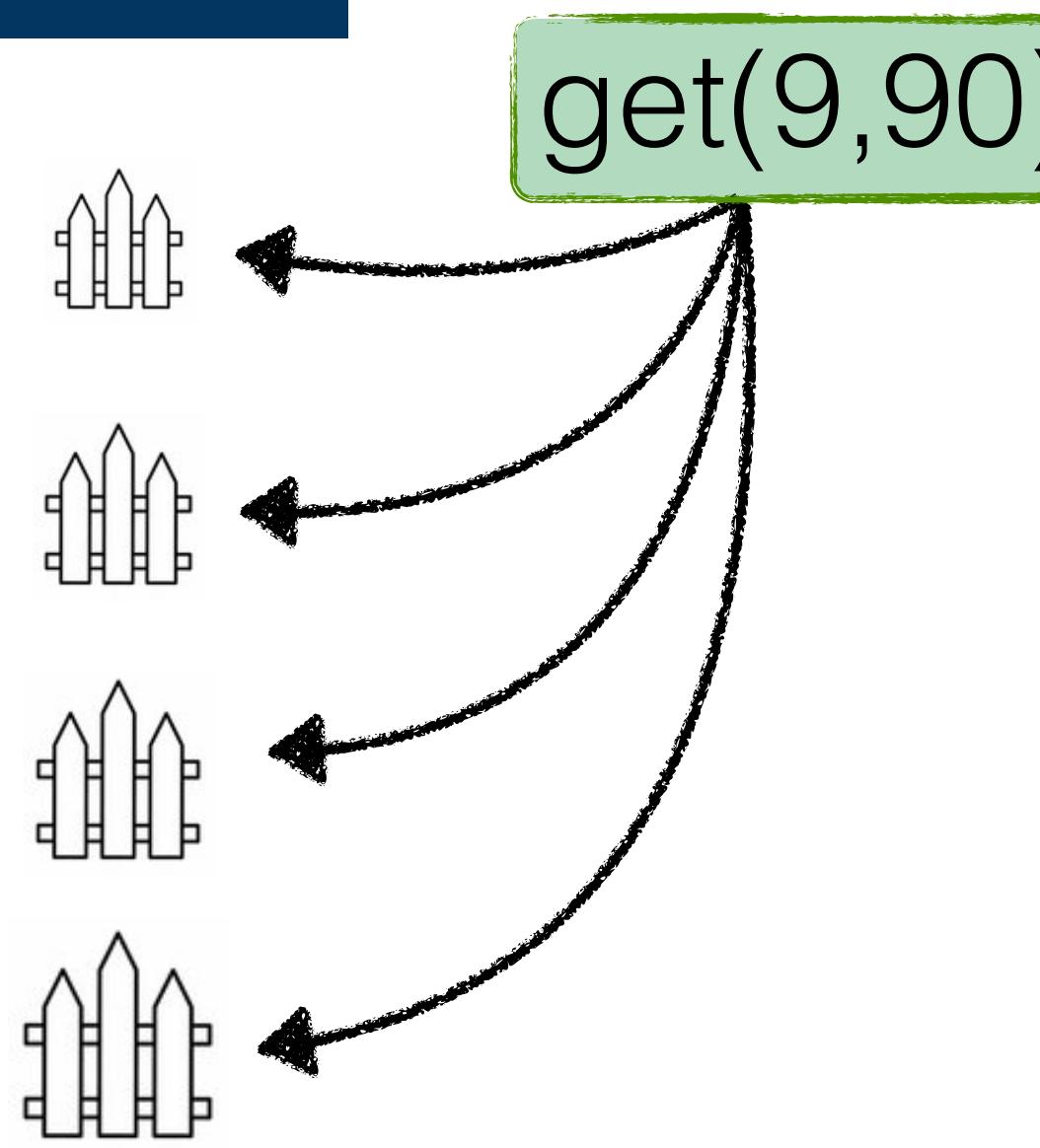
Looking for keys in a range

s = selectivity of the range query



**fence
pointers**

(page-wise zone map)



total entries in tree = N

#entries per page = B

#pages in tree = N/B

Cost of range lookup = $s \cdot N/B$

What about the **range query cost** in a **tiered LSM-tree**?

same cost for
leveled & tiered LSM

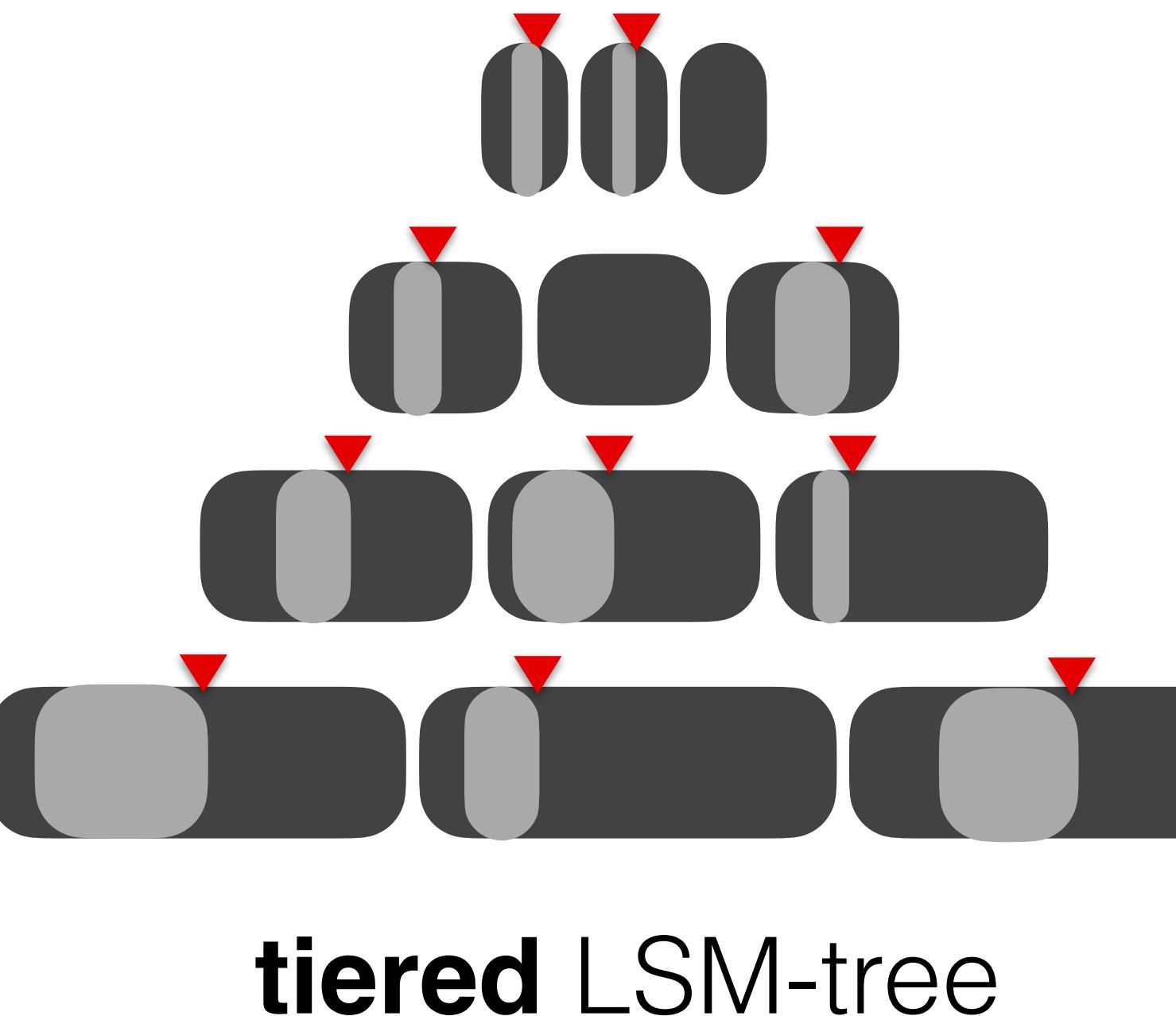


P : pages in buffer
 B : entries/page
 L : #levels
 T : size ratio
 N : #entries in tree

Range lookup cost

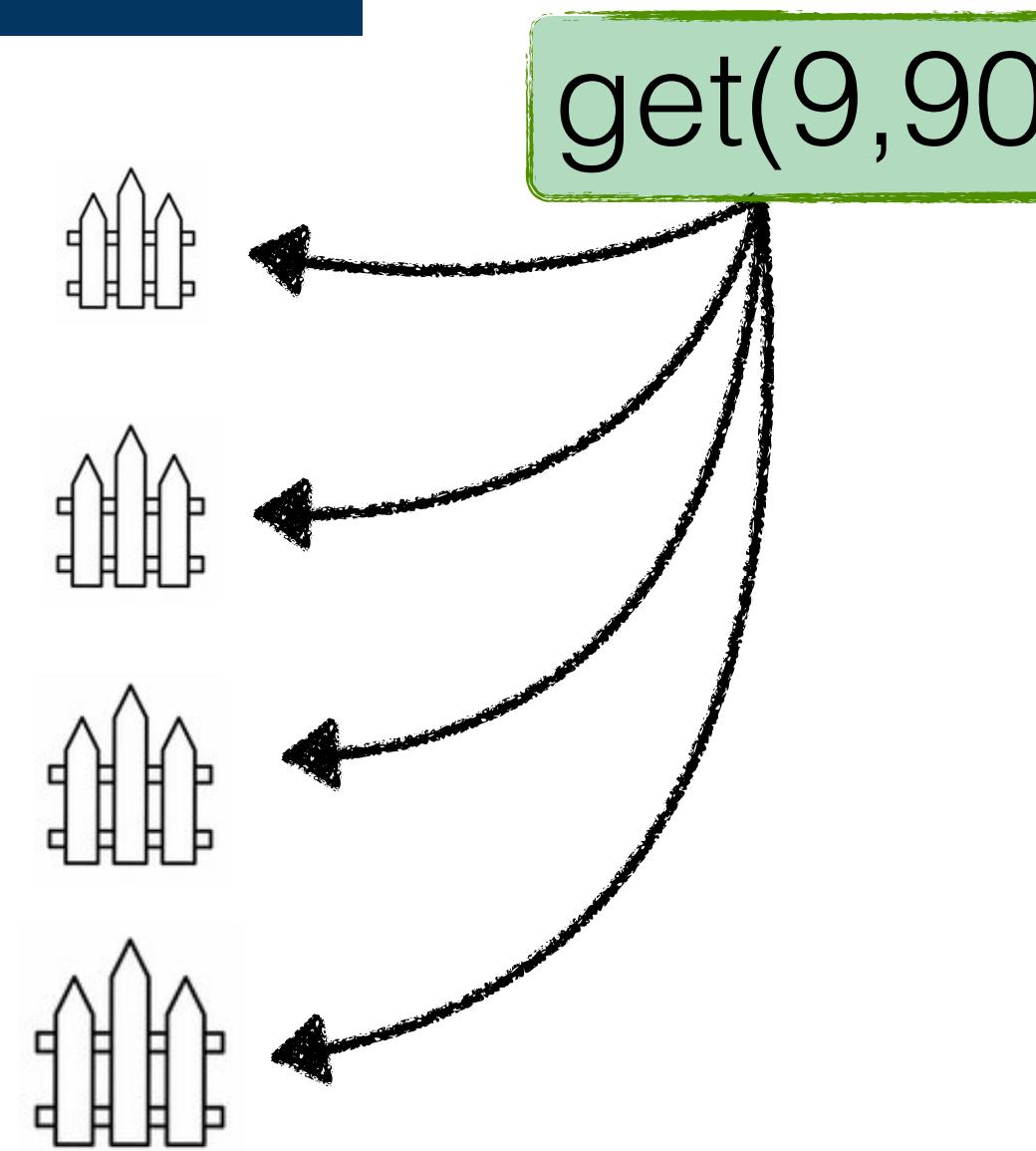
Looking for keys in a range

$s = \text{selectivity}$ of the range query



**fence
pointers**

(page-wise zone map)



total entries in tree = N

#entries per page = B

#pages in tree = N/B

Cost of range lookup = $s \cdot N/B$

What about the **range query cost** in a **tiered LSM-tree**?

same cost for
tiered partitioned LSM



Very different story when workload has **update/deletes**.

Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | range lookup cost |
|------------------|--------------------|---------------------------------|--------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ |
| B+-tree | | | |
| Sorted array | | | |
| Log | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)



Brandeis
UNIVERSITY

Monkey shaves off the “L” factor from the cost

Cost analysis

Counting all I/Os

* long range lookups

| data structure | ingestion cost | point lookup cost * | range lookup cost * |
|------------------|--------------------|---------------------------------|---------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ |
| B+-tree | | | |
| Sorted array | | | |
| Log | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)



Brandeis
UNIVERSITY

Monkey shaves off the “L” factor from the cost

P : pages in buffer

B : entries/page

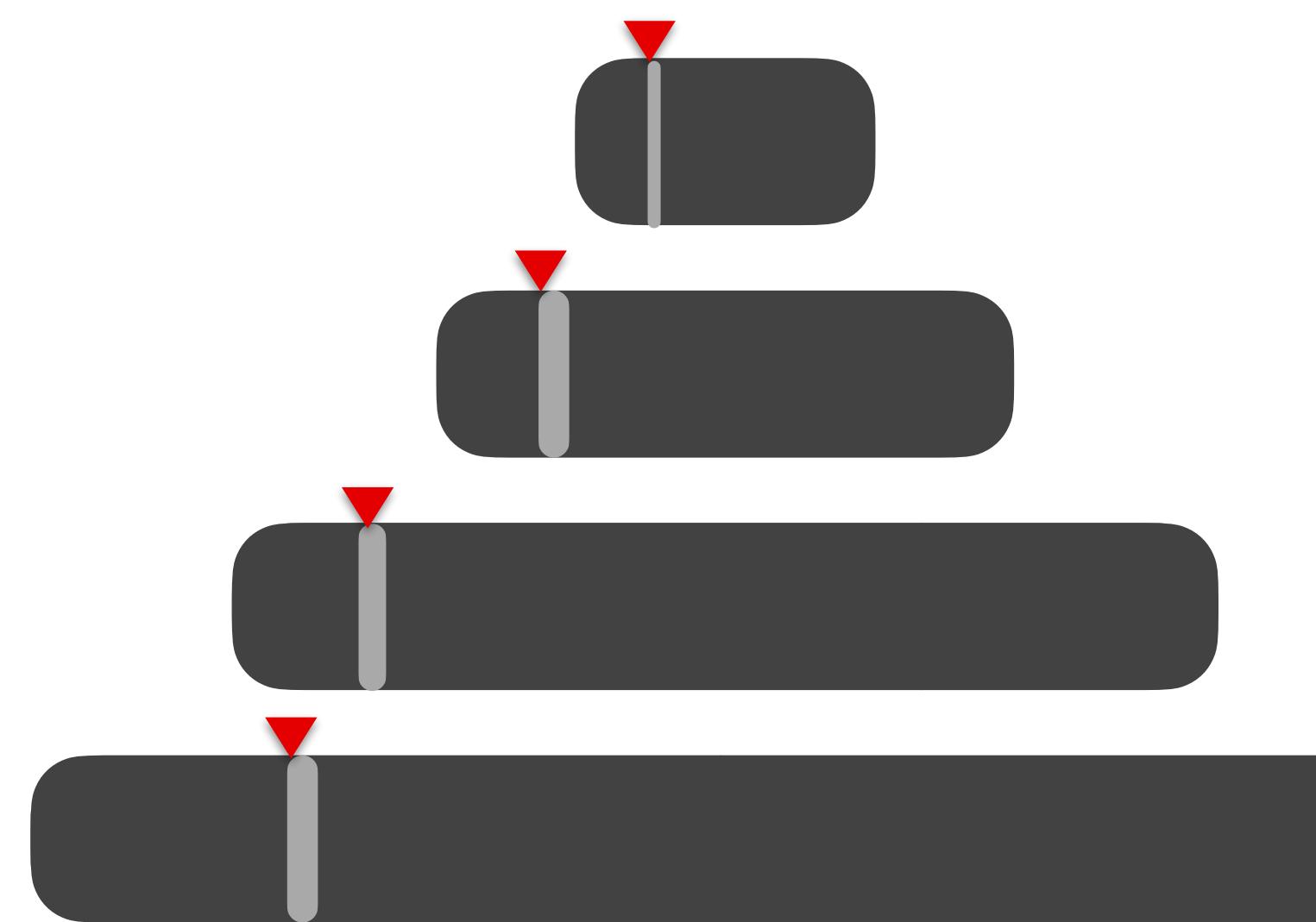
L : #levels

T : size ratio

N : #entries in tree

Range lookup cost

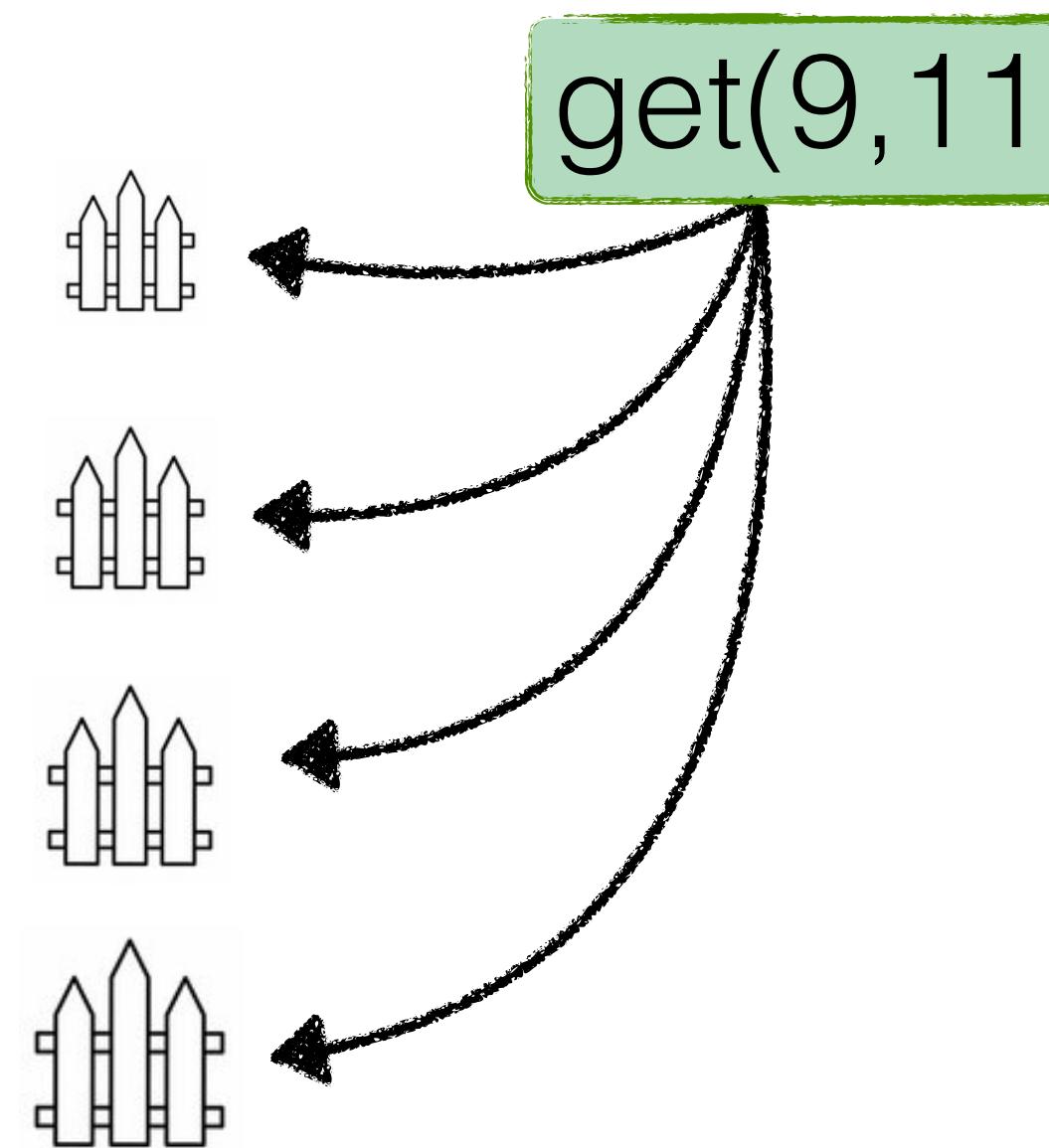
Looking for keys in a range



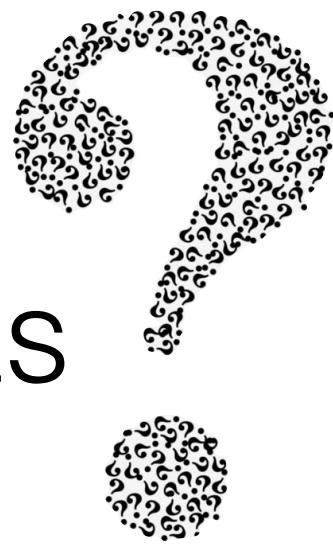
leveled LSM-tree

**fence
pointers**

(page-wise zone map)



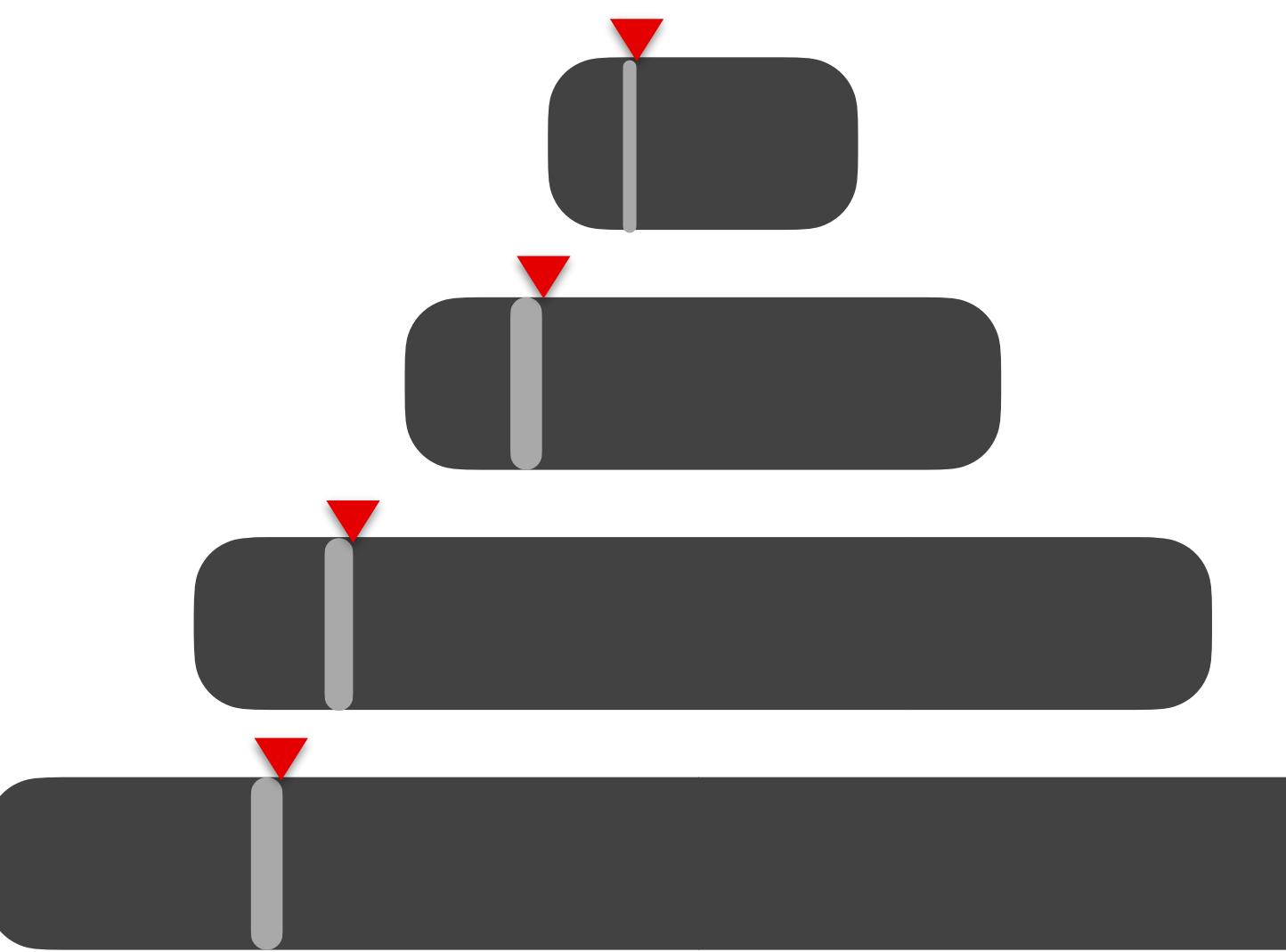
What if the **range query** has
a **very low selectivity**?



P : pages in buffer
 B : entries/page
 L : #levels
 T : size ratio
 N : #entries in tree

Range lookup cost

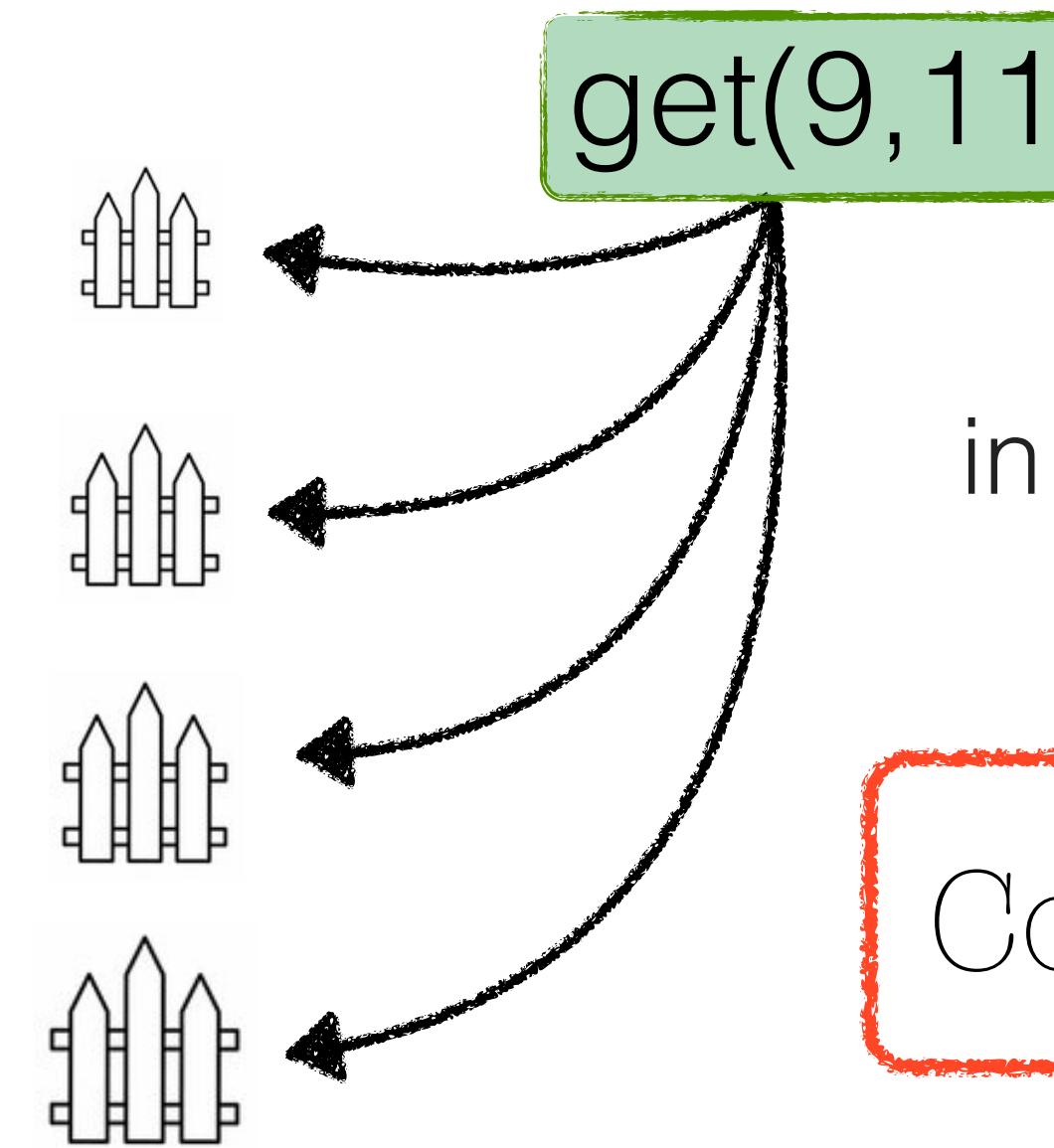
Looking for keys in a range



leveled LSM-tree

**fence
pointers**

(page-wise zone map)



What if the **range query** has
a **very low selectivity**?

in the **worst case**,
need to read **2 pages per sorted run**

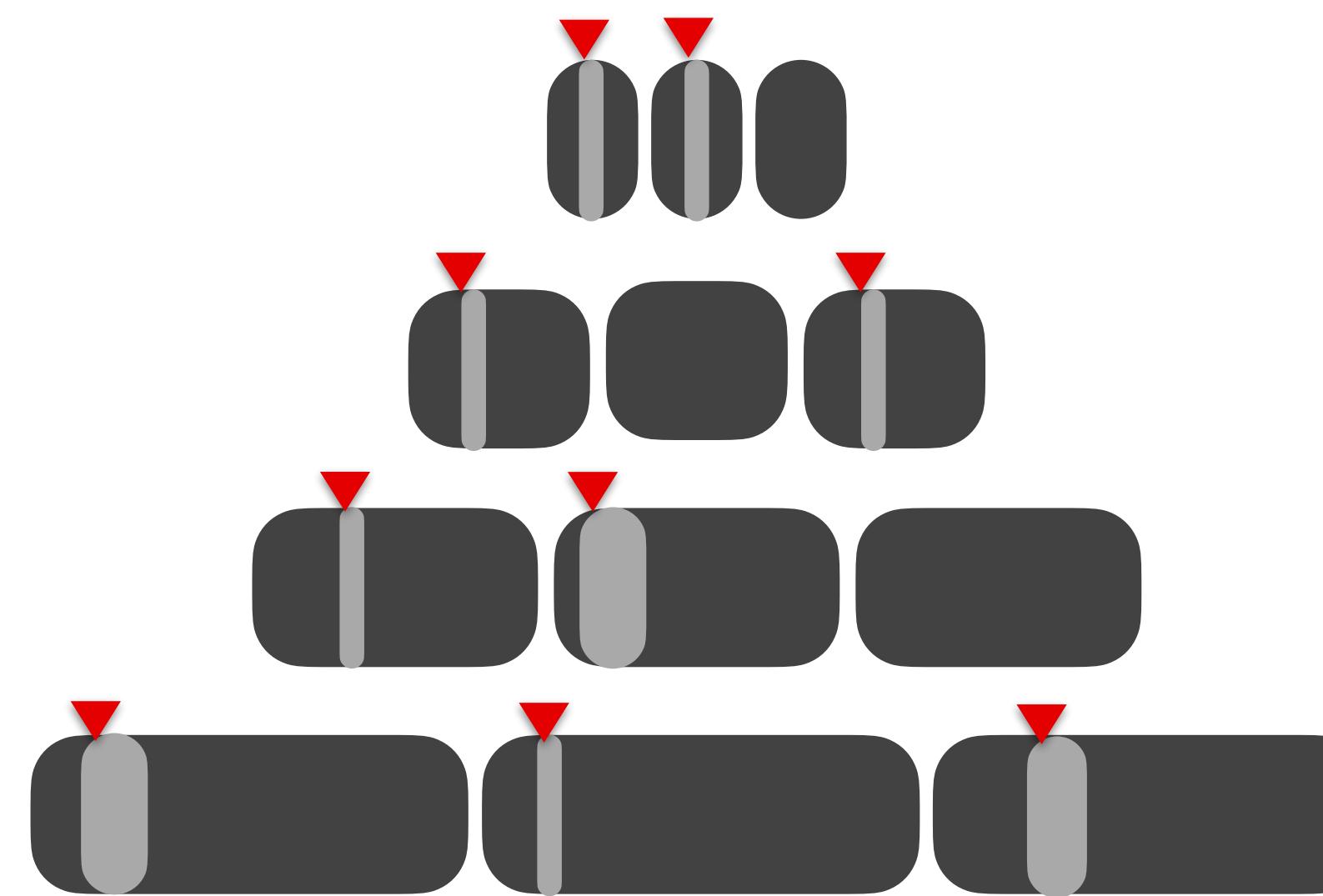
Cost of short range lookup = $2 \cdot L$

What about the **tiering**?

P : pages in buffer
 B : entries/page
 L : #levels
 T : size ratio
 N : #entries in tree

Range lookup cost

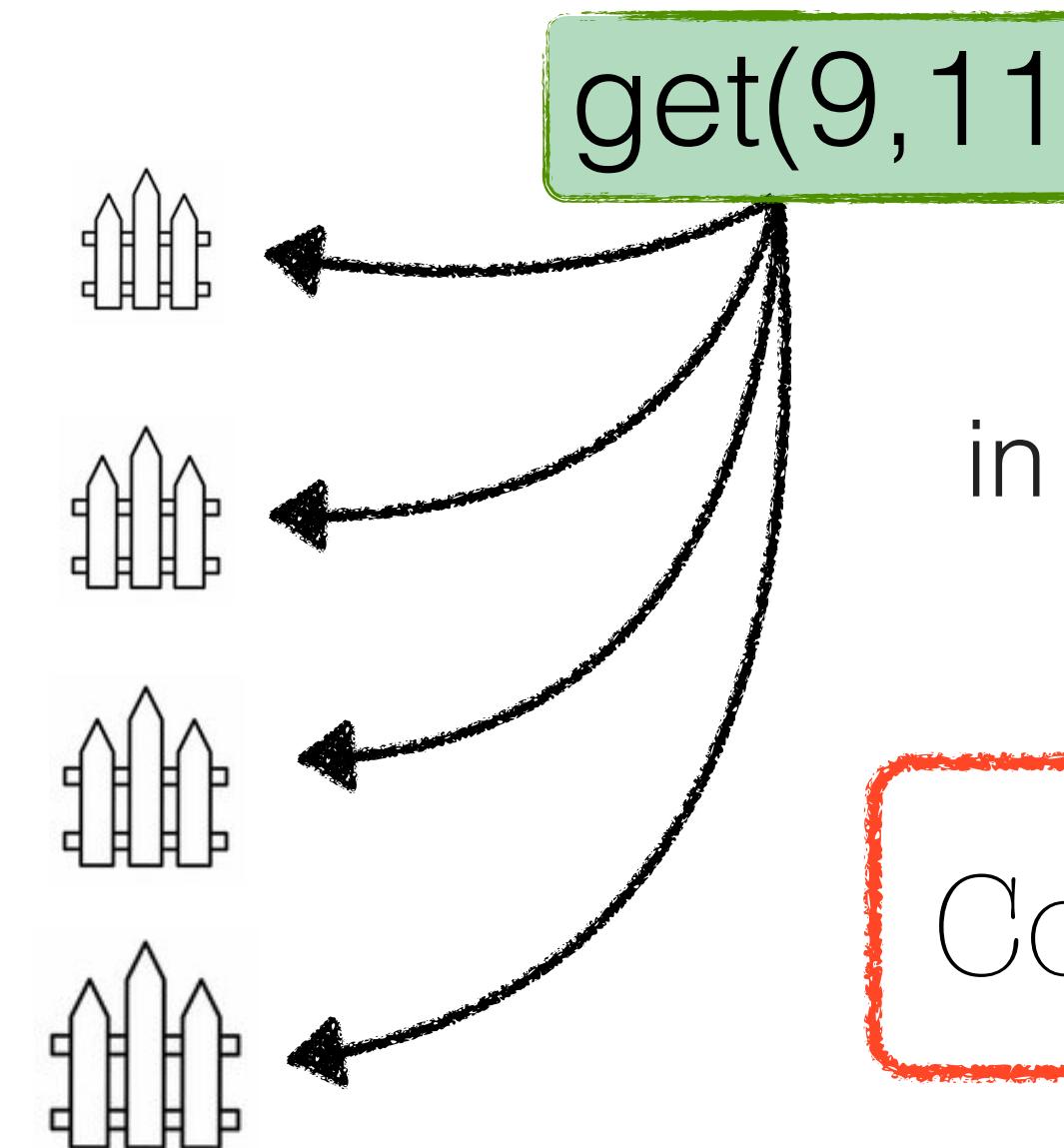
Looking for keys in a range



tiered LSM-tree

**fence
pointers**

(page-wise zone map)



What if the **range query** has
a **very low selectivity**?

in the **worst case**,
need to read **2 pages per sorted run**

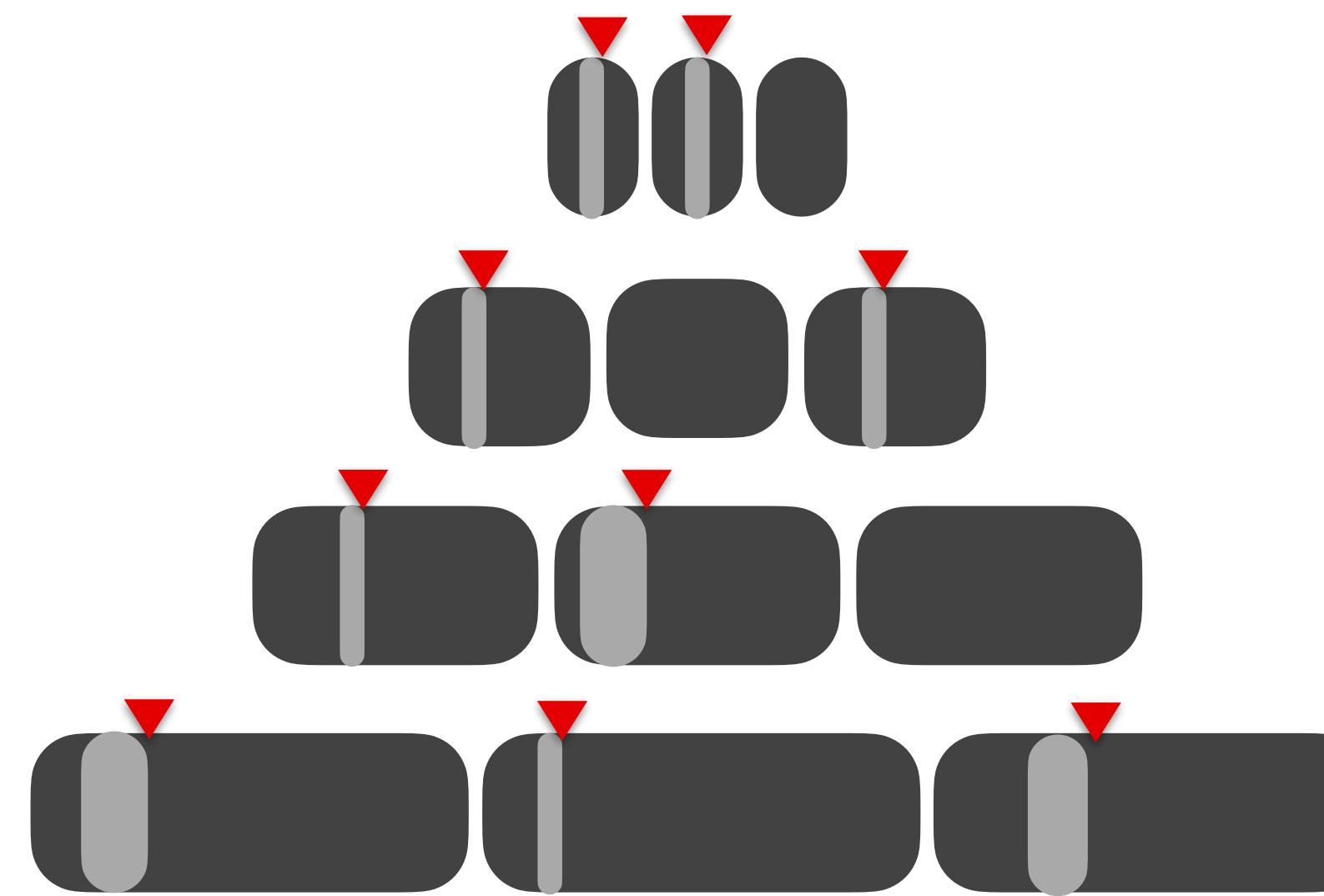
Cost of short range lookup = $2 \cdot L$

What about the **tiering**?

P : pages in buffer
 B : entries/page
 L : #levels
 T : size ratio
 N : #entries in tree

Range lookup cost

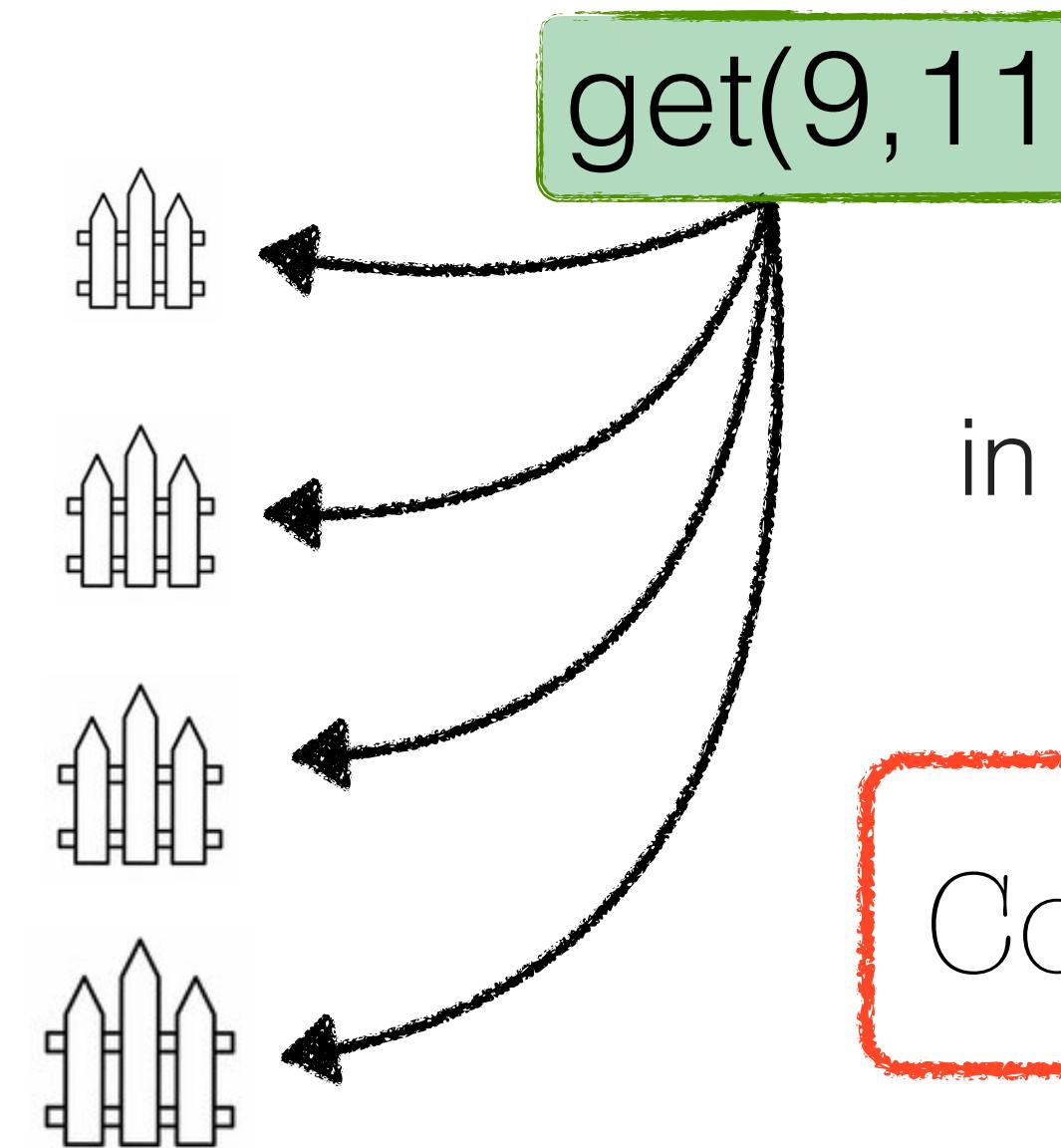
Looking for keys in a range



tiered LSM-tree

**fence
pointers**

(page-wise zone map)



What if the **range query** has a **very low selectivity**?

in the **worst case**,
need to read **2 pages per sorted run**

Cost of short range lookup = $2 \cdot L$

What about the **tiering**?

in the **worst case**,
need to read **2 pages per sorted run**

P : pages in buffer

B : entries/page

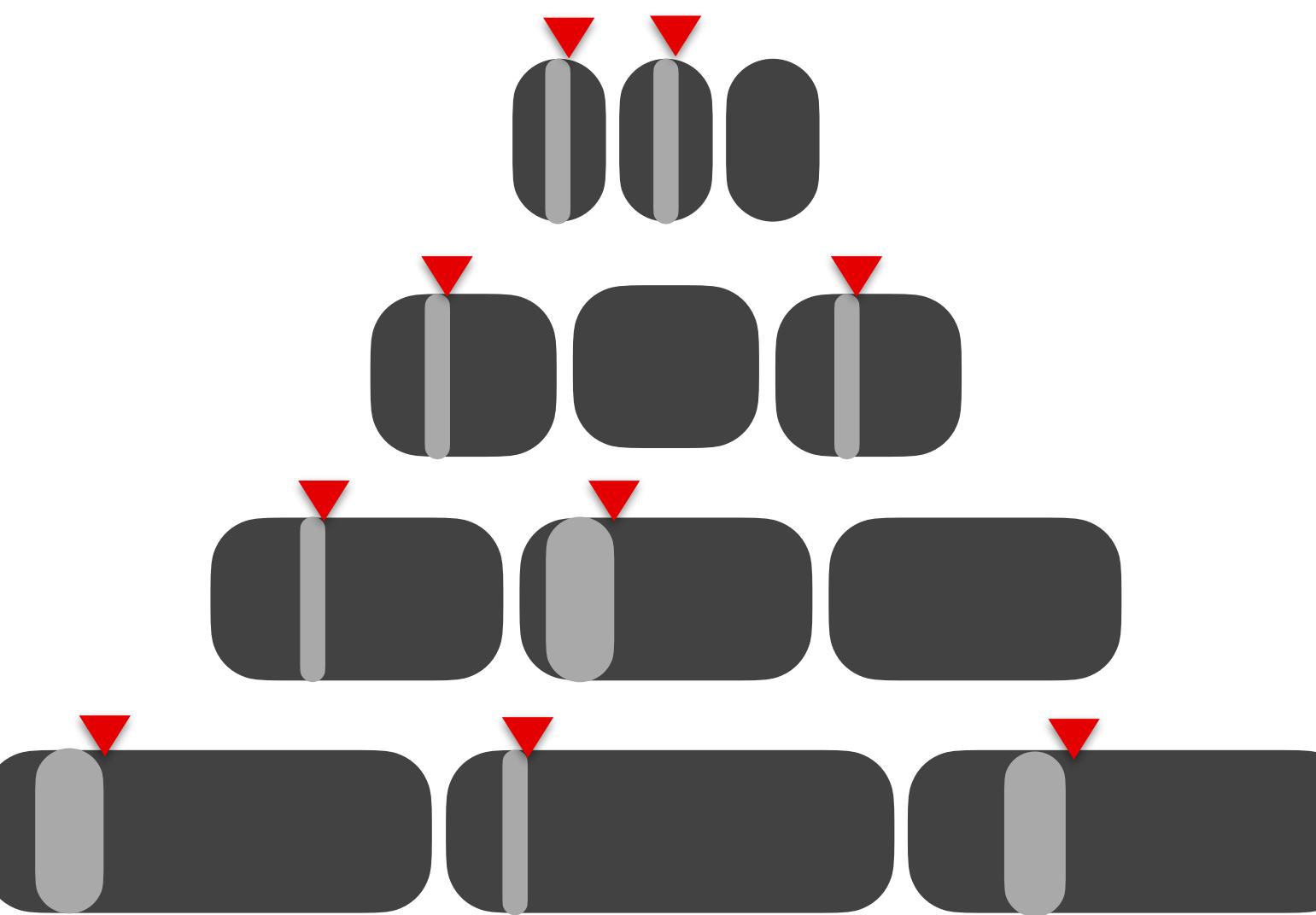
L : #levels

T : size ratio

N : #entries in tree

Range lookup cost

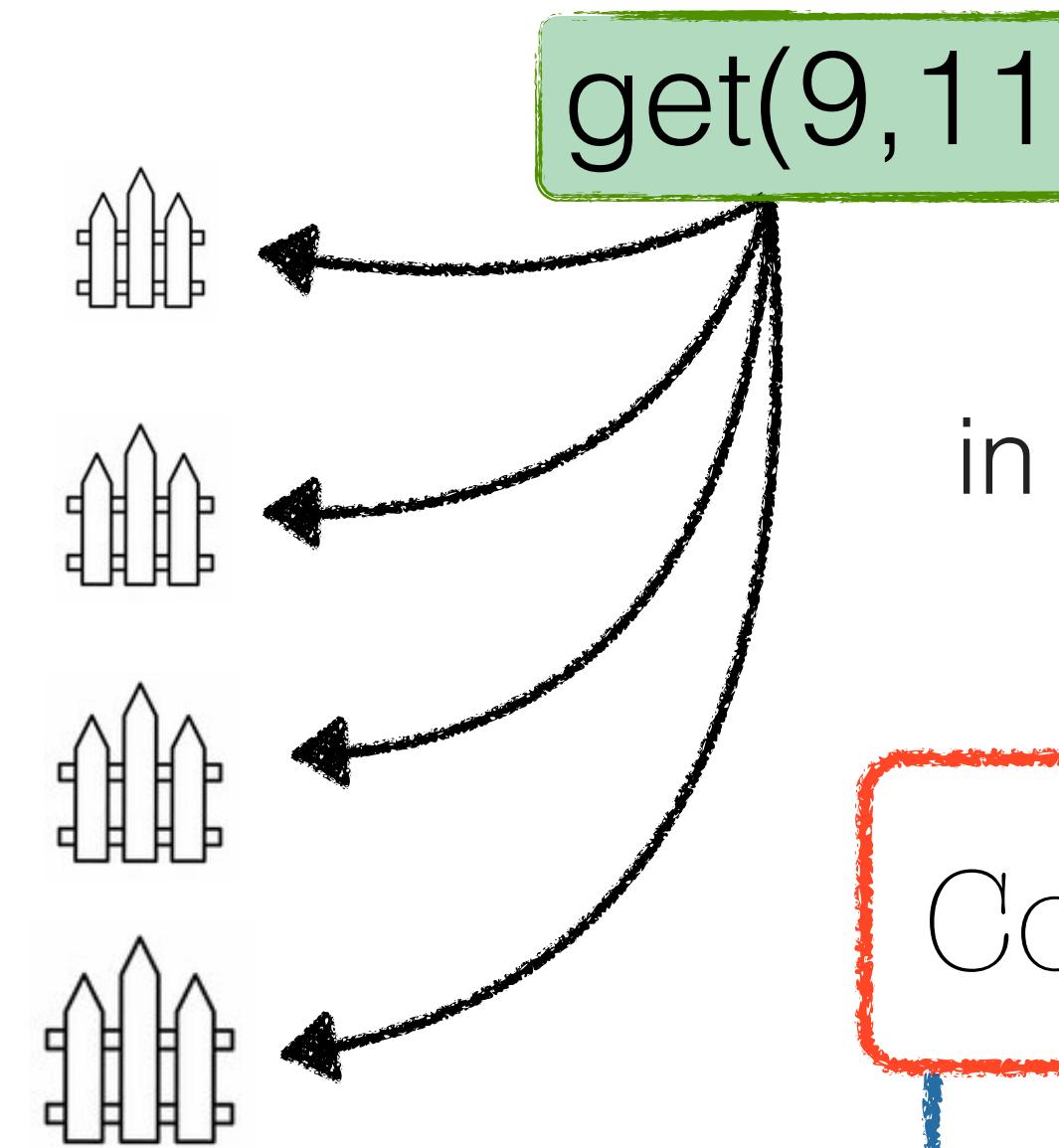
Looking for keys in a range



tiered LSM-tree

**fence
pointers**

(page-wise zone map)



What if the **range query** has
a **very low selectivity**?

in the **worst case**,
need to read **2 pages per sorted run**

Cost of short range lookup = $2 \cdot L$

tiering

Cost of short range lookup = $2 \cdot L \cdot T$



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | | | | |
| Sorted array | | | | |
| Log | | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | ? | ? | ? | ? |
| Sorted array | | | | |
| Log | | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)



B+-trees

The go to index data structures for relational databases



*It could be said that the world's information
is at our fingertips because of B-trees.*

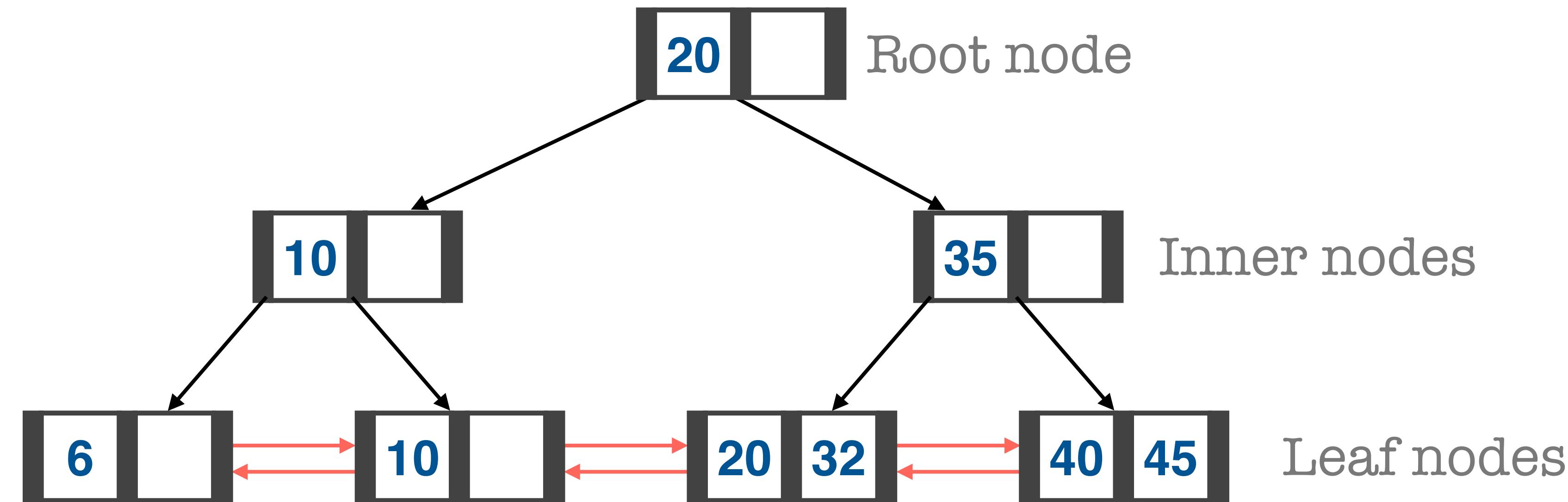
Goetz Graefe, Google, Ex-Microsoft, HP Fellow
Google ACM Software System Award



Brandeis
UNIVERSITY

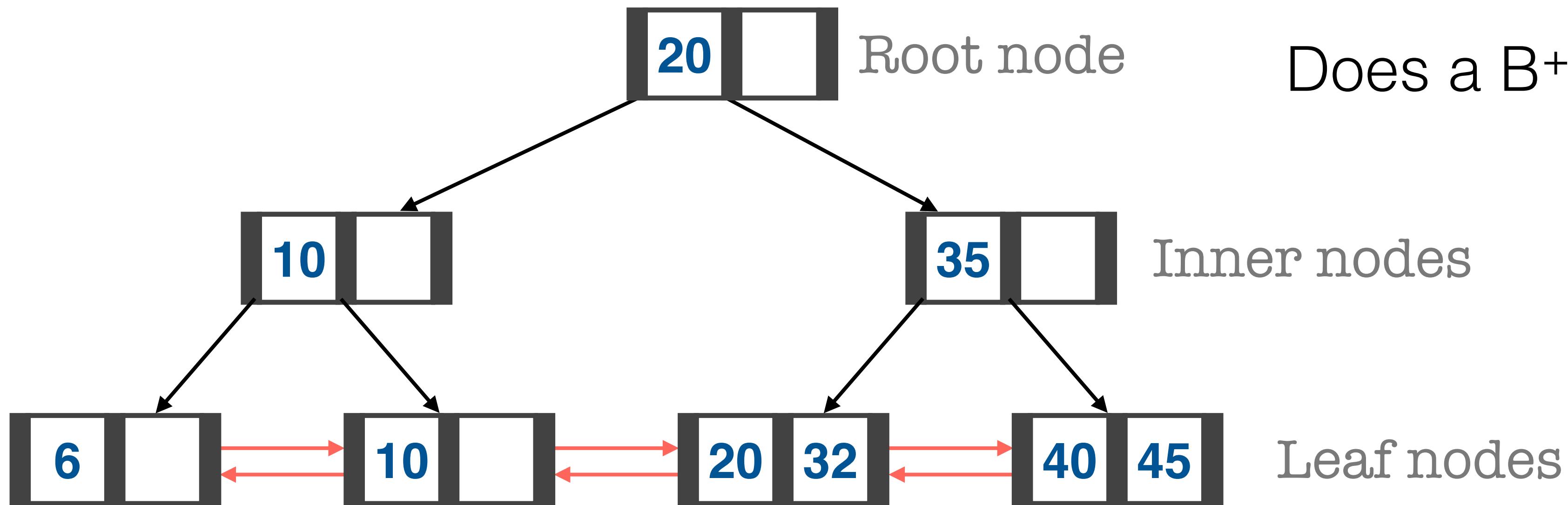
B+-trees

The go to index data structures for relational databases



B+-trees

The go to index data structures for relational databases

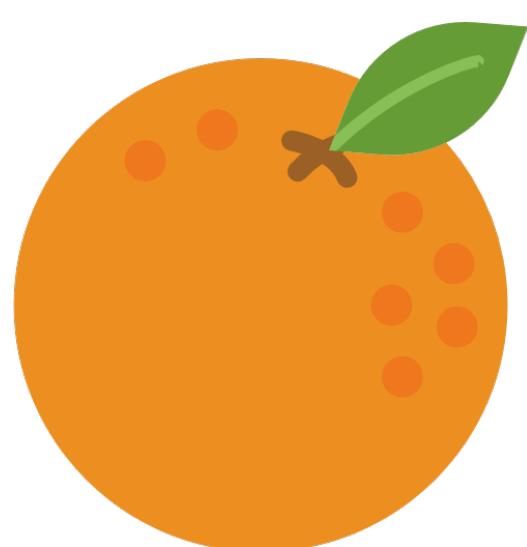


Does a B+-tree have a **buffer**?

No!

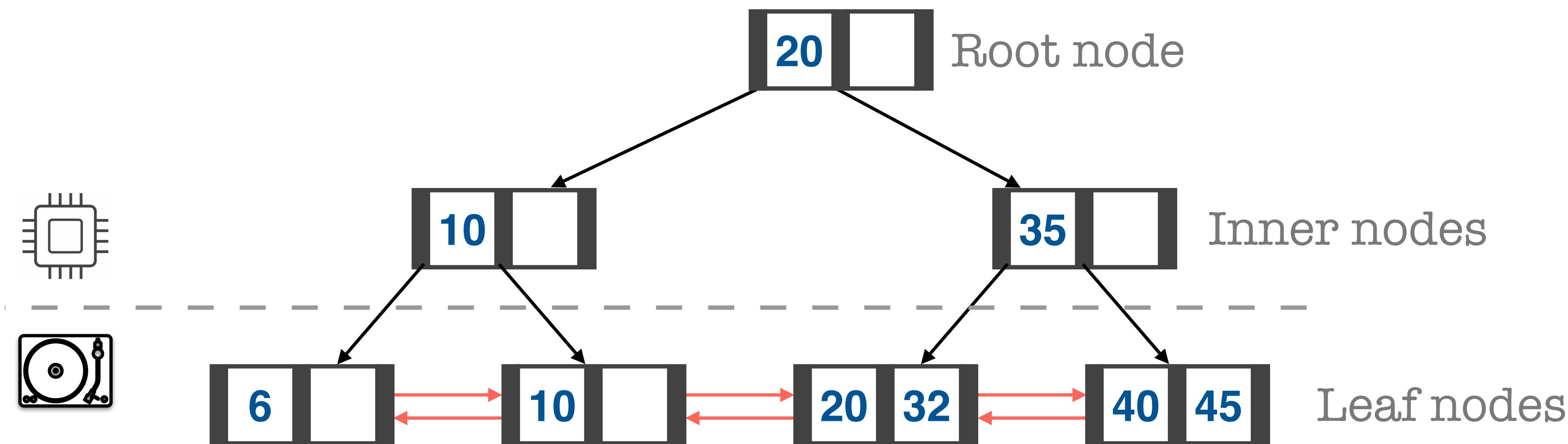


VS.



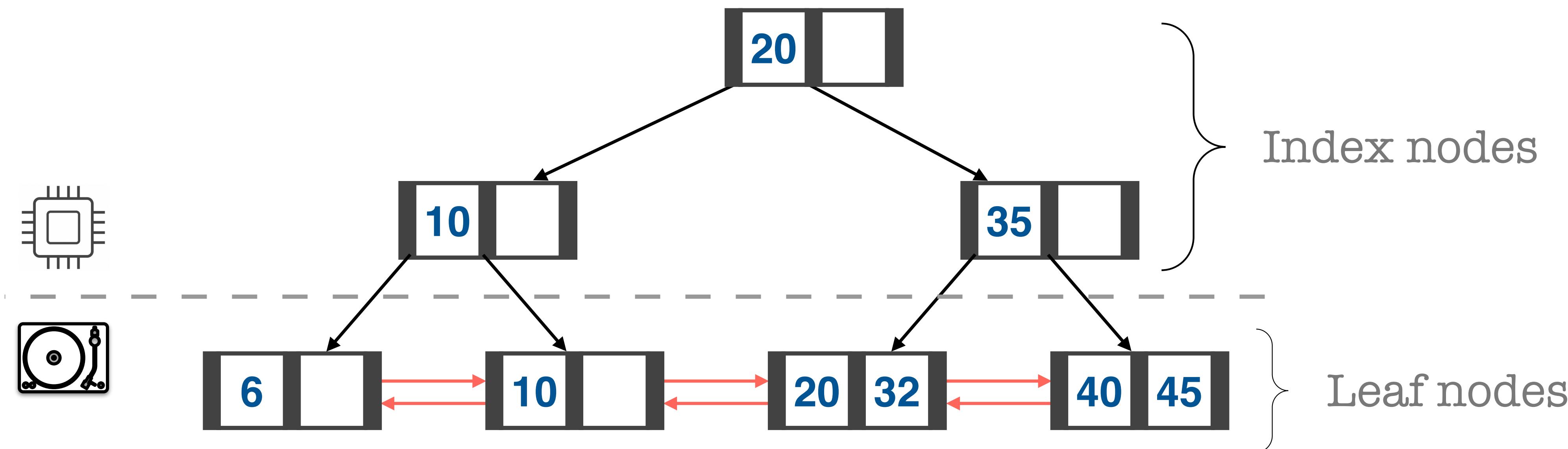
B+-trees

The go to index data structures for relational databases



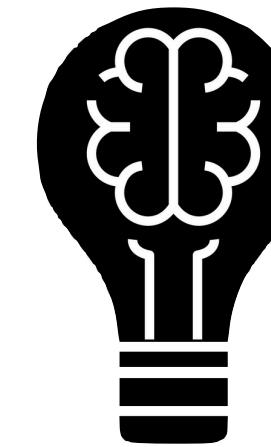
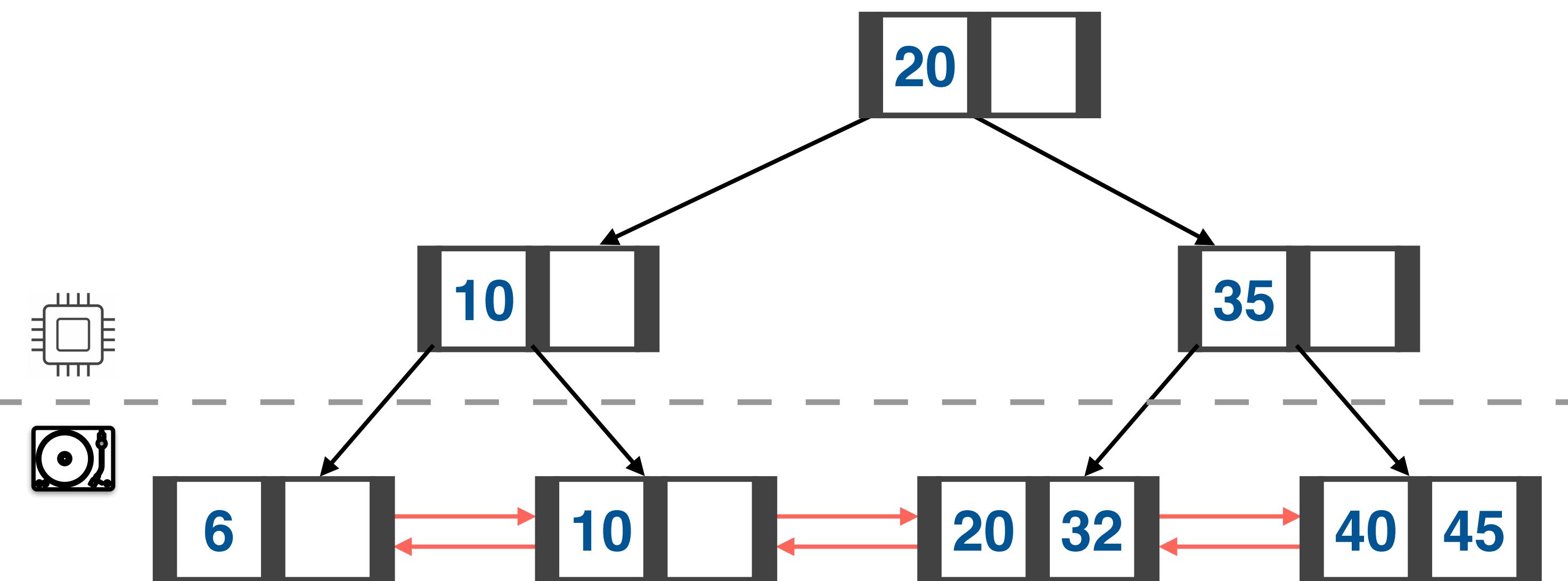
B+-trees

The go to index data structures for relational databases



B+-trees

The go to index data structures for relational databases



Thought Experiment 1

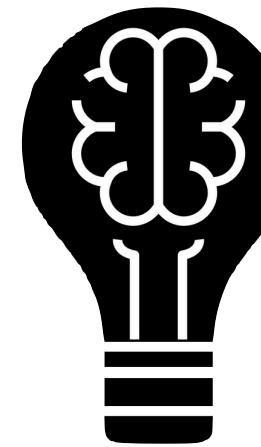
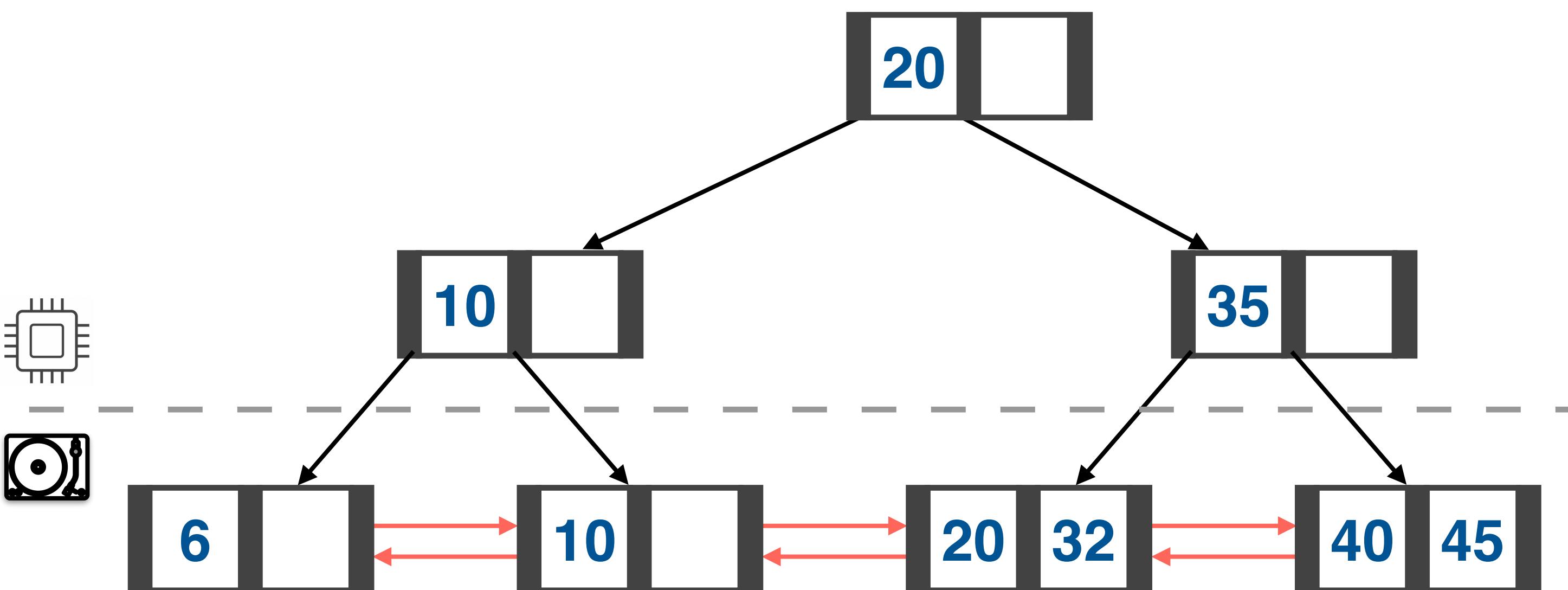
What is the **insert cost** in
a **buffered B+-tree**?

2 I/Os per insert

1 to read, 1 to write

B+-trees

The go to index data structures for relational databases



Thought Experiment 1.

What is the **insert cost** in
a **buffered B+-tree**?

2 I/Os per insert

1 to read, 1 to write

Cost of ingestion = 2



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|---------------------------|-----------------------|---------------------------------------|-------------------------------|--------------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B⁺-tree | $O(1)$ | ? | ? | ? |
| Sorted array | | | | |
| Log | | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | ? | ? | ? |
| Sorted array | | | | |
| Log | | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | ? | ? |
| Sorted array | | | | |
| Log | | | | |

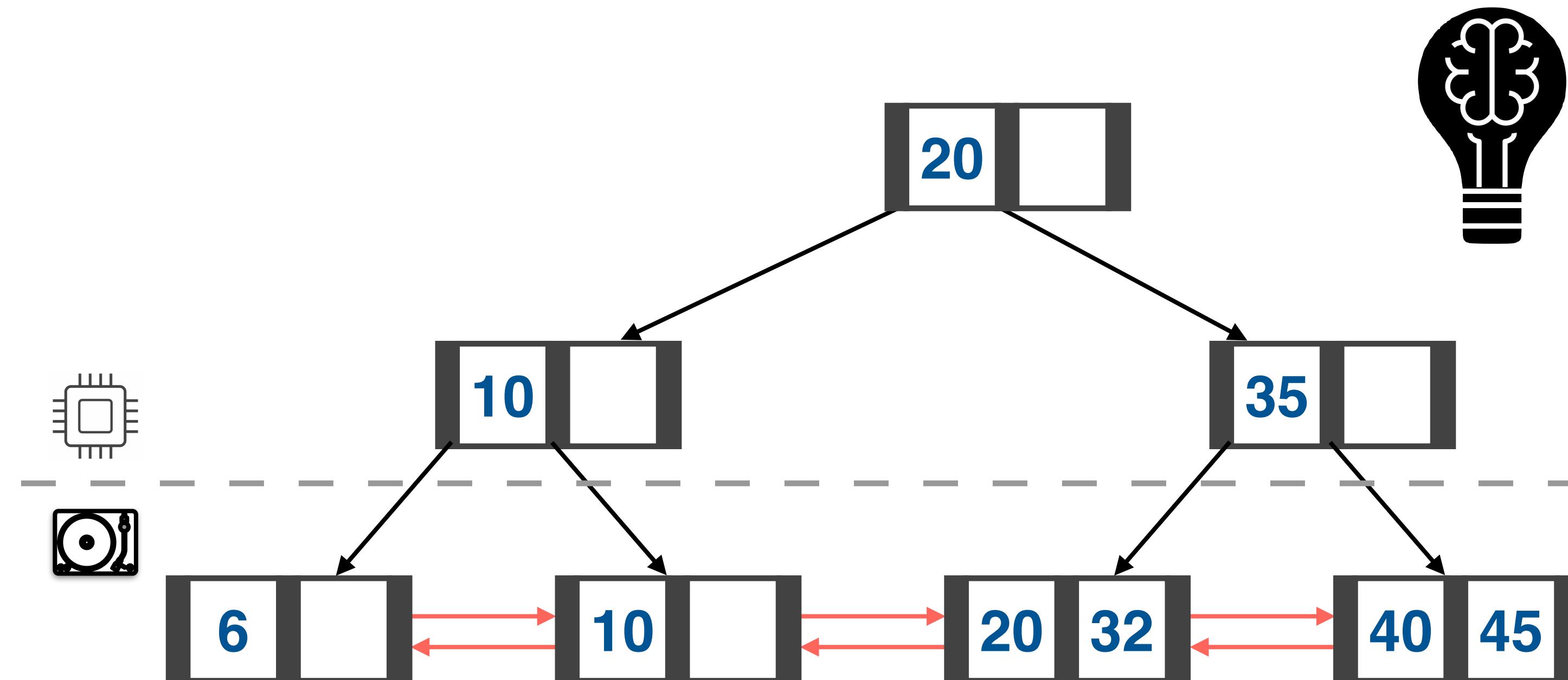
* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)



B+-trees

The go to index data structures for relational databases



s = **selectivity** of the range query

Thought Experiment 2
What is the **range lookup cost** in a **buffered B+-tree**?

total entries in tree = N

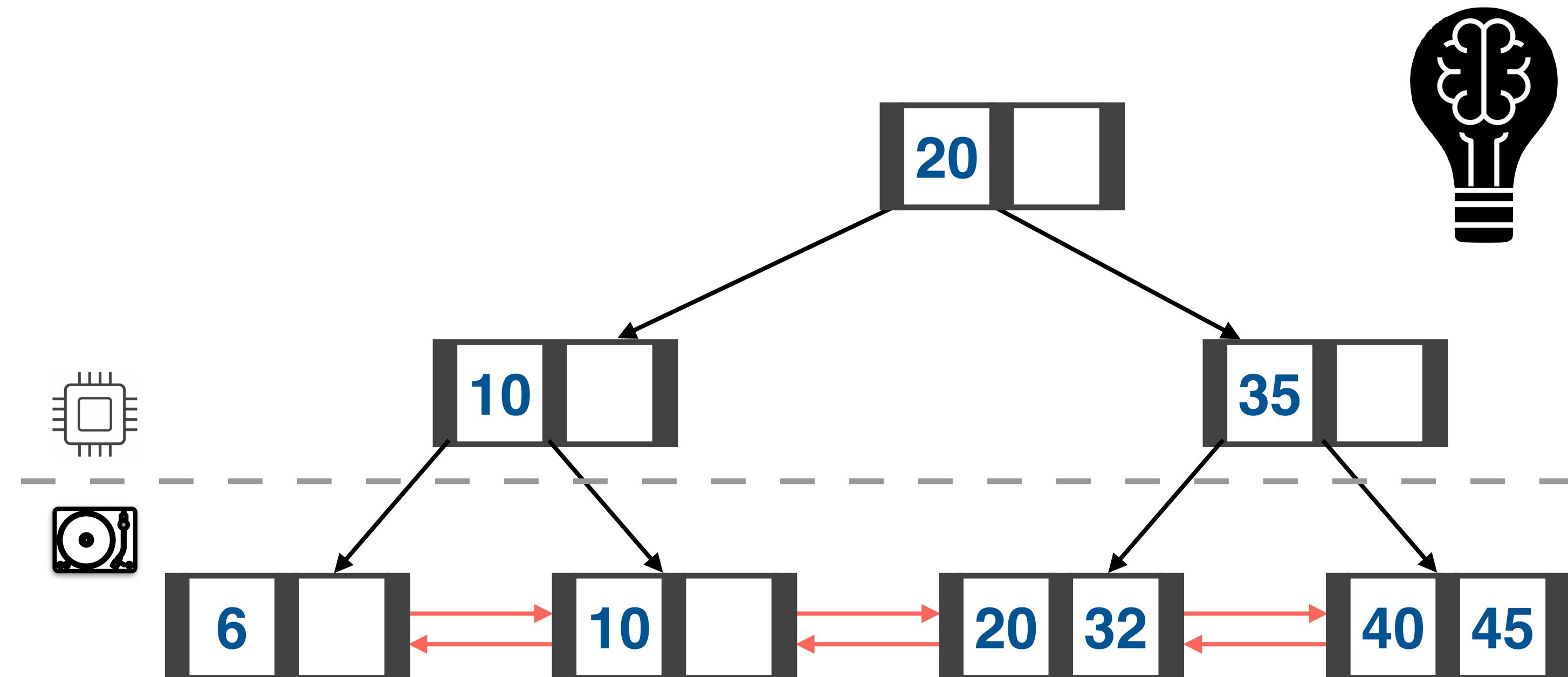
#entries per page = B

#pages in tree = N/B

Cost of range lookup = $s \cdot N/B$

B+-trees

The go to index data structures for relational databases



s = **selectivity** of the range query

Thought Experiment 2
What is the **range lookup cost** in a **buffered B+-tree**?

total entries in tree = **N**

#entries per page = **B**

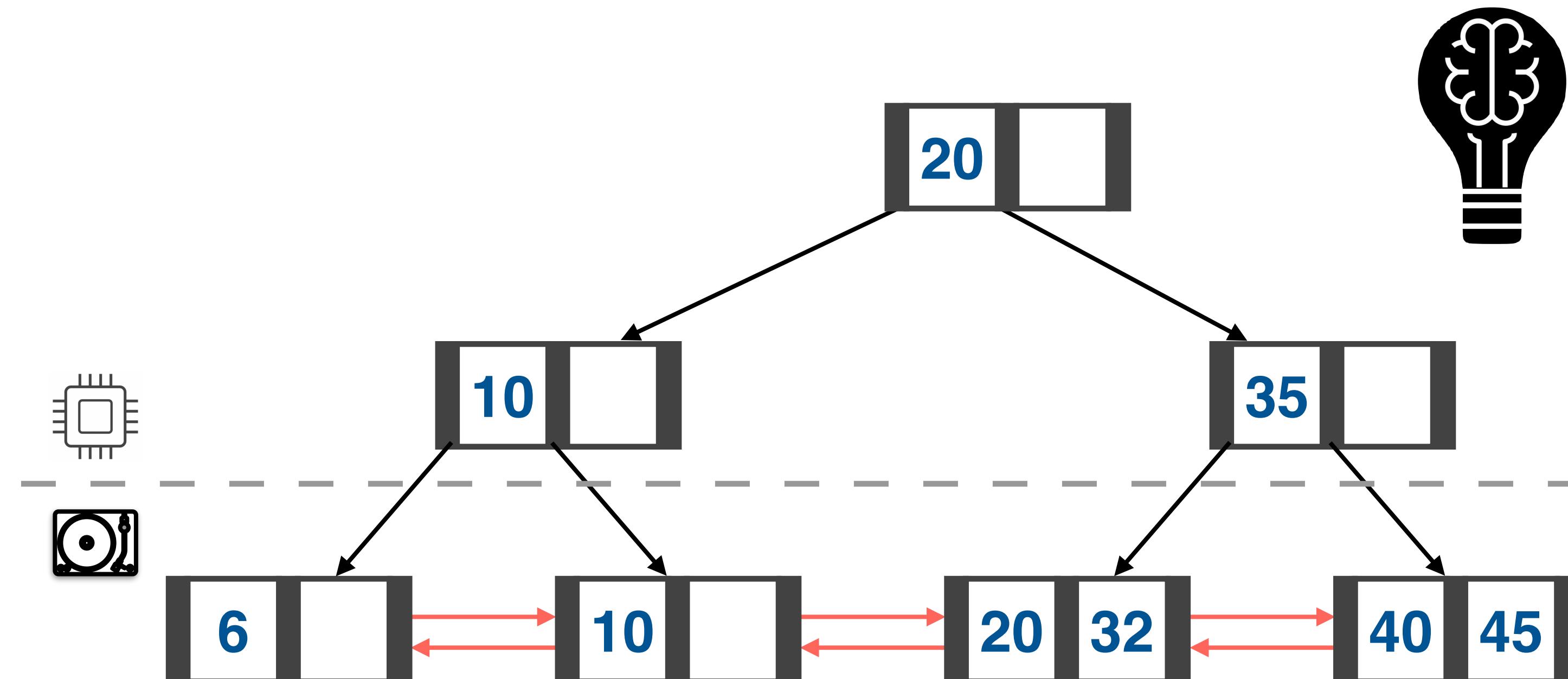
#pages in tree = **N/B**

Cost of range lookup = **$s \cdot N/B$**

On average, nodes in a B+-tree are **67% full!**

B+-trees

The go to index data structures for relational databases



Thought Experiment 2
What is the **range lookup cost** in a **buffered B+-tree**?

total entries in tree = N

#entries per page = B

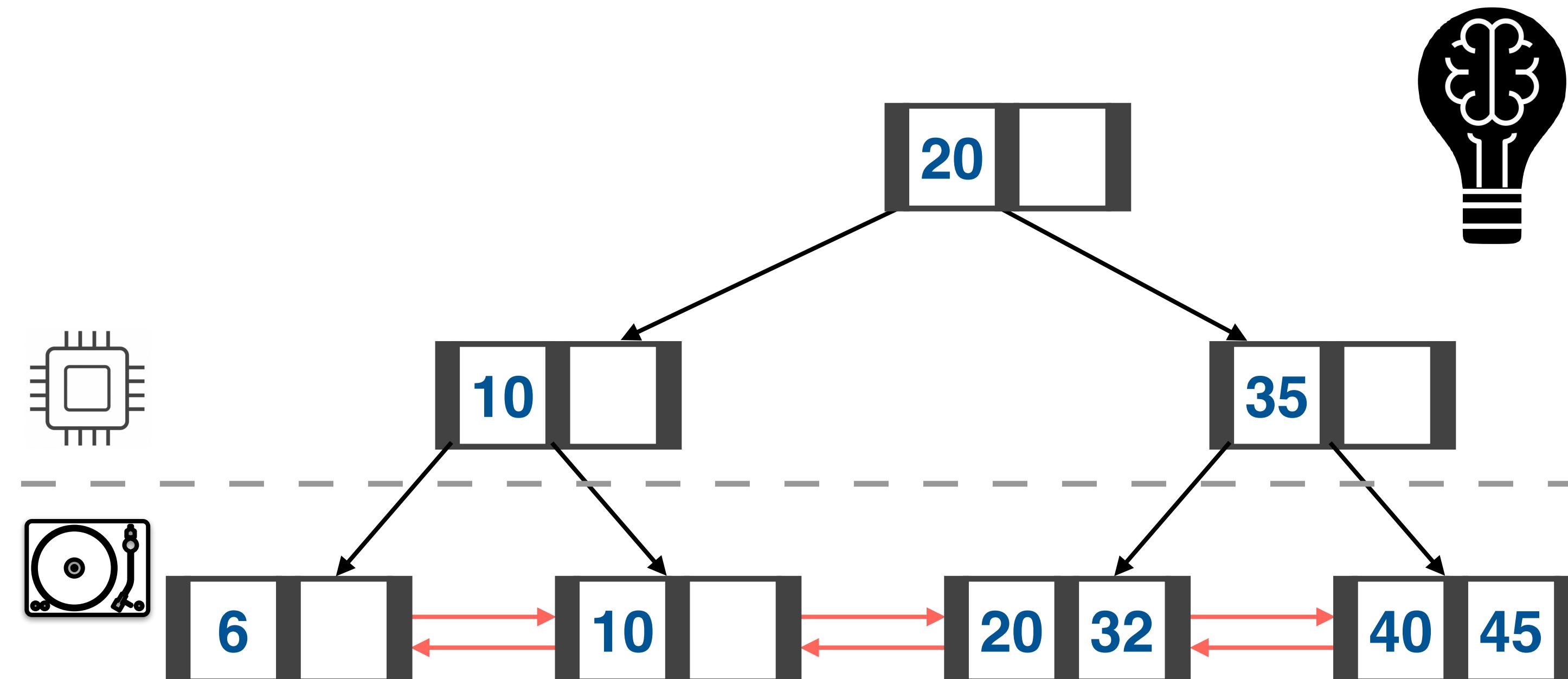
#pages in tree = N/B

On average, nodes in a B+-tree are **67% full!**

On average, B+-tree have a **50% read amplification!**

B+-trees

The go to index data structures for relational databases



s = **selectivity** of the range query

Thought Experiment 2
What is the **range lookup cost** in a **buffered B+-tree**?

total entries in tree = N

#entries per page = B

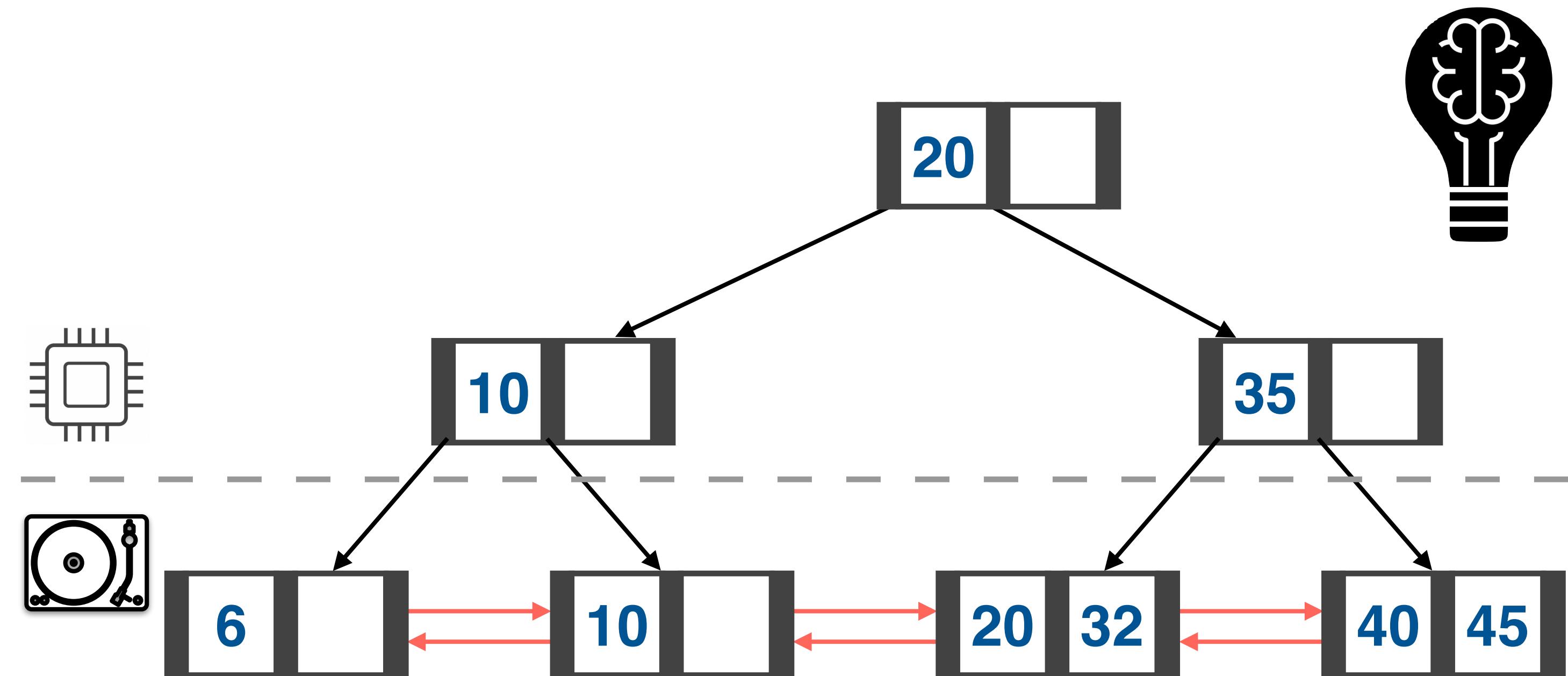
#pages in tree = N/B

Cost of range lookup = $s \cdot N/B$

x1.5

B+-trees

The go to index data structures for relational databases



s = **selectivity** of the range query

Thought Experiment 2
What is the **range lookup cost** in a **buffered B+-tree**?

total entries in tree = N

#entries per page = B

#pages in tree = N/B

Cost of range lookup = $s \cdot N/B$

x1.5

Cost of range lookup = $1.5 \cdot s \cdot N/B$

Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | ? |
| Sorted array | | | | |
| Log | | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|---|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ |  |
| Sorted array | | | | |
| Log | | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | ? | ? | ? | ? |
| Log | | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

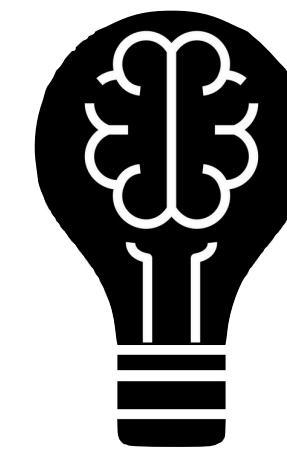
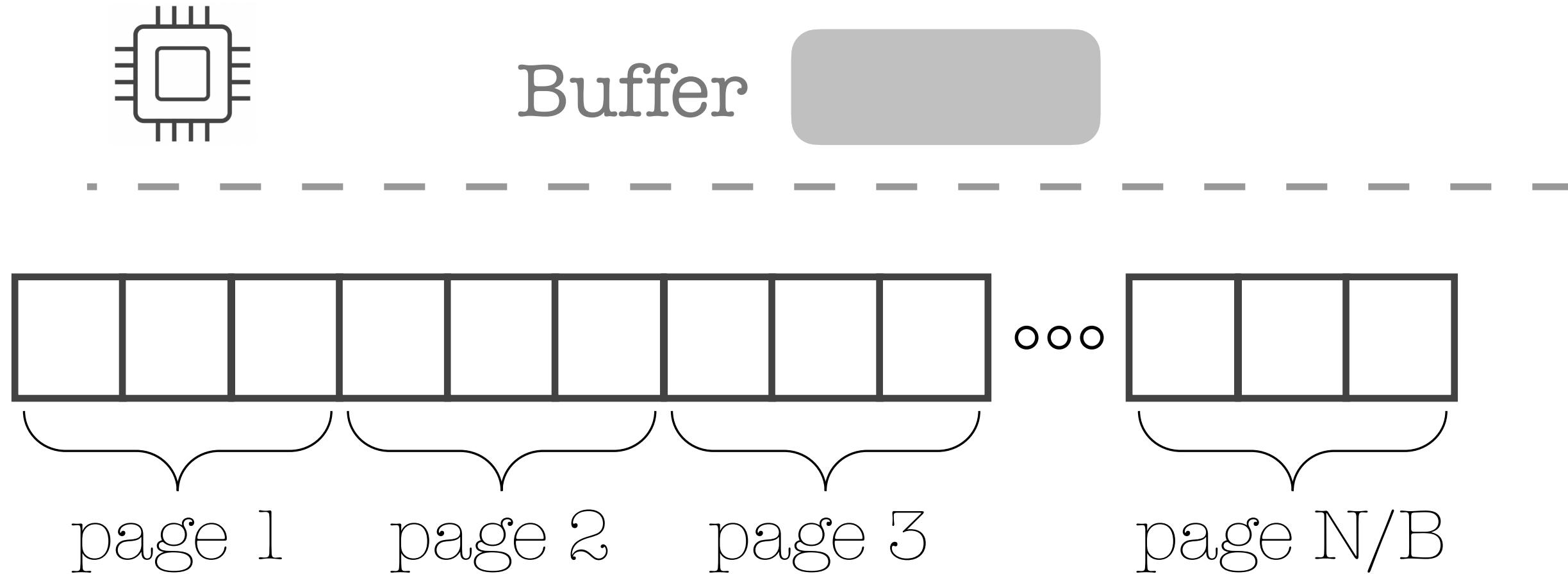
* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost



Sorted array

Optimizing for queries



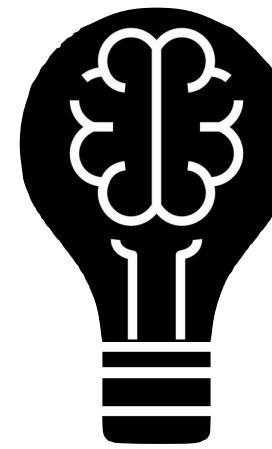
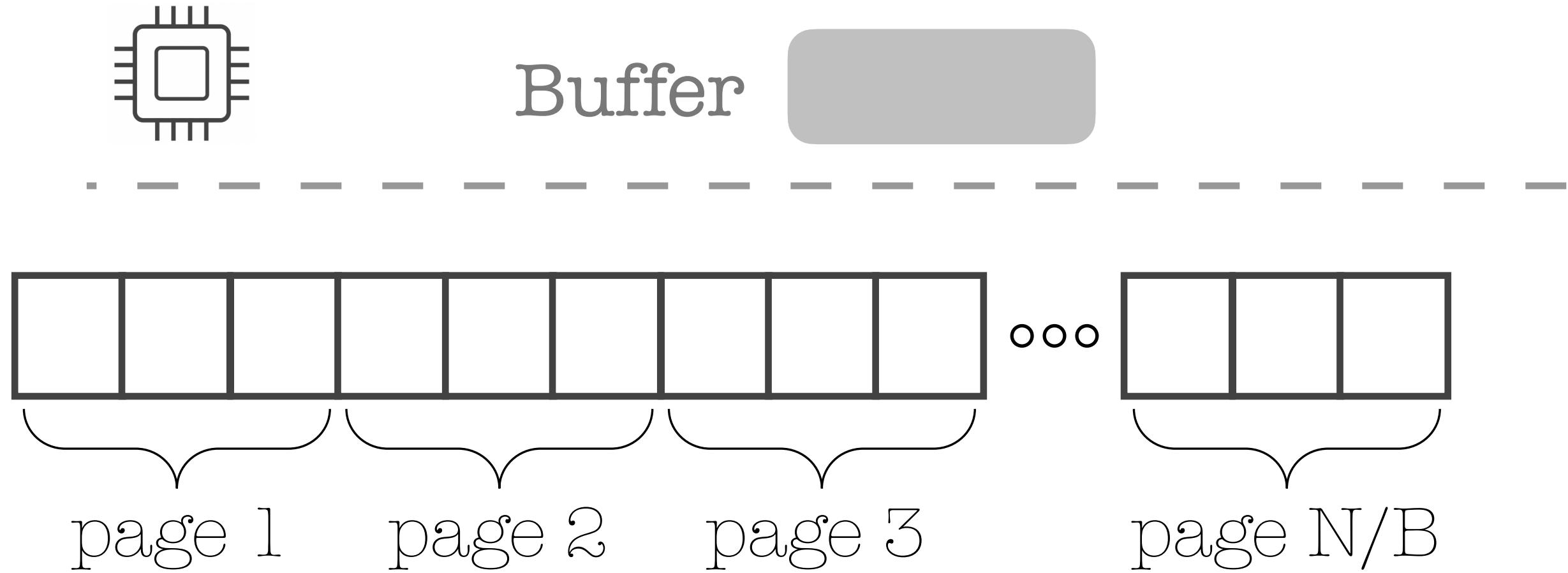
Thought Experiment 3

What is the **insert cost** in a
sorted array with a buffer?



Sorted array

Optimizing for queries



Thought Experiment 3

What is the **insert cost** in a
sorted array with a buffer?

read + write all N/B pages
for uniform data distribution

B entries are written to disk per I/O

Cost of ingestion = N/B^2

Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | ? | ? | ? |
| Log | | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | ? | ? | ? |
| Log | | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | ? | ? |
| Log | | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|---|---|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ |  |  |
| Log | | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | ? |
| Log | | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|---|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ |  |
| Log | | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | | | | |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost  | long range lookup cost | short range lookup cost |
|------------------|---|---|---|---|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log |  |  |  |  |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | ? | ? | ? |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost  | long range lookup cost | short range lookup cost |
|------------------|--------------------|---|---|---|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ |  |  |  |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ | ? | ? |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost  | long range lookup cost | short range lookup cost |
|------------------|--------------------|---|---|---|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ |  |  |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

 1.5x costlier than LSM-trees



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ | $O(N/B)$ | ? |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|---|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ | $O(N/B)$ |  |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ | $O(N/B)$ | $O(N/B)$ |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ | $O(N/B)$ | $O(N/B)$ |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ | $O(N/B)$ | $O(N/B)$ |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ | $O(N/B)$ | $O(N/B)$ |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost * | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ | $O(N/B)$ | $O(N/B)$ |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost * | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ | $O(N/B)$ | $O(N/B)$ |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ | $O(N/B)$ | $O(N/B)$ |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ | $O(N/B)$ | $O(N/B)$ |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ | $O(N/B)$ | $O(N/B)$ |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost * | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ | $O(N/B)$ | $O(N/B)$ |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost * | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ | $O(N/B)$ | $O(N/B)$ |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost



Cost analysis

Counting all I/Os

| data structure | ingestion cost | point lookup cost [*] | long range lookup cost | short range lookup cost |
|------------------|--------------------|---------------------------------|------------------------|-------------------------|
| Leveled LSM-tree | $O(L \cdot T / B)$ | $O(1 + \phi \cdot L)^*$ | $O(s \cdot N / B)$ | $O(L)$ |
| Tiered LSM-tree | $O(L / B)$ | $O(1 + \phi \cdot L \cdot T)^*$ | $O(s \cdot N / B)$ | $O(L \cdot T)$ |
| B+-tree | $O(1)$ | $O(1)$ | $O(s \cdot N / B)^*$ | $O(1)$ |
| Sorted array | $O(N/B^2)$ | $O(1)$ | $O(s \cdot N / B)$ | $O(1)$ |
| Log | $O(1/B)$ | $O(N/B)$ | $O(N/B)$ | $O(N/B)$ |

* with **fence pointers & Bloom filter** with $FPR = \phi$

cost for **non-empty lookups** (remove “ $1 +$ ” to get cost of empty lookups)

* 1.5x costlier than LSM-trees

* **Monkey** shaves off the “ L ” factor from the cost





Projects



Projects

Let's get our hands dirty

Class Project

Groups of 2

Out **tonight**; due in **December**

Multiple milestones in between

Systems project

Research project

Class Project



Projects

Let's get our hands dirty

Systems project

Research project

implementation-heavy project

develop, experiment, and analyze

Class Project



Projects

Let's get our hands dirty

Systems project

implementation-heavy project

develop, experiment, and analyze

Research project

pick a topic (list available *tonight*)

design, develop, and analyze

large-scale experimentation





Class project: Theme

Working with state-of-the-art systems



NoSQL key-value stores



RocksDB



cassandra

APACHE
HBASE



redis



Google
BigTable

amazon
DynamoDB



Class project: Theme

Working with state-of-the-art systems



NoSQL key-value stores



RocksDB

Asterix^{DB}
TM

Google
BigTable



cassandra

APACHE
HBASE



MEMCACHED

amazon
DynamoDB

redis



Systems Project 1

Developing your way through!

Implementing an LSM-based KV store

Data layout: **leveling & tiering**

File structure: **sorted run** as **one or more files**; **files** have **multiples pages**

Auxiliary data structures: **Bloom filters & fence pointers**

Granularity: filters **per sorted run / file**; fence pointers **per page**

APIs: **insert, update, delete, point** and **range queries**

Parameterize everything!



Report **all relevant performance numbers!**





Systems Project 2

Developing your way through!

Implementing Compactions on RocksDB

Working with **RocksDB — C++**

Data layout: **leveling, tiering, hybrids**

Data movement policy: **partial-level, full-level, tiered**

File picking policy: **coldest, oldest, most tombstones**

Benchmark performance for different workloads





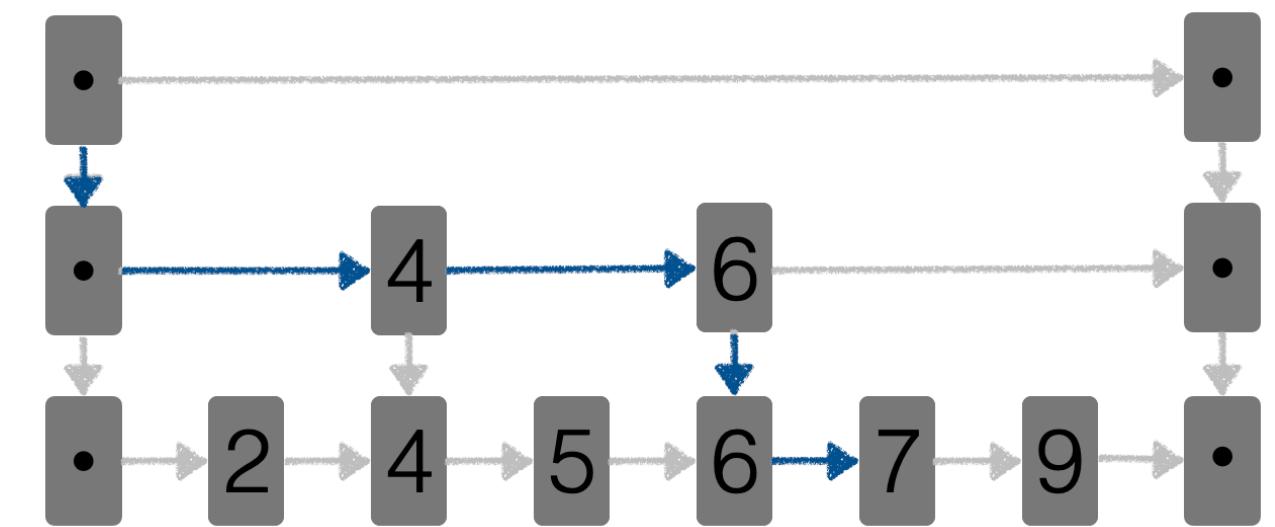
Reserach projects

Solving problems on your way through!

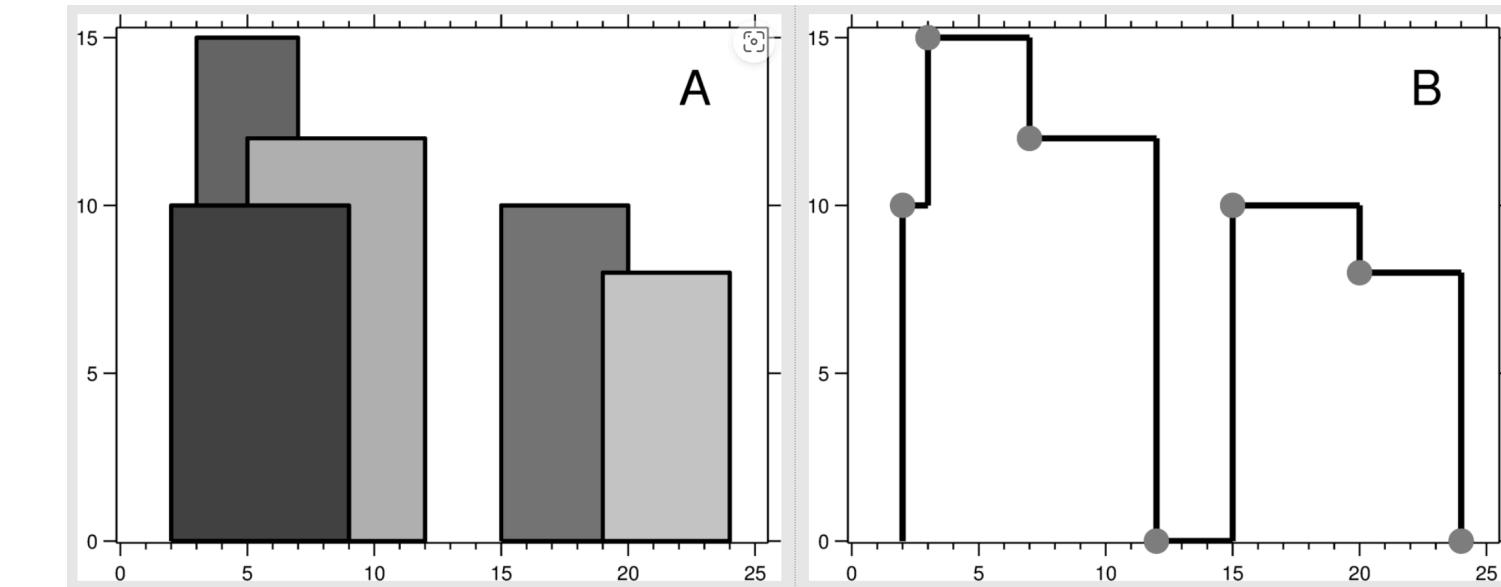


Reserach projects

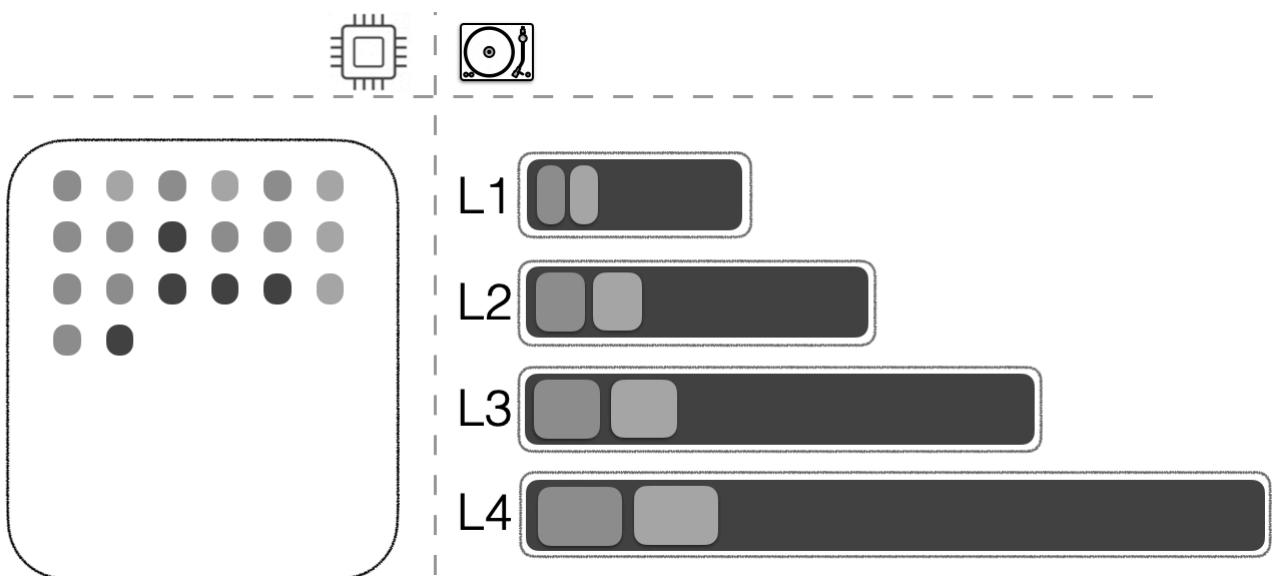
Solving problems on your way through!



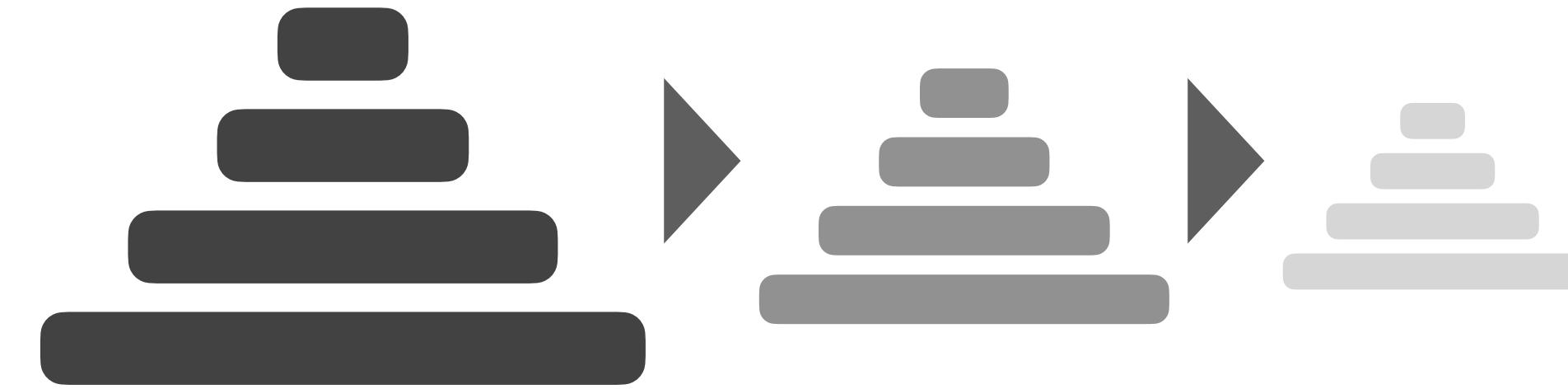
Self-designing LSM Buffer



Range Deletes in LSM



Optimal Caching in LSM

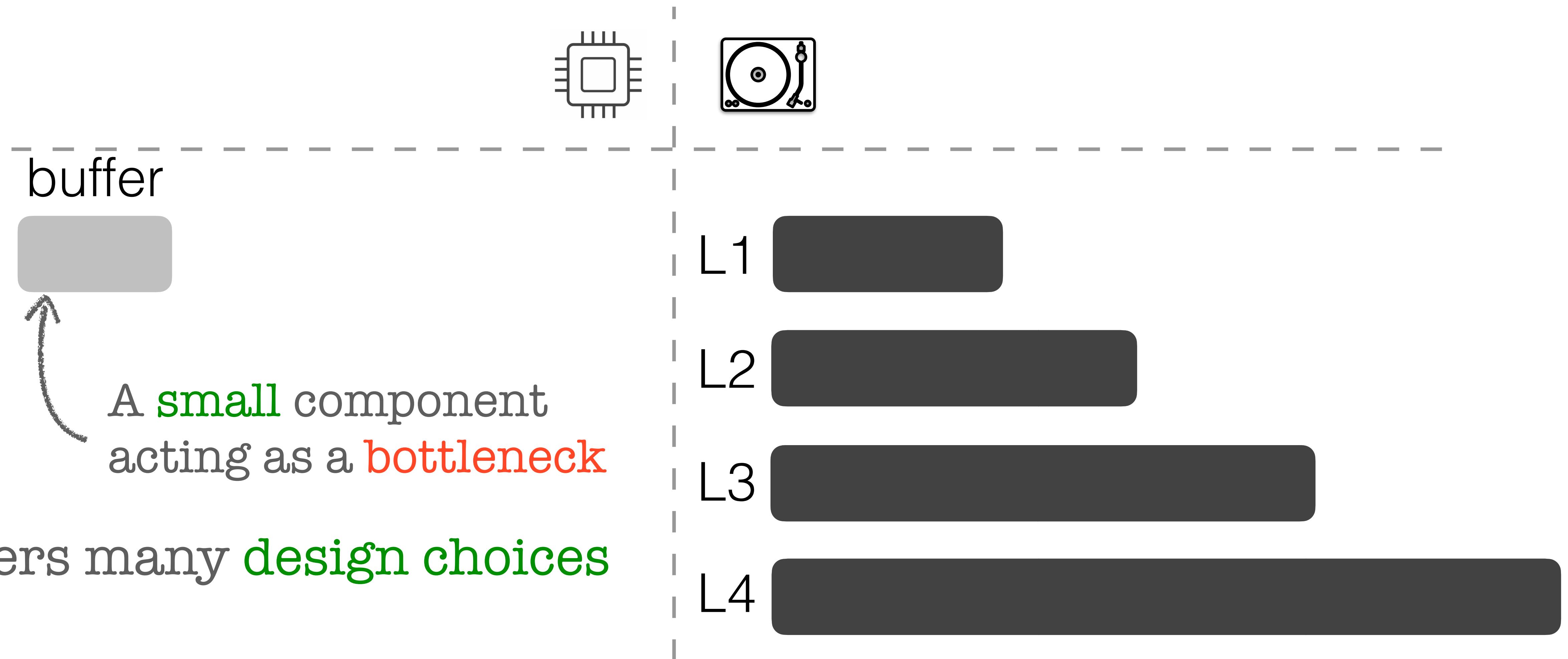


Time-Traveling LSM



Buffer Design

Buffer Design



Offers many design choices

P : pages in buffer

B : entries/page

Buffer Implementation

vector

ingestion
cost

 $\mathcal{O}(1)$

skiplist

 $\mathcal{O}(\log(P \cdot B))$

hashmap

 $\mathcal{O}(1)$

point query
cost

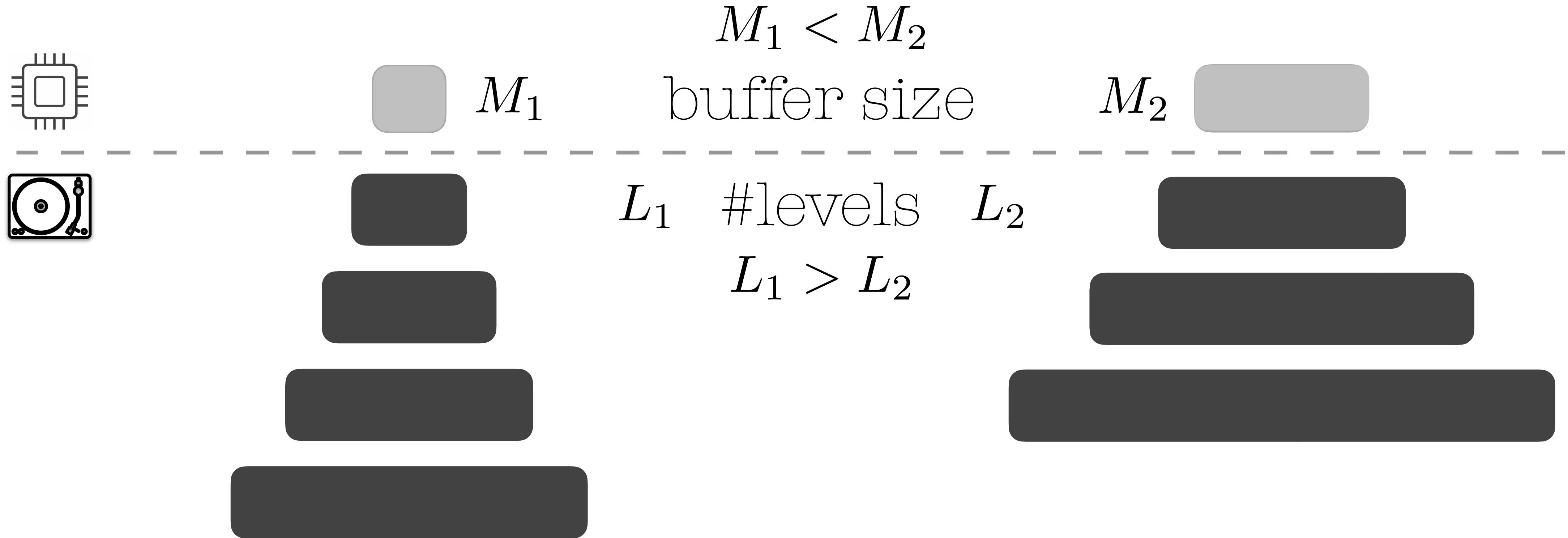
 $\mathcal{O}(P \cdot B)$ $\mathcal{O}(\log(P \cdot B))$ $\mathcal{O}(1)$

Ingestion-only
workloads

Mixed
workloads

I/O-bound
workloads

Size of the Buffer

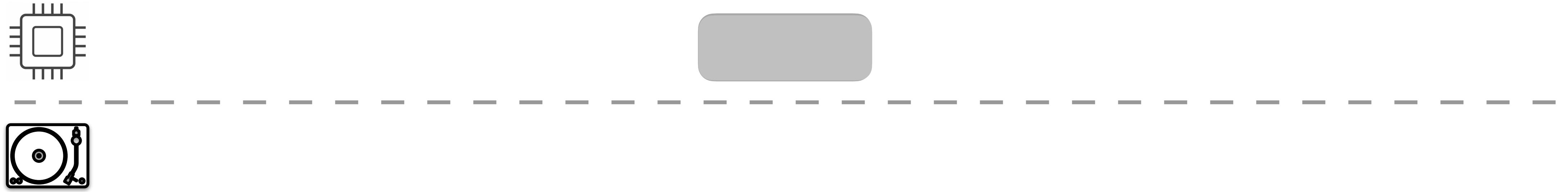


- frequent flushes
- smaller but more levels
- poor read performance

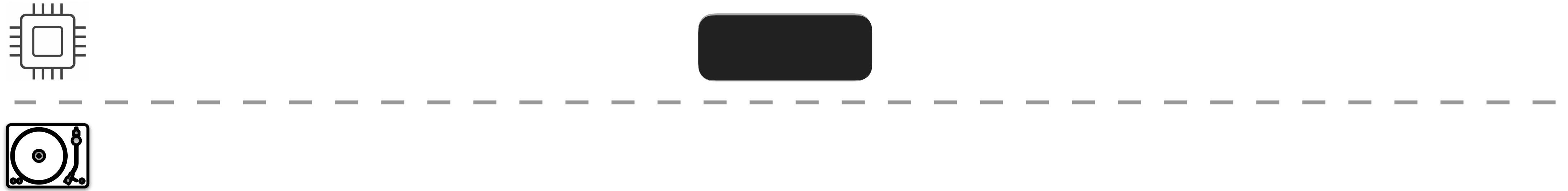
- fewer larger levels
- good for reads
- high tail latency



#Buffer Components

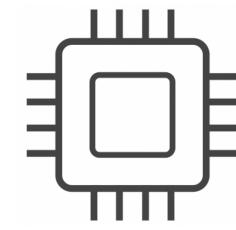


#Buffer Components



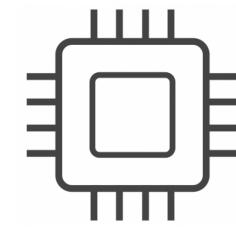
#Buffer Components

immutable
buffers



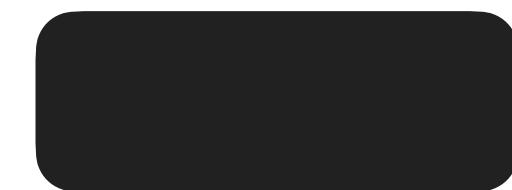
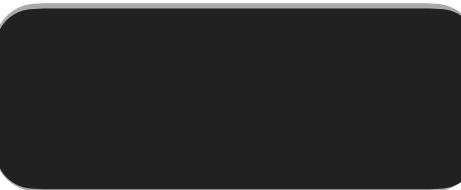
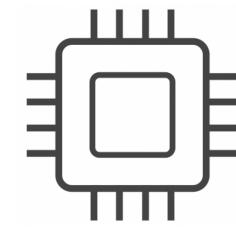
#Buffer Components

immutable
buffers



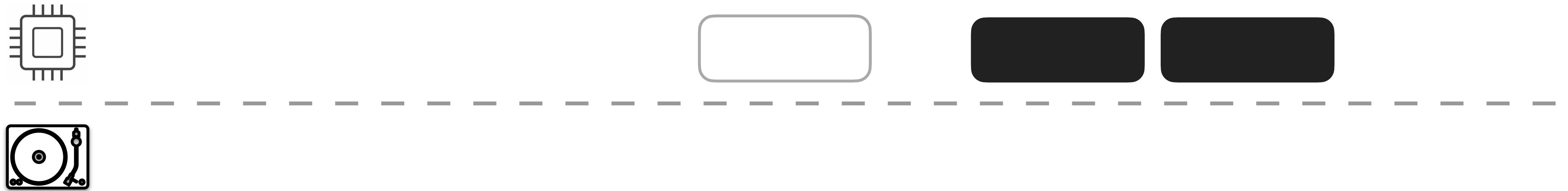
#Buffer Components

immutable
buffers



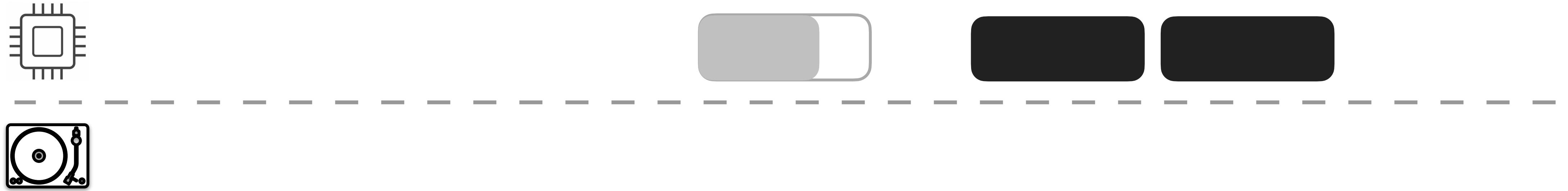
#Buffer Components

immutable
buffers



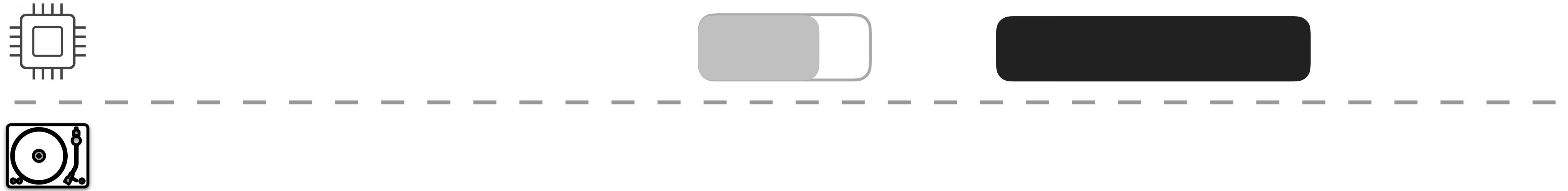
#Buffer Components

immutable
buffers



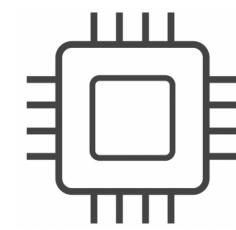
#Buffer Components

immutable
buffers



#Buffer Components

immutable
buffers



lazy flushing

- avoid write stalls
- improved ingestion throughput
- better bandwidth utilization
- requires more memory



Research Project 1

Solving problems on your way through!

Self-designing LSM Buffer

Which buffer implementation to choose?

How to tune the particular buffer implementation?

What if the **workload changes**?

What if the **application requirements** change?

Benchmark performance for different workloads & performance goals

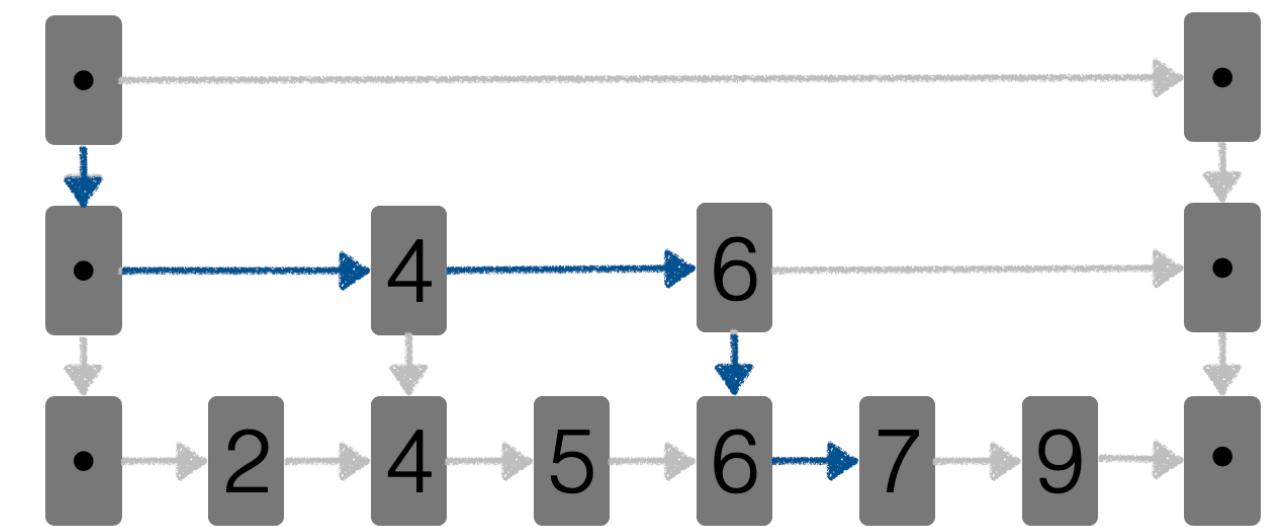
Design an **ML-based optimizer**

Integrate the **self-designing buffer** with RocksDB

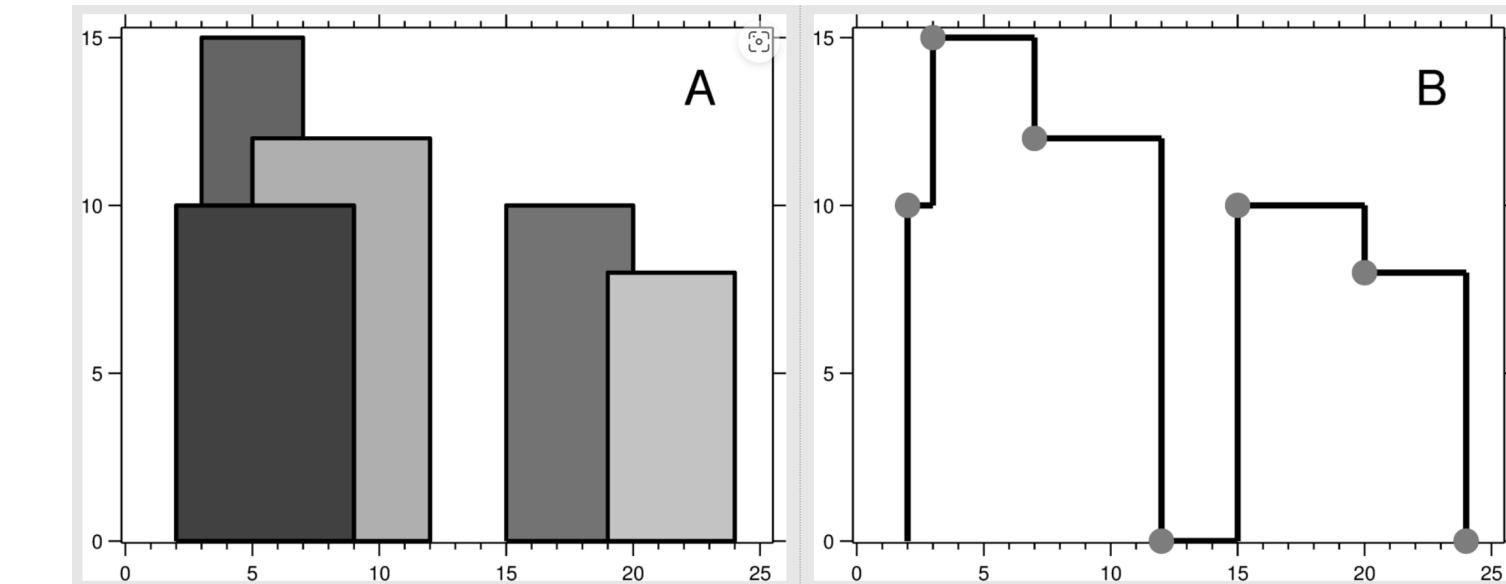


Reserach projects

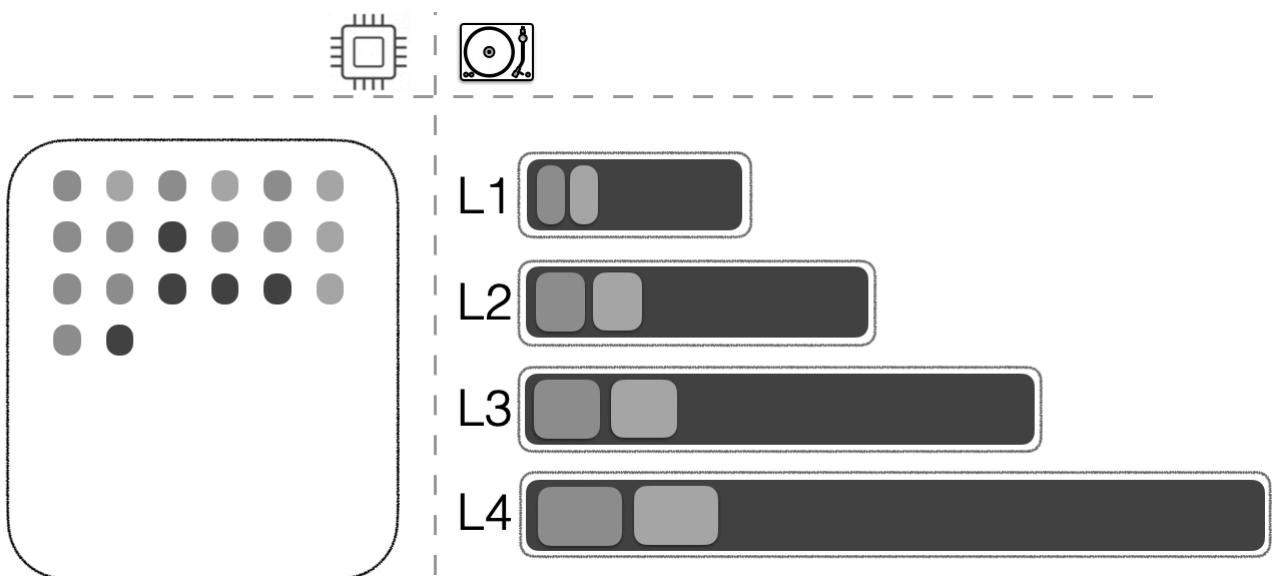
Solving problems on your way through!



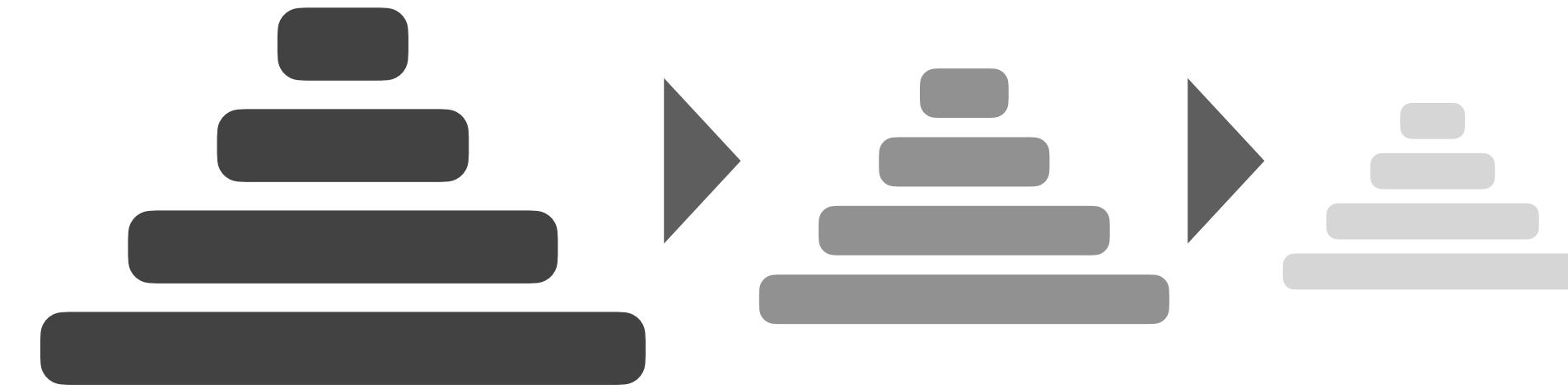
Self-designing LSM Buffer



Range Deletes in LSM



Optimal Caching in LSM



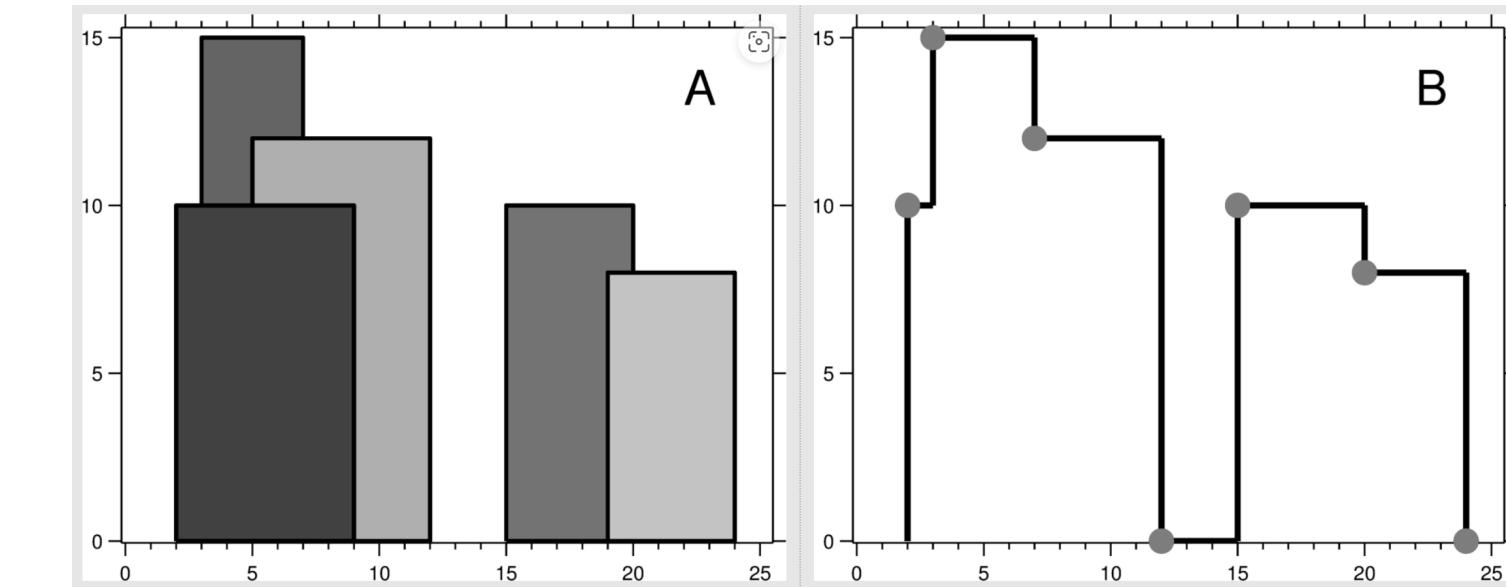
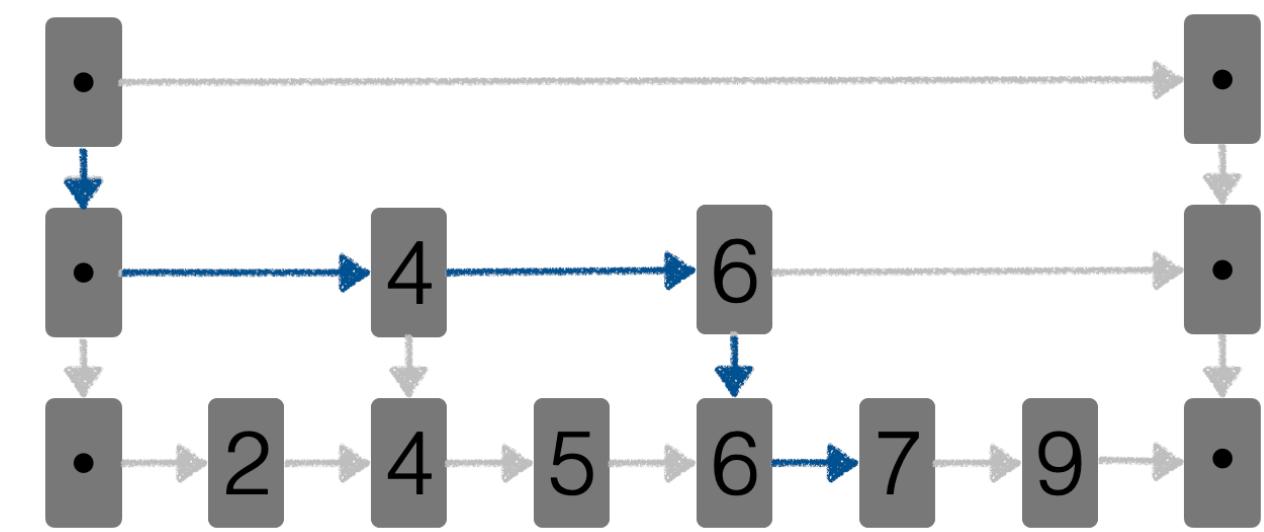
Time-Traveling LSM





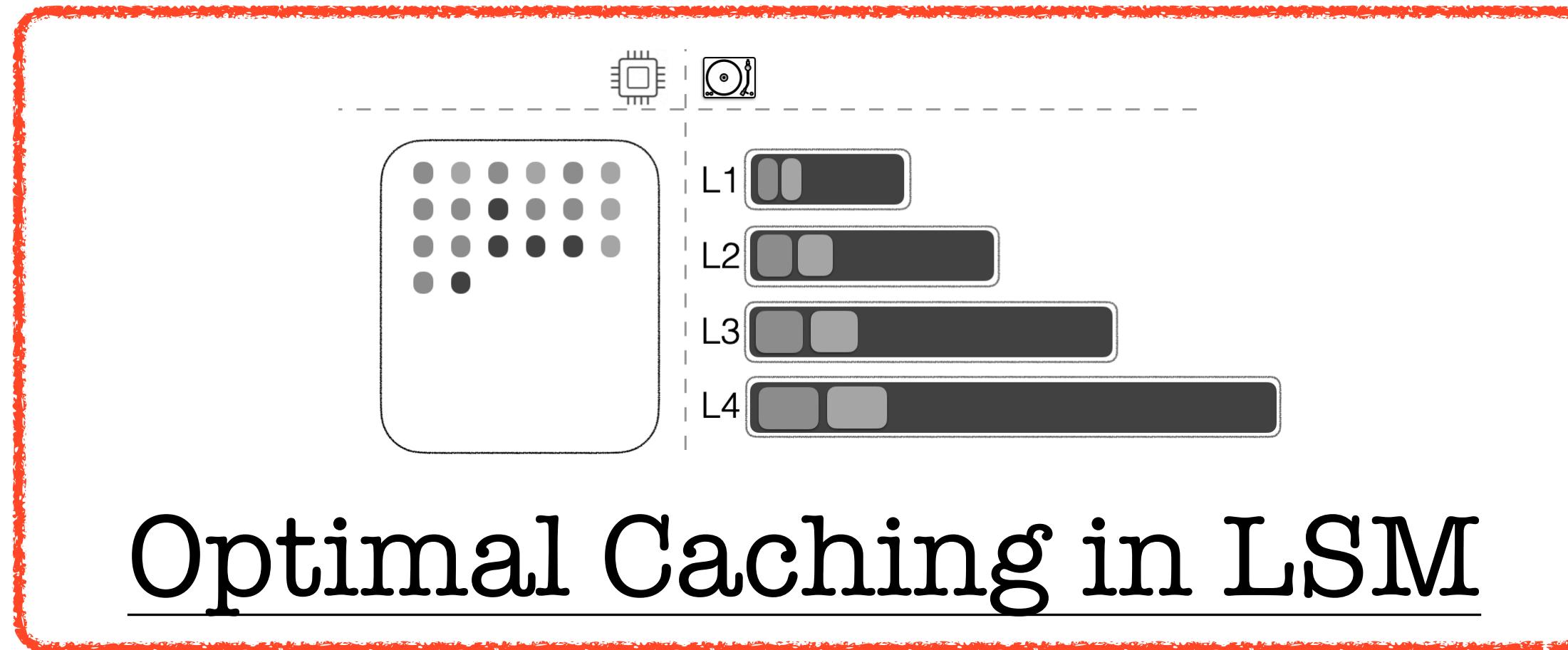
Reserach projects

Solving problems on your way through!

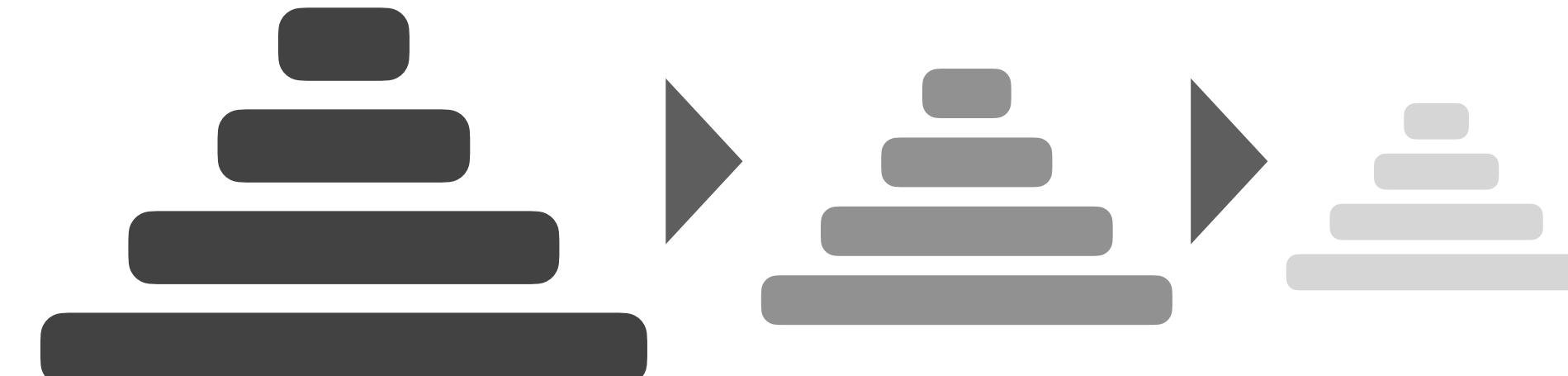


Self-designing LSM Buffer

Range Deletes in LSM



Optimal Caching in LSM

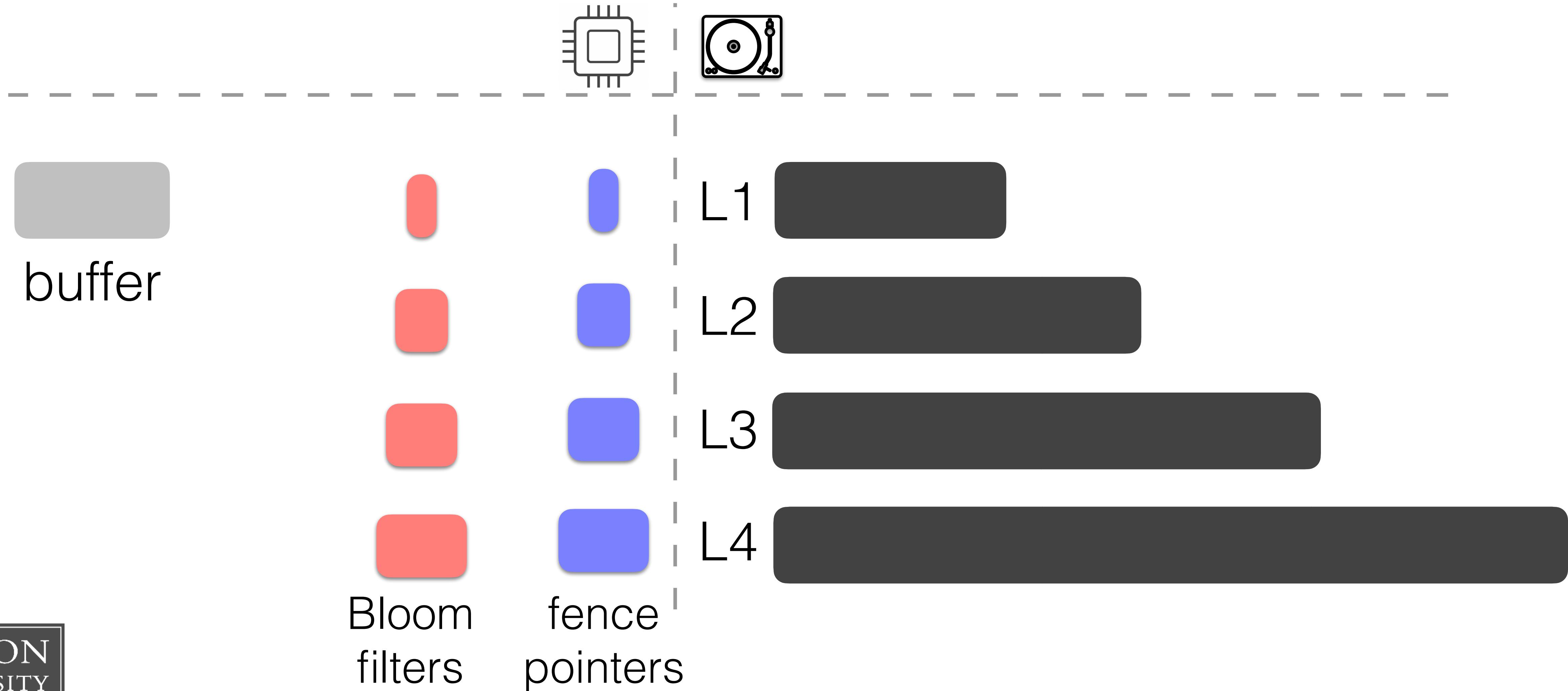


Time-Traveling LSM



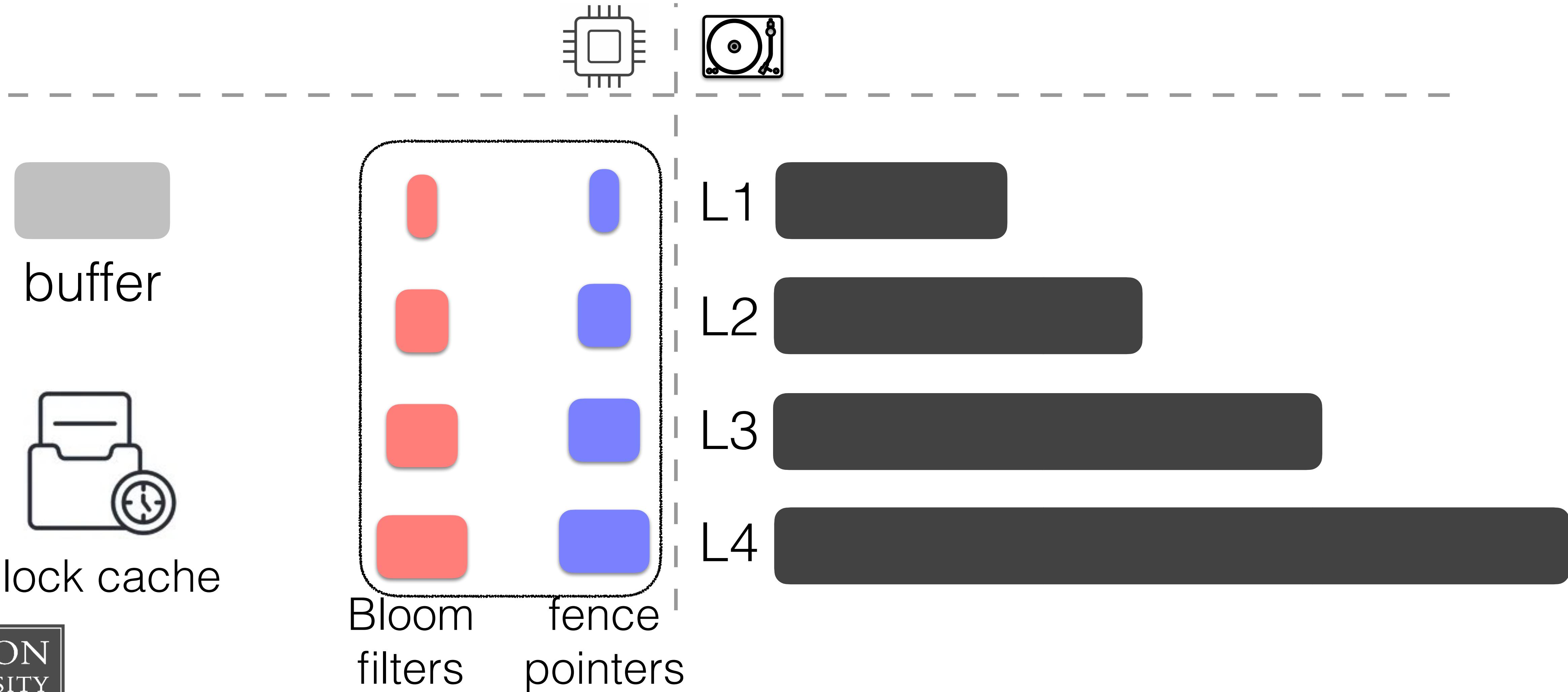
Block cache

Saving trips to disk



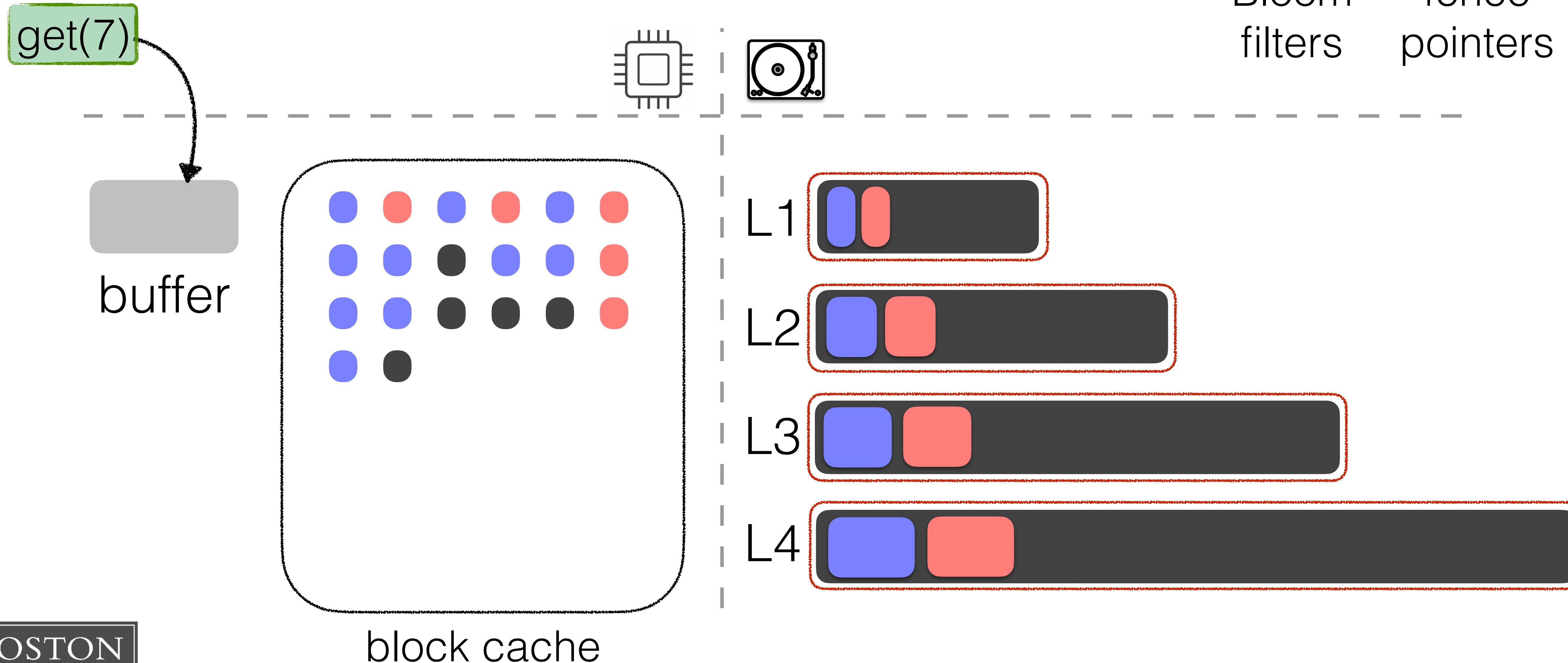
Block cache

Saving trips to disk



Block cache

Saving trips to disk





Research Project 2

Solving problems on your way through!

Optimal Caching in LSM

Memory is finite!

How useful is **block-based caching**?

Which blocks to cache: **index, filter, data**?

What is the impact of **pinning blocks**?

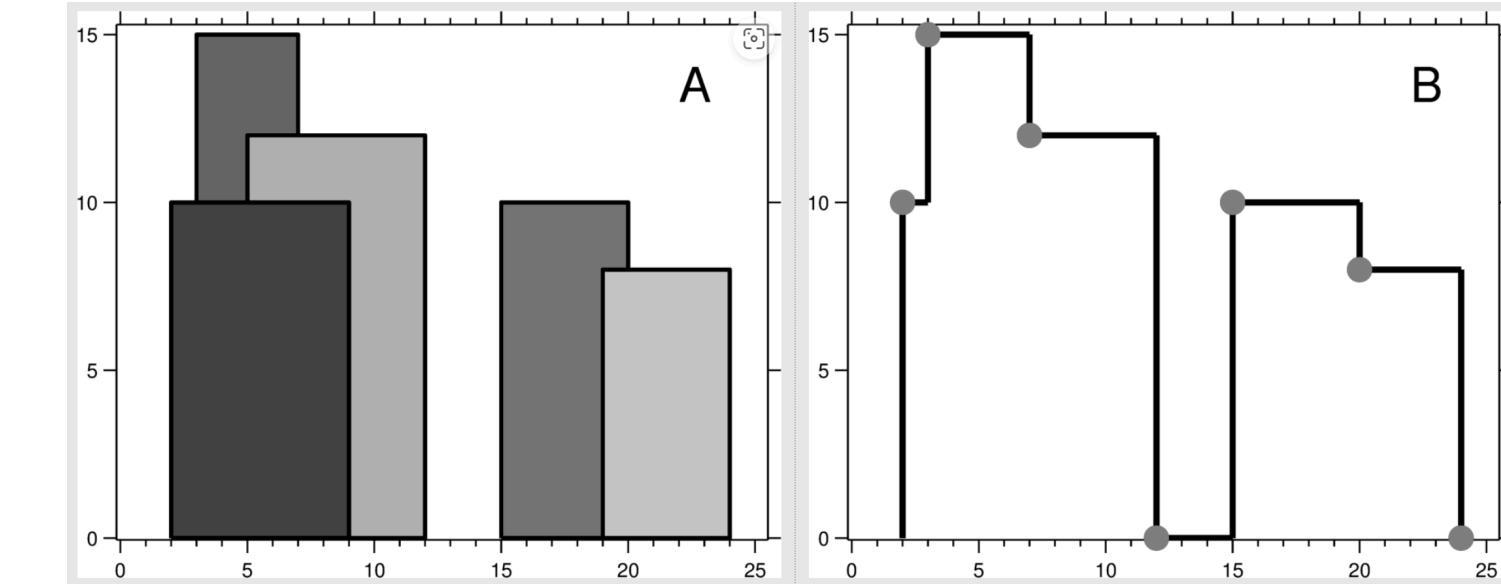
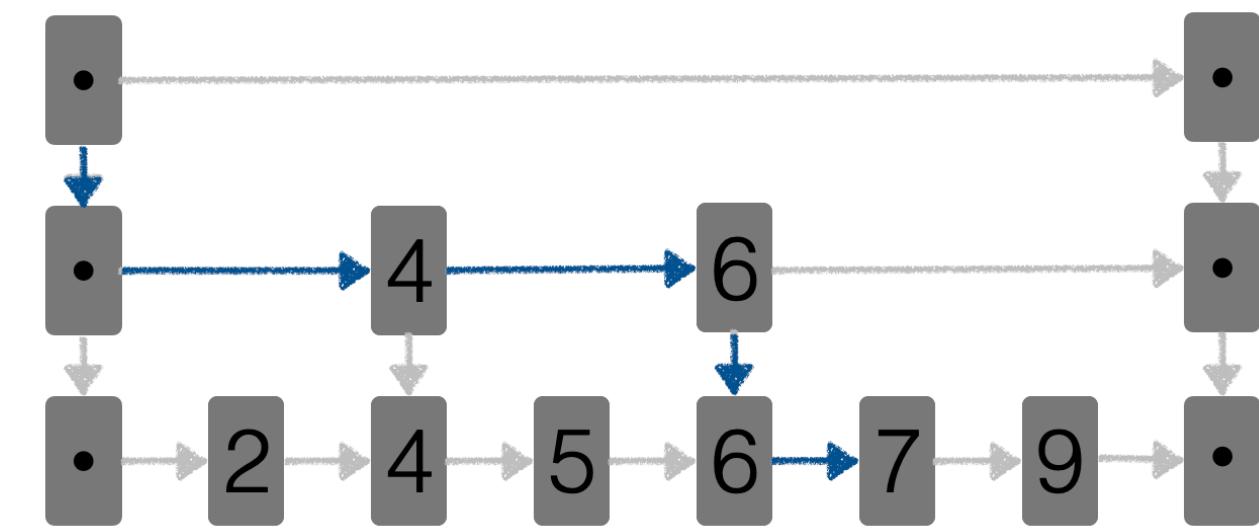
Which blocks to **evict**?

Benchmark performance for different caching schemes



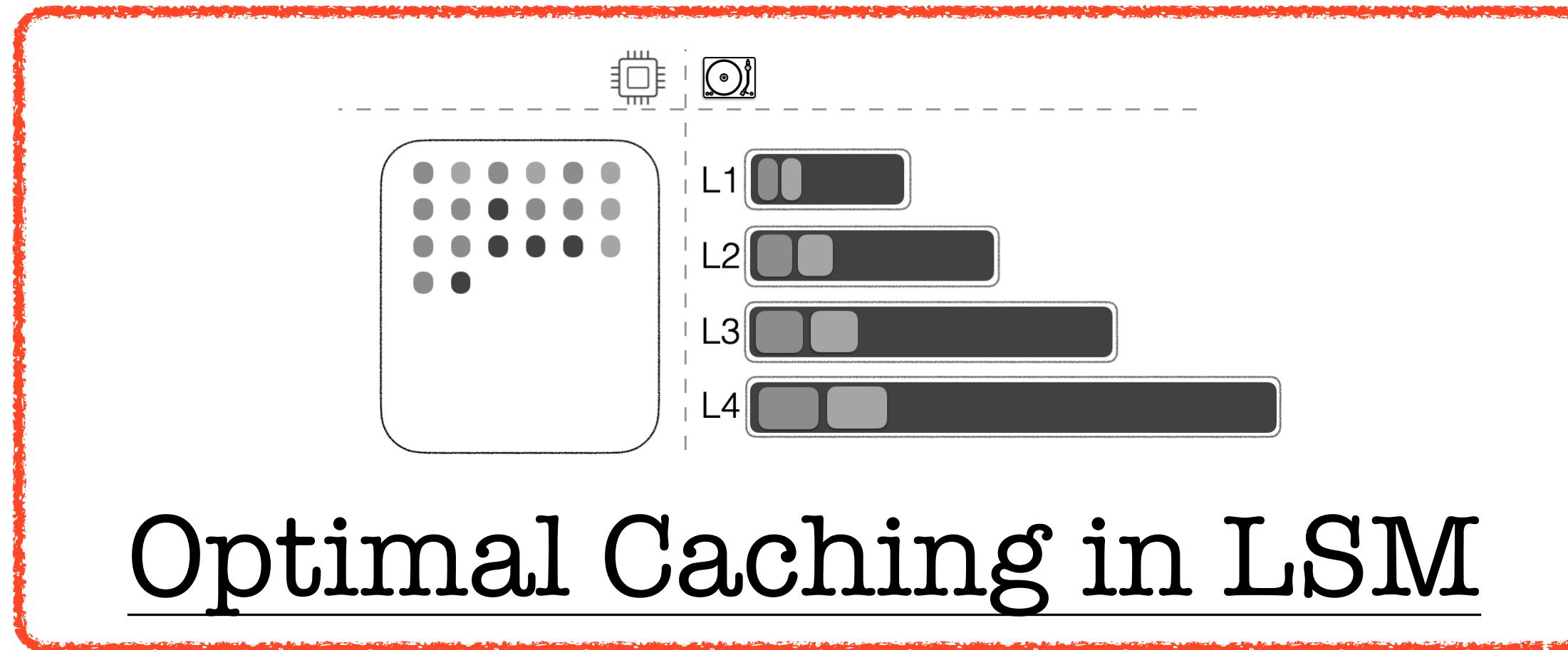
Reserach projects

Solving problems on your way through!

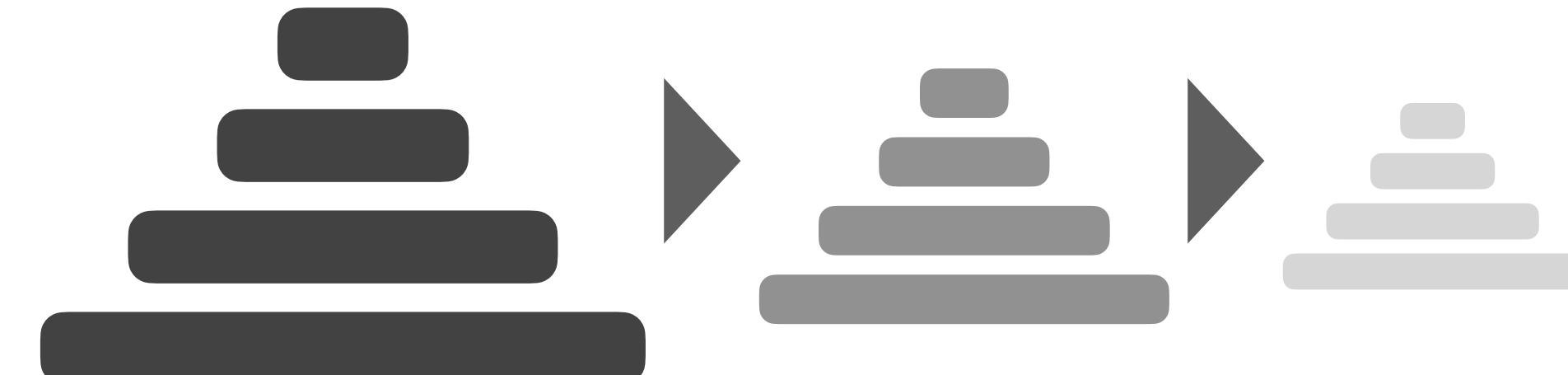


Self-designing LSM Buffer

Range Deletes in LSM



Optimal Caching in LSM



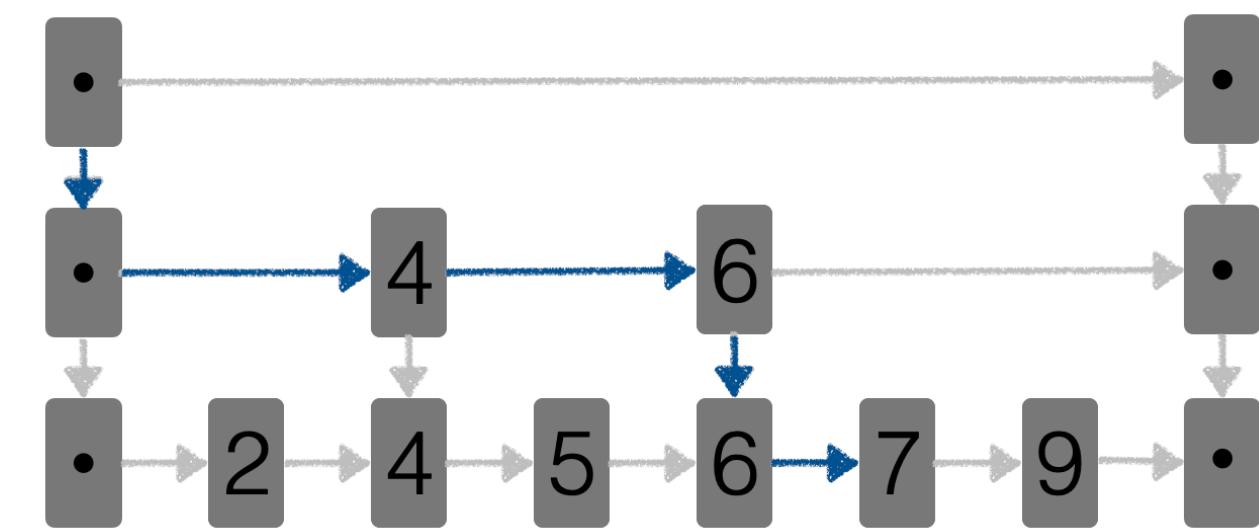
Time-Traveling LSM



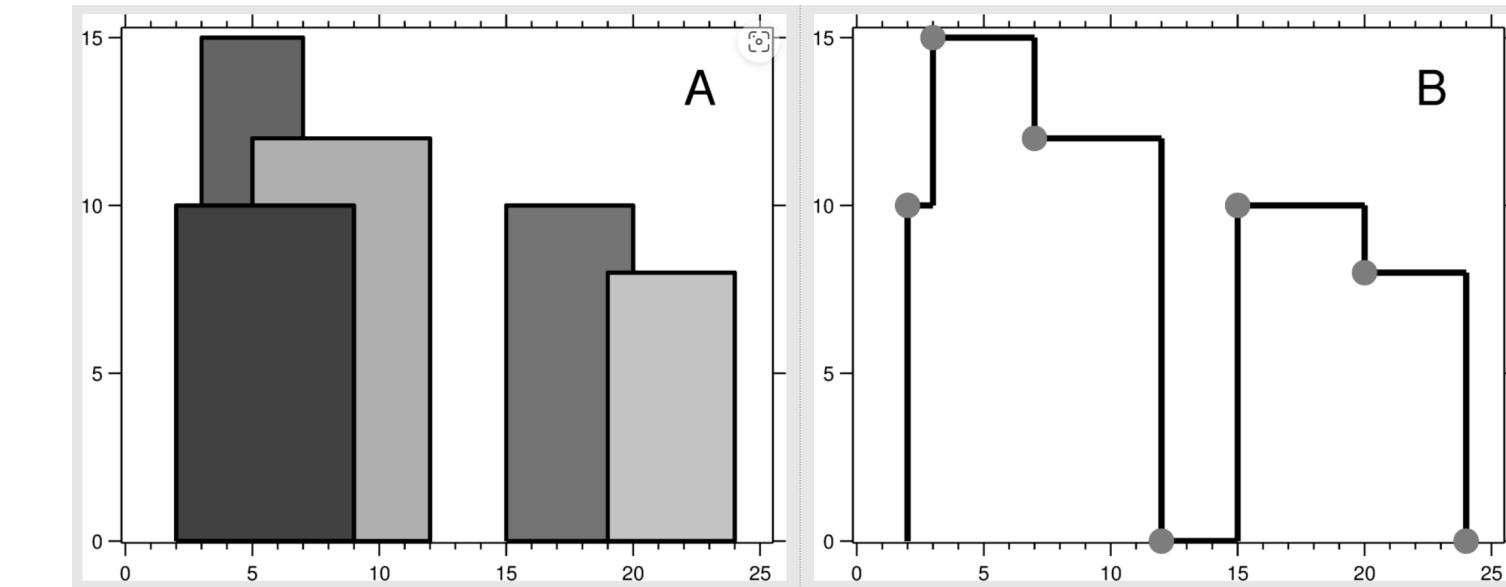


Reserach projects

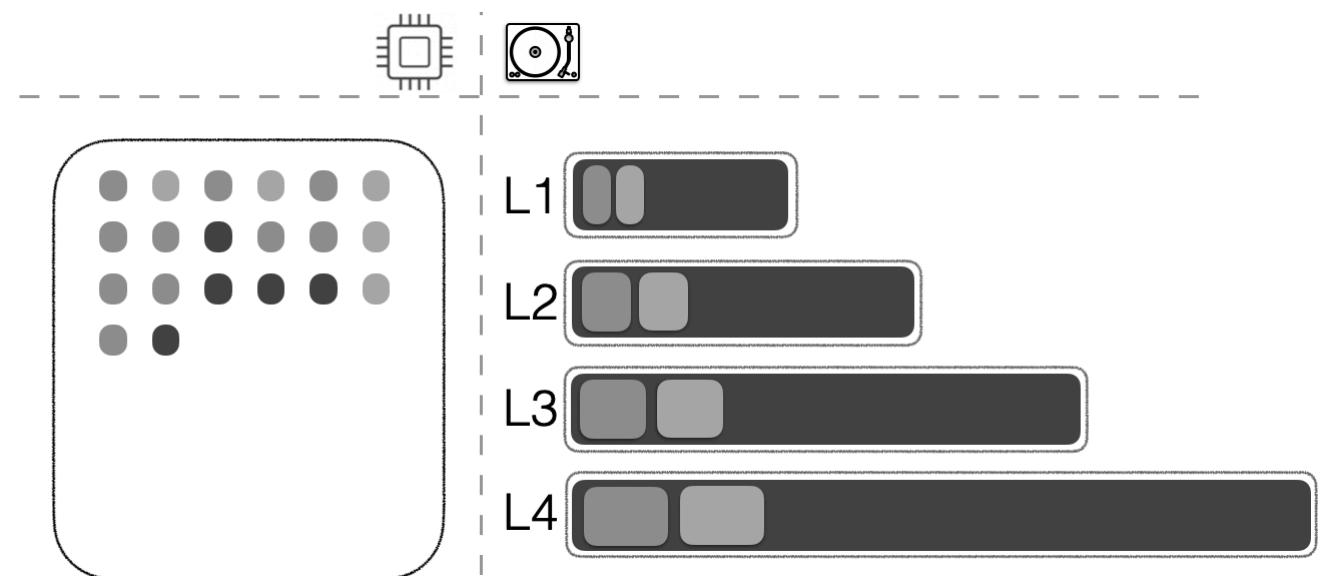
Solving problems on your way through!



Self-designing LSM Buffer



Range Deletes in LSM



Optimal Caching in LSM



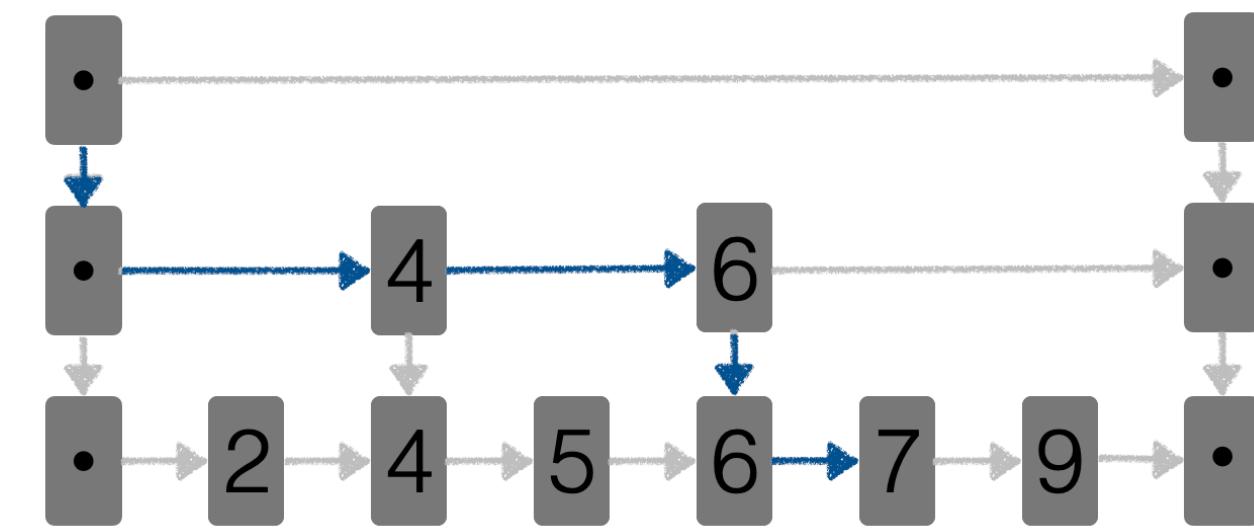
Time-Traveling LSM



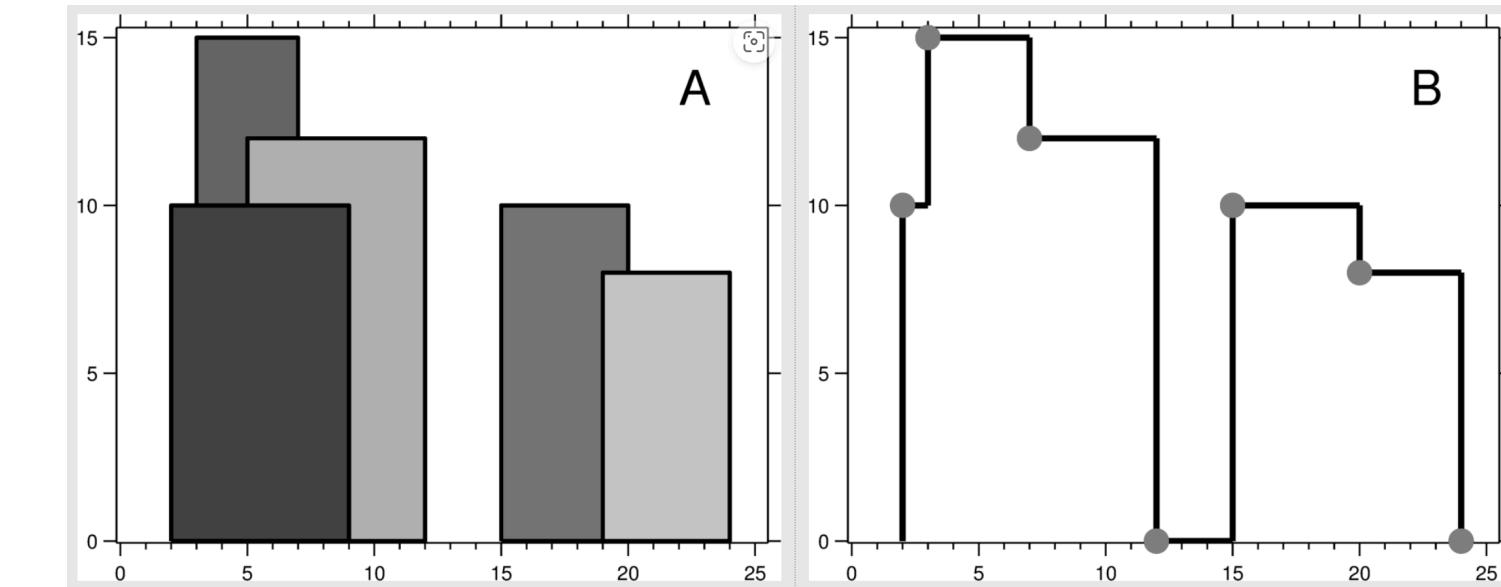


Reserach projects

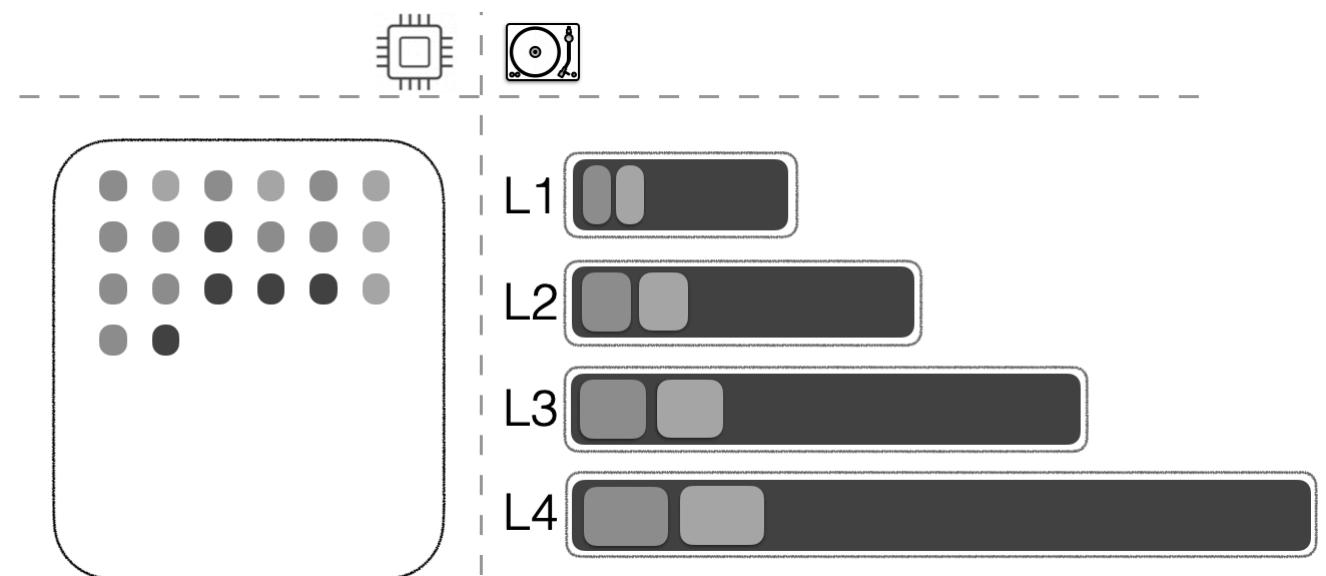
Solving problems on your way through!



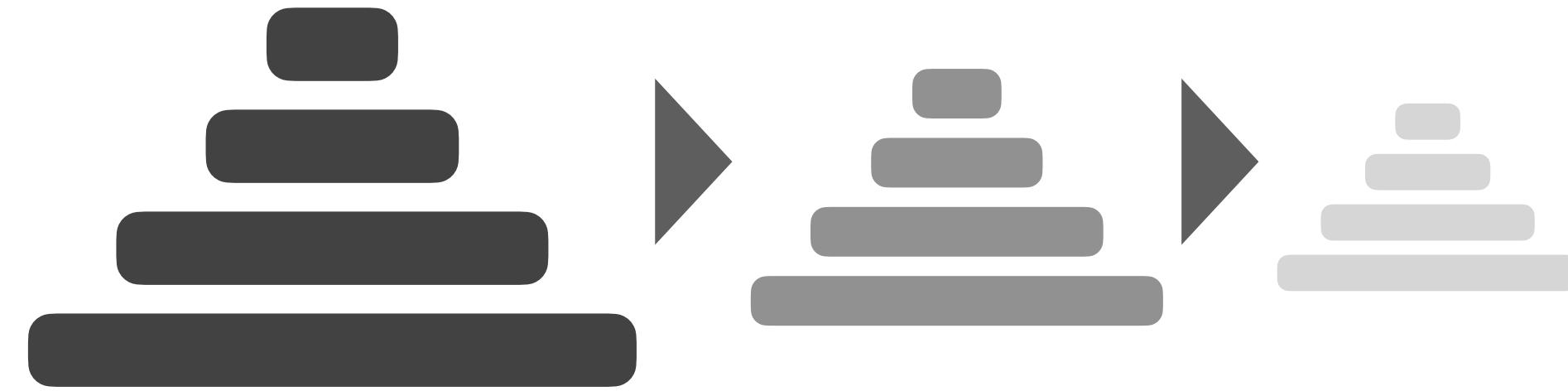
Self-designing LSM Buffer



Range Deletes in LSM



Optimal Caching in LSM



Time-Traveling LSM



Next time in COSI 167A

More on LSMs

LSM buffer design space

[P] ["Anatomy of the LSM Memory Buffer: Insights & Implications"](#), DBTest, 2024

TECHNICAL QUESTION 3 [How does the memory allocation strategy affect the query latency for a pre-allocated vector vs. a dynamically allocated one? Given a workload, how would do decide the prefix length for a hash-hybrid buffer implementation?](#)

[B] ["Breaking Down Memory Walls: Adaptive Memory Management in LSM-based Storage Systems"](#), VLDB, 2020

COSI 167A

Advanced Data Systems

Class 7

Class Projects

Prof. Subhadeep Sarkar

<https://ssd-brandeis.github.io/COSI-167A/>

