

# Sorting Algorithms: Comparison and Analysis

## Introduction

Sorting algorithms are fundamental in computer science for arranging data in a specific order. Different algorithms have varying performance characteristics depending on input size and nature.

## Common Sorting Algorithms

| Algorithm             | Type                          | Best Case     | Average Case  | Worst Case    | Space Complexity | Stable? |
|-----------------------|-------------------------------|---------------|---------------|---------------|------------------|---------|
| <b>Bubble Sort</b>    | Comparison                    | $O(n)$        | $O(n^2)$      | $O(n^2)$      | $O(1)$           | Yes     |
| <b>Selection Sort</b> | Comparison                    | $O(n^2)$      | $O(n^2)$      | $O(n^2)$      | $O(1)$           | No      |
| <b>Insertion Sort</b> | Comparison                    | $O(n)$        | $O(n^2)$      | $O(n^2)$      | $O(1)$           | Yes     |
| <b>Merge Sort</b>     | Comparison / Divide & Conquer | $O(n \log n)$ | $O(n \log n)$ | $O(n \log n)$ | $O(n)$           | Yes     |
| <b>Quick Sort</b>     | Comparison / Divide & Conquer | $O(n \log n)$ | $O(n \log n)$ | $O(n^2)$      | $O(\log n)$      | No      |
| <b>Heap Sort</b>      | Comparison / Heap             | $O(n \log n)$ | $O(n \log n)$ | $O(n \log n)$ | $O(1)$           | No      |
| <b>Counting Sort</b>  | Non-comparison                | $O(n+k)$      | $O(n+k)$      | $O(n+k)$      | $O(k)$           | Yes     |
| <b>Radix Sort</b>     | Non-comparison                | $O(nk)$       | $O(nk)$       | $O(nk)$       | $O(n+k)$         | Yes     |

*Note:*  $n$  = number of elements,  $k$  = range of input values

## Time Complexity Comparison

Sorting algorithms can be visualized in terms of time complexity, where array size ( $n$ ) is on the x-axis and runtime is on the y-axis.

## Observations

- **Bubble, Selection, Insertion:** Quadratic time; inefficient for large arrays.
- **Merge, Quick, Heap:** Linearithmic time; efficient for large arrays.
- **Counting, Radix:** Nearly linear time if  $k$  is small; suitable for integer keys.

## Conclusion

Choosing a sorting algorithm depends on input size, data type, and stability requirements. For small arrays, insertion or bubble sort is acceptable. For large datasets, merge, quick, or heap sort is recommended. Non-comparison sorts excel when data has specific constraints.

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