Bit Manipulation

Bitwise operators and their application

Note: Time complexity of all the bitwise operator are approx O(1)

        => bitwise AND
| => bitwise OR
^   => bitwise XOR
>>   => bitwise Right shift
<<   => bitwise Left shift
~   => bitwise NOT

Note that & (bitwise AND) is different from && (logical AND) , | (bitwise OR) is different from || (logical OR) and ~ (bitwise NOT) is different from ! (logical NOT)

Rules->
      AND

                0&0=0
                0&1=0
                1&0=0
                1&1=1

OR

                0&0=0
                0&1=1
                1&0=1
                1&1=1

XOR

                0&0=0
                0&1=1

$$1\&0=1$$
$$1\&1=0$$

Properties of XOR:
$$a\text{\textasciicircum}a=0$$
$$0\text{\textasciicircum}a=a$$

NOT
$$\sim0=1$$
$$\sim1=0$$

```
int a=5 (101), b=7 (111);
cout << a&b ;   // (101) & (111)=(101)=5
cout << a|b ;   // (101) | (111)=(111)=7
cout << a^b ;   // (101) ^ (111)=(010)=2
cout << ~a ;    // ~(101)=(010)=2
```

Left shift operator(<<)
>   a   ->   0000001110
>   a<<1 -> 000011100

Right shift operator(>>)
>   a   ->   0000001110
>   a>>1 ->   0000000111

E.g   int a=5;
>   a=a<<1; // then a? = 10   (2*a);
>   a=5;
>   a=a>>1; // then a? = 2   (a/2) e.g (5/2)=2;

Sol
>   a=5(00101);
>   a<<1 -> (01010) = 10;

Q.) You are given a number and find the value of (a<<b)?

Ans: $a*(2^b)$

Q.) You are given a number and find the value of (a>>b)?

Ans: $a/(2^b)$

Why?   2^3   2^2   2^1   2^0 (2^2+2^0=5)
a=5 =>   0   1   0   1
a<<1 =>   1   0   1   0

(2^3+2^1)=2(2^2+2^0)=2*a;

Thus, (1<<n) is equivalent to 2^n

Q.) You are given an array of N numbers in which all the numbers are repeated twice except one number which is present exactly once then find out that number?
Link: https://www.hackerrank.com/challenges/lonely-integer/problem

e.g-> {2,3,4,4,2} so Answer=3;

Hint-> use XOR property
a^a=0;
a=5 => (101) then a^a (101)^(101) = (000)=0;
If we use xor of all the numbers present in the array i.e
2^3^4^4^2 = 3

If And-> (1&2&4&4&2)=>(1&2&3&4) No Need.

```cpp
int main()
{
int n;
cin>>n;
vector<int> arr(n);
for(int i=0;i<n;i++) cin>>arr[i];
int ans = 0;
for(int i=0;i<n;i++){
ans=ans^arr[i];
```

```
}
cout<<ans;
}
```

Q.) You have to check whether the given number is odd or even but you are not allowed to use % operator then how do you do that?

a=5-> (0101)
b=10-> (1010)
a&1=>(0101)&(0001)=(0001)=1
b&1=>(1010)&(0001)=(0000)=0

```
if((a&1)==1){
cout<<"ODD"<<endl;
}
else {
cout<<"EVEN"<<endl;
}
```

Q.) How to check whether ith bit (from right) is 1 or 0 for the given input number n.

001010101010
….43210 (index)
0->0
1->1
(1<<i) -> 000000010000000
i

Answer:

```
if(n&(1<<i))
{
    cout<<"i-th bit is set"<<endl;
}
else
```

```
{
    cout<<"i-th bit is not set"<<endl;
}
```

Q.) How to set the ith bit to 1 for the given input number n;

Ans:
n = n|(1<<i);

Q.) How to set the ith bit to 0 for the given input number n;
Ans:
n=n&(~(1<<i))

```
            a-> 0000010101010100000
                        i
       (1<<i)   0000000010000000000
       ~(1<<i)  11111111101111111111
```

Q.) How to calculate the number of setbits(1) in the given number.
0<=n<=2^63-1
Sol:-
```
    long long n;   // 0<=n<=2^63-1
    cin>>n;
    long long ans=0;
 // ans stores the number of set bits
    for(int i=0;i<64;i++){
  // 1<<i -> int
  // 1LL<<i -> long long int
        if(n&(1LL<<i)){
            ans++;
        }
    }
    cout<<ans;
```

Q.) How to swap two numbers using the XOR operator.
Sol: $(x\wedge y)\wedge y \rightarrow x$

$(x\wedge y)\wedge x \rightarrow y$

$x = x\wedge y;$ // $x = x\wedge y, y=y$

$y = x\wedge y;$ // $y = (x\wedge y)\wedge y \rightarrow x$ // $x = x\wedge y, y = x$

$x = x\wedge y;$ // $x\wedge y\wedge x = y$ // $x=y, y=x$

Q.) How to generate all possible non empty subsequences of the given string.

e.g-> (abc) has following subsequences:
a,b,c,ab,bc,ac,abc

Subsequence -> delete some elements from anywhere in the string and concatenate the remaining.
Eg abcdefgh -> del c,f,h -> abdeg
Substring -> delete some elements from the beginning and some from the end.
Eg abcdefgh -> del a,b from begin and g,h from end
-> cdef

Sol :-
Assume that length of string is n.
Represent any subsequence of this string as a binary number of length n.
Eg abc -> binary number of length 3
If binary digit is 1 -> then that char is present in this sequence.
Else it is deleted.
abc
110 -> ab 1 to 7 -> 001,010,011,100,101,110,111
                    ->   c, b , bc, a   ,ac ,ab , abc
101-> ac
N -> 1 to $2\wedge n-1$

```cpp
vector<string> seq;
// stores all non empty subsequences
   string s;
   cin>>s;
```

```cpp
int n = s.length();
//n<=15
for(int i=1;i<(1<<n);i++){   // 1 to 2^n-1
    string temp="";
    for(int j=0;j<n;j++){
        if(i&(1<<j)){   // if jth bit in i is set
            temp+=s[j];
        }
    }
    seq.push_back(temp);
}
for(int i=0;i<seq.size();i++){
    cout<<seq[i]<<" ";
}
```

Q. https://www.hackerrank.com/challenges/and-product/problem

N queries -> a and b
Output a&(a+1)&(a+2)...b
12 and 15 -> 1100 and 1111 -> 1100 ->   12
14 15 -> 1110 and 1111 -> 1110 -> 14
1001 and 1101 -> 1000 -> 8
1001&1010&1011&1100&1101 -> 1000 - >8
01111 and 10000 -> 0

```cpp
string x;
for(int i=31;i>=0;i--){
    if(a&(1<<i)){
        x+='1';
    else{
        x+='0';
}
```

```cpp
while(a){
    int x = a%2;
```

```
        x+=('0'+x);
        x/=2;
    }
    reverse(x.begin(),x.end());
```

Q. https://www.hackerrank.com/challenges/sansa-and-xor/problem

3 4 5
3
4
5
3,4
4,5
3,4,5
Answer=> (3)^(4)^(5)^(3^4)^(4^5)^(3^4^5)

-> If occurence is even then don't take it.
    4 -> a^a^a^a = 0
-> If occurence is odd then include it in your answer.
    5 -> a^a^a^a^a = a

```
int sansaXor(vector<int> arr) {
    int ans=0;
    int n=arr.size();
    for(int i=0;i<n;i++){
        long occ=(i+1)*(n-i);
        if(occ&1) ans^=arr[i];
    }
    return ans;
}
```