

String Algorithms and Trie

Youtube link :

<https://youtu.be/Fn9u8CMTVEw>

Contents:

1. String Matching Algorithms
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String Matching Algorithms

Q. Given a string S and a pattern P, find all the occurrences of P in S.

Brute Force / Naive Approach

S: a b a b c a b c a b a b a b d

P: a b a b d

✓✓✓✓x

S: a b a b c a b c a b a b a b d

P: a b a b d

x

S: a b a b c a b c a b a b a b d

P: a b a b d

✓✓x

S: a b a b c a b c a b a b a b d

P: a b a b d

x

We are sliding pattern by 1 step right, if a mismatch occurs.

Visualise at:

<http://whocouldthat.be/visualizing-string-matching/>

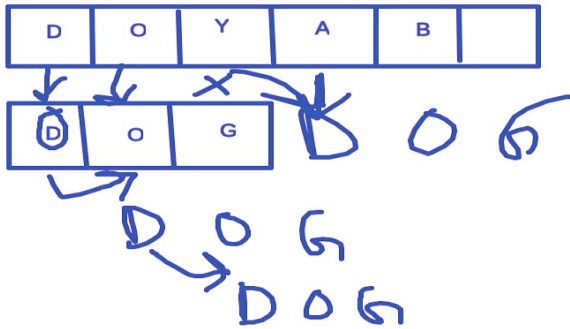
s.length(); // gives length of string s

```
// m = length of given string S
// n = length of given pattern P

for(int i=0; i<=m-n; i++)
{
    for(int j=0; j<m; j++)
    {
        if(S[i]!=P[j])
            break;
    }
    if(j==m)
    {
        cout<<"Pattern found at "<<i;
    }
}
```

Time Complexity: $O(n * m)$

Intuition for KMP



In the example on left, we can shift the pattern by 2 steps, instead of shifting by 1 (since all characters of pattern are distinct)

```
0 1 2 3 4 5 6
S: D E A D E L E P Q S R
P: D E A D E Y E
    0 1 2 3 4 5 6
    ✓✓✓✓✓✗
```

We can move i to 5 and j to 2 and repeat this process, in above example. (Instead by shifting the pattern only by 1 step)

Intuition: In pattern, find where the prefix of pattern is repeating.

LPS Array (Longest Prefix Suffix Array):
(also called "Pi array" or "Failure Function")

$LPS[i]$ = Longest proper prefix of the string that is also a suffix of $string[0 \dots i]$

Proper prefix: Prefix of a string which is not the same as the given string. Prefix means any substring from the starting.

Suppose , $s = \text{"ababcdef"}$

Proper Prefixes of s are $a, ab, aba, ababc, ababcd$, etc.

But $ababcdef$ is not a proper prefix.

Suffix: Any substring from the end of the string

Suppose , $s = \text{"ababcdef"}$

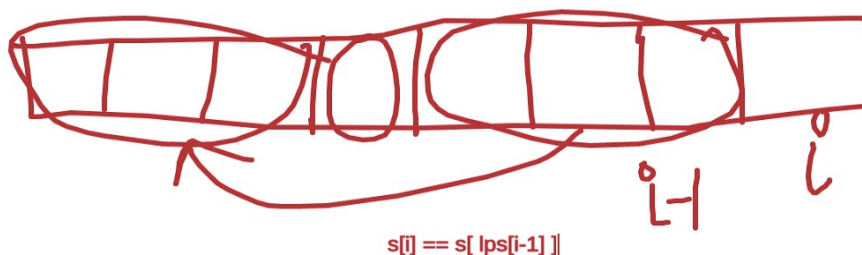
Suffixes of s are $def, abcdef, babcdef, ef, f$

```
i    0 1 2 3 4 5 6 7 8 9
      a b c d a b e a b f
lps[i]: 0 0 0 0 1 2 0 1 2 0
```

```
i    0 1 2 3 4 5 6 7 8 9
      a a b c a d a a b e
lps[i]: 0 1 0 0 1 0 1 2 3 0
```

Note: $lps[i]$ can **increase** by a maximum of 1.

Finding the LPS array



Idea: 1. `lps[0]=0;` // Since, there is no proper prefix of `s[0]`
2. `if(s[i] == s[lps[i-1]]) lps[i]=lps[i-1]+1;`

```
int n=s.length();
vector<int> lps(n);
lps[0]=0;
for(int i=1; i<n; i++)
{
    int j=lps[i-1];
    while(j>0 && s[i]!=s[j] )
    {
        j=lps[ j-1 ];
    }

    if(s[i] == s[j])
    {
        j++;
    }
    lps[i]=j;
}
```

Time complexity of finding LPS array: $O(n)$

Q. Given a string S and a pattern P, find all the occurrences of P in S.

KMP Algorithm

1. Find LPS array of pattern p
2. Just similar to naive algorithm,

let i is index in string s

let j is index in pattern p

if(s[i] == p[j])

{

 i++;

 j++;

}

else

{

 if(j>0)

 j = lps[j-1]

 else

 i++

}

i=0

j=0

S: a b a b c a b c a b a b a b d

P: a b a b d

lps: 0 0 1 2 0

T T T T

i=4

j=2

S: a b a b c a b c a b a b a b d

P: a b a b d

lps: 0 0 1 2 0

i=4

j=0

Since, j=0, we can't decrease j further.

So, increase i by 1

i=5

j=0

0 1 2 3 4 5

S: a b a b c a b c a b a b a b d

P: a b a b d

lps: 0 0 1 2 0

i=6

j=0

Visualise at:

<https://algorithm-visualizer.org/dynamic-programming/knuth-morris-pratts-string-search>

Code:

```
int n=p.length();  
vector<int> lps(n);  
lps[0]=0;
```

```
for(int i=1; i<n; i++)
{
    int j=lps[i-1];
    while(j>0 && p[i]!=p[j] )
    {
        j=lps[ j-1 ];
    }

    if(p[i] == p[j])
    {
        j++;
    }
    lps[i]=j;
}
```

```
int m=s.length();
```

```
int i=0,j=0;
```

```
while(i<m)
{

    if(s[i]==p[j])
    {
        i++;
        j++;
    }
}
```



```

        if(j==n)
        {
            cout<<"Pattern found at "<<i-j; // 1-based index
        }
    }
else if(i<m && s[i] != p[j] ) {
    if(j>0)
        j=lps[j-1];
    else
        i++;
}
}
}

```

Time complexity: $O(m + n)$

Building lps array of pattern takes $O(n)$
and search will take $O(m)$

Time Complexity of KMP Intuition

Consider the worst case scenario, which would be when the pattern appears the maximum number of times, in the string

0 1 2 3 4 5 6 7 8 9 10

S: a a a a a a a a a a a

P: a a a a a

lps: 0 1 2 3 4

Taking input when number of testcases is not given

When no. of testcases is not given, use `cin>>` in while loop.

(Eg. in problem SPOJ NHAY)

Reference:

<https://www.geeksforgeeks.org/using-return-value-cin-to-take-unknown-number-inputs-c/>

```
int n;
while(cin>>n)
{
    string p;
    cin>>p;
    string s;
    cin>>s;
    // ....
}
```

Practice Problems

1. <https://www.spoj.com/problems/NHAY/>
2. <https://www.spoj.com/problems/PERIOD/>
3. <https://www.codechef.com/problems/BORDER>
4. <https://www.spoj.com/problems/EDIST/>

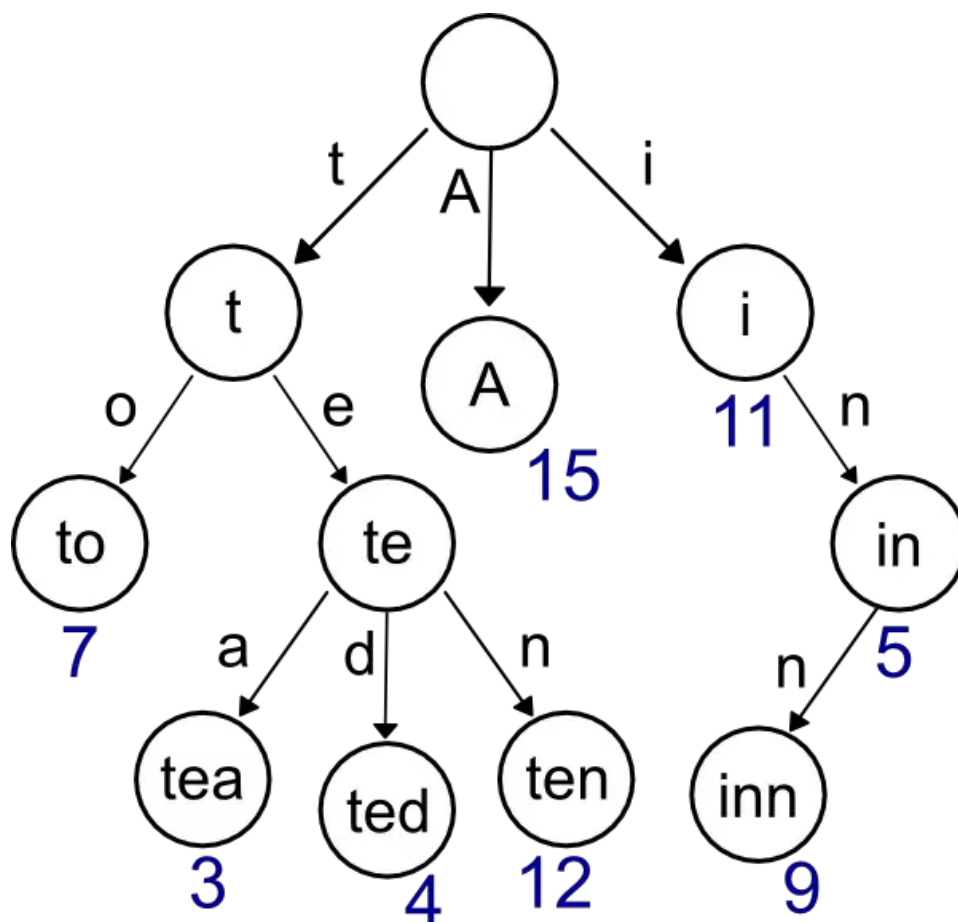
Don't use in-built functions for string matching, they use naive algorithm. Always use KMP algorithm.

Tries

A trie is a tree-like data structure that stores strings.

Each node is a string, and each edge is a character.

The root is the empty string, and every node is represented by the characters along the path from the root to that node. **This means that every prefix of a string is an ancestor of that string's node.**



$26 + 26 * 26 + 26 * 26 * 26 + \dots 26^i$

input="tea"

input="ted"

find "tex"

te->freq?

int a=10;

```
struct node
{
    int freq;
    node* child[26]; //array of pointers to children
    node() //constructor
    {
        freq=0;
        for(int i=0; i<26; i++)
            child[i]=NULL;
    }
};
```

```
node* root=new node(); //pointer to a new node
node* tmp;
tmp->freq
while(n--)
```

```

{
    string s;
    cin>>s;
    tmp=root;

    for(int i=0;i<s.size();i++)
    {
        if(tmp->child[(s[i]-'a')]==NULL)
        {
            node* z=new node();//child create
            tmp->child[(s[i]-'a')]=z;
        }
        tmp=tmp->child[(s[i]-'a')];
        tmp->freq++;
    }

    tmp=root;
    s->input..
    int res=0;
    for(int i=0;i<s.size();i++)
    {
        if(tmp->child[(s[i]-'a')]==NULL)
            break;
        tmp=tmp->child[(s[i]-'a')]
        if(i==(s.size()-1))
            res=tmp->freq;
    }
    cout<< res;

```

}

Try this problem:

<https://www.hackerrank.com/challenges/contacts/problem>

(If you are stuck, look at my submission, given at last of this doc)

Note: Instead of making child as an array of size 26, you can also make it, an `unordered_map<int,node*>` to save space.

Space Complexity of Trie:

Just see how many nodes are possible in the trie.

And multiply that with the size of 1 node.

Like in the above problem, **if you sum up the number of characters of all the strings**, there would be $n \times 21$ total characters. So, in the worst case, we need $n \times 21$ Trie nodes. And if size of 1 node is 26, space complexity is approximately: $O(n \times 21 \times 26) \approx 10^7$

Bit manipulation problems using Trie

7->111

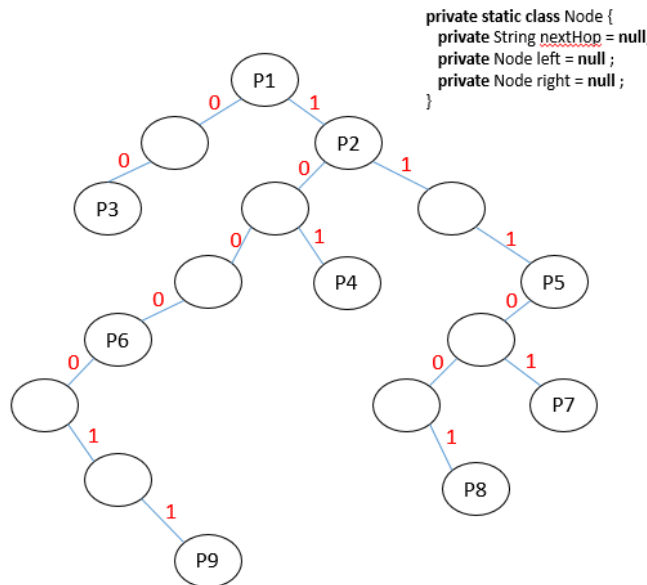
5->101

4->100

$s[0] \rightarrow 1 \ll 30$

Prefix database

P1 *
P2 1*
P3 00*
P4 101*
P5 111*
P6 1000*
P7 11101*
P8 111001*
P9 1000011*



```
private static class Node {
    private String nextHop = null;
    private Node left = null;
    private Node right = null;
}
```

//If a prefix node
//Left node with an address bit 0
//Right node with an address bit 1

110

111

Q)n->length array

$2 \leq n \leq 10^5$

$1 \leq \text{arr}[i] \leq 10^9$

i,j(i!=j)

$\text{arr}[i] \text{ xor } \text{arr}[j] \rightarrow \text{min}$

Link:

<https://practice.geeksforgeeks.org/problems/minimum-x-or-value-pair/0/>

(Look at my submission at the end of the doc, only if you are stuck)

$\log_2(\text{arr}[i]) + 1 \rightarrow 111$

$\log_2(10^9) \approx 30$

$O(32 \cdot n) \rightarrow \text{time trie construction..}$

$\text{arr}[i] = 1010101000$

$\text{arr}[j] = 1001100011$

$\text{arr}[k] = 0111111111$

```

ans1=2^8+...
ans2=2^7+...
2^3
2^2+2^1+2^0
arr[i]->string convert(s)
for(int j=30;j>=0;j--)
    if((1<<j)&arr[i])
        s+='1';
    else
        s+='0'

```

1101011
 2^x

Also try these problems:

1.

<https://www.hackerrank.com/challenges/no-prefix-set/problem>

2.

<https://www.hackerrank.com/challenges/maximum-xor/problem>

My submission for Geeks Minimum XOR value:

<https://csacademy.com/code/tkmdyzSq/>

My submission for Hackerrank Contacts:

(Don't look, if you have not tried by yourself)

<https://csacademy.com/code/yZgfTzc9/>

My submission for Hackerrank No Prefix Sets:

(Don't look, if you have not tried by yourself)

<https://csacademy.com/code/6buXyAYv/>

My submission for Hackerrank No Prefix Sets:

(Don't look, if you have not tried by yourself)

<https://csacademy.com/code/AHZcCYhO/>