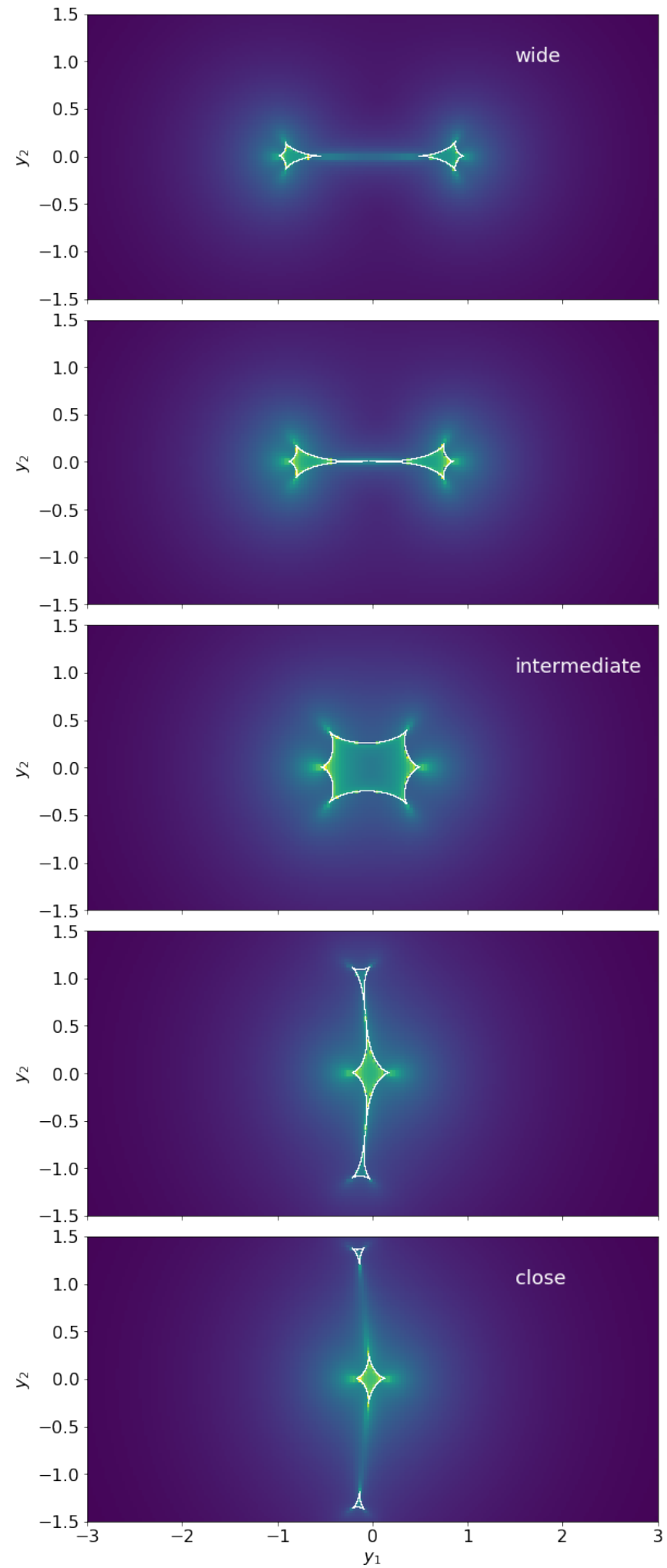
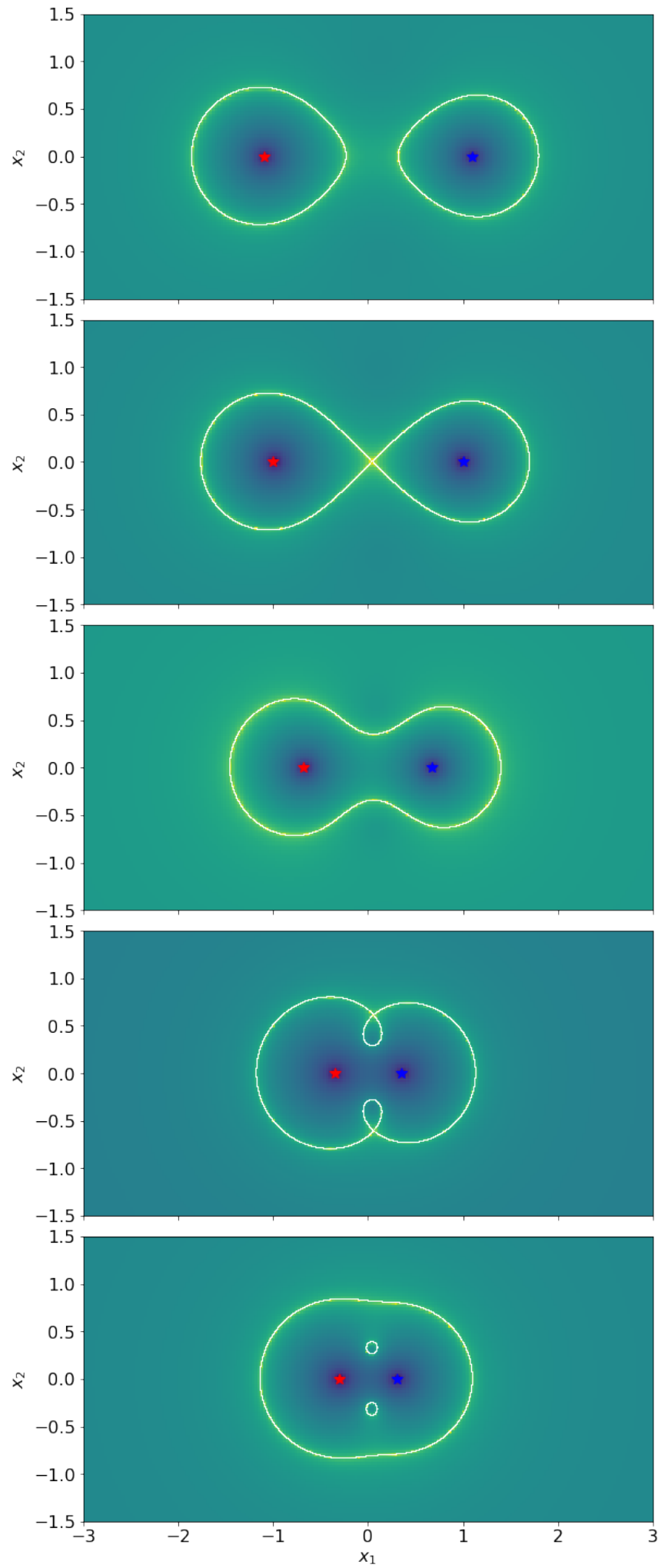


GRAVITATIONAL LENSING

15 – BINARY LENSES

Massimo Meneghetti
AA 2018-2019

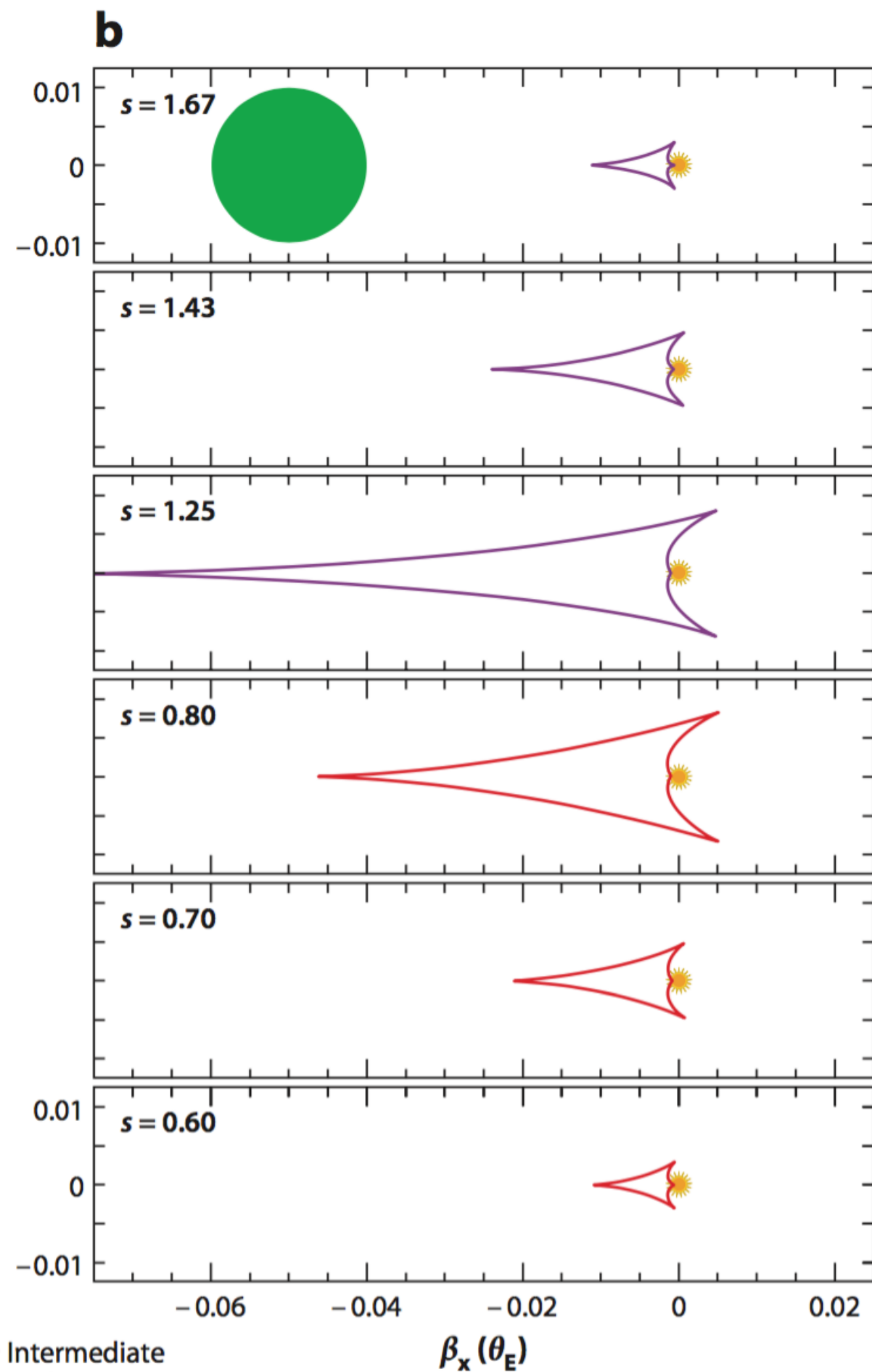
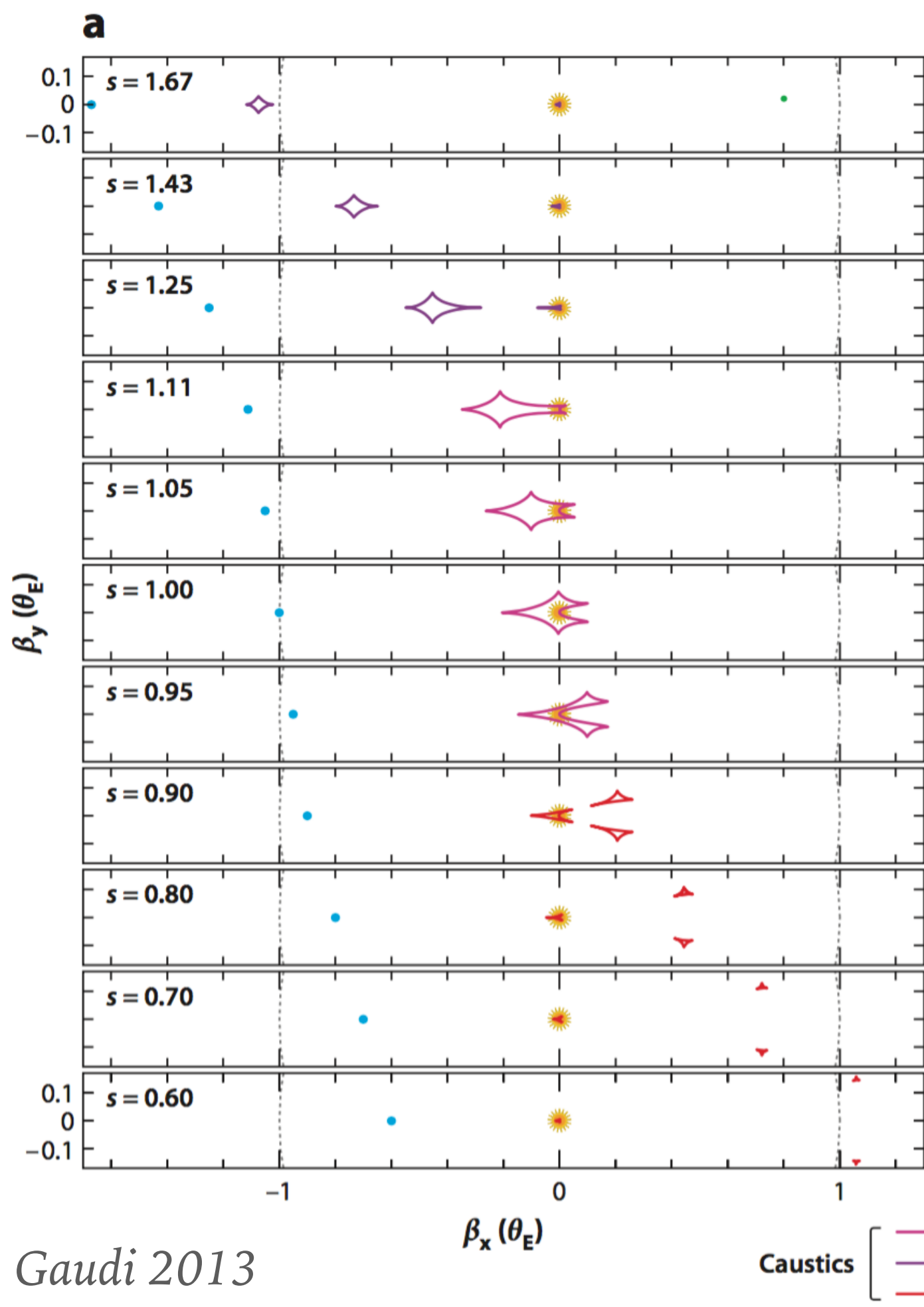


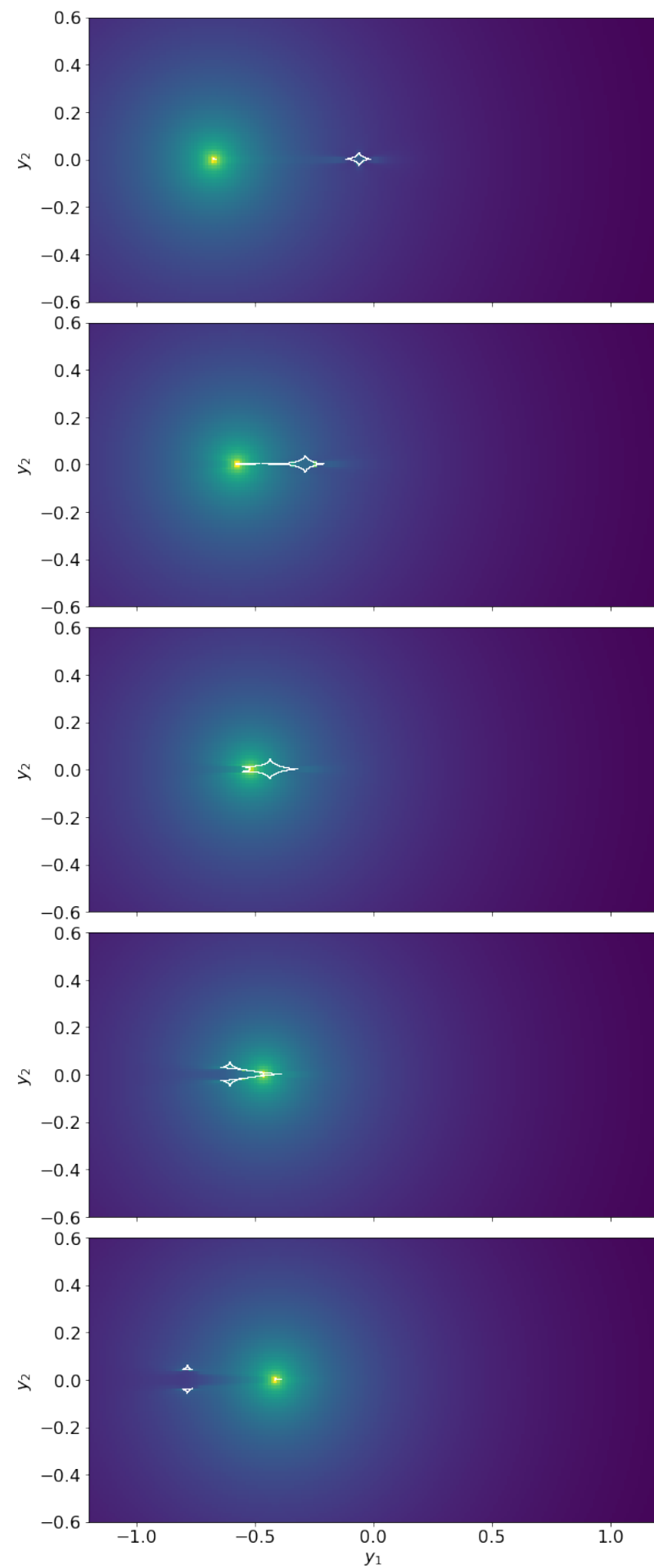
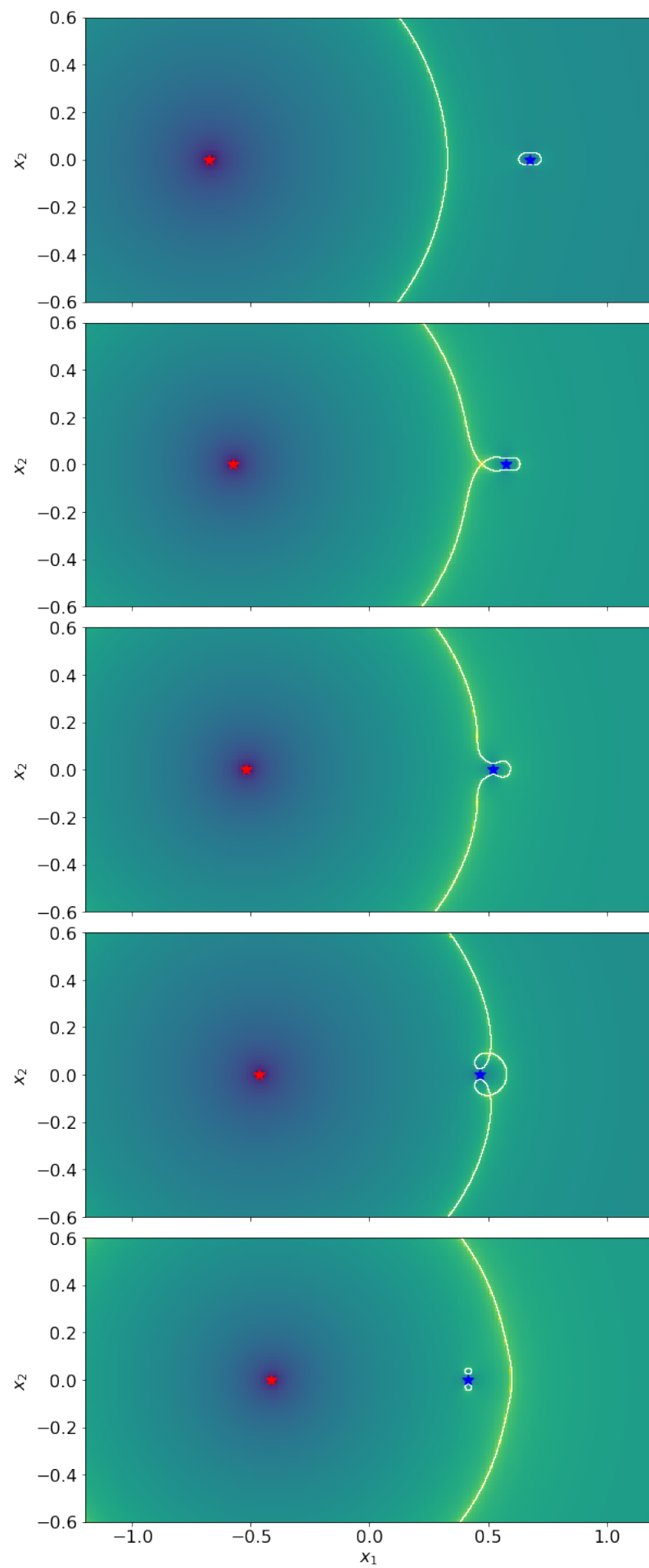
PLANETARY MICROLENSING

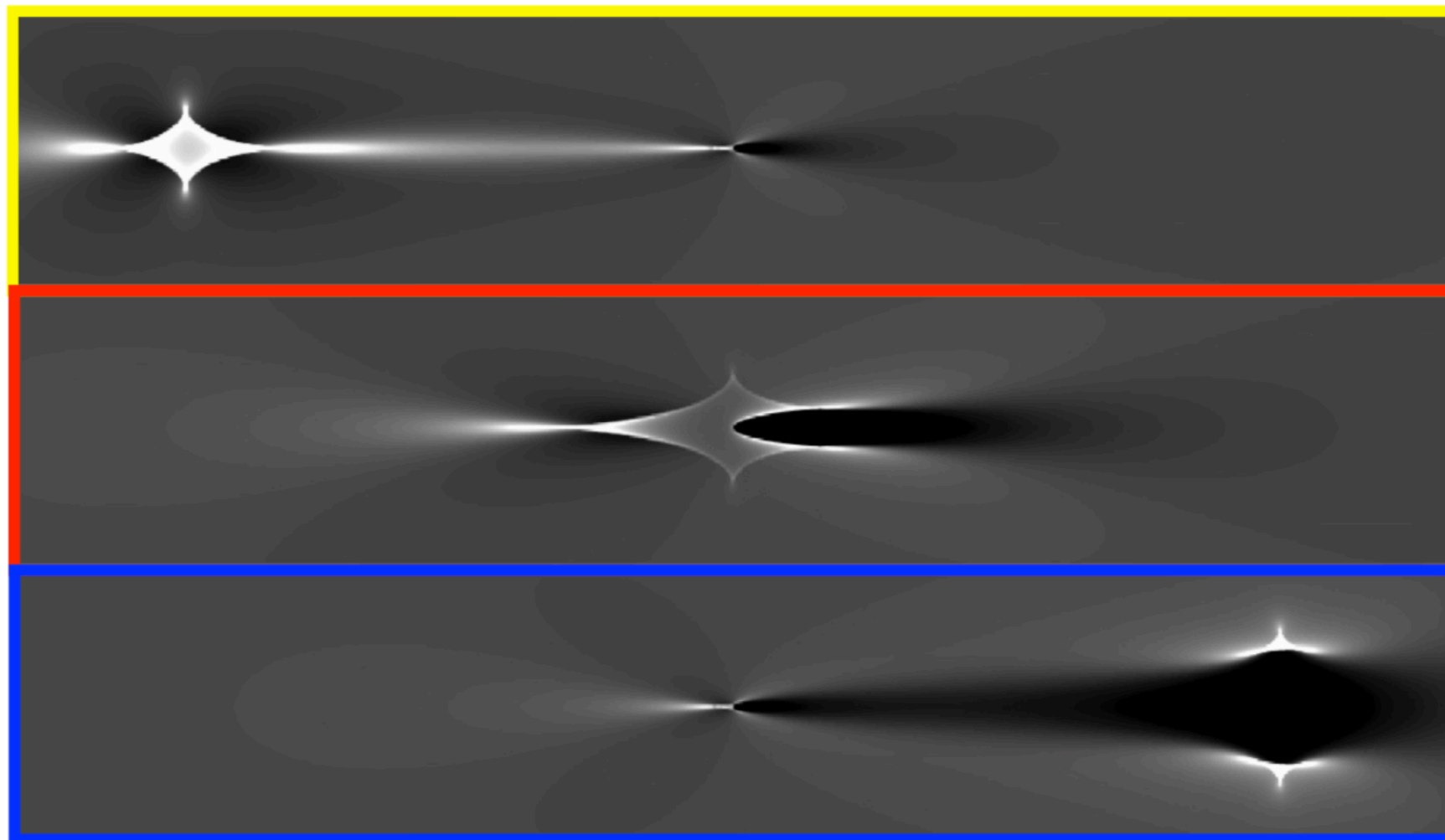
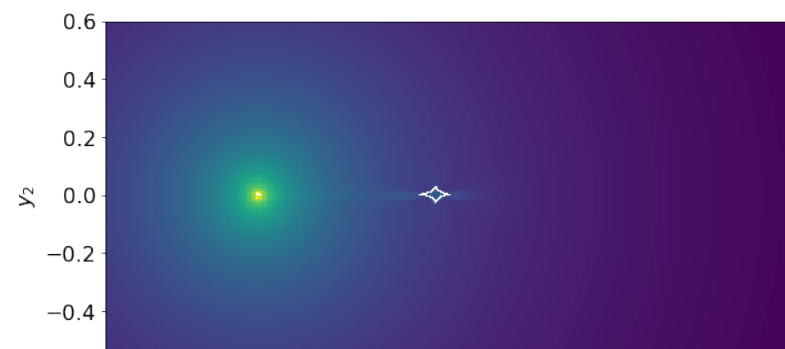
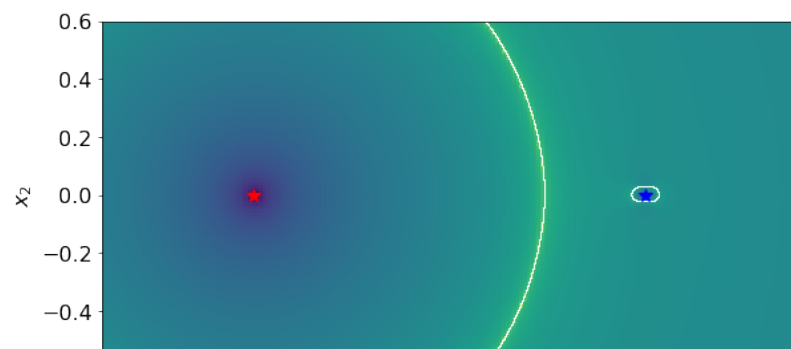
- Let us consider the system consisting of an host star and a planet orbiting around it.
- This is an example of **binary** lens
- The host star is of course much heavier than the planet!
 - example: for a Jupiter-like planet $q=0.001$ (solar mass star)
 - example: for a Earth-like planet $q=0.0000003$

WHAT KIND OF SIGNAL?

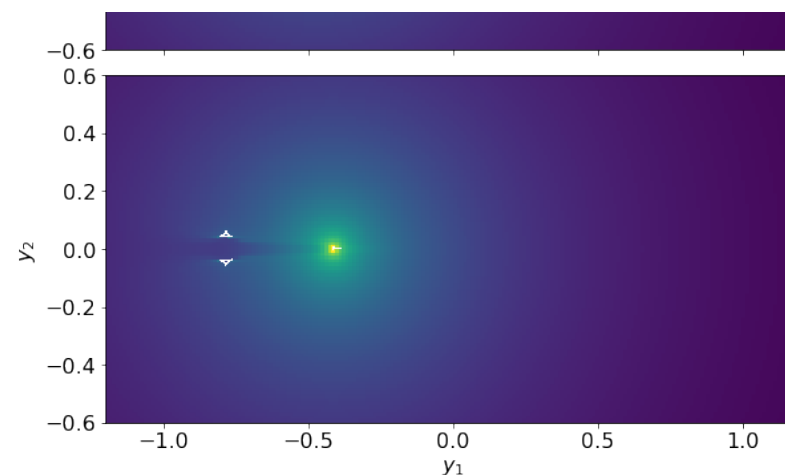
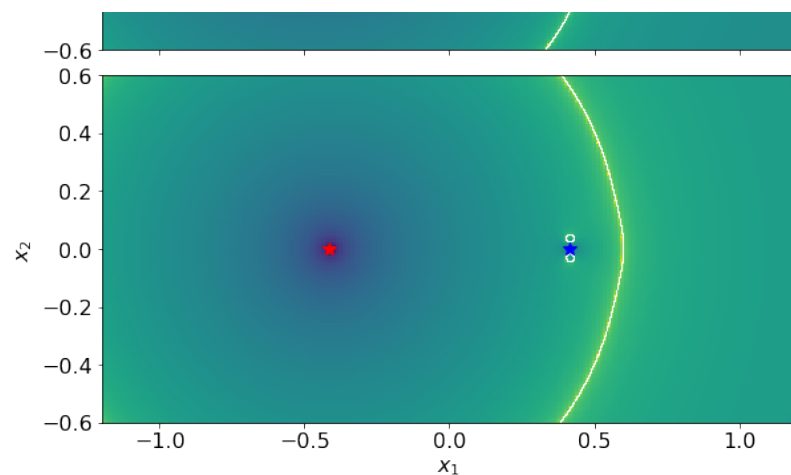
- The light curve is that of the star...
- The planet produces only a small perturbation to the magnification pattern, localized in a small region around the caustics
- Must cross one of these perturbed regions in order for the planet to be detected.
- The shape of the perturbation is determined by the caustic configuration...



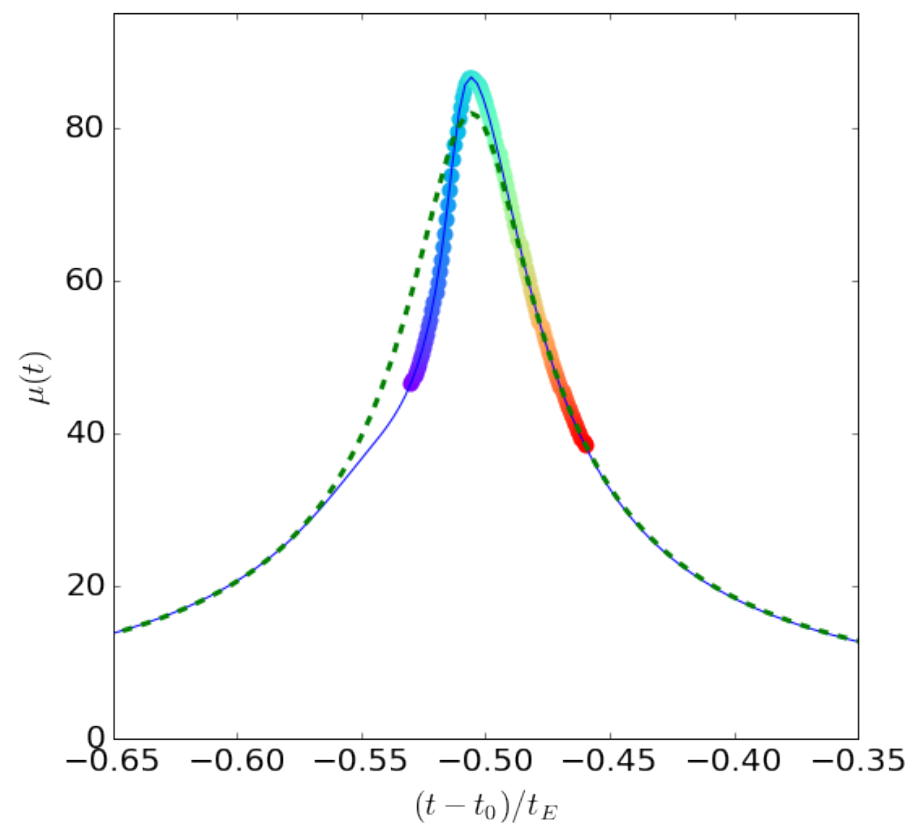
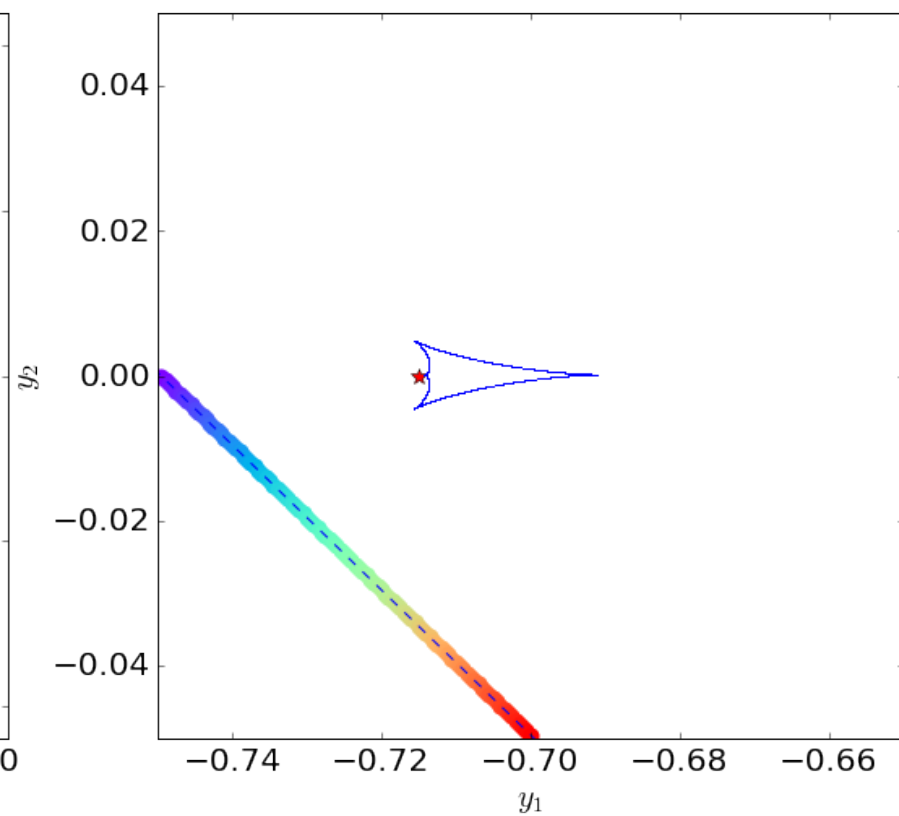
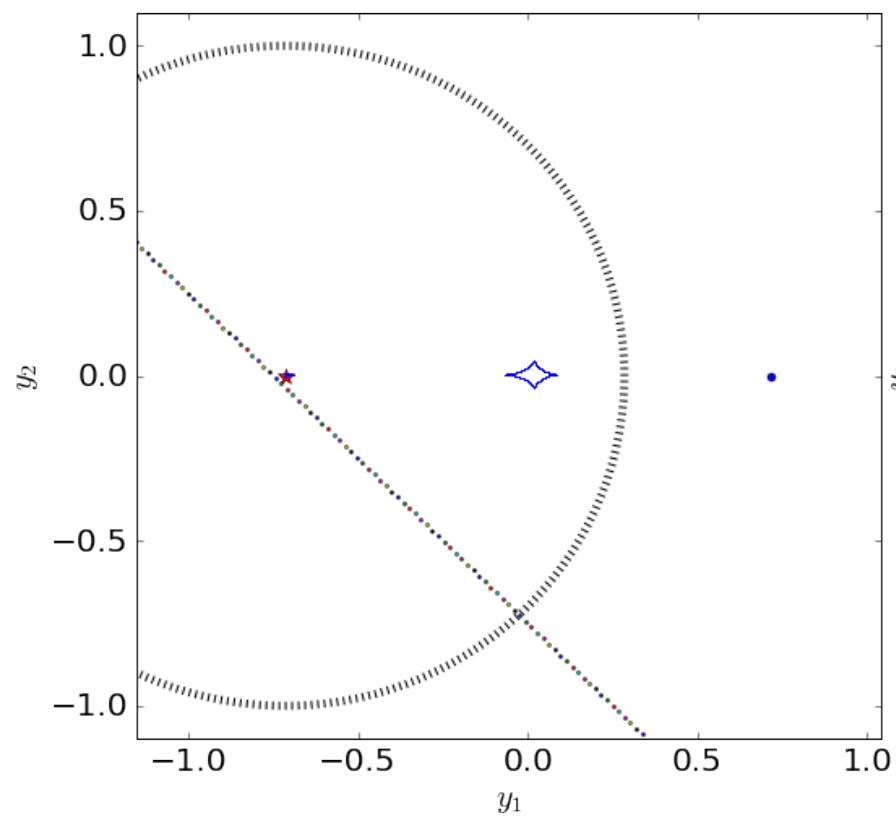
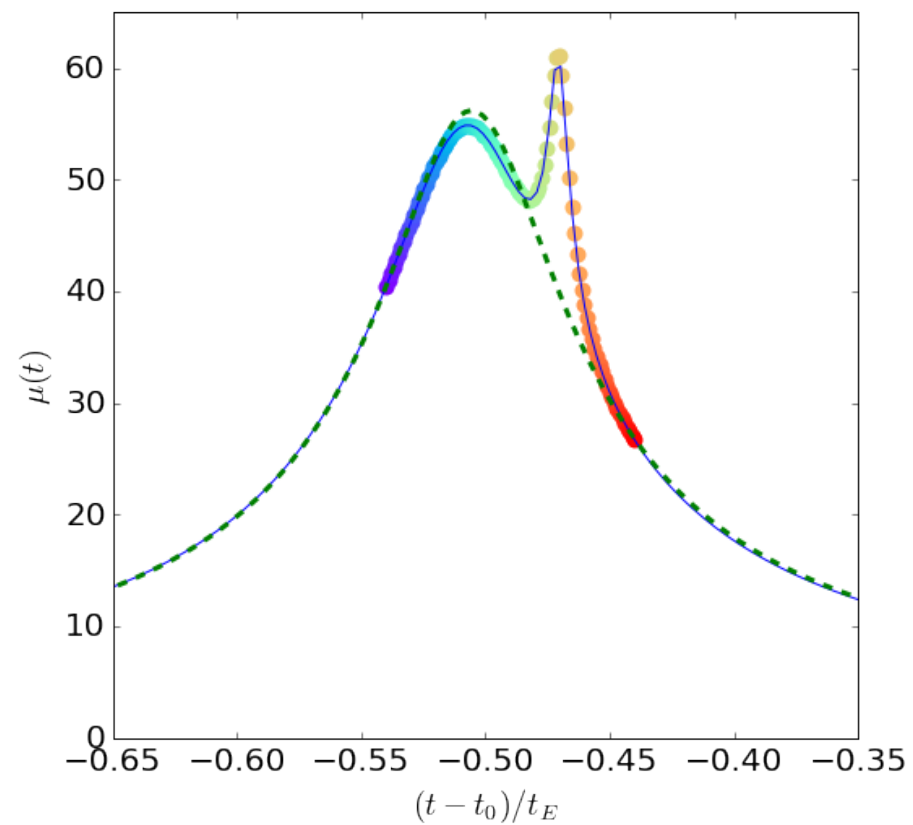
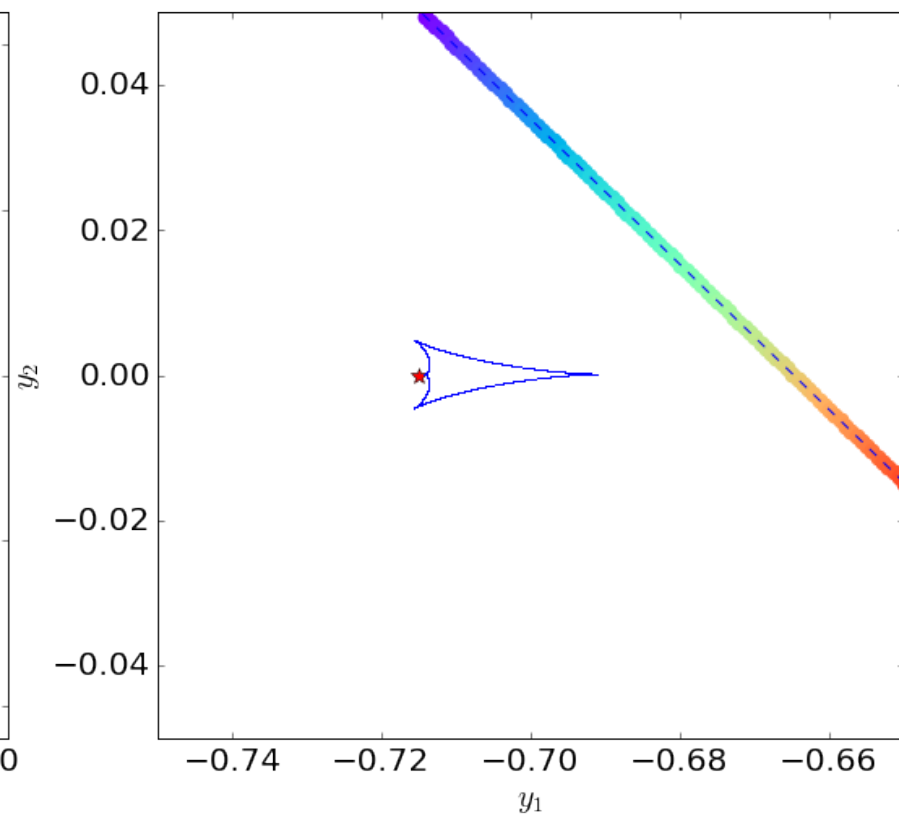
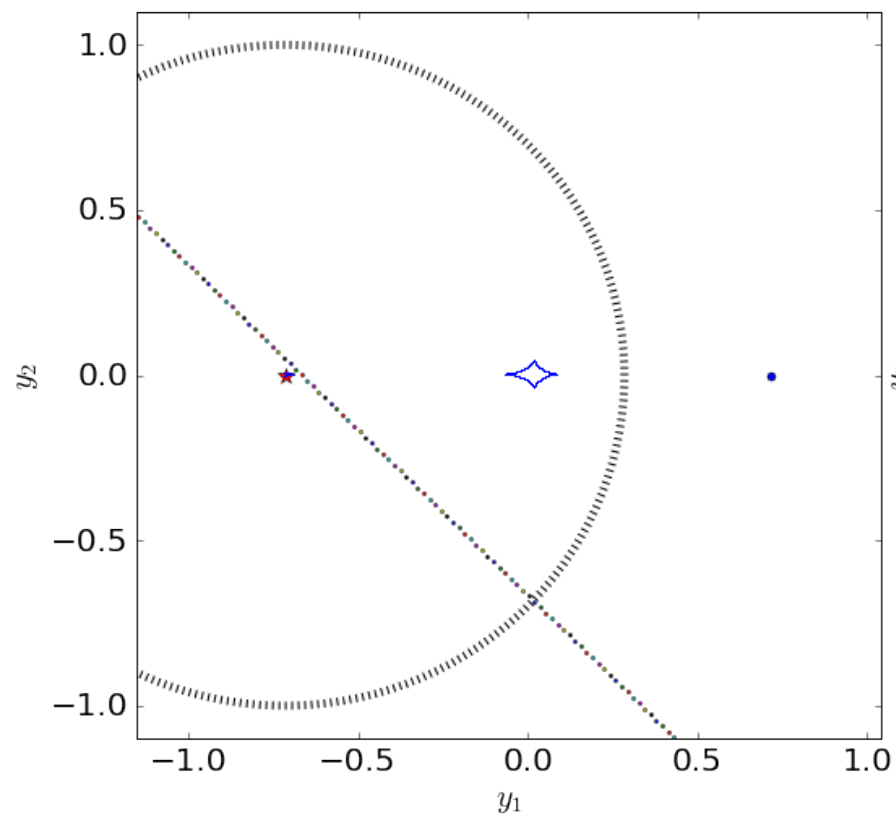




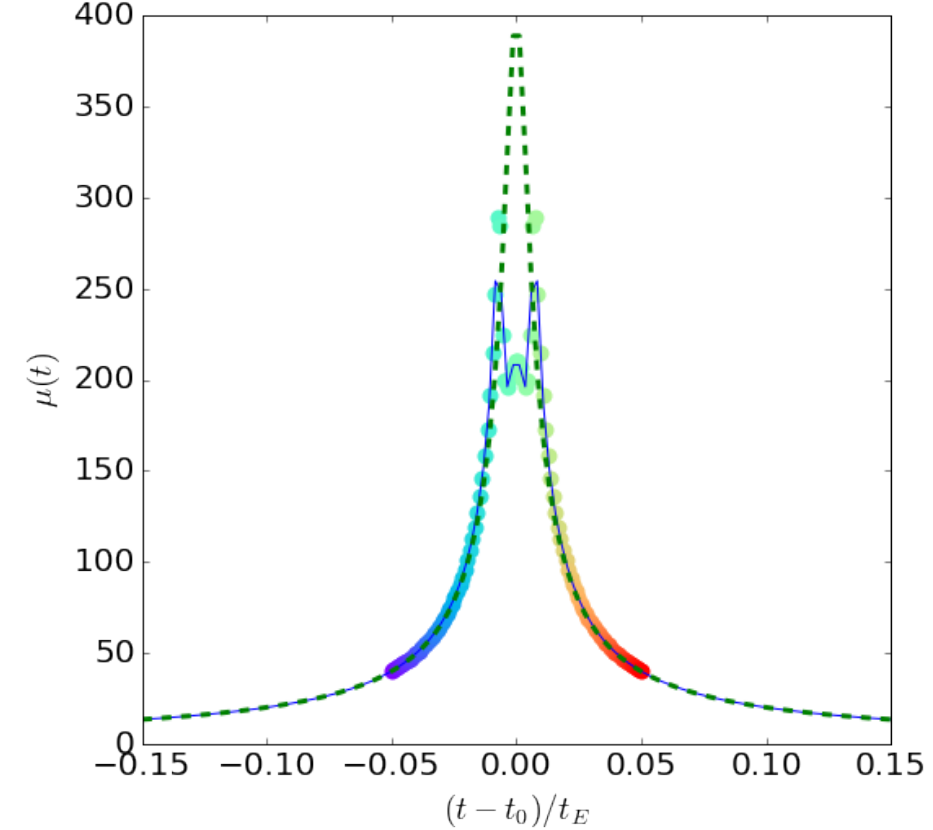
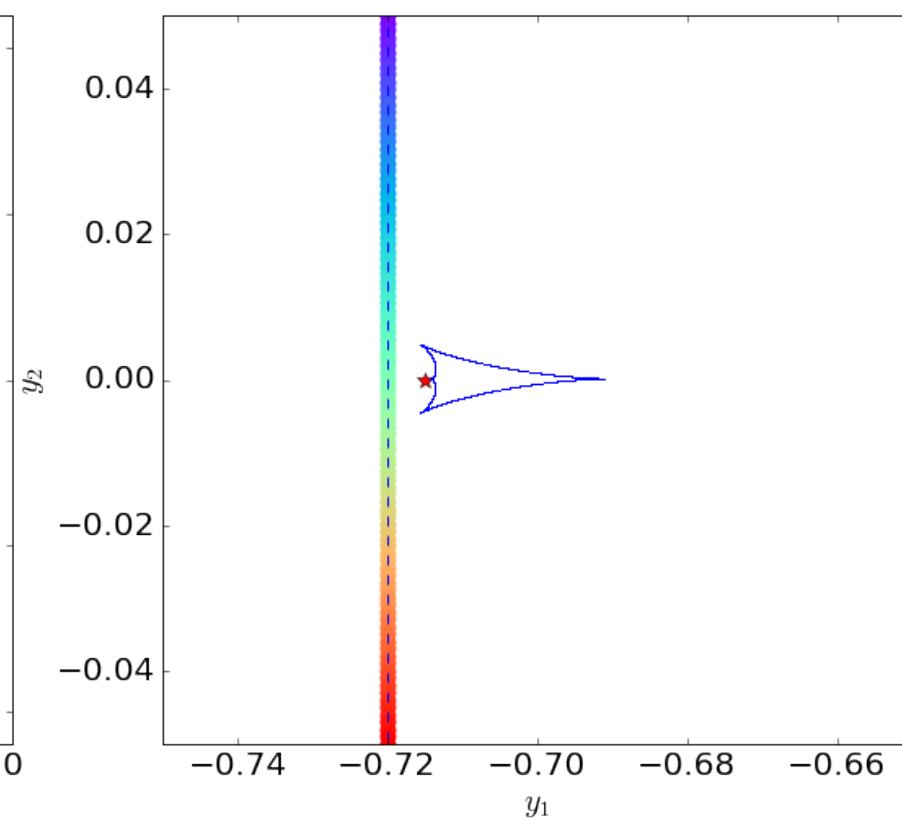
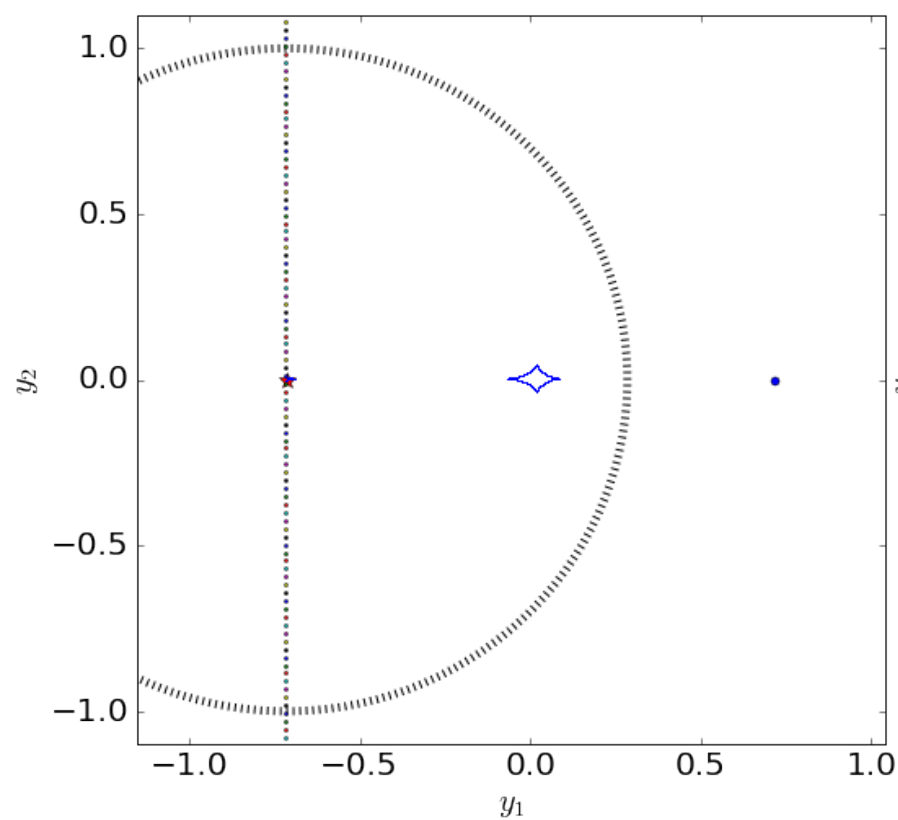
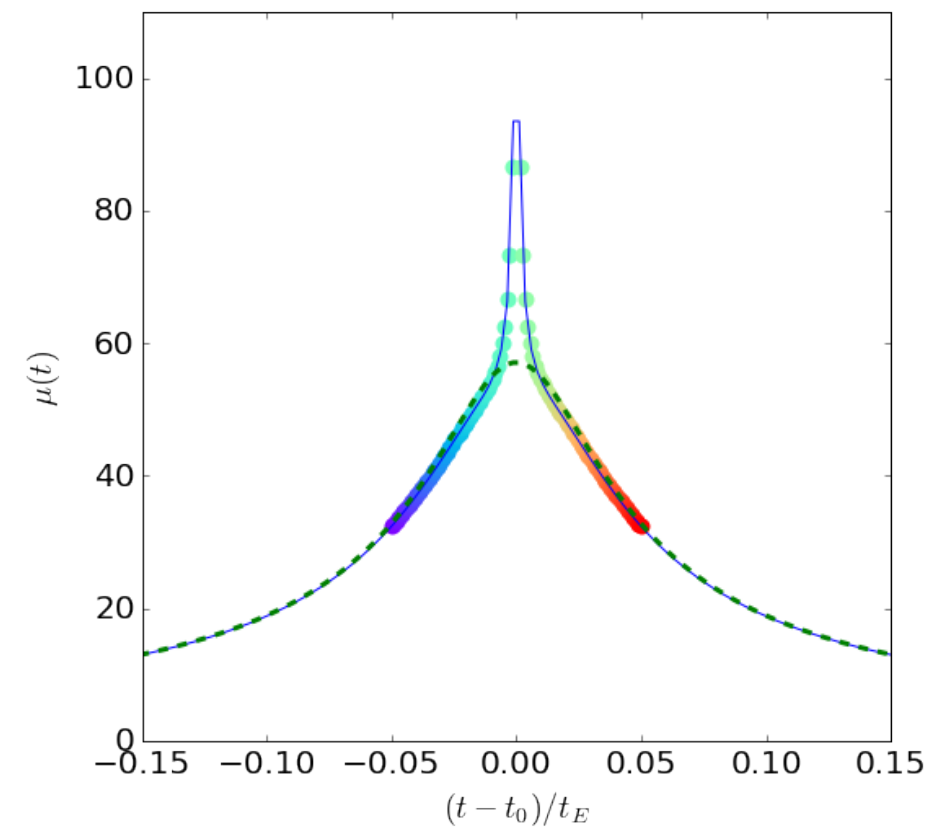
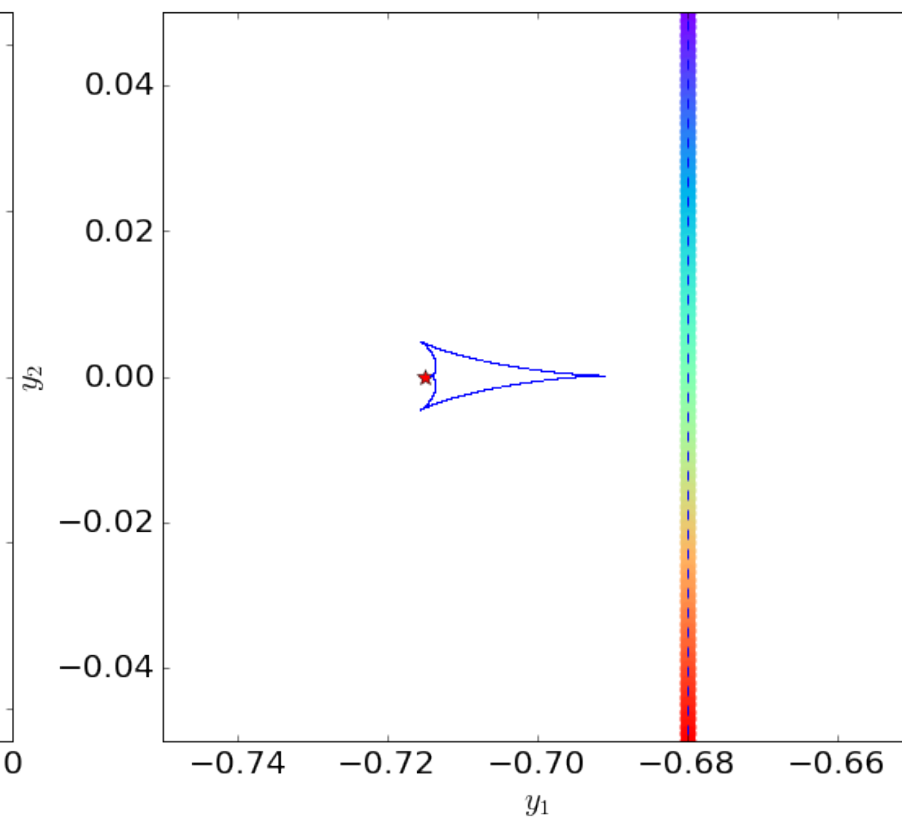
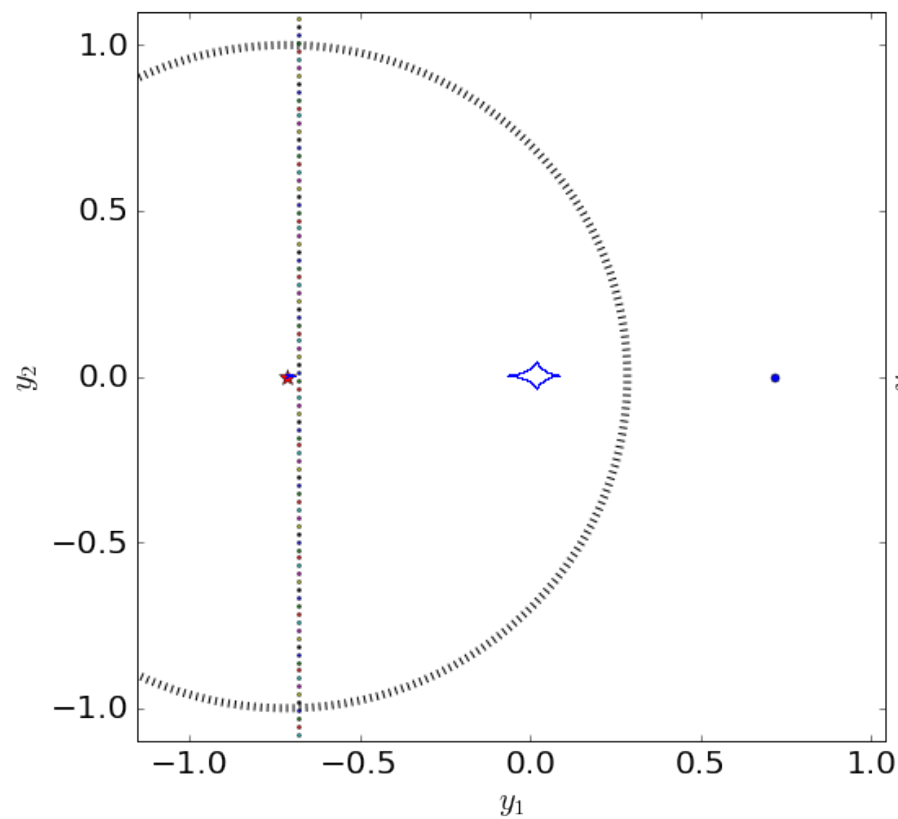
Wide
Intermediate/
Resonant
Close



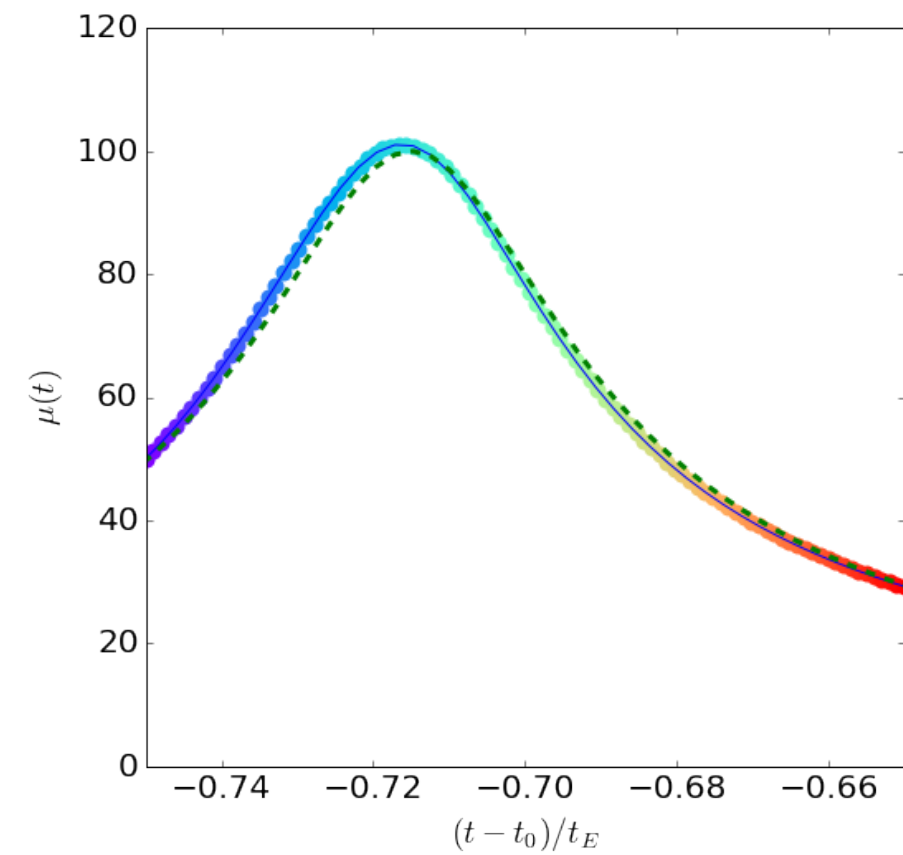
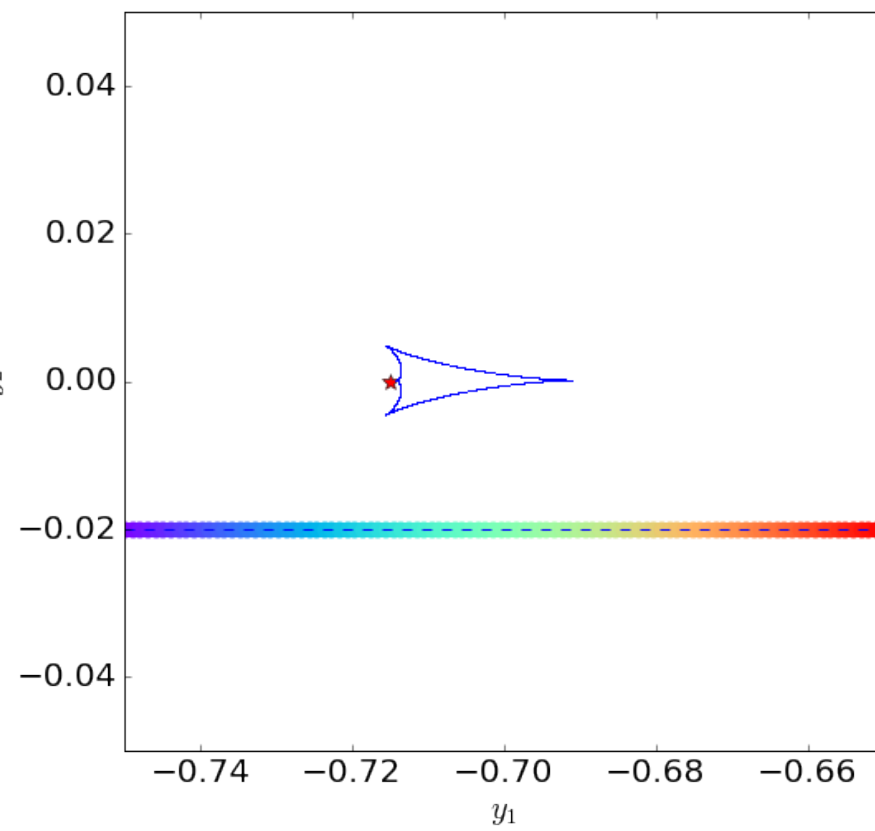
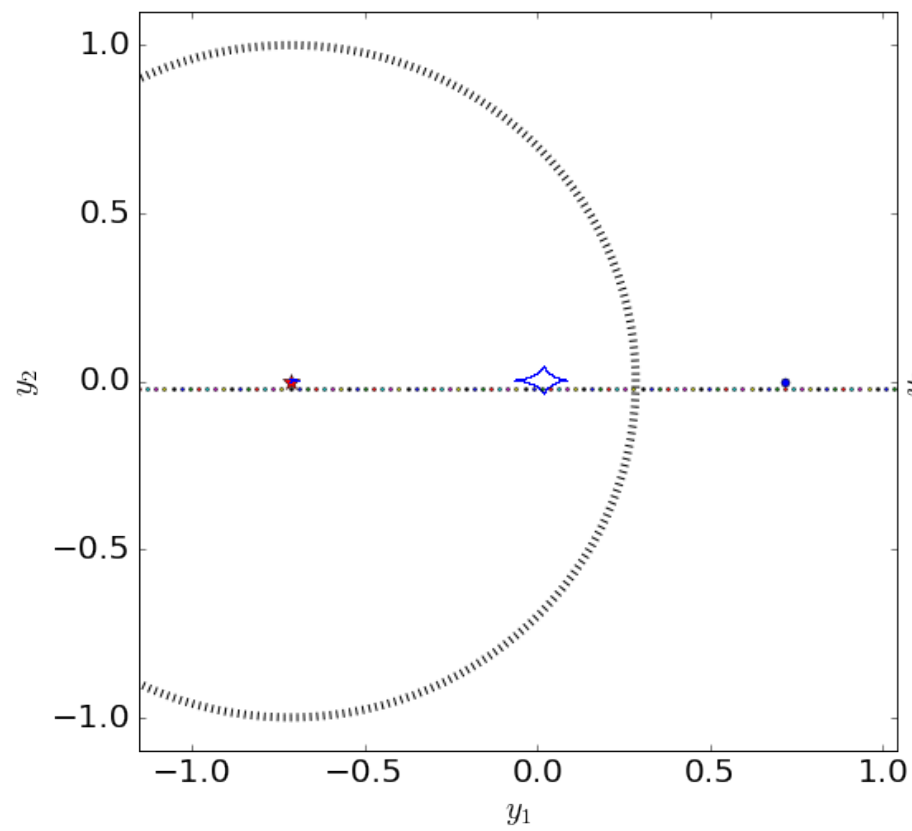
CENTRAL CAUSTIC PERTURBATIONS



CENTRAL CAUSTIC PERTURBATIONS



CENTRAL CAUSTIC PERTURBATIONS



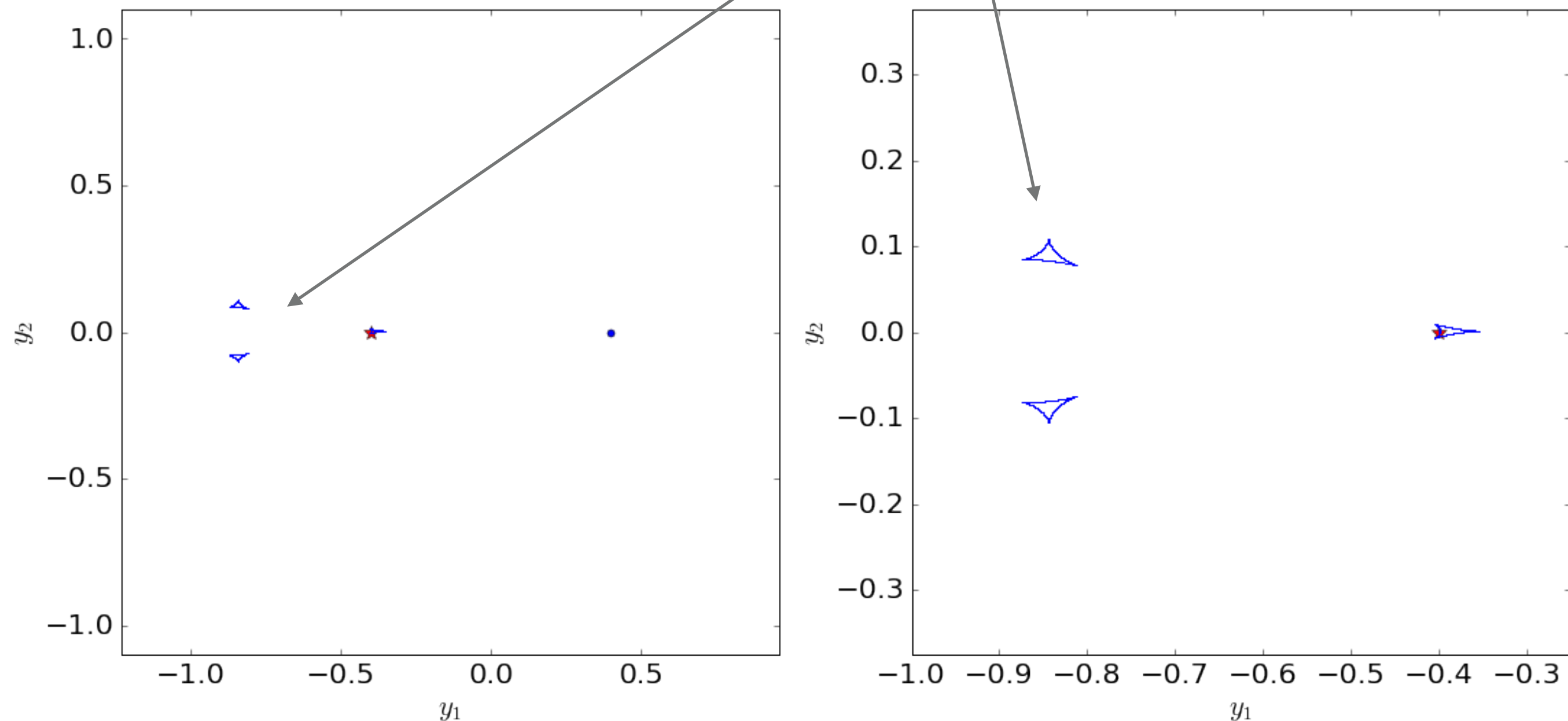
PLANET DETECTION THROUGH CENTRAL CUSP PERTURBATIONS

- Only possible in the case of high magnification events (sources passing very close to the host stars)
- For this reason, they are rare events
- Advantages:
 - near the peak of the event
 - can sometimes be predicted in advance
 - high magnification makes possible to follow-up the events using small telescopes
 - more accurate photometry (and easier separation of source and lens)
- Disadvantages:
 - degeneracy wide-close topologies

PLANETARY CAUSTICS IN CLOSE TOPOLOGIES

planetary caustics

Han 2006

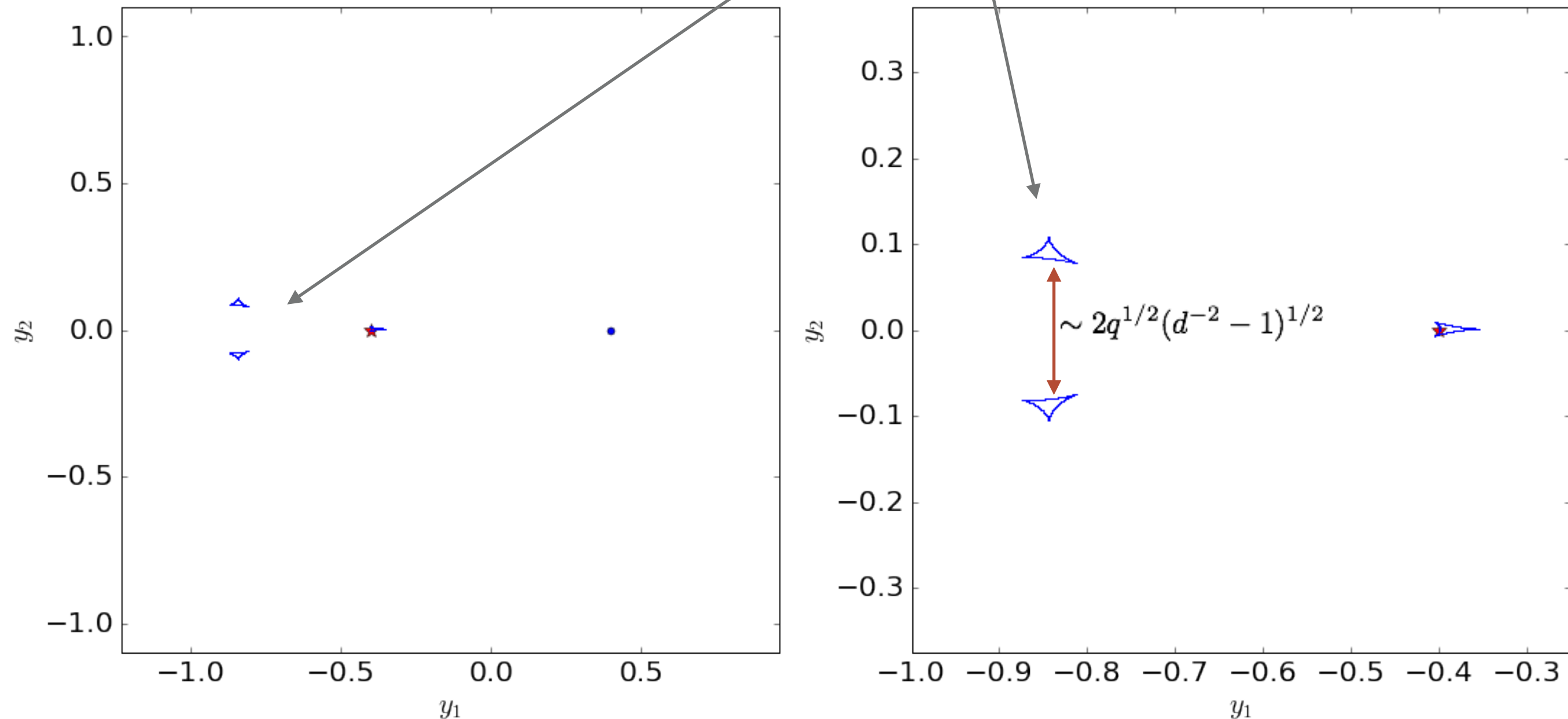


Recommended reading: Han, C., 2006, ApJ, 638, 1080

PLANETARY CAUSTICS IN CLOSE TOPOLOGIES

planetary caustics

Han 2006

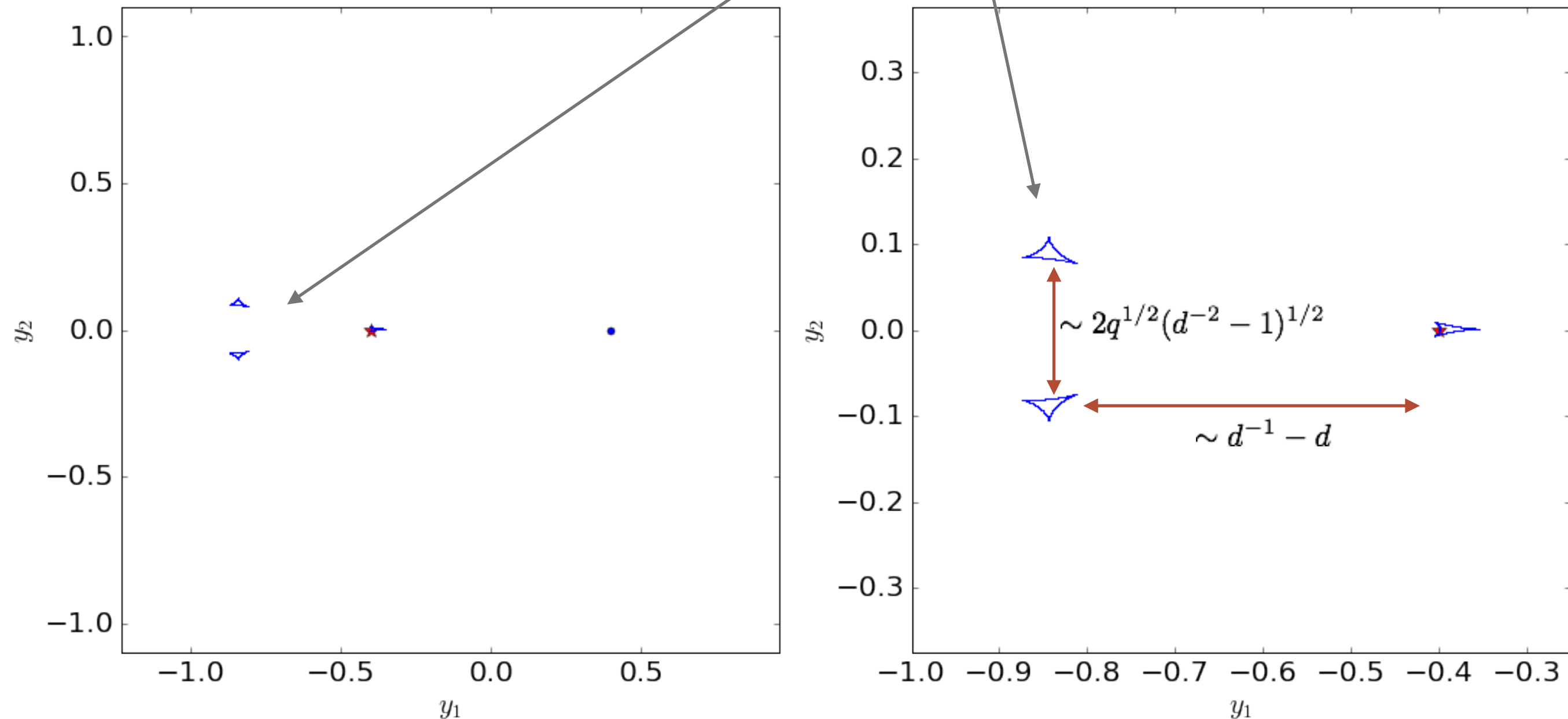


Recommended reading: Han, C., 2006, ApJ, 638, 1080

PLANETARY CAUSTICS IN CLOSE TOPOLOGIES

planetary caustics

Han 2006

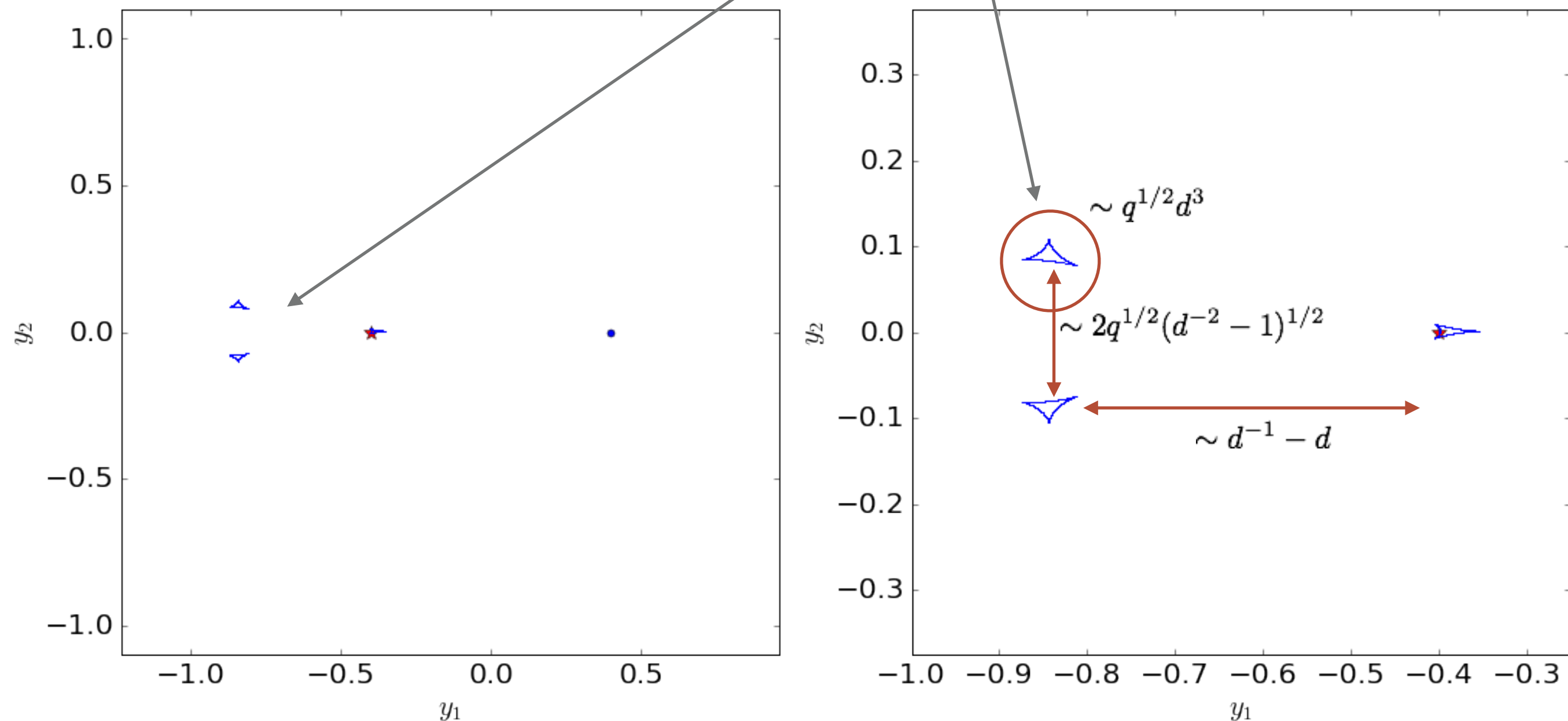


Recommended reading: Han, C., 2006, ApJ, 638, 1080

PLANETARY CAUSTICS IN CLOSE TOPOLOGIES

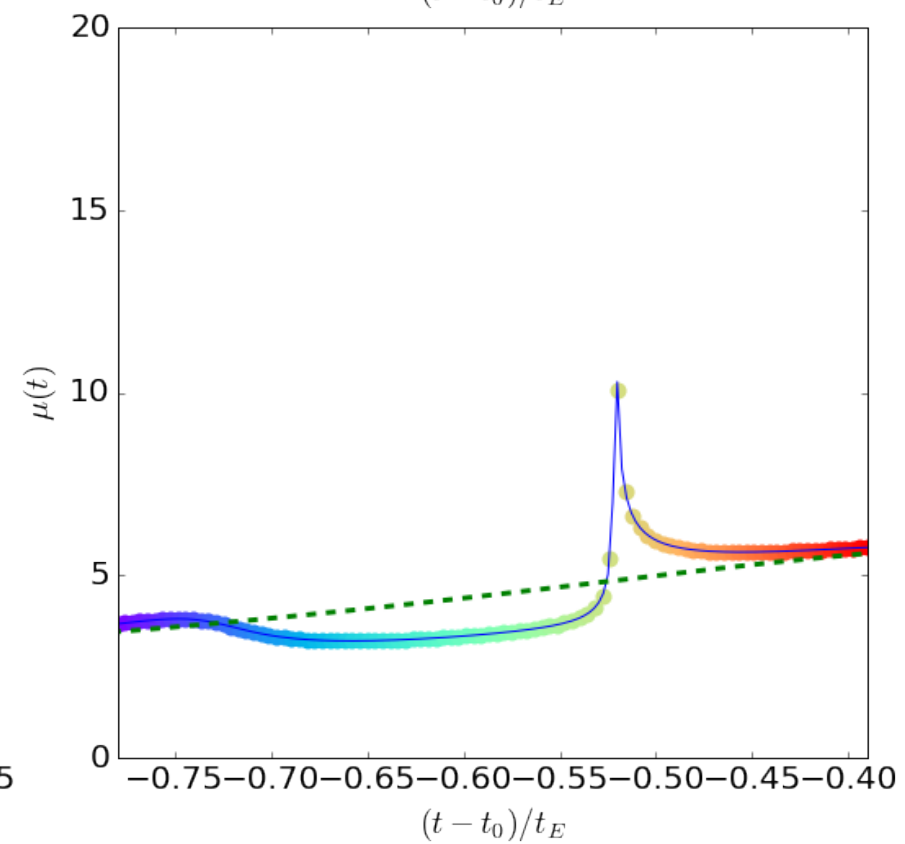
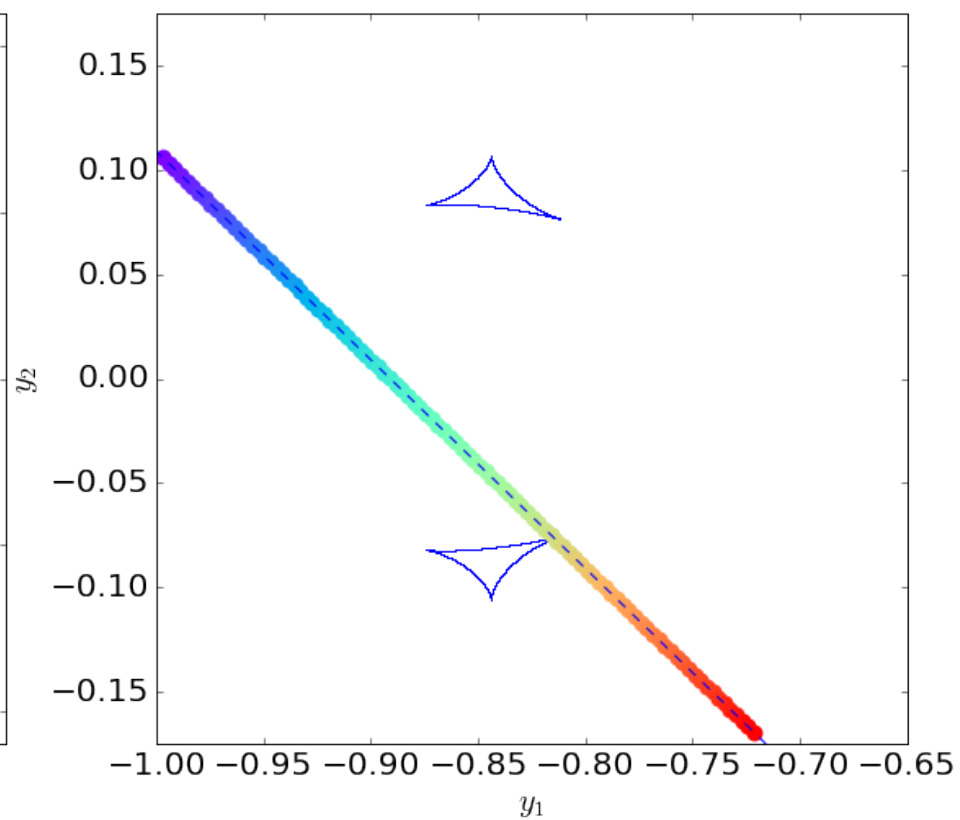
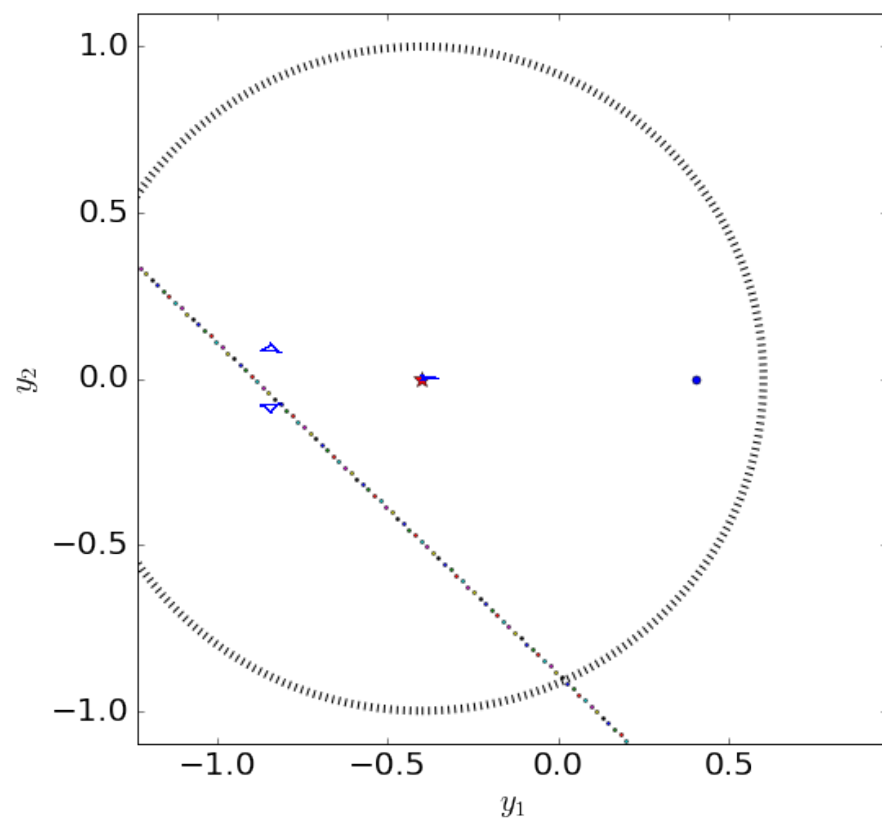
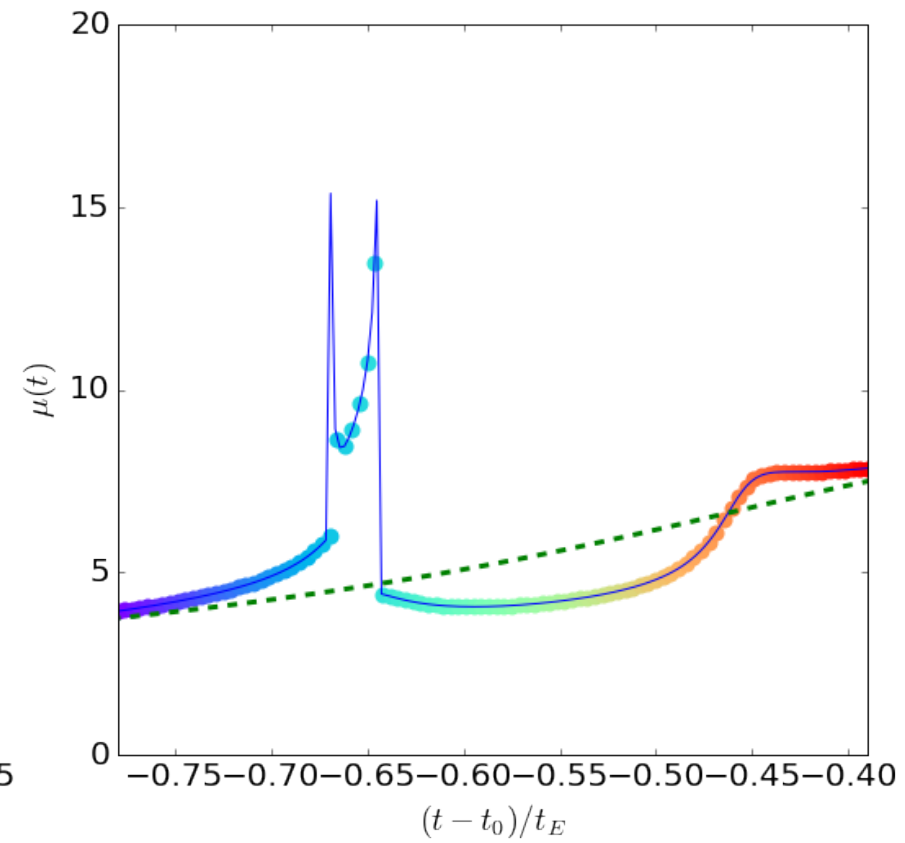
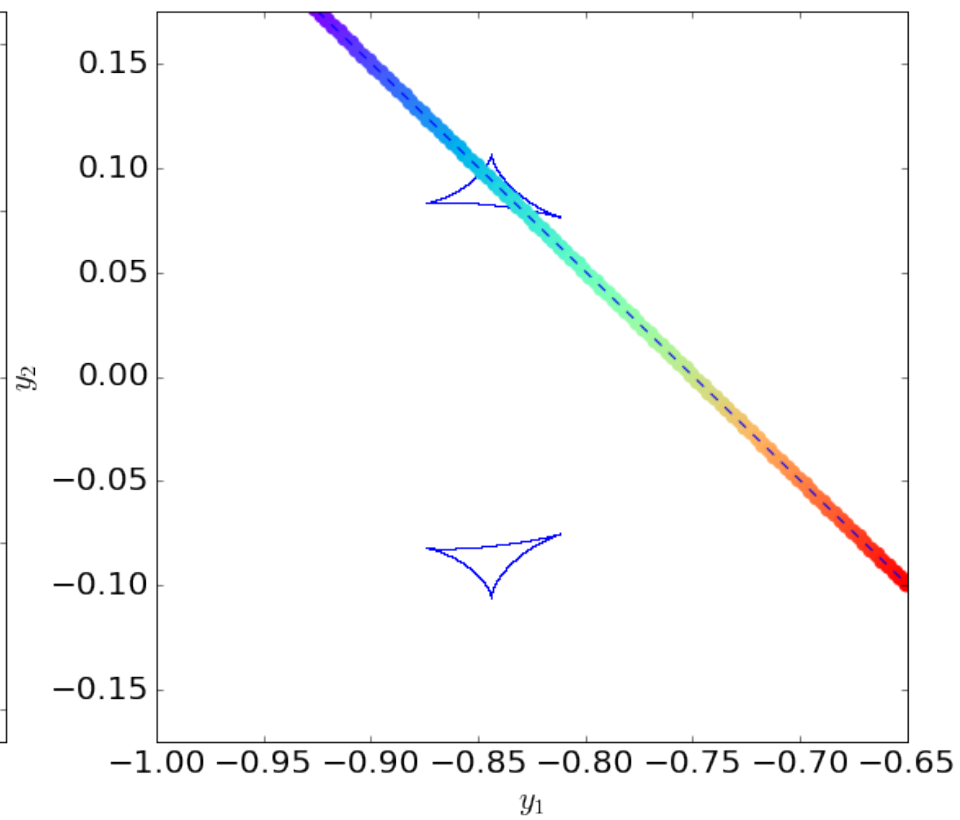
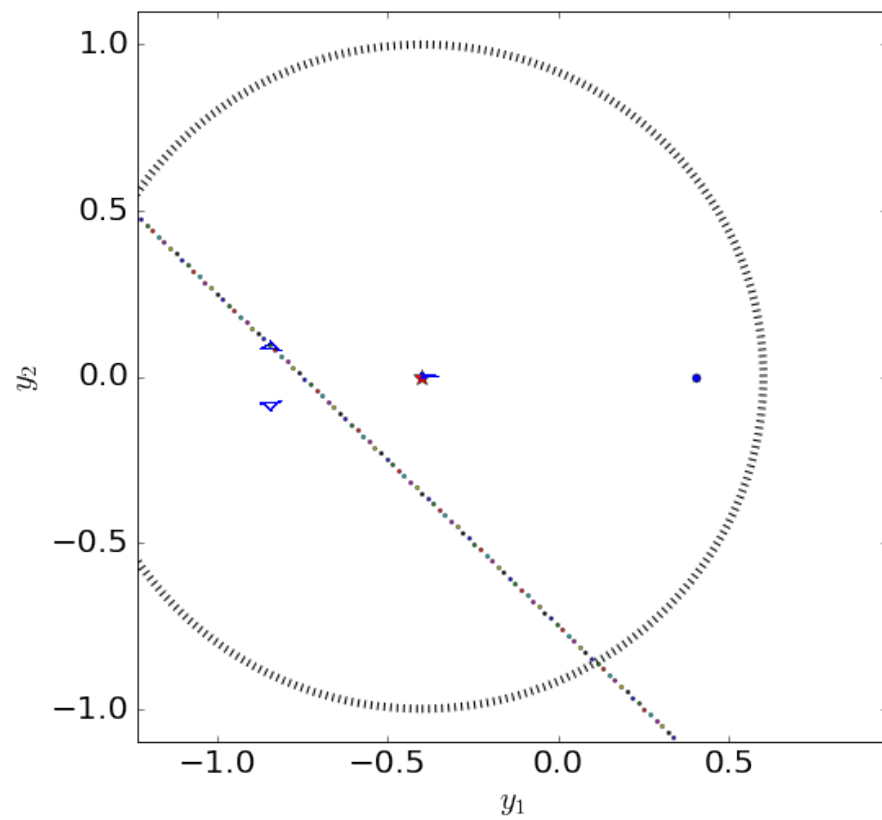
planetary caustics

Han 2006

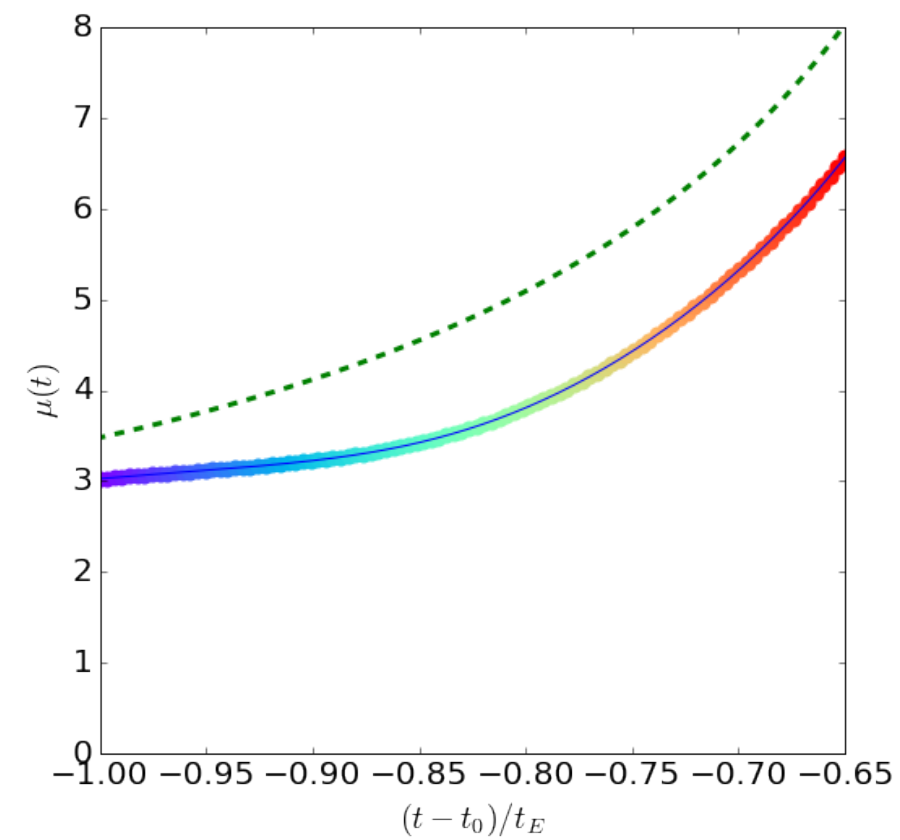
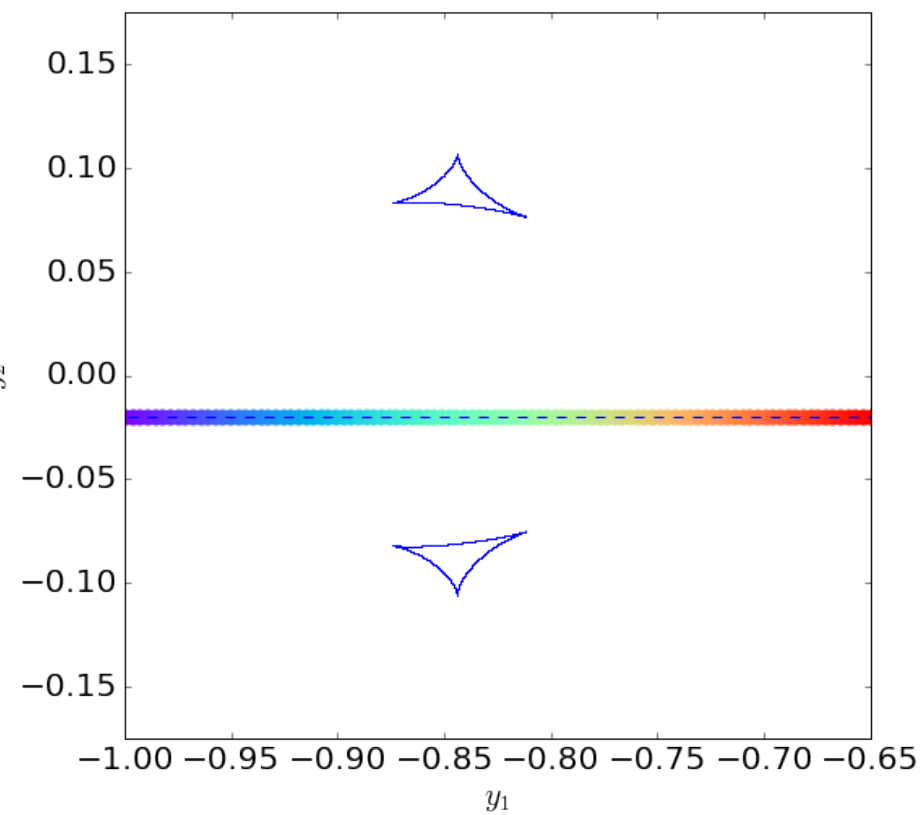
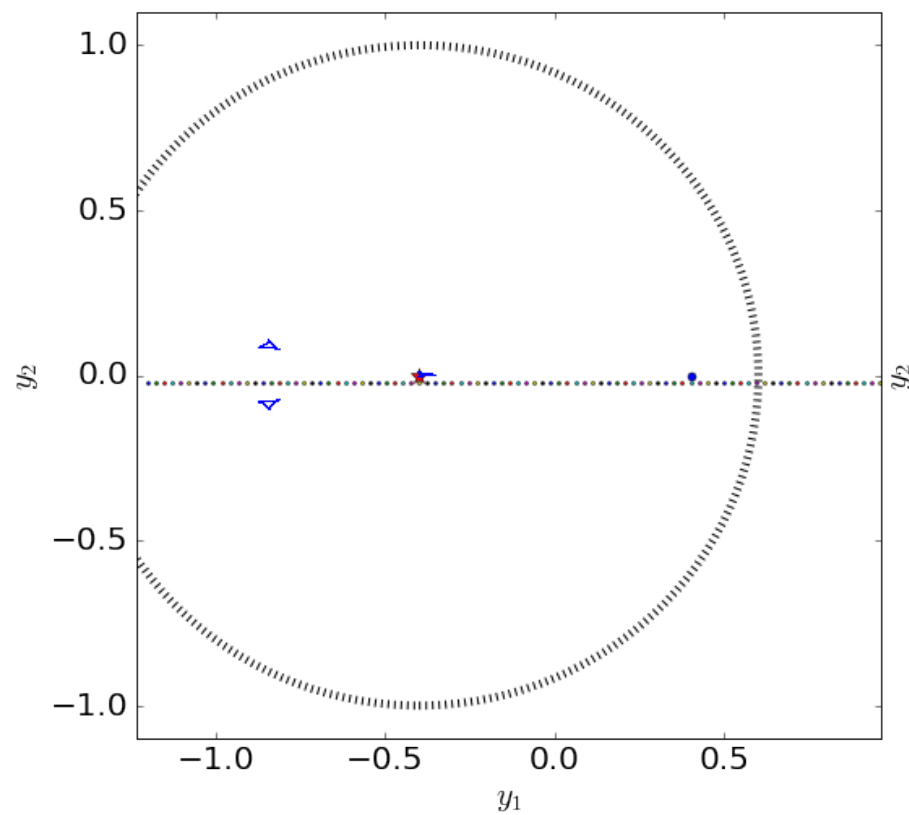
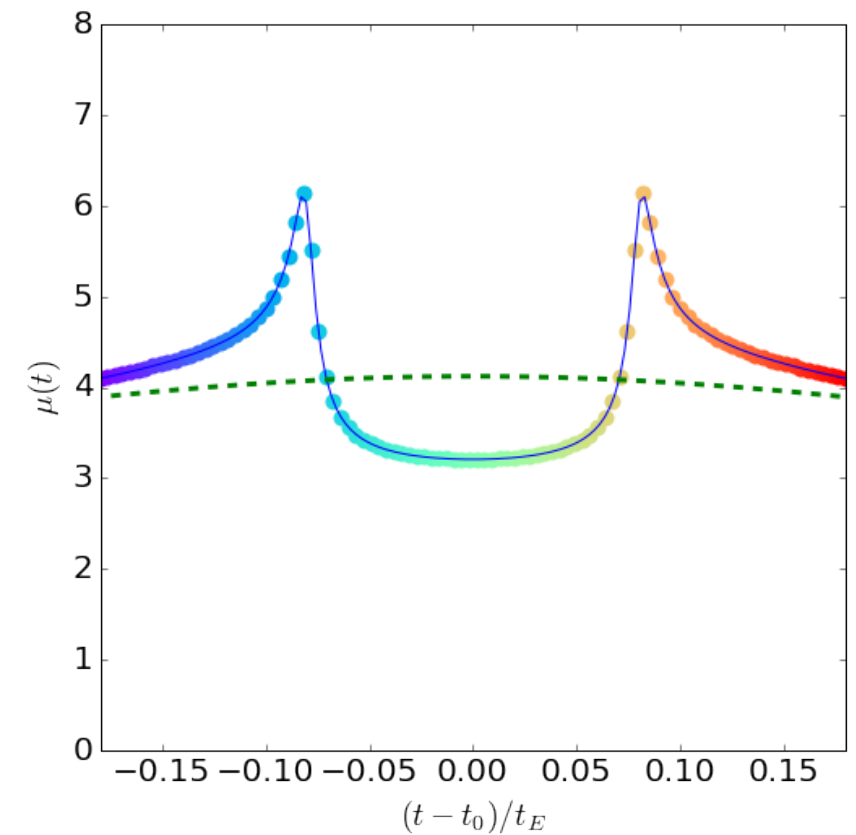
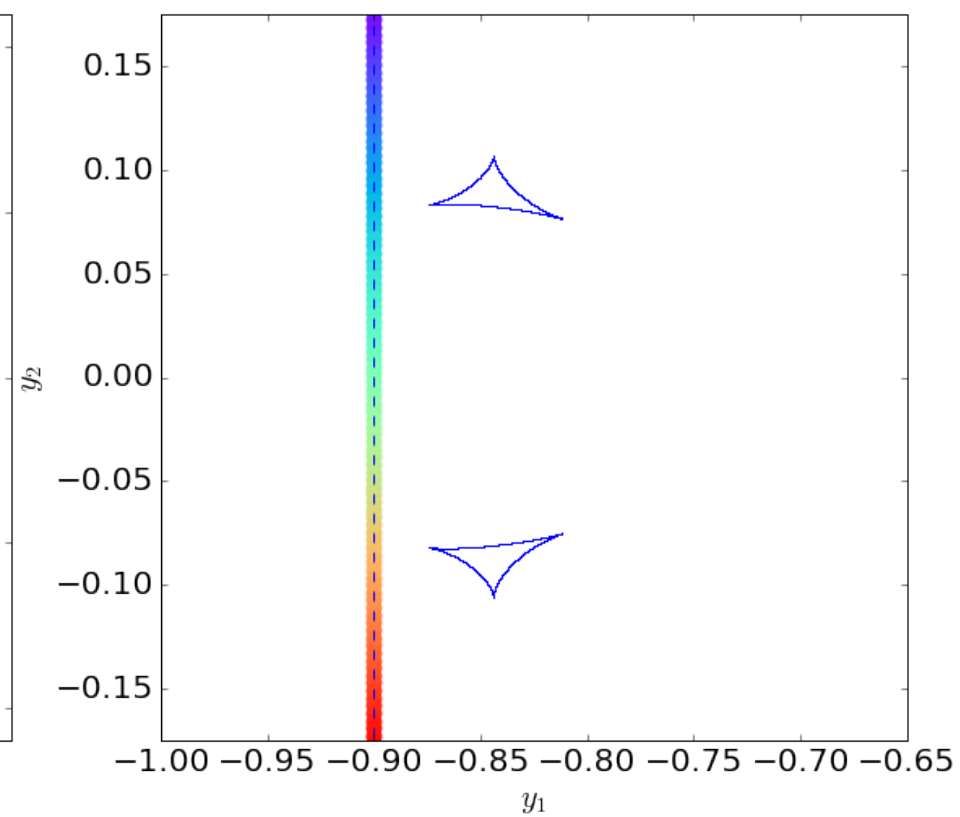
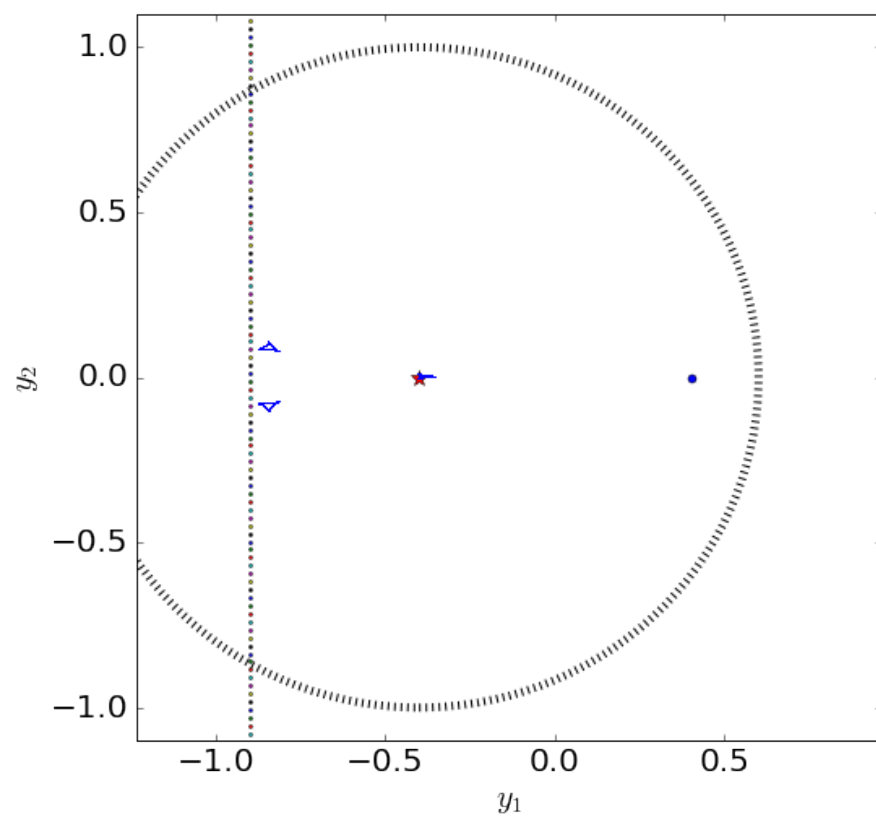


Recommended reading: Han, C., 2006, ApJ, 638, 1080

PLANETARY CAUSTICS PERTURBATIONS IN CLOSE TOPOLOGIES

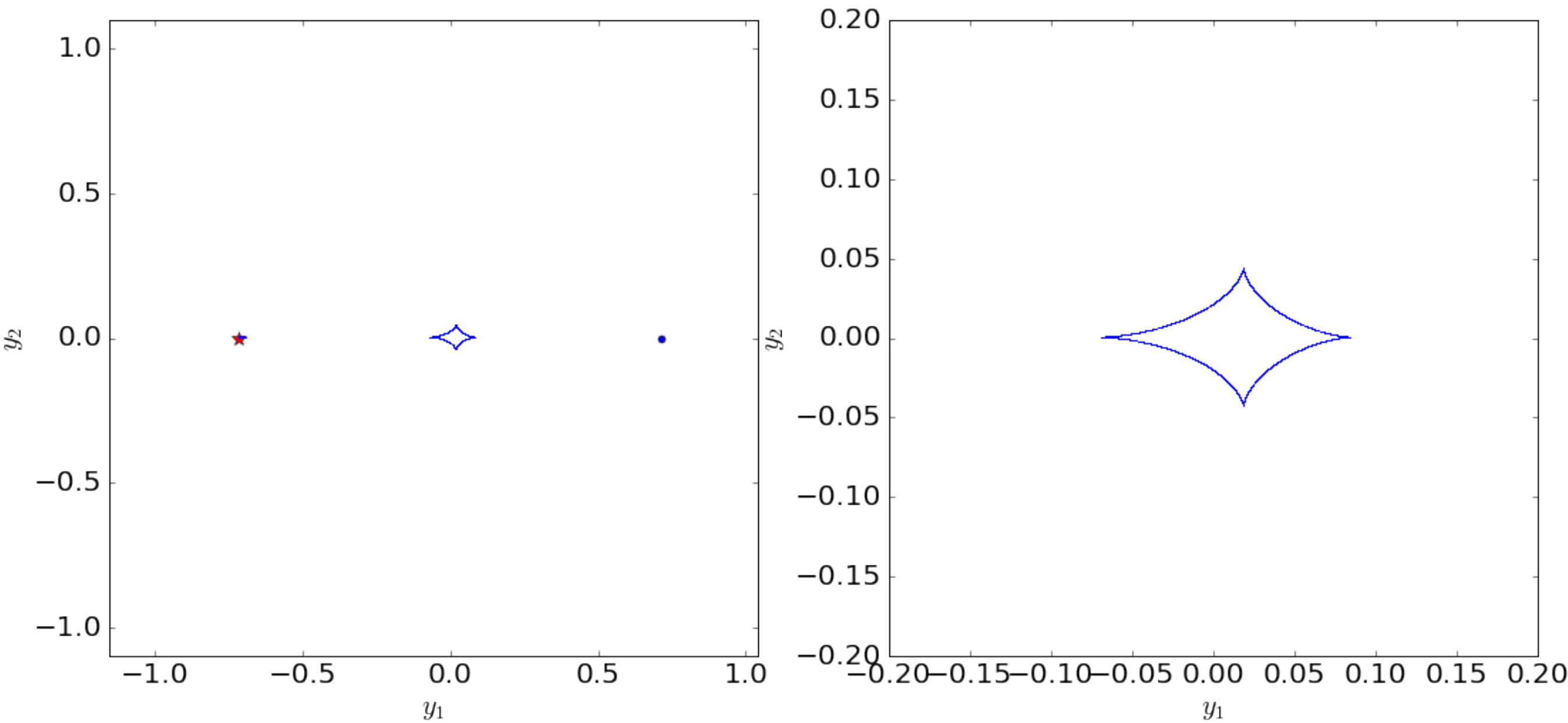


PLANETARY CAUSTICS PERTURBATIONS IN CLOSE TOPOLOGIES

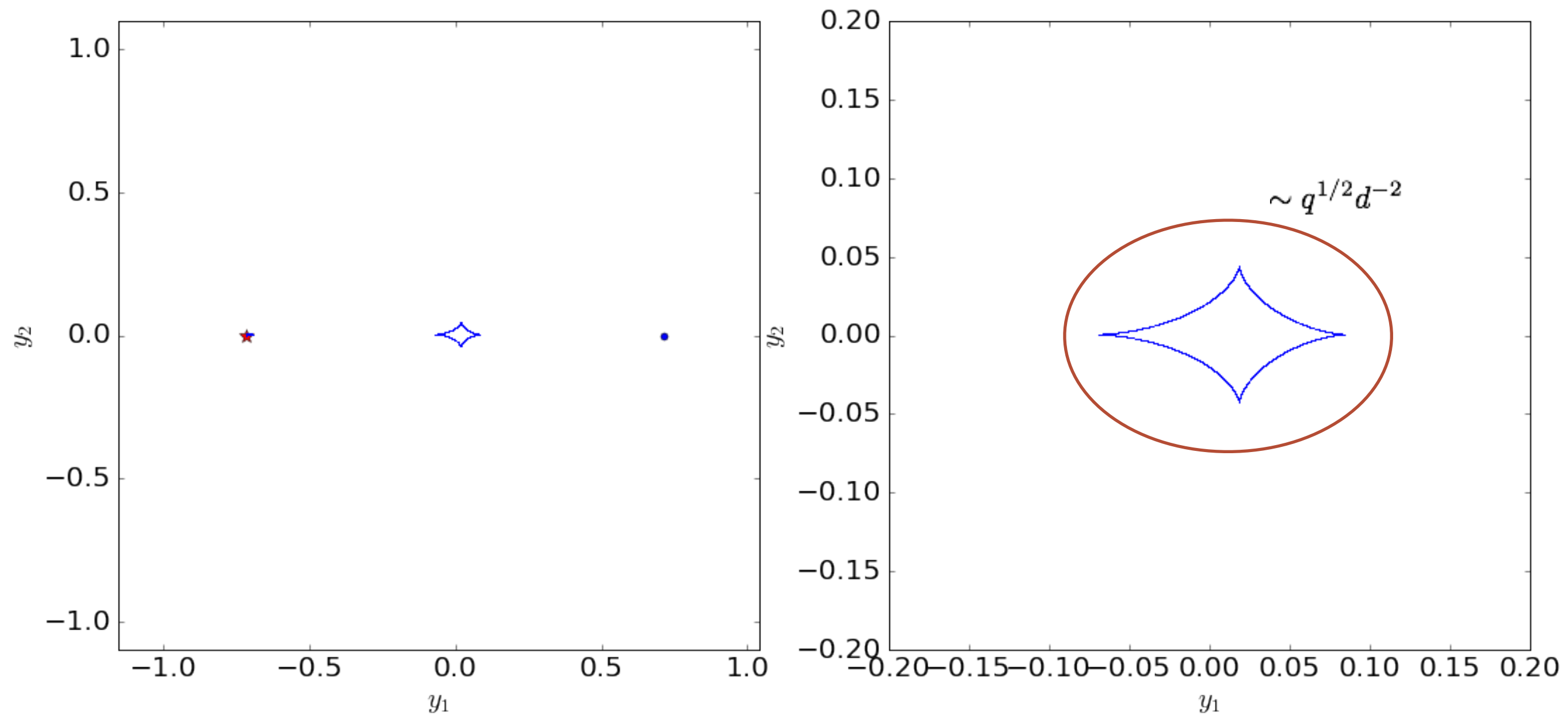


PLANETARY CAUSTICS IN WIDE TOPOLOGIES

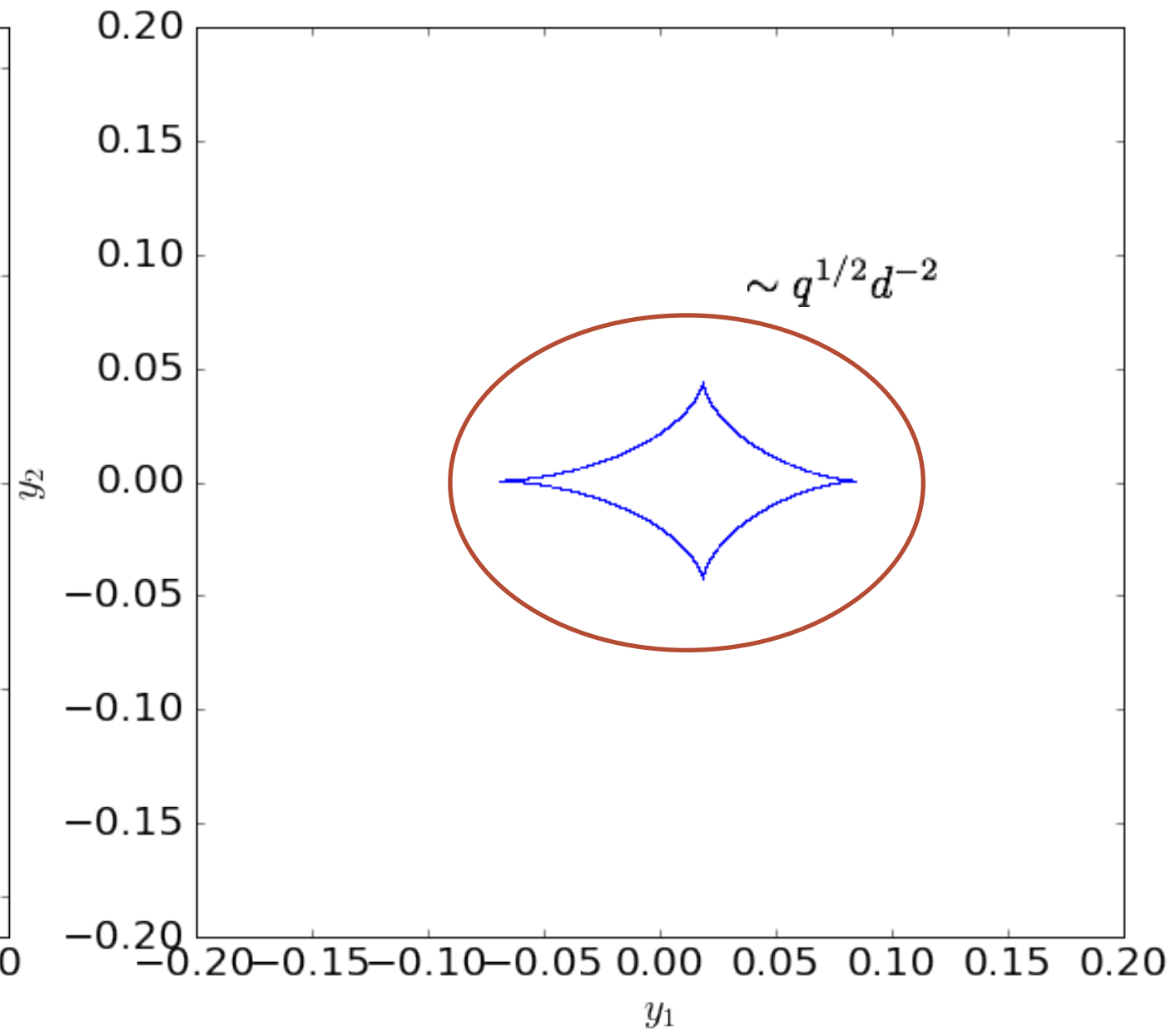
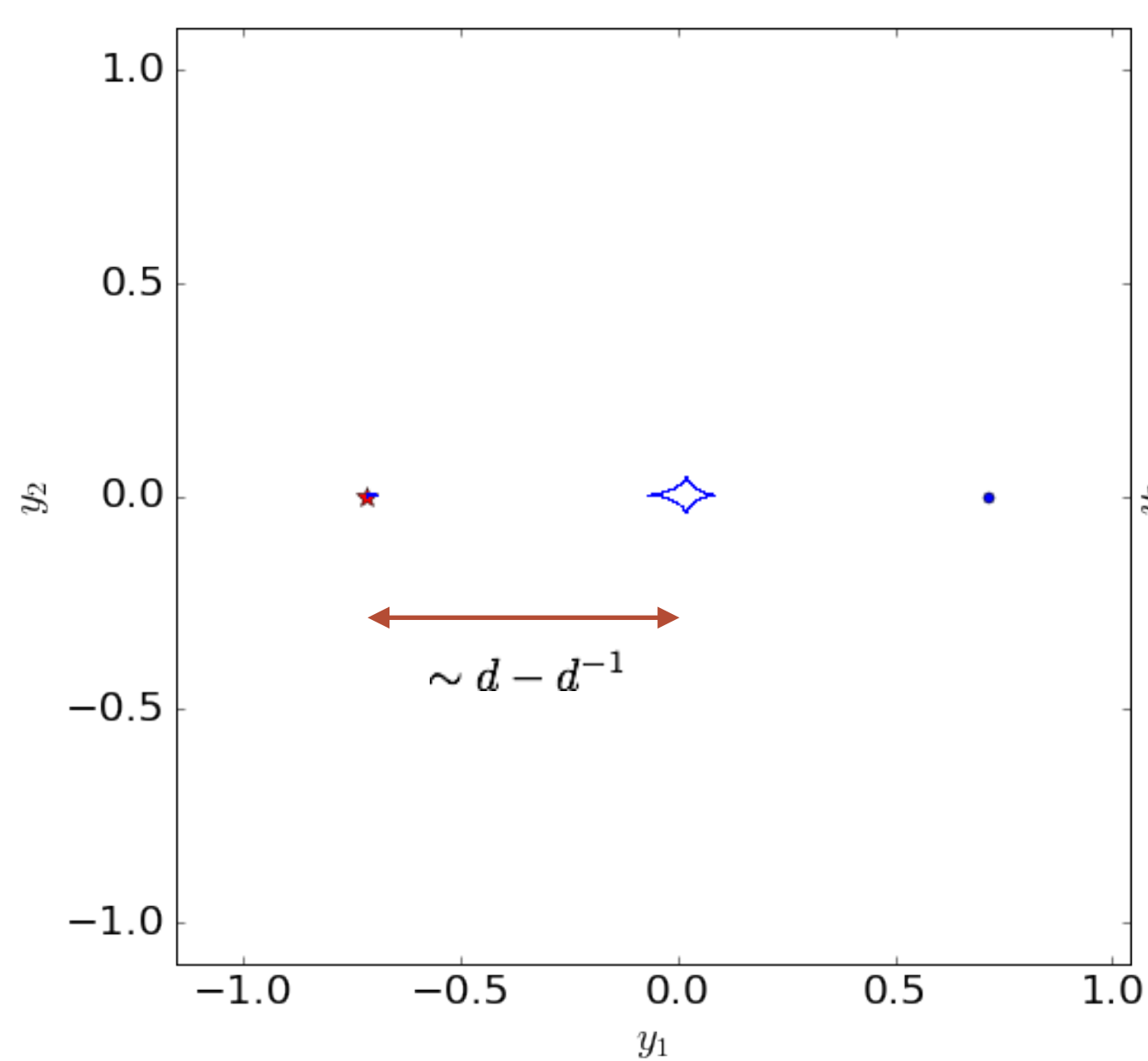
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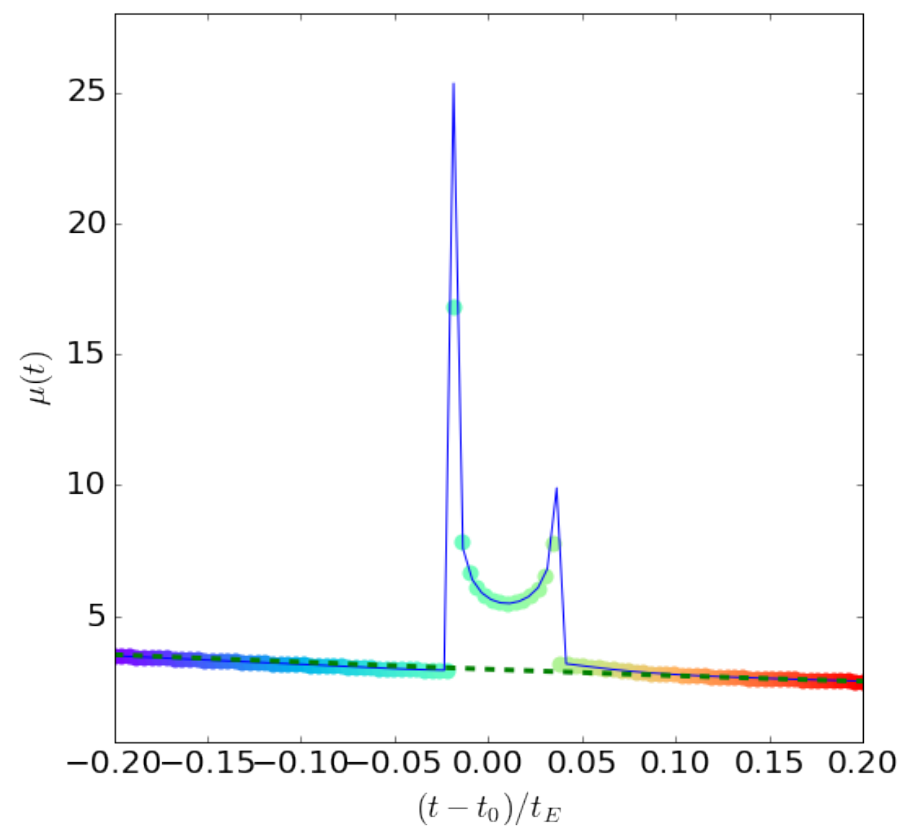
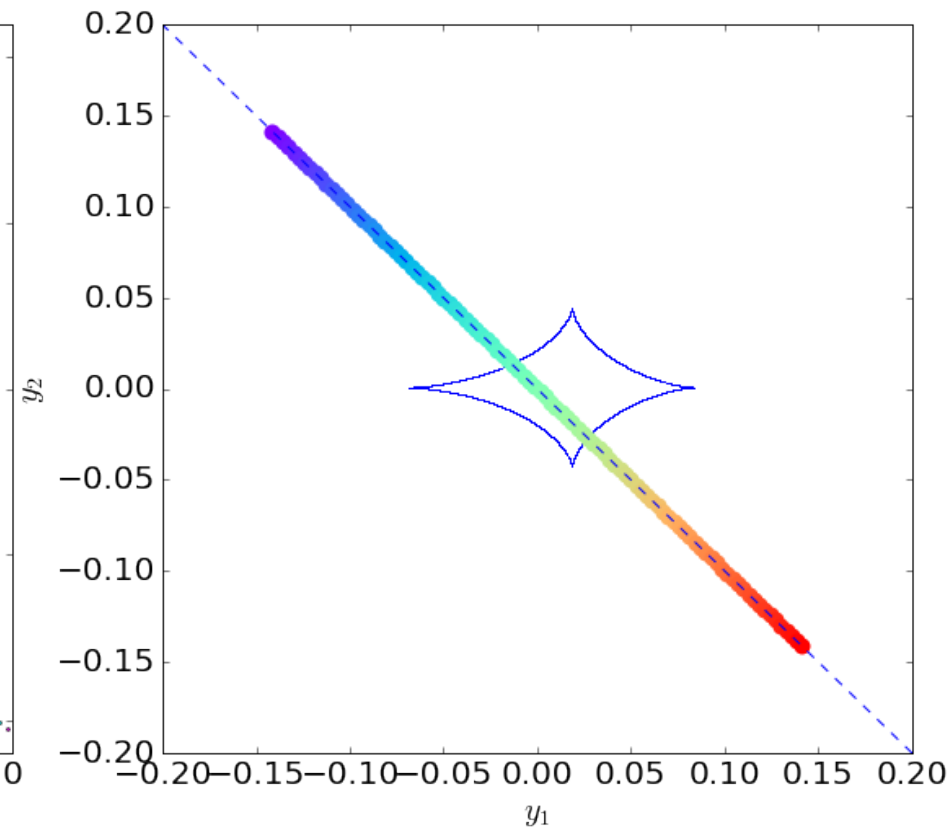
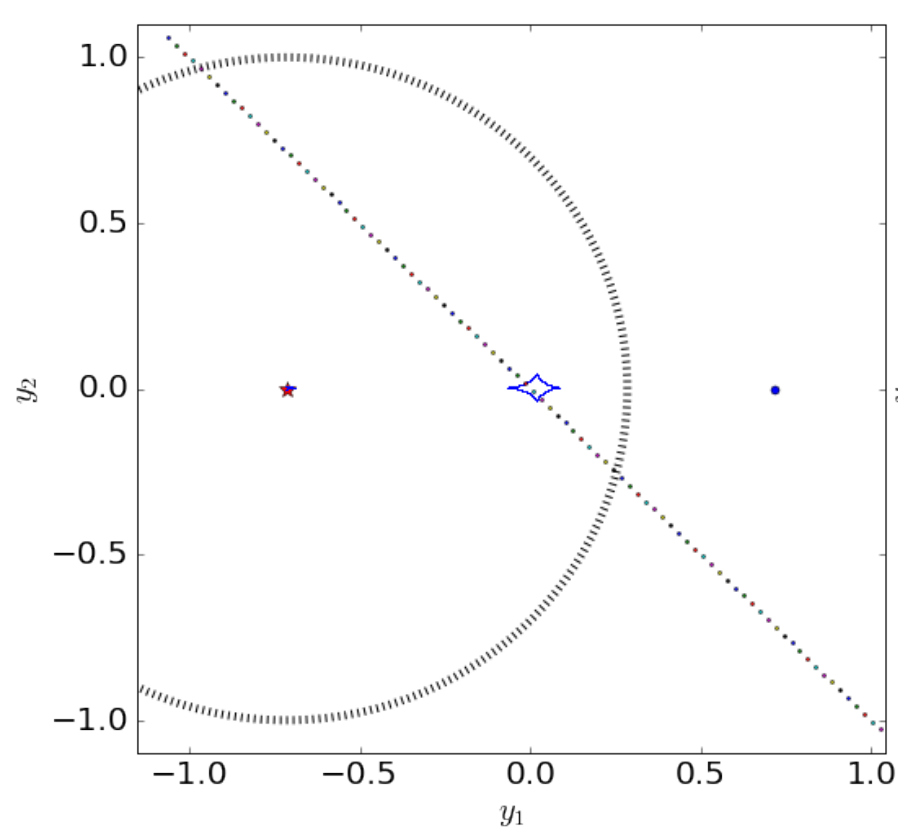
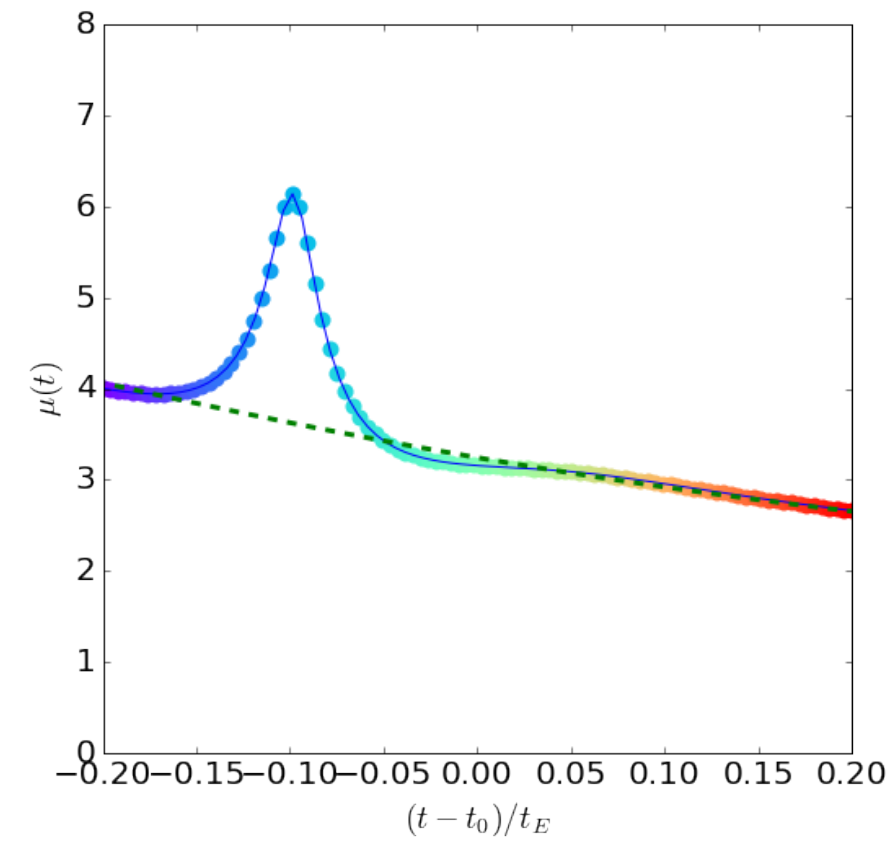
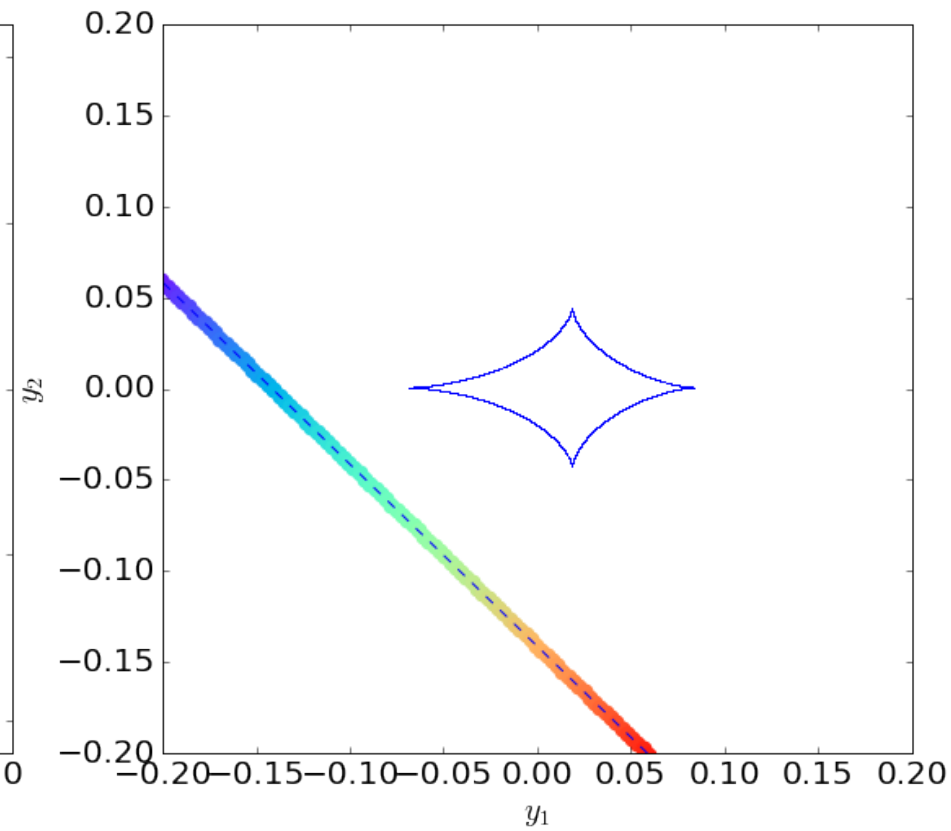
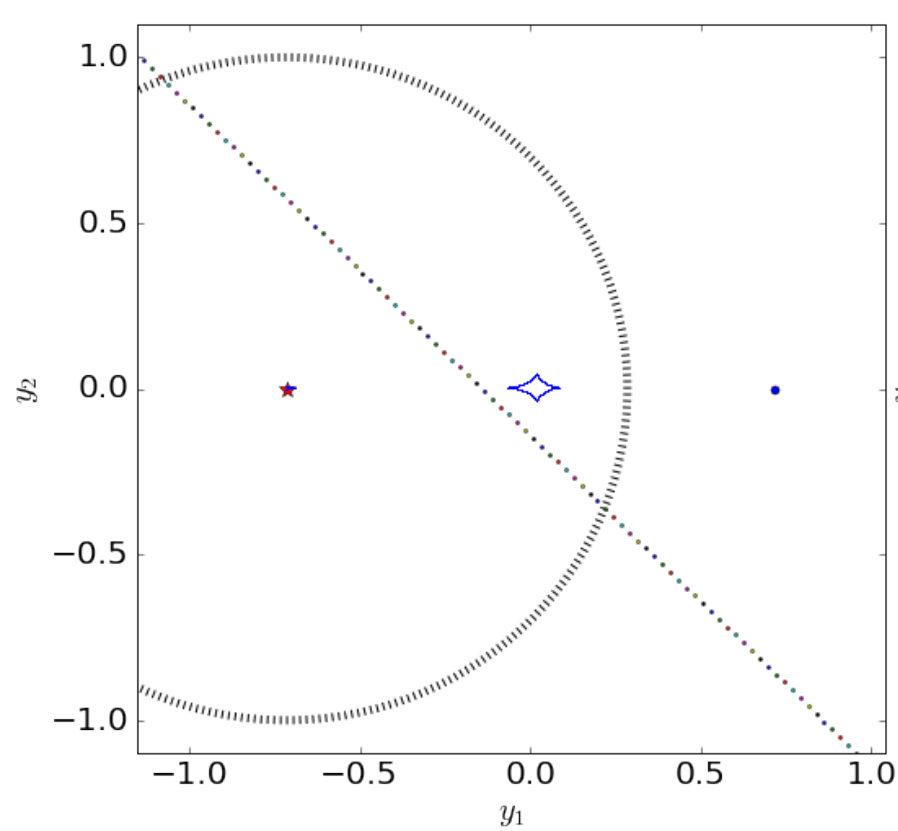
PLANETARY CAUSTICS IN WIDE TOPOLOGIES



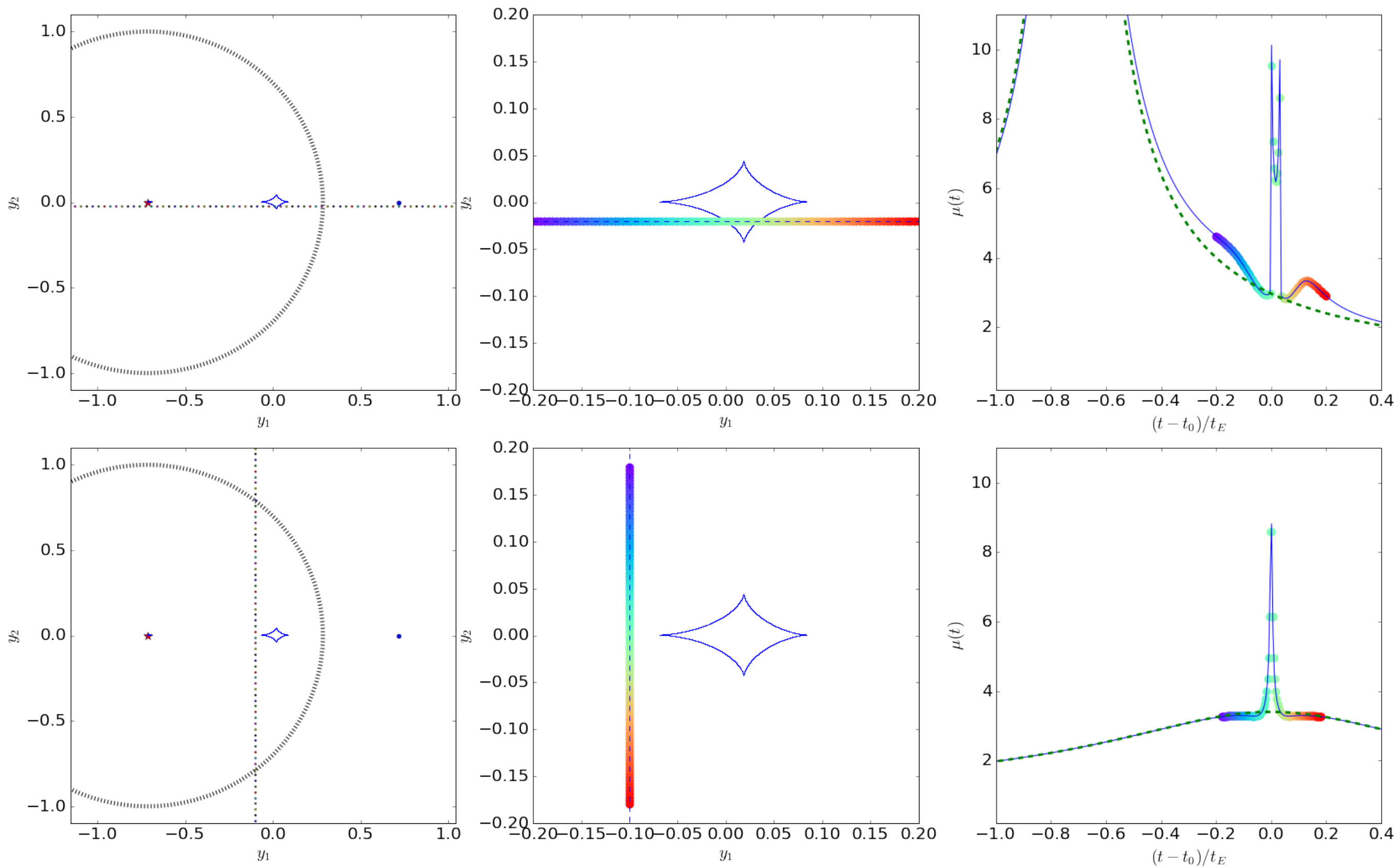
PLANETARY CAUSTICS IN WIDE TOPOLOGIES



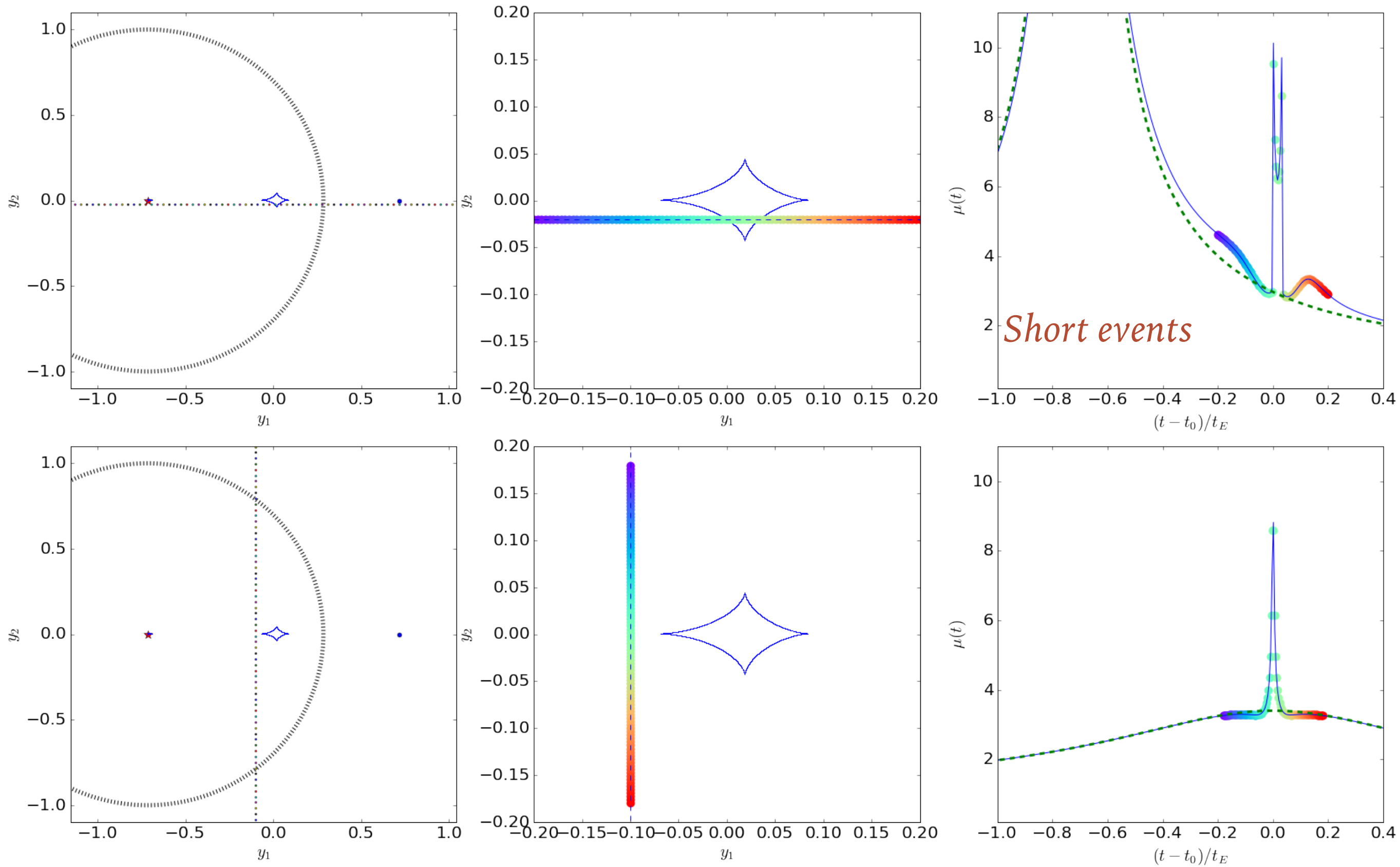
PLANETARY CAUSTICS PERTURBATIONS IN WIDE TOPOLOGIES



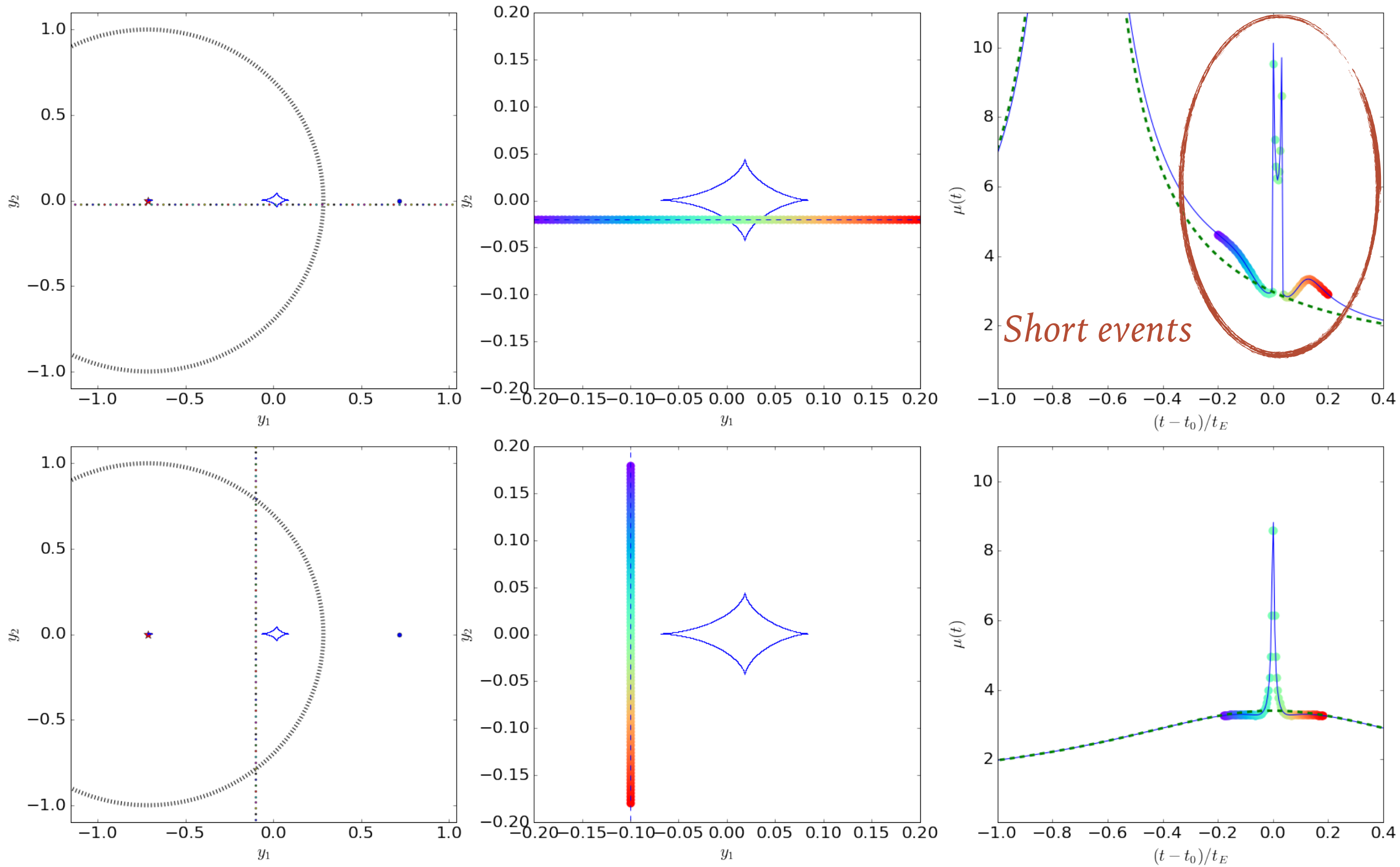
PLANETARY CAUSTICS PERTURBATIONS IN WIDE TOPOLOGIES



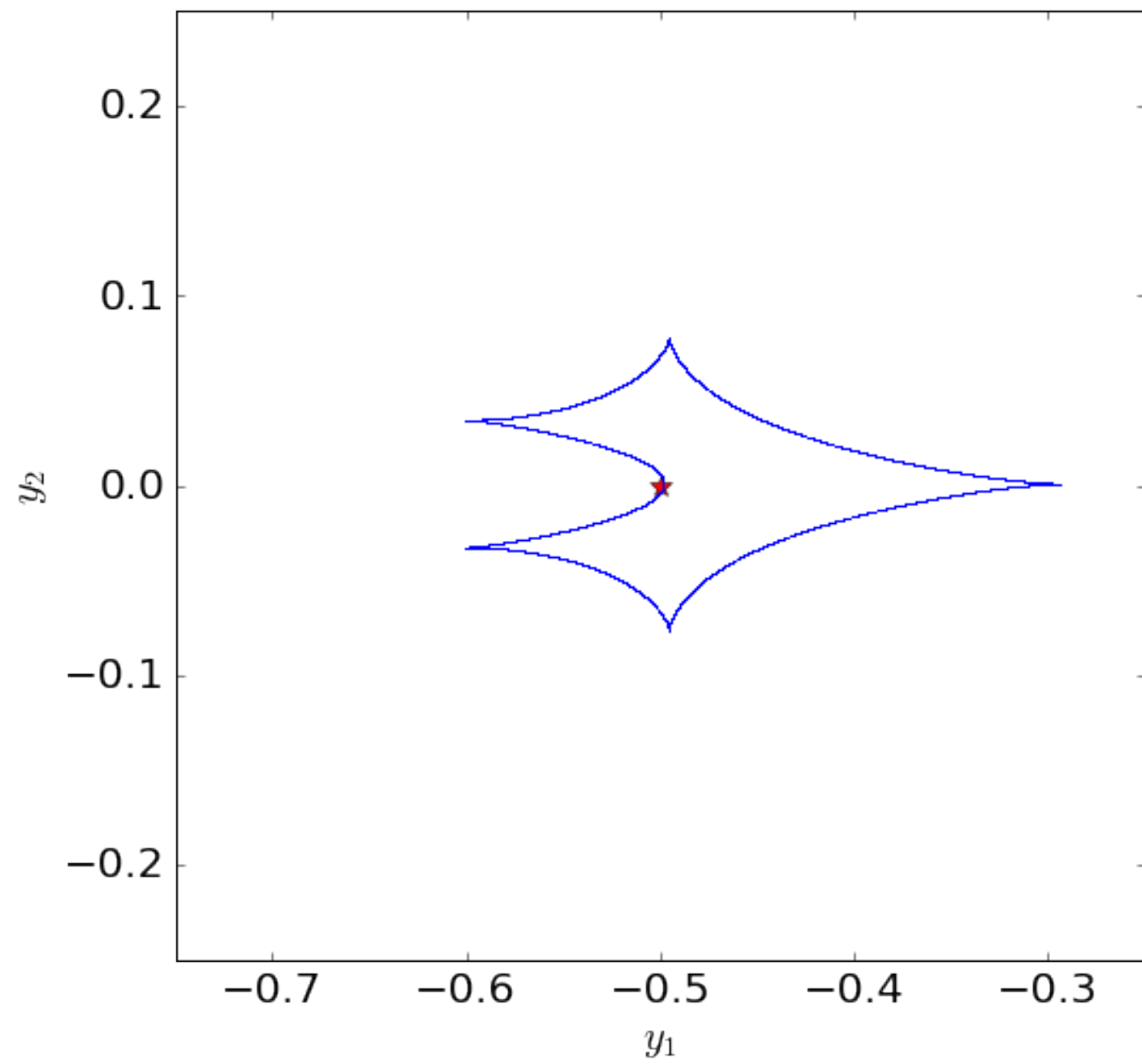
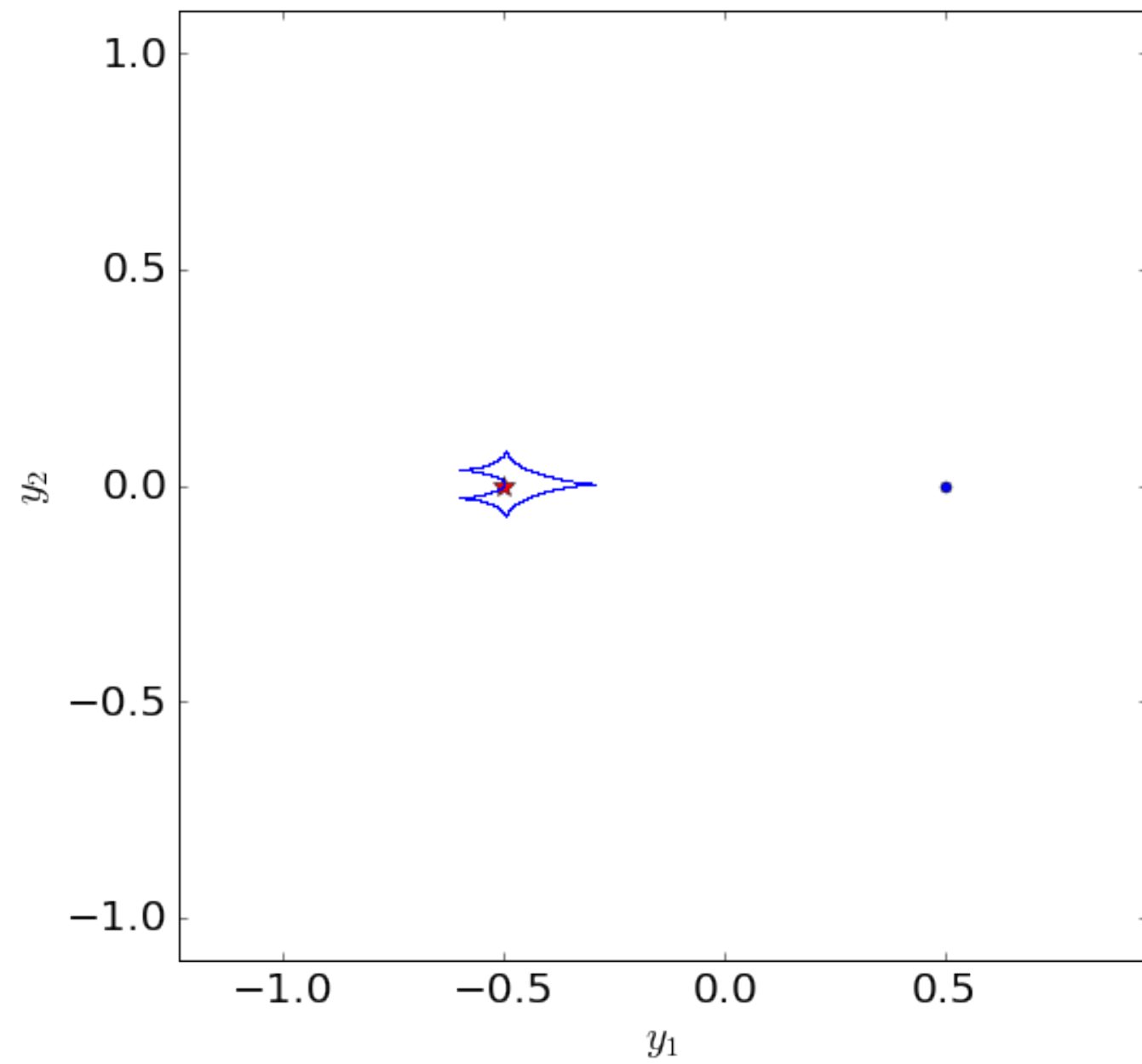
PLANETARY CAUSTICS PERTURBATIONS IN WIDE TOPOLOGIES



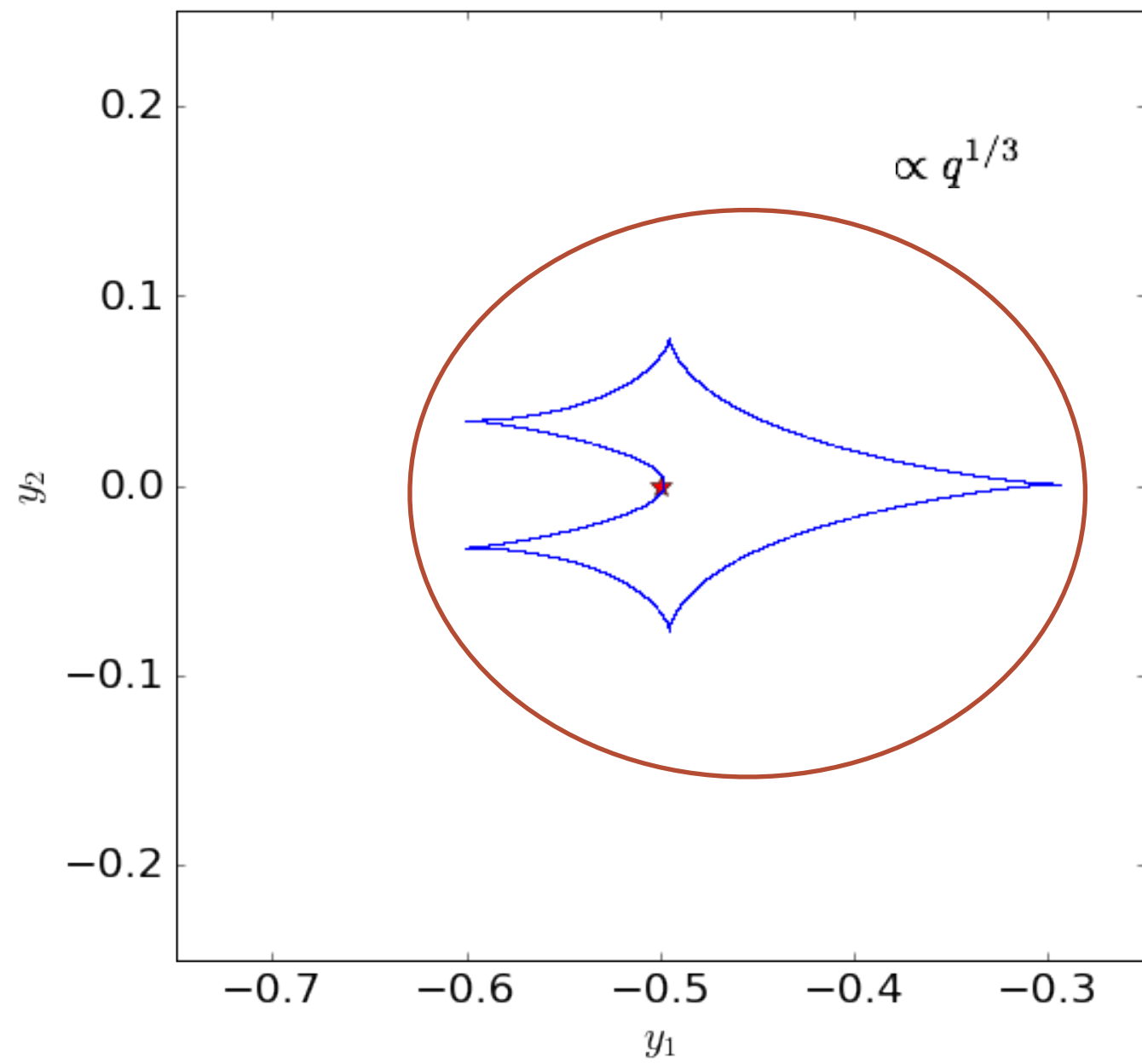
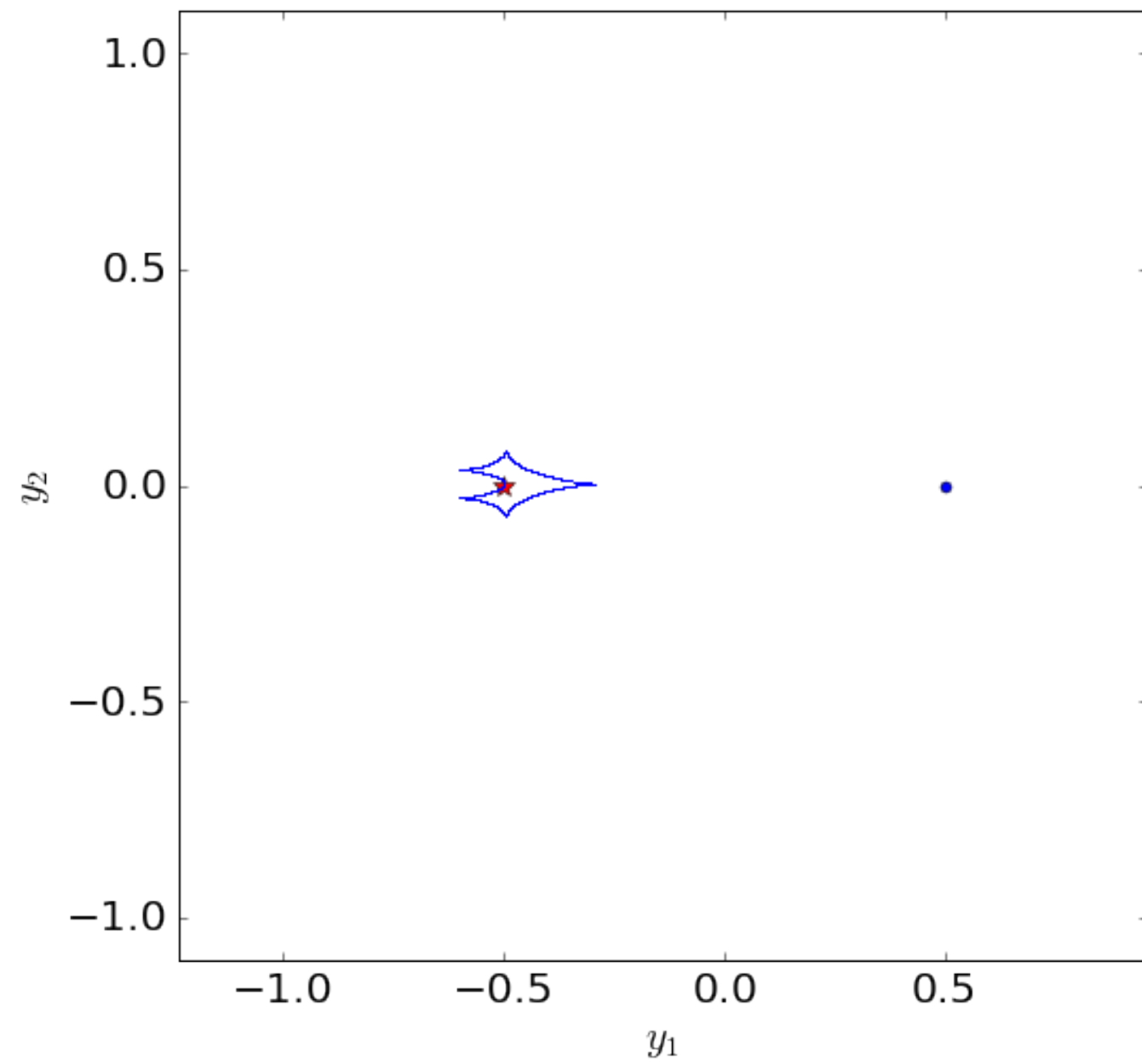
PLANETARY CAUSTICS PERTURBATIONS IN WIDE TOPOLOGIES



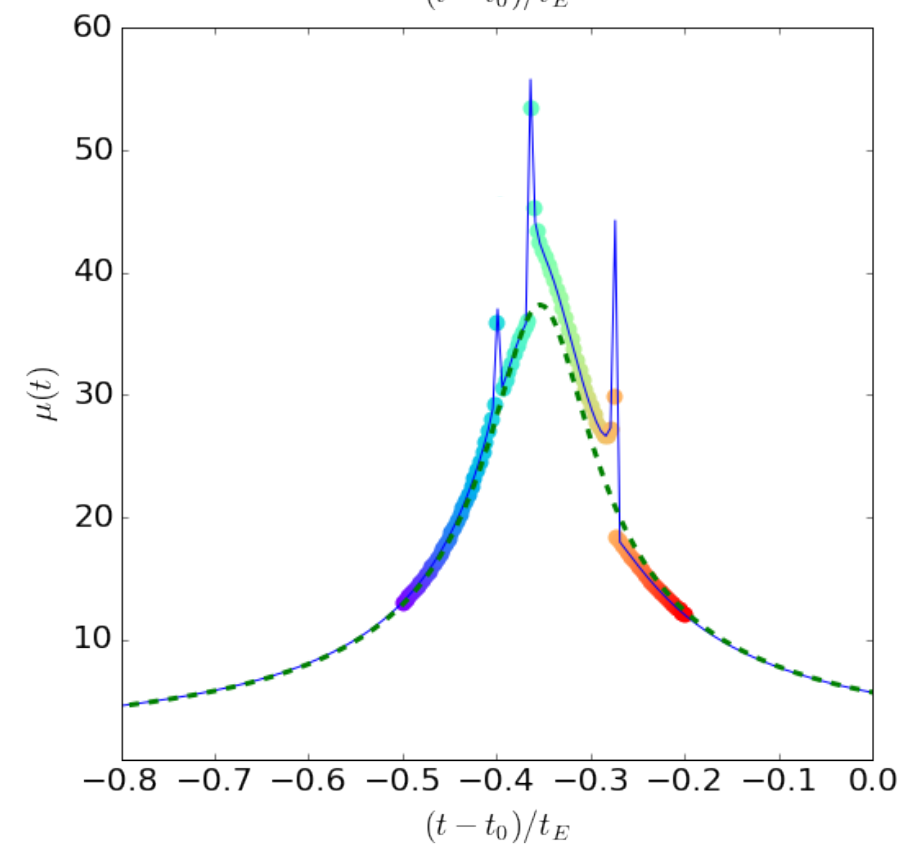
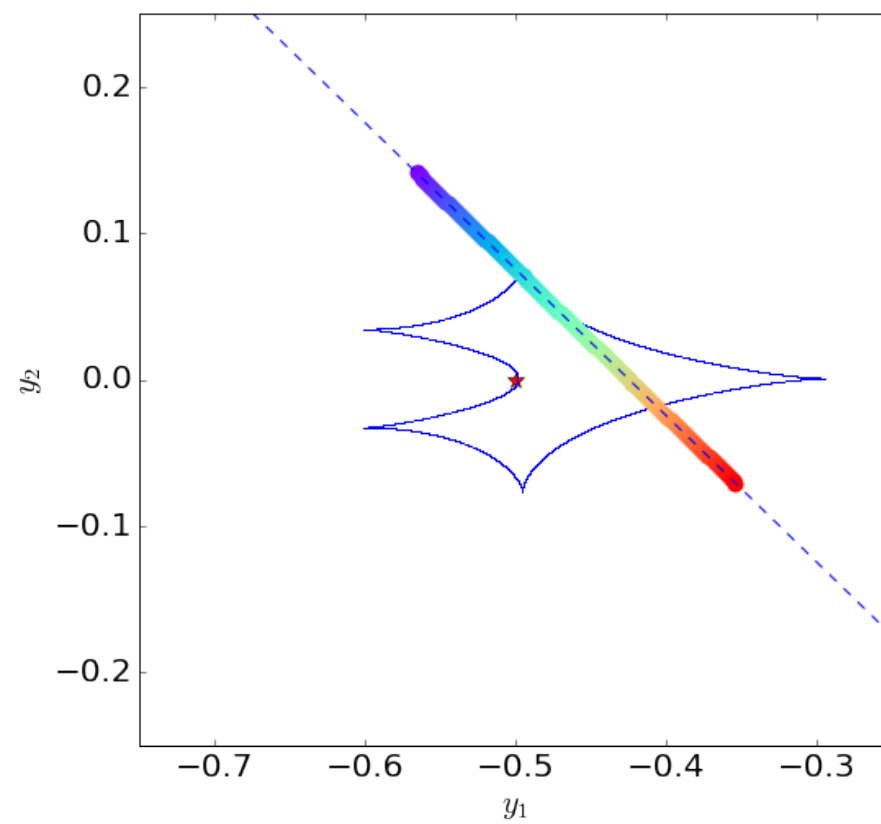
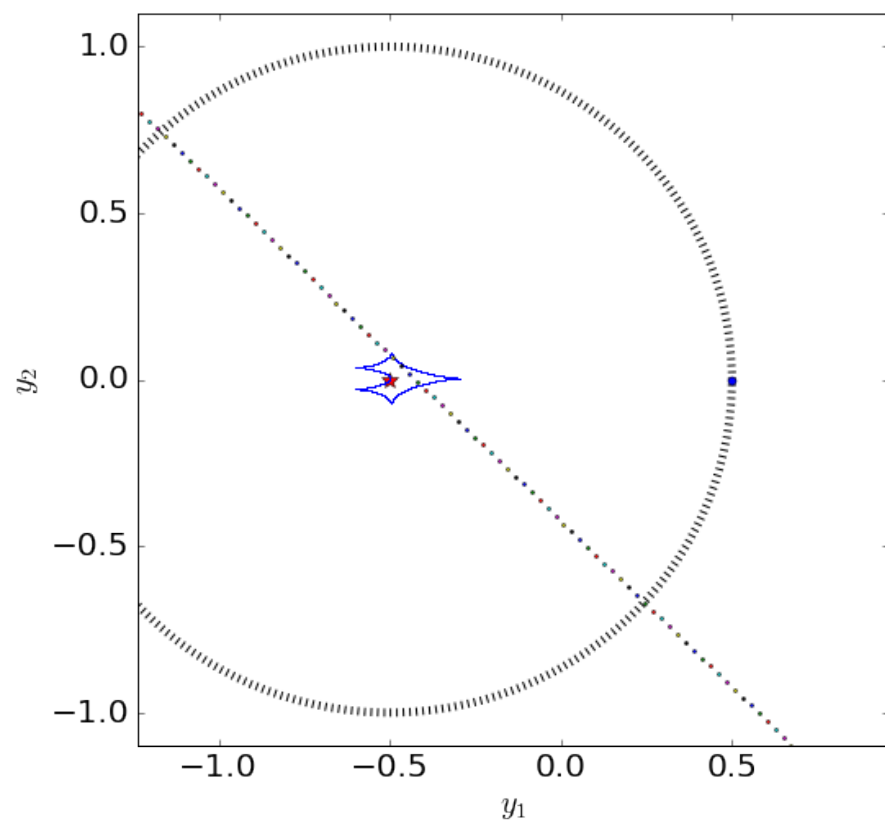
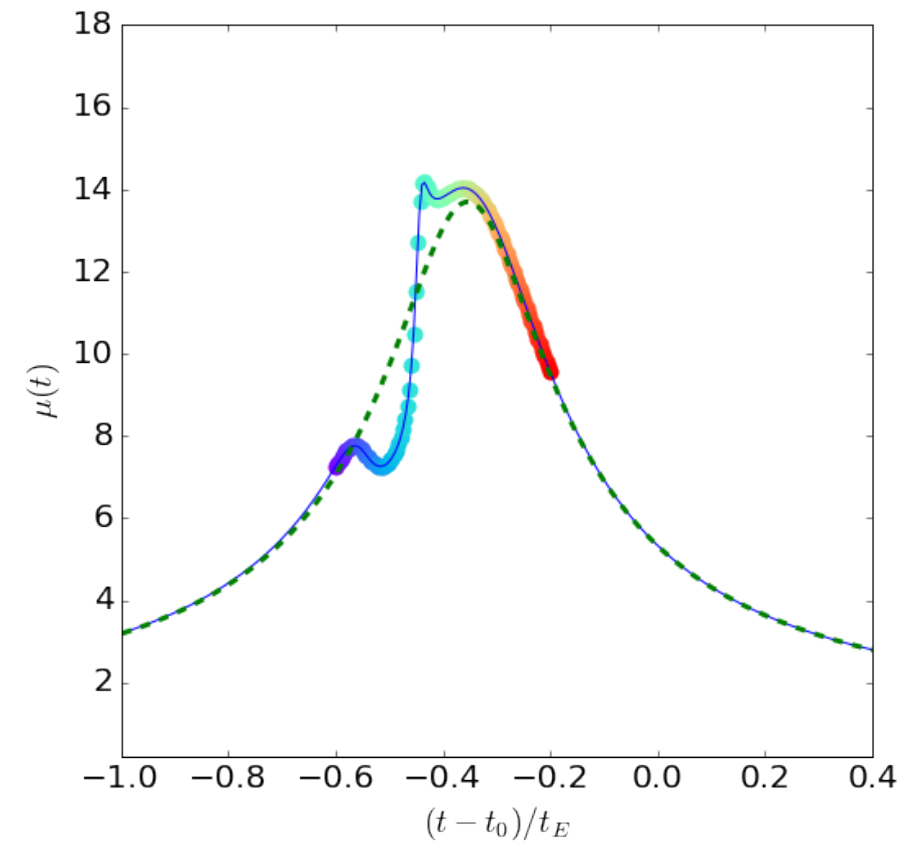
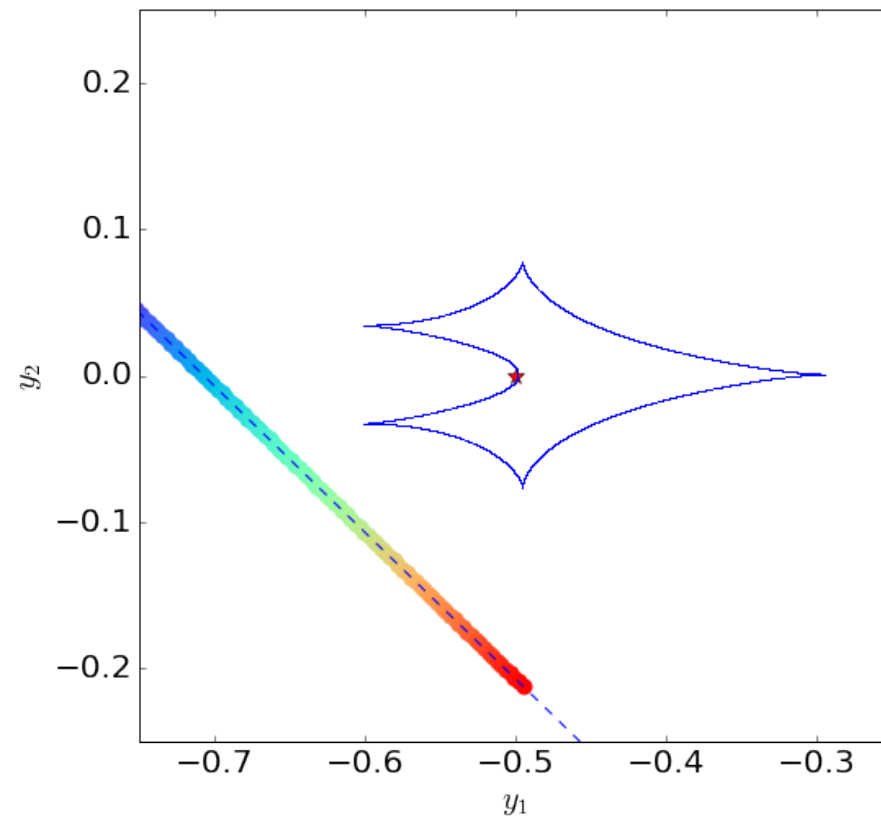
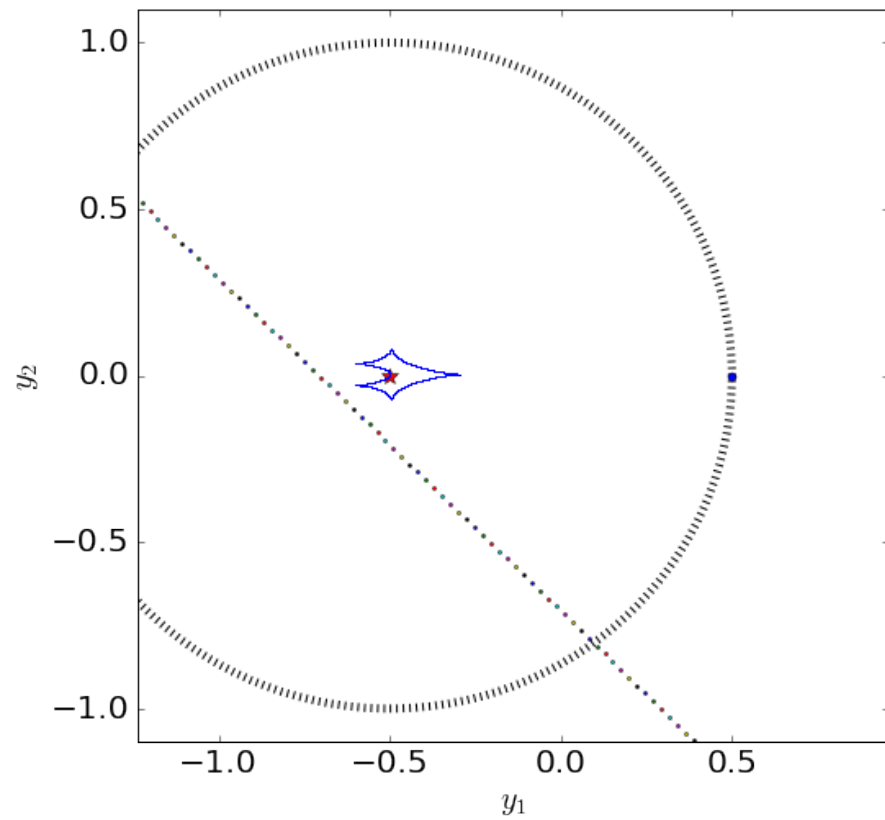
PLANETARY CAUSTICS IN INTERMEDIATE TOPOLOGIES



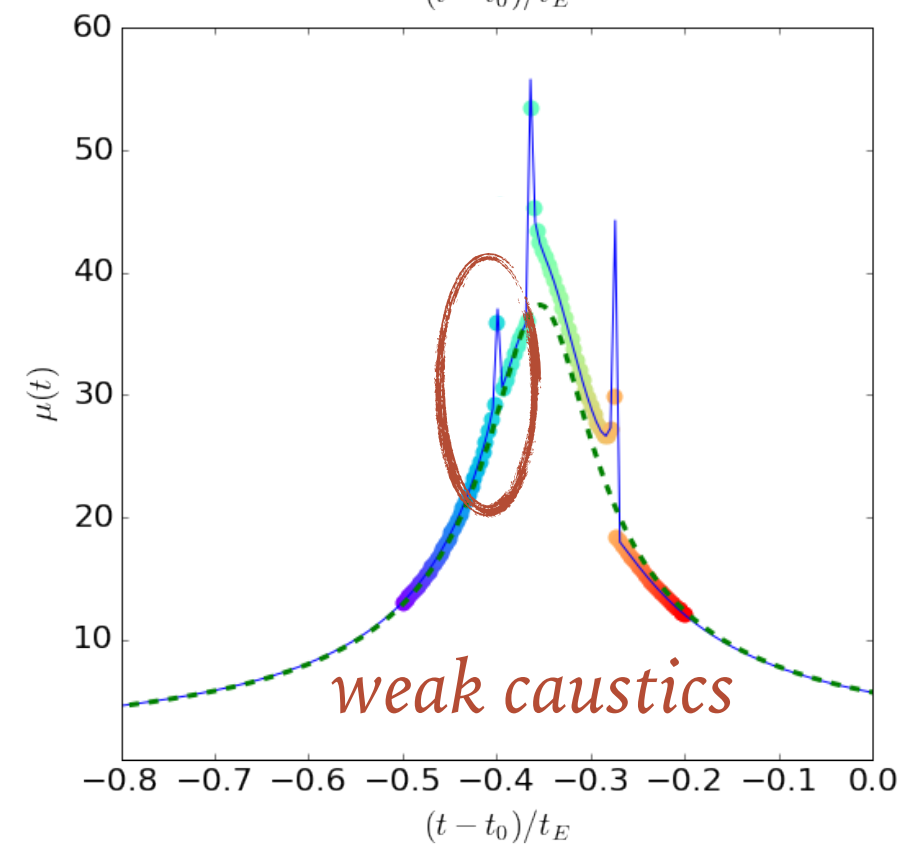
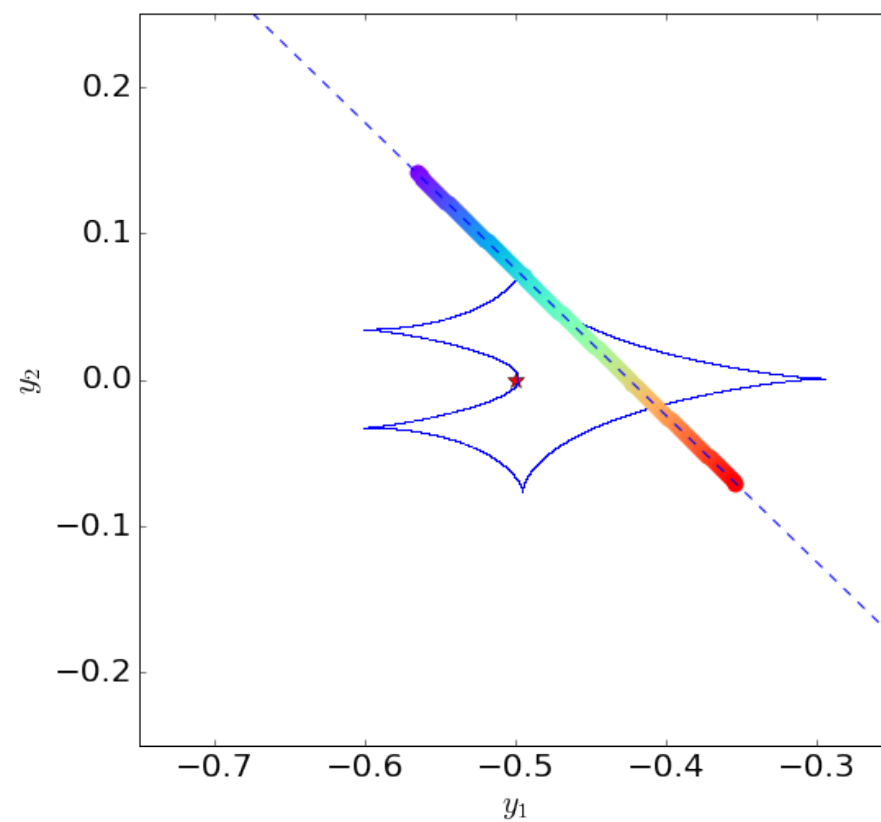
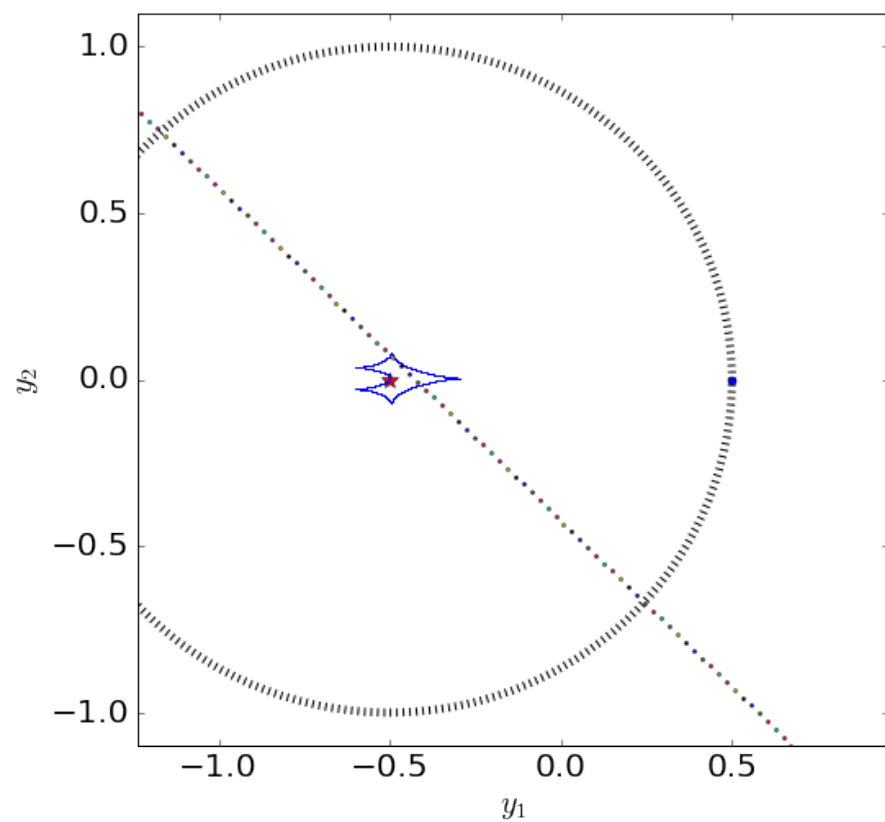
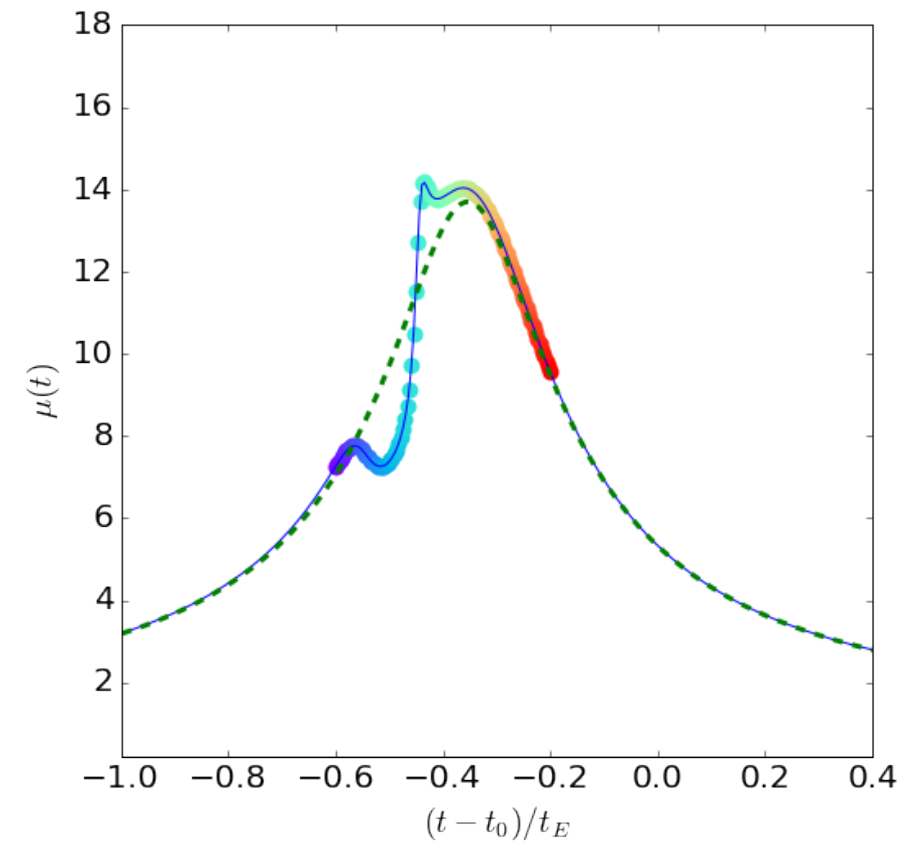
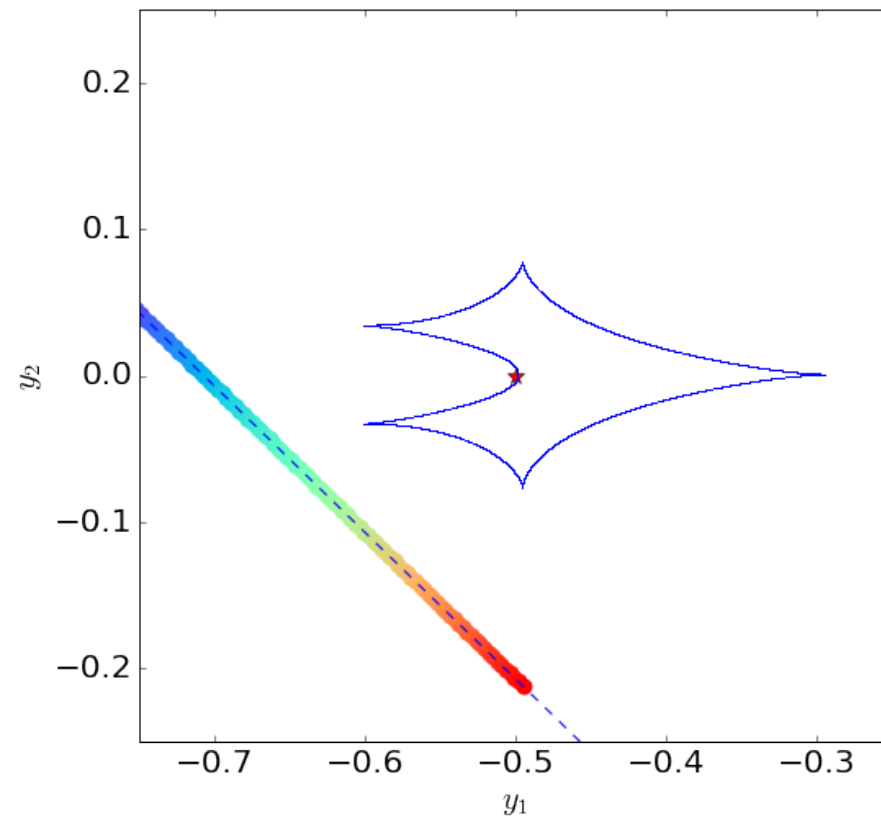
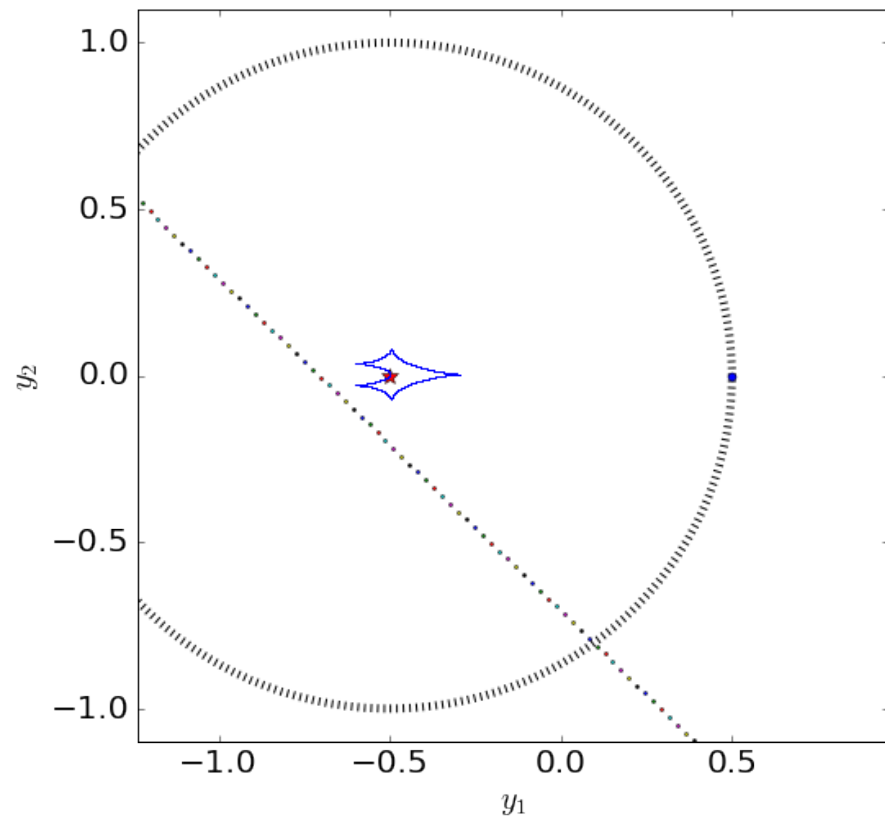
PLANETARY CAUSTICS IN INTERMEDIATE TOPOLOGIES



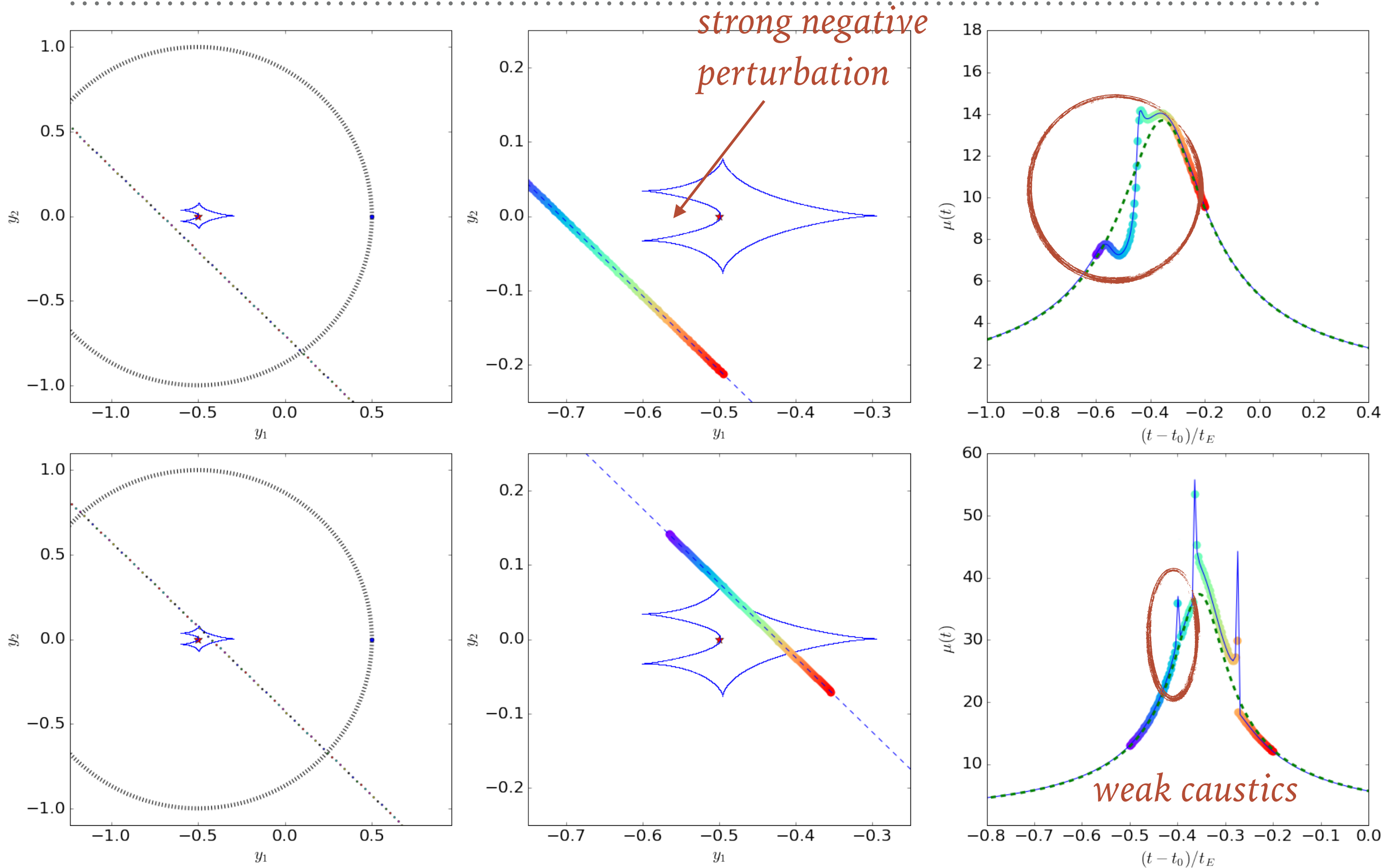
PLANETARY CAUSTICS PERTURBATIONS IN INTERMEDIATE TOPOLOGIES



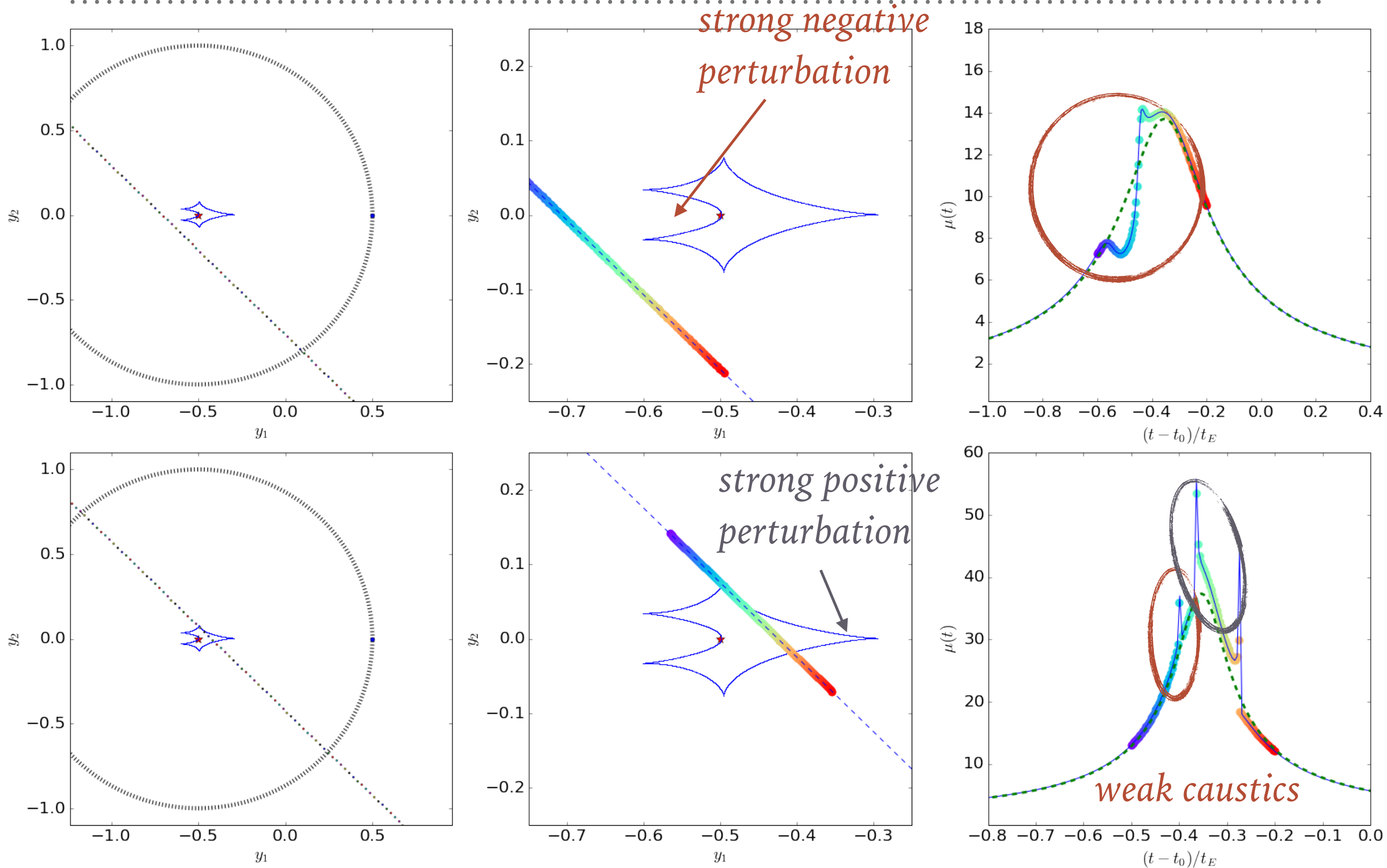
PLANETARY CAUSTICS PERTURBATIONS IN INTERMEDIATE TOPOLOGIES



PLANETARY CAUSTICS PERTURBATIONS IN INTERMEDIATE TOPOLOGIES

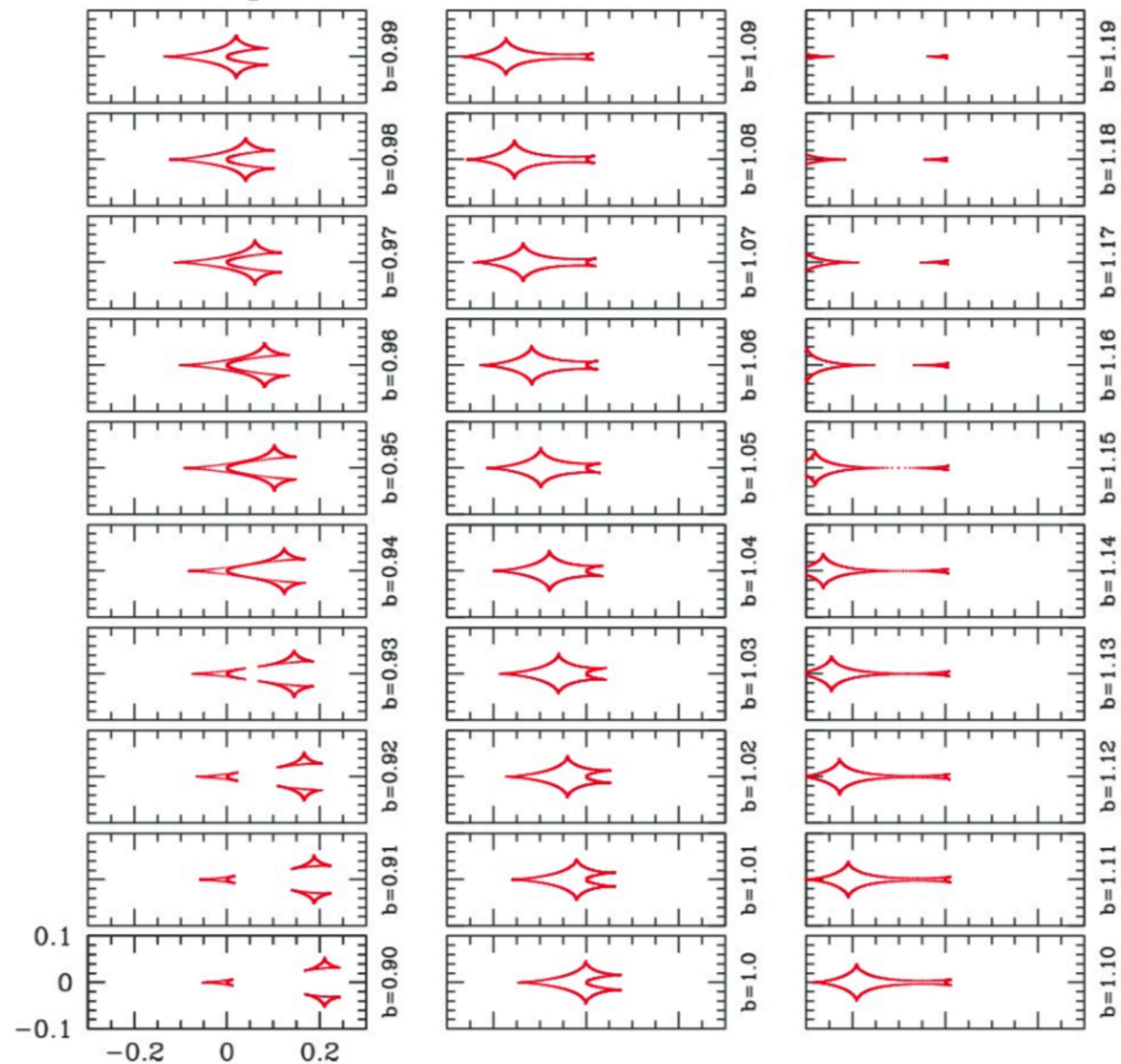


PLANETARY CAUSTICS PERTURBATIONS IN INTERMEDIATE TOPOLOGIES



SHAPE OF THE RESONANT CAUSTIC VS D

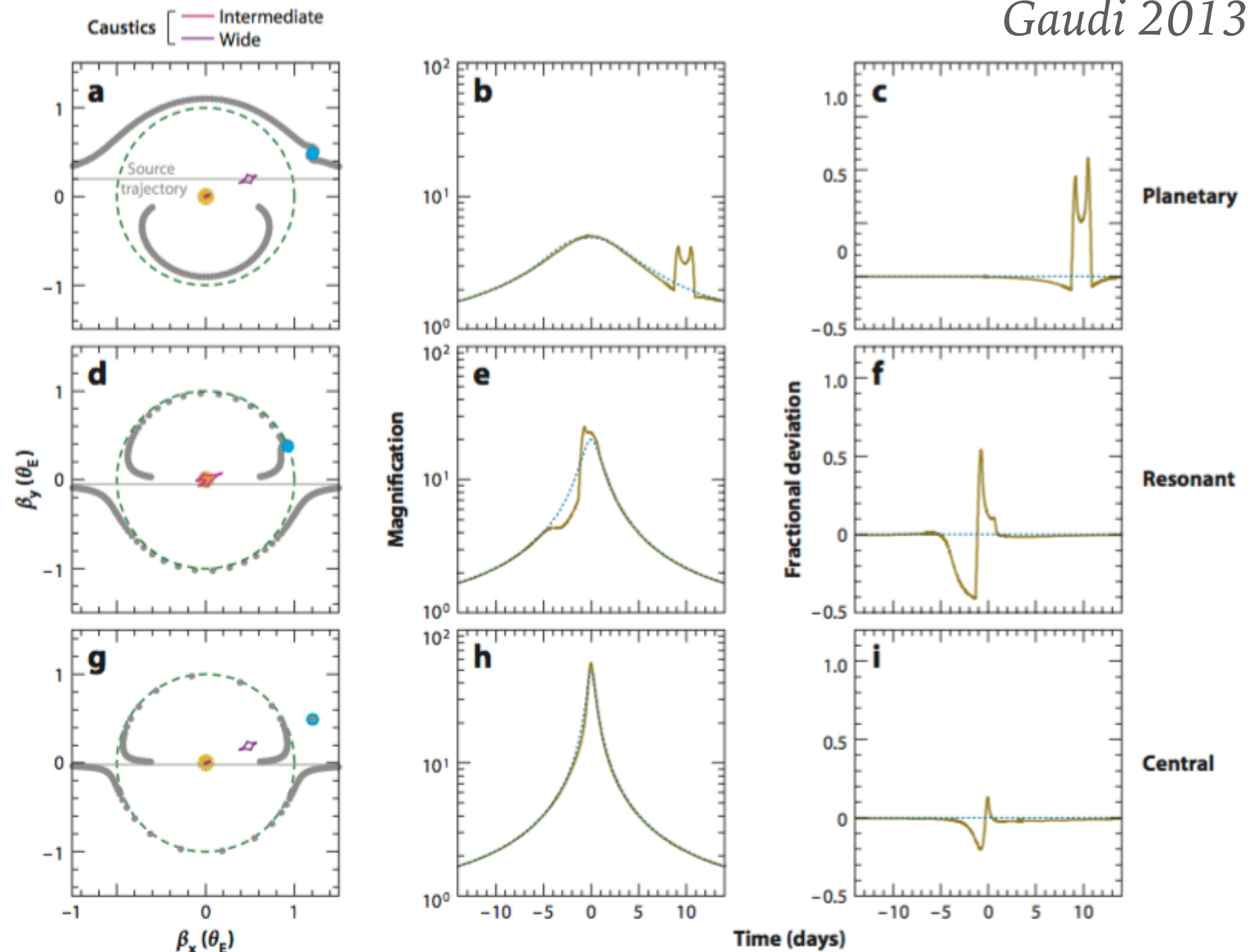
$$q = 0.001, s = 0.90 - 1.19, \Delta s = 0.29$$



A COMPLEMENTARY VIEW

The planet can be detected when it perturbs one of the two images of the source!

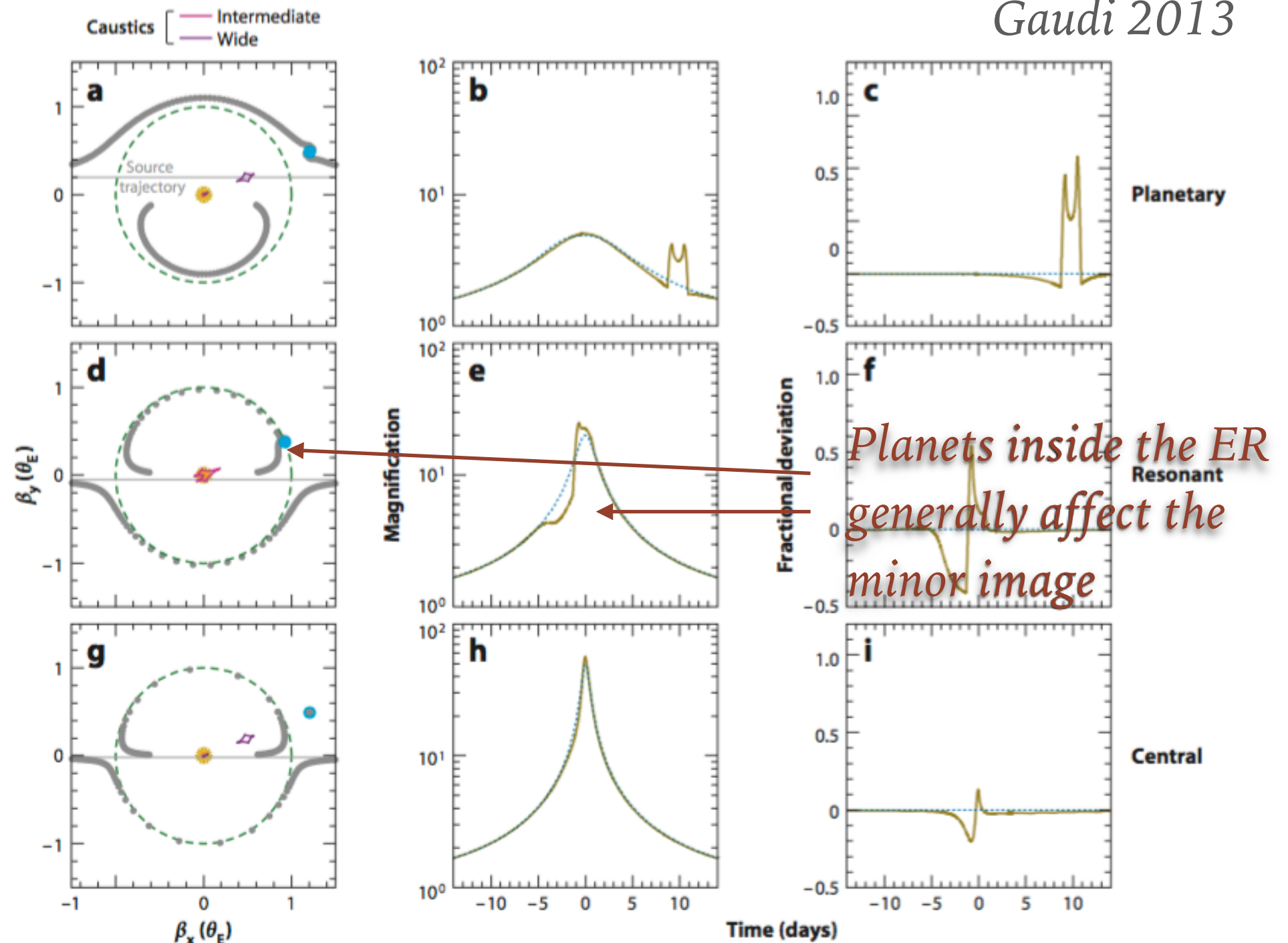
Gaudi 2013



A COMPLEMENTARY VIEW

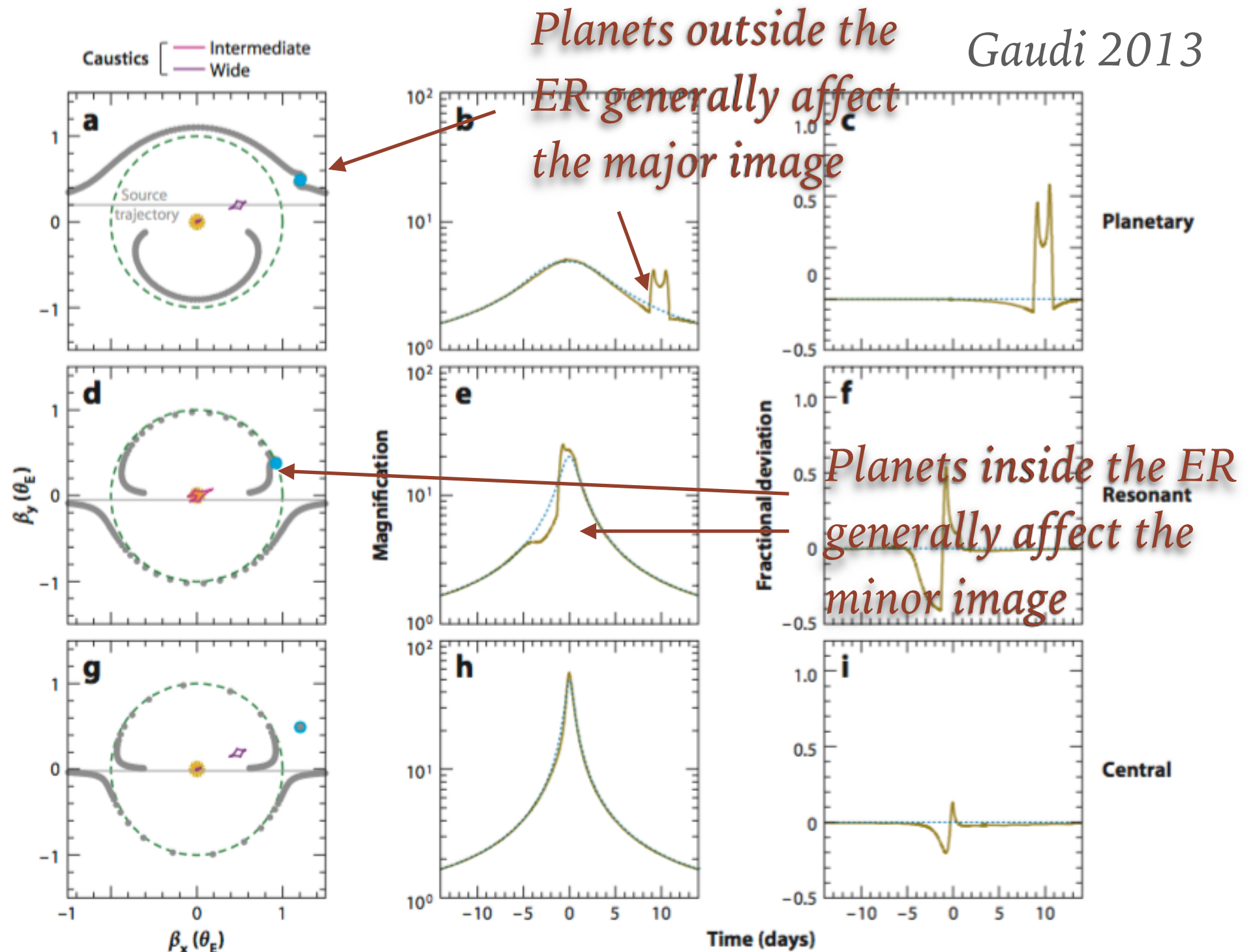
Gaudi 2013

The planet can be detected when it perturbs one of the two images of the source!



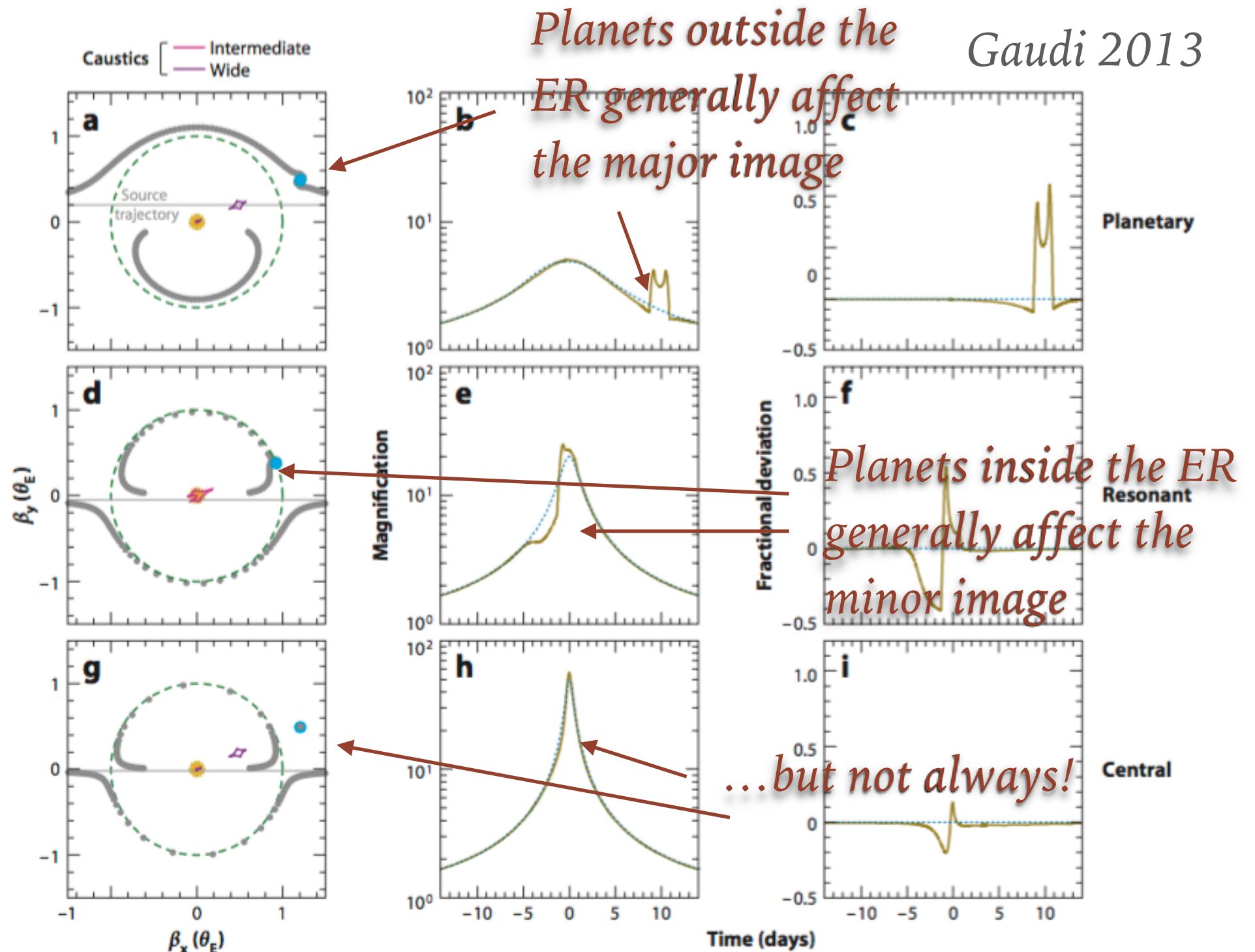
A COMPLEMENTARY VIEW

The planet can be detected when it perturbs one of the two images of the source!



A COMPLEMENTARY VIEW

The planet can be detected when it perturbs one of the two images of the source!



INTERPRETING THE LIGHT CURVES

If we notice a planetary caustic perturbation, it means that the planet is located at the position of one of the images:

$$x_{\pm} = d$$

Consequently the caustic which is being crossed has a position which can be derived from the lens equation (which is satisfied by the images)

$$y_c = |d - d^{-1}|$$