```
from matplotlib import pyplot as plt
import numpy as np
def initialize():
  RMin = 0.0
  RMax = 10.0
  lOrbital = 0
  Dim = 400
  return RMin, RMax, lOrbital, Dim
def potential(r):
  return r*r
#get the boundary, orbital momentum and number of integration matrix
RMin, RMax, lOrbital, Dim = initialize()
print(RMin, RMax, lOrbital, Dim)
#initialize the constant
Step = RMax/(Dim+1)
DiagConst = 2.0/ (Step*Step)
NondiagConst = -1.0/ (Step*Step)
OrbitalFactor = lOrbital * (lOrbital + 1.0)
print(Step, DiagConst, NondiagConst, OrbitalFactor)
#calculate array of potential values
v = np.zeros(Dim)
r = np.linspace(RMin, RMax, Dim)
#print(v, r)
for i in range(Dim):
  r[i] = RMin + (i+1)* Step
  v[i] = potential(r[i]) + OrbitalFactor/(r[i]*r[i])
  #print(r[i], v[i])
#setting up the tridiagonal matrix and find eigenvectors and eigenvalues
Hamiltonian = np.zeros((Dim,Dim))
Hamiltonian[0,0] = DiagConst + v[0];
Hamiltonian[0,1] = NondiagConst;
for i in range(1, Dim-1):
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Hamiltonian[i,i-1] = NondiagConst;
  Hamiltonian[i,i] = DiagConst + v[i];
  Hamiltonian[i,i+1] = NondiagConst;
Hamiltonian[Dim-1, Dim-2] = NondiagConst;
Hamiltonian[Dim-1, Dim-1] = DiagConst + v[Dim-1];
print(Hamiltonian)
#use linalg.eig to find eigenvector and eigenvalues
EigValues, EigVectors = np.linalg.eig(Hamiltonian)
#sort eigenvalues and eigenvector
permute = EigValues.argsort()
EigValues = EigValues[permute]
EigVectors = EigVectors[:,permute]
#plot the result for the three lowest lying eigenstates
for i in range(3):
  print(EigValues[i])
FirstEigvector = EigVectors[:,0]
SecondEigvector =EigVectors[:,1]
ThirdEigvector = EigVectors[:,2]
plt.plot(r, FirstEigvector**2, 'b-', r, SecondEigvector**2, 'g-', r, ThirdEigvector*
plt.axis([0,4.6,0.0,0.025])
plt.xlabel(r'$r$')
plt.ylabel('Radial probability $r^2|R(r)|^2$')
plt.title(r'Radial probability distributions for three lowest-lying states')
plt.savefig('eigenvector.pdf')
plt.savefig('eigenvector.png')
plt.show()
```

```
0.0 10.0 0 400
0.02493765586034913 3216.019999999999 -1608.009999999999 0.0
[[ 3216.02062189 -1608.01
                                     0.
      0.
                                ]
                      0.
 [-1608.01]
                  3216.02248755 -1608.01
                                                         0.
      0.
                      0.
                                ]
                                  3216.02559698 ...
 [
      0.
                 -1608.01
                                                         0.
      0.
                      0.
                                ]
                      0.
      0.
                                     0.
                                                 ... 3314.52933763
  -1608.01
                      0.
                                ]
                                     0.
      0.
                      0.
                                                 ... -1608.01
   3315.02498131 -1608.01
      0.
                      0.
                                     0.
                                                          0.
                                                 . . .
  -1608.01
                  3315.52186877]]
2.9998056468165792
```

6.999028164531277

10.997628541598054

