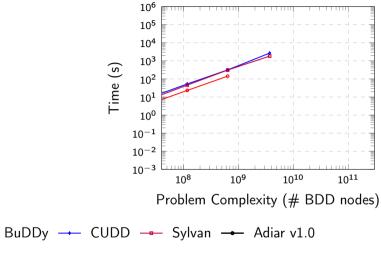
Predicting Memory Demands of BDD Operations using Maximum Graph Cuts

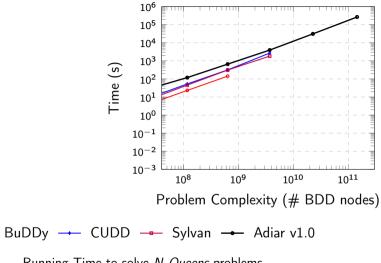
Steffan Christ Sølvsten and Jaco van de Pol

ATVA 2023

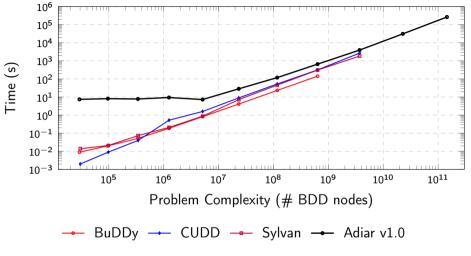




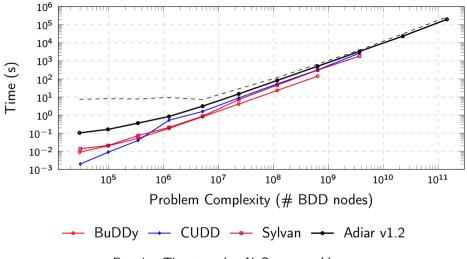
Running Time to solve *N-Queens* problems.



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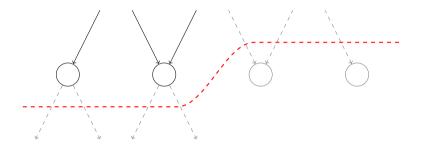


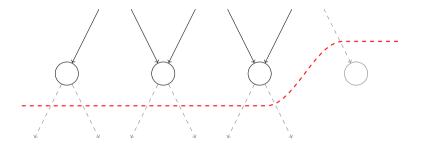
Running Time to solve *N-Queens* problems.

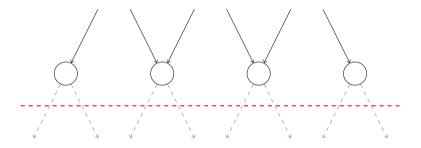




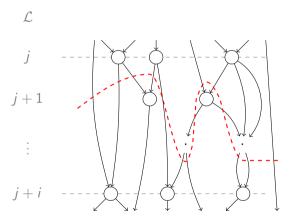




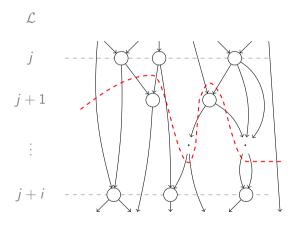




i-level cut



i-level cut

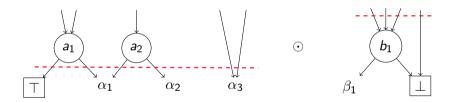


Lemma (Sølvsten, Van de Pol 2023) The maximum i-level cut problem is in P for $i \in \{1, 2\}$.

Theorem (Lampis, Kaouri, Mitsou 2011) The maximum i-level cut problem is NP-complete for $i \geq 4$.

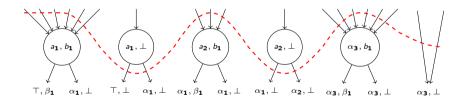
Theorem (Sølvsten, Van de Pol 2023) Given maximum 2-level cuts size C_f for f and C_g for g, the maximum 2-level cut for $f \odot g$ is less than or equal to $C_f \cdot C_g$.

Proof.



Theorem (Sølvsten, Van de Pol 2023) Given maximum 2-level cuts size C_f for f and C_g for g, the maximum 2-level cut for $f \odot g$ is less than or equal to $C_f \cdot C_g$.

Proof.

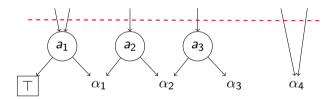


Lemma (Sølvsten, Van de Pol 2023)

The maximum 2-level cut for f is at most $\frac{3}{2}$ larger than its maximum 1-level cut.

Proof.

The maximum 1-level cut bounds the number of available in-going and out-going edges.

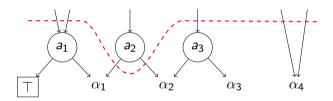


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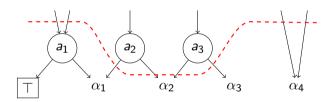


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The maximum 2-level cut for f is at most $\frac{3}{2}$ larger than its maximum 1-level cut.

Proof.

The maximum 1-level cut bounds the number of available in-going and out-going edges.



Possible to process a

1.1 GiB BDD

with only

128 MiB Memory

Adiar v1.0 : 56.5 hours

Running time to verify the 15 smallest EPFL instances.

Adiar v1.0: 56.5 hours

Adiar v1.2 : 4.0 hours $(-93\%)^1$

Running time to verify the 15 smallest EPFL instances.

¹ 52.1 of these hours were saved on just verifying the sin circuit alone.

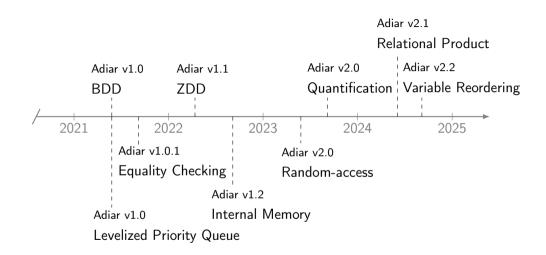
Steffan Christ Sølvsten

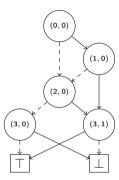
- soelvsten@cs.au.dk
- ssoelvsten.github.io

Adiar

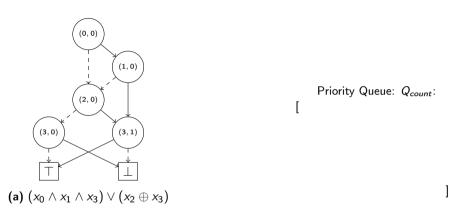
- github.com/ssoelvsten/adiar
- ssoelvsten.github.io/adiar

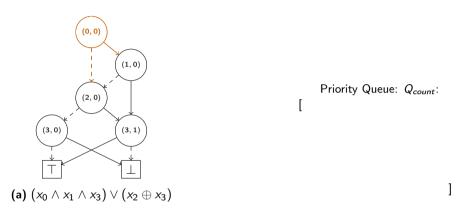


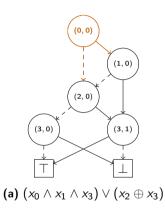




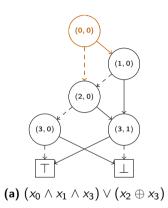
(a) $(x_0 \land x_1 \land x_3) \lor (x_2 \oplus x_3)$



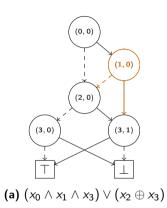




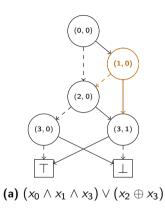
Priority Queue:
$$Q_{count}$$
:
$$[((0,0) \xrightarrow{\top} (1,0), 1), ((0,0) \xrightarrow{\bot} (2,0), 1),$$

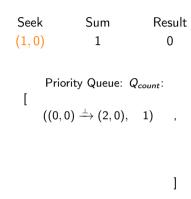


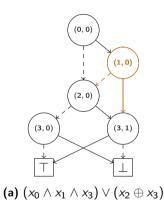
See (1, 0	•	Sum 0	Re	esul 0
]	((0,0)	Queue: $\xrightarrow{\top}$ $(1,0)$, $\xrightarrow{\bot}$ $(2,0)$,	1)	,
				1



Seek	Sum	Result
(1,0)	0	0
	prity Queue: $(0) \stackrel{ op}{\longrightarrow} (1,0),$	





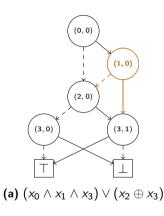


Seek Sum Result
$$(1,0)$$
 1 0

Priority Queue:
$$Q_{count}$$
:
$$((0,0) \xrightarrow{\perp} (2,0), \quad 1) \quad ,$$

$$((1,0) \xrightarrow{\top} (2,0), \quad 1) \quad ,$$

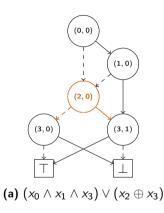
$$((1,0) \xrightarrow{\top} (3,1), \quad 1) \quad ,$$



Priority Queue:
$$Q_{count}$$
:
$$((0,0) \xrightarrow{\perp} (2,0), \quad 1) \quad ,$$

$$((1,0) \xrightarrow{\top} (2,0), \quad 1) \quad ,$$

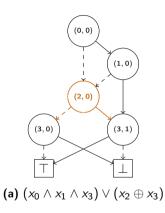
$$((1,0) \xrightarrow{\top} (3,1), \quad 1) \quad ,$$



Priority Queue:
$$Q_{count}$$
:
$$((0,0) \xrightarrow{\perp} (2,0), \quad 1) \quad ,$$

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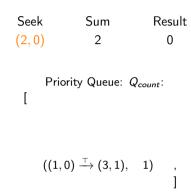
$$((1,0) \xrightarrow{\top} (3,1), \quad 1) \quad ,$$

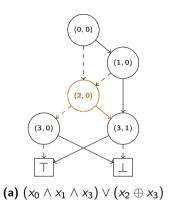


Priority Queue:
$$Q_{count}$$
:
$$((1,0) \xrightarrow{\perp} (2,0), \quad 1) \quad ,$$

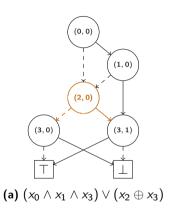
$$((1,0) \xrightarrow{\top} (3,1), \quad 1) \quad ,$$





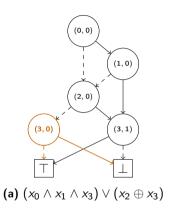


Seek		Sum	Result
(2, 0)		2	0
]	Priority	Queue:	Q_{count} :

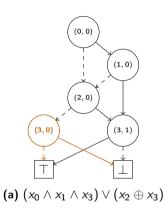


Seek		Sum	Result
(3,0)		0	0
[Priority	Queue:	Q_{count} :

$$((2,0) \xrightarrow{\perp} (3,0), 2)$$
, $((1,0) \xrightarrow{\top} (3,1), 1)$, $((2,0) \xrightarrow{\top} (3,1), 2)$



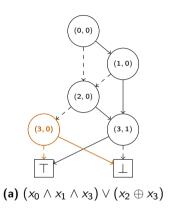
Seek		Sum	Result
(3, 0		0	0
[Priority	Queue:	Q_{count} :





Priority Queue:
$$Q_{count}$$
:

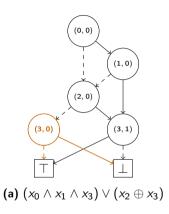
$$((1,0) \xrightarrow{\top} (3,1), 1)$$
, $((2,0) \xrightarrow{\top} (3,1), 2)$

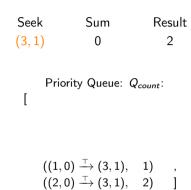


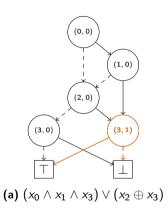


Priority Queue:
$$Q_{count}$$
:

$$((1,0) \xrightarrow{\top} (3,1), 1)$$
, $((2,0) \xrightarrow{\top} (3,1), 2)$



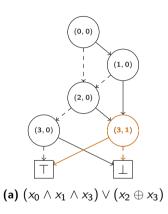




Seek Sum Result (3,1) 0 2

Priority Queue:
$$Q_{count}$$
:

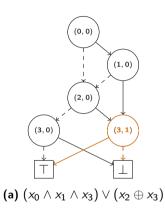
[
$$((1,0) \xrightarrow{\top} (3,1), 1), ((2,0) \xrightarrow{\top} (3,1), 2)$$

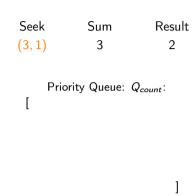


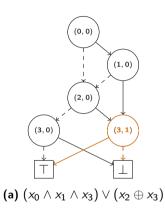


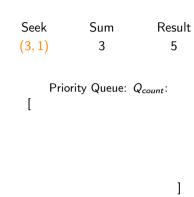
Priority Queue: Q_{count} :

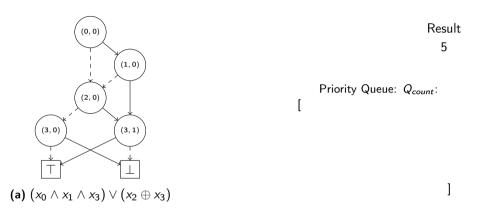
$$((2,0) \xrightarrow{\top} (3,1), \quad 2) \qquad]$$











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Adiar

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