## Random Access on Narrow Decision Diagrams in External Memory

**Steffan Christ Sølvsten**, Casper Moldrup Rysgaard, and Jaco van de Pol SPIN 2024



## Adiar

I/O-efficient Decision Diagrams

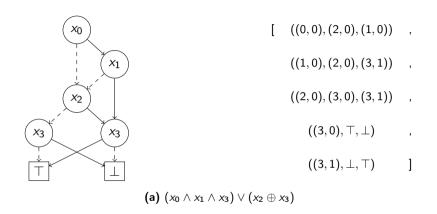
github.com/ssoelvsten/adiar

## **£** Features

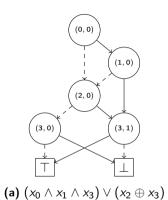


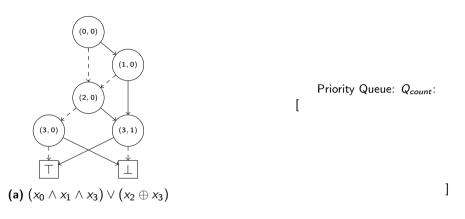


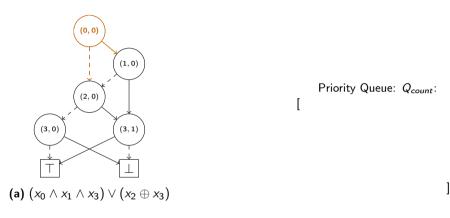


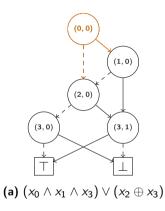


Serialized Representation of a Binary Decision Diagram.

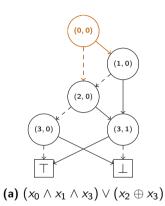








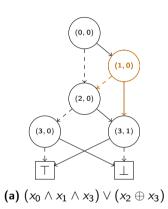
Priority Queue: 
$$Q_{count}$$
:
$$[ ((0,0) \xrightarrow{\top} (1,0), 1), ((0,0) \xrightarrow{\bot} (2,0), 1),$$



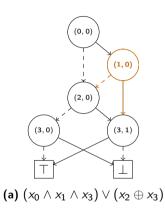
Seek	Sum	Result
(1,0)	0	0

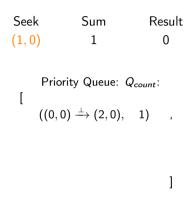
Priority Queue: 
$$Q_{count}$$
:
$$[ ((0,0) \xrightarrow{\top} (1,0), 1) , ((0,0) \xrightarrow{\bot} (2,0), 1) ,$$

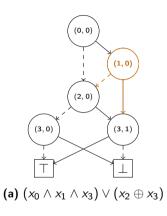
]



See (1, (		Sum 0	Re	sul 0
[	((0,0)	Queue: $(1,0)$ , $\xrightarrow{\top}$ $(2,0)$ ,	1)	,





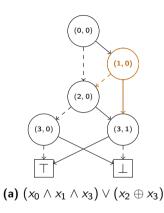


Seek	Sum	Result
(1,0)	1	0

Priority Queue: 
$$Q_{count}$$
:
$$((0,0) \xrightarrow{\perp} (2,0), \quad 1) \quad ,$$

$$((1,0) \xrightarrow{\top} (2,0), \quad 1) \quad ,$$

$$((1,0) \xrightarrow{\top} (3,1), \quad 1) \quad ,$$

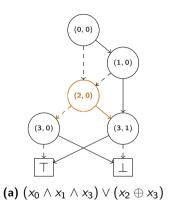


Seek	Sum	Result
(2,0)	0	0

Priority Queue: 
$$Q_{count}$$
:

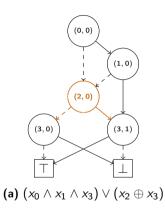
$$((0,0) \xrightarrow{\perp} (2,0), \quad 1) \quad ,$$

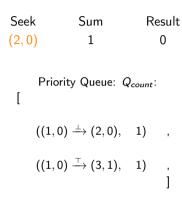
$$((1,0) \xrightarrow{\top} (3,1), \quad 1) \quad ,$$

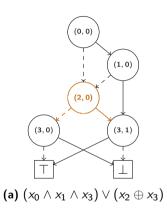


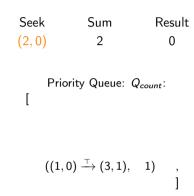
Seek	Sum	Result
(2,0)	0	0

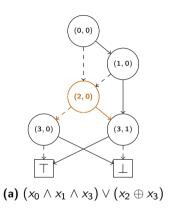
Priority Queue: 
$$Q_{count}$$
: [ 
$$((0,0) \xrightarrow{\perp} (2,0), \quad 1) \quad , \\ ((1,0) \xrightarrow{\perp} (2,0), \quad 1) \quad , \\ ((1,0) \xrightarrow{\top} (3,1), \quad 1) \quad , \\ ]$$



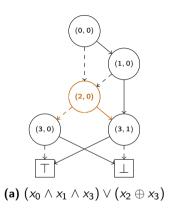




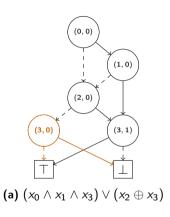




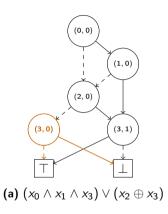
Seek	Sum	Result
(2,0)	2	0
P [	riority Queue:	$Q_{count}$ :

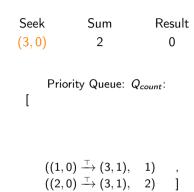


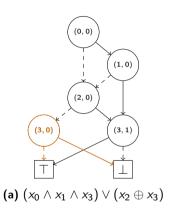
Seek (3, 0)	Sum 0	Result 0
[	Priority Queue: <i>Q</i>	count:
(	$(2,0) \xrightarrow{\perp} (3,0),$ $(1,0) \xrightarrow{\top} (3,1),$ $(2,0) \xrightarrow{\top} (3,1),$	2) , 1) , 2) ]

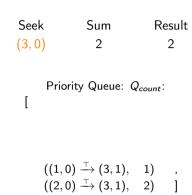


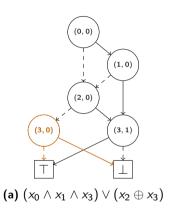
Seek	_	Sum	Result
(3, 0)		0	0
]	Priority (	Queue:	$Q_{count}$ :

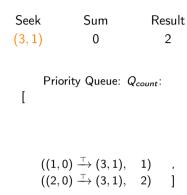


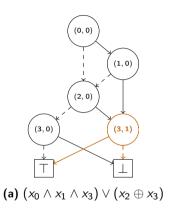


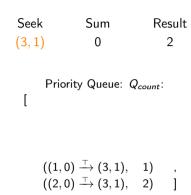


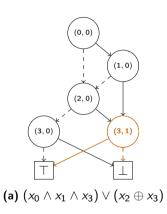








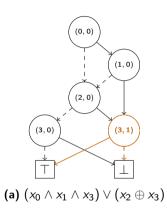




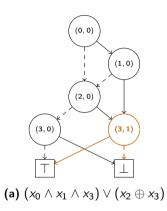


Priority Queue: Q<sub>count</sub>:

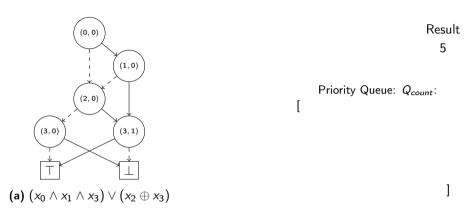
$$((2,0) \xrightarrow{\top} (3,1), \quad 2) \qquad ]$$



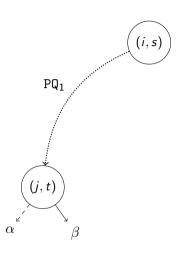
Seek (3, 1)	Sum 3	Result 2
Prio [	rity Queue: G	Q <sub>count</sub> :
		1

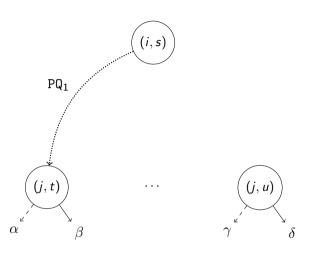


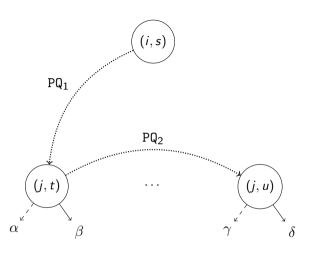
Seek (3, 1)	Sum 3	Result 5
Prio [	rity Queue: (	Q <sub>count</sub> :
		1

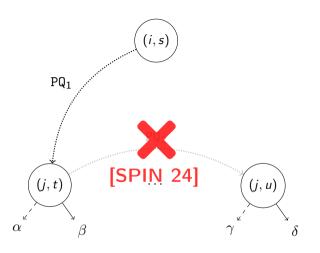


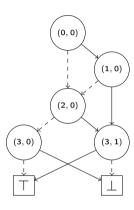


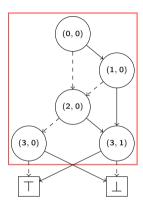


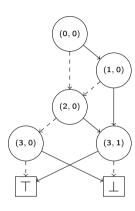


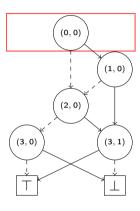


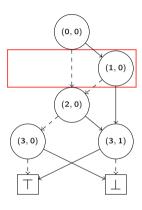


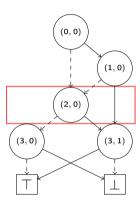


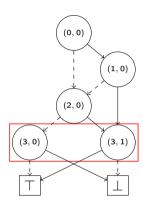


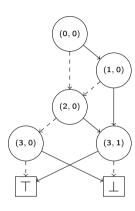


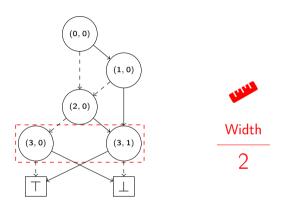


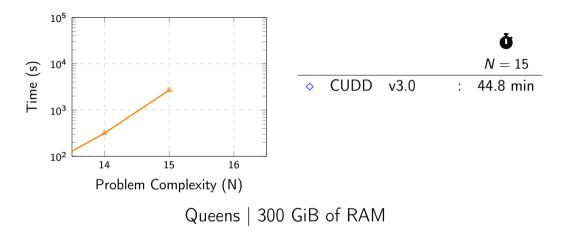


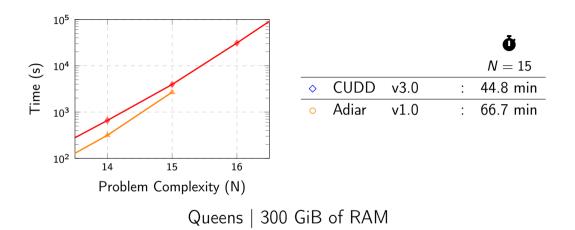


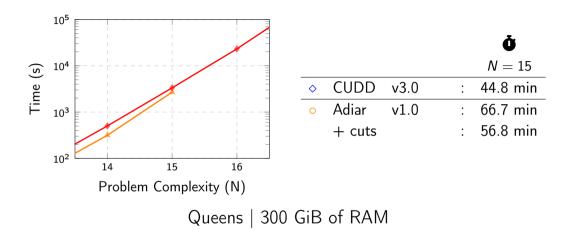


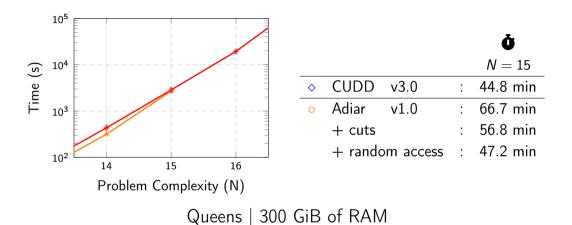


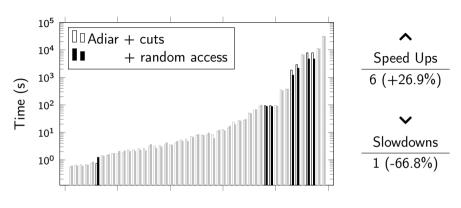












EPFL Circuit Verification | 300 GiB of RAM

## Steffan Christ Sølvsten

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## **Adiar**

- github.com/ssoelvsten/adiar
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