An External Memory Relational Product

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- 1-Var / Push: Apply π in $O(L_N)$ extra time during the final bottom-up Reduce sweep.
- Bounce:

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to be continued...