

# Specification of move data

Explain the move data implemented using Gauss code in VirtualLink class.

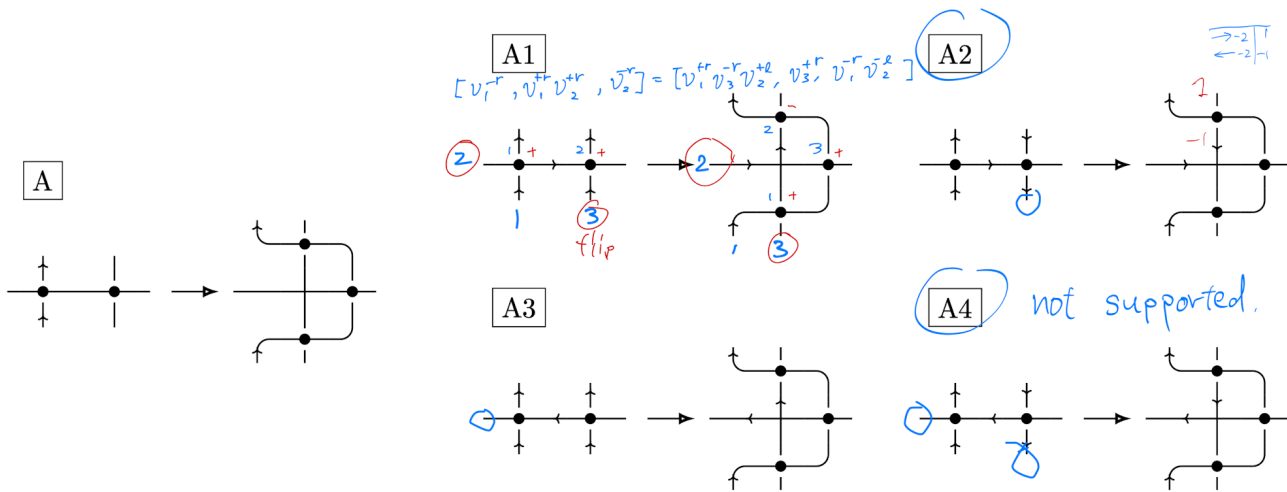
## Reference:

Muramatsu, K., Suzuki, S., & Taguchi, K. (2024). On Matveev-Piergallini moves for branched spines. *arXiv preprint arXiv:2405.18743*.

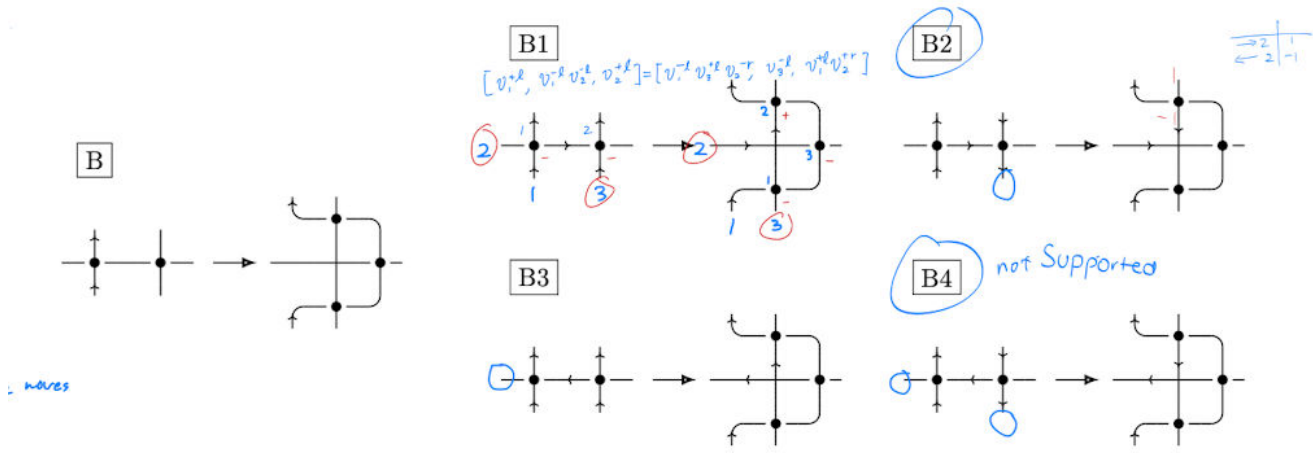
URL: <https://arxiv.org/abs/2405.18743>

## MP moves

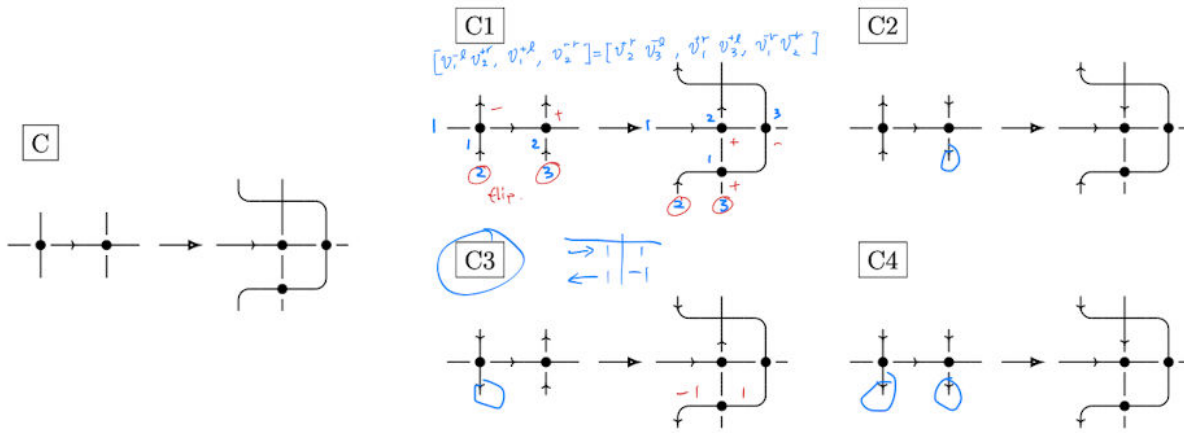
16 types of MP moves are classified into types [A,B,C,D] and [1,2,3,4].



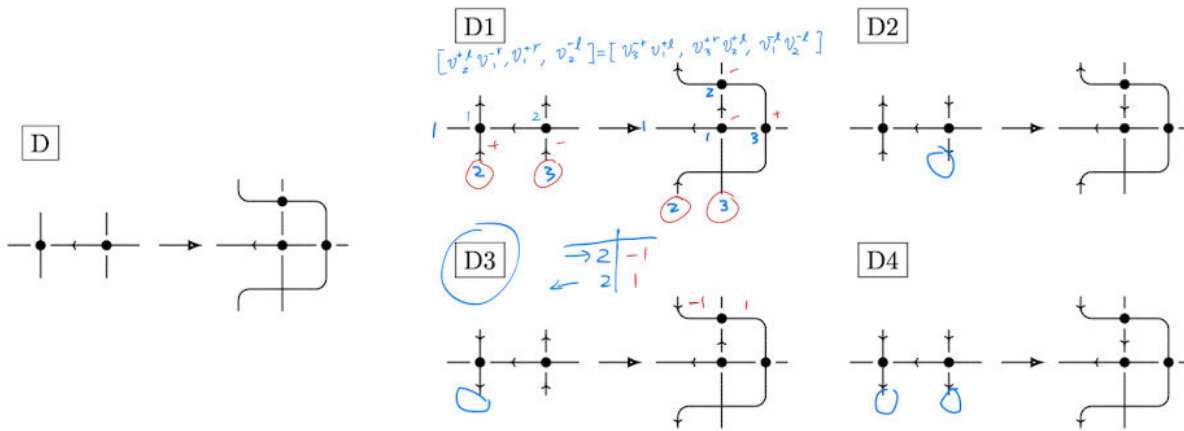
**Figure 2.18.** MP moves of type A.



**Figure 2.19.** MP moves of type B.



**Figure 2.20.** MP moves of type C.



**Figure 2.21.** MP moves of type D.

gc : Gauss Code of strand {[array of signed vertices]}, ori : orientations, signatures of crossings

T\_MP\_L : left hand side of MP move (2 vertices), T\_MP\_R : right hand side of MP move (3 vertices)

## LHS

```
load("MPmoveData.mat")
disp(T_MP_L(:,["param","gc","ori"]))
```

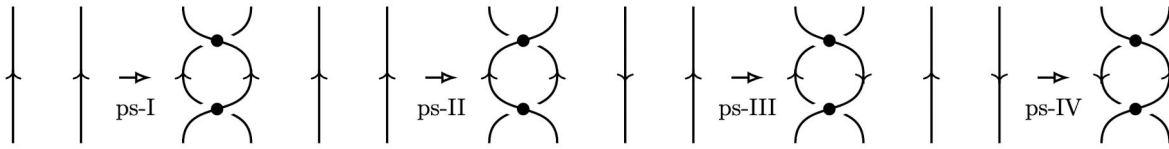
param	gc			ori	
"A1"	$\begin{bmatrix} -1 \end{bmatrix}$	$\begin{bmatrix} 1 & 2 \end{bmatrix}$	$\begin{bmatrix} -2 \end{bmatrix}$	1	1
"B1"	$\begin{bmatrix} 1 \end{bmatrix}$	$\begin{bmatrix} -1 & -2 \end{bmatrix}$	$\begin{bmatrix} 2 \end{bmatrix}$	-1	-1
"C1"	$\begin{bmatrix} -1 & 2 \end{bmatrix}$	$\begin{bmatrix} 1 \end{bmatrix}$	$\begin{bmatrix} -2 \end{bmatrix}$	-1	1
"D1"	$\begin{bmatrix} 2 & -1 \end{bmatrix}$	$\begin{bmatrix} 1 \end{bmatrix}$	$\begin{bmatrix} -2 \end{bmatrix}$	1	-1
"A2"	$\begin{bmatrix} -1 \end{bmatrix}$	$\begin{bmatrix} 1 & 2 \end{bmatrix}$	$\begin{bmatrix} -2 \end{bmatrix}$	1	-1
"B2"	$\begin{bmatrix} 1 \end{bmatrix}$	$\begin{bmatrix} -1 & -2 \end{bmatrix}$	$\begin{bmatrix} 2 \end{bmatrix}$	-1	1
"C2"	$\begin{bmatrix} -1 & 2 \end{bmatrix}$	$\begin{bmatrix} 1 \end{bmatrix}$	$\begin{bmatrix} -2 \end{bmatrix}$	-1	-1
"D2"	$\begin{bmatrix} 2 & -1 \end{bmatrix}$	$\begin{bmatrix} 1 \end{bmatrix}$	$\begin{bmatrix} -2 \end{bmatrix}$	1	1
"A3"	$\begin{bmatrix} -1 \end{bmatrix}$	$\begin{bmatrix} 2 & 1 \end{bmatrix}$	$\begin{bmatrix} -2 \end{bmatrix}$	-1	-1
"B3"	$\begin{bmatrix} 1 \end{bmatrix}$	$\begin{bmatrix} -2 & -1 \end{bmatrix}$	$\begin{bmatrix} 2 \end{bmatrix}$	1	1
"C3"	$\begin{bmatrix} -1 & 2 \end{bmatrix}$	$\begin{bmatrix} 1 \end{bmatrix}$	$\begin{bmatrix} -2 \end{bmatrix}$	1	1
"D3"	$\begin{bmatrix} 2 & -1 \end{bmatrix}$	$\begin{bmatrix} 1 \end{bmatrix}$	$\begin{bmatrix} -2 \end{bmatrix}$	-1	-1
"A4"	$\begin{bmatrix} -1 \end{bmatrix}$	$\begin{bmatrix} 2 & 1 \end{bmatrix}$	$\begin{bmatrix} -2 \end{bmatrix}$	-1	1
"B4"	$\begin{bmatrix} 1 \end{bmatrix}$	$\begin{bmatrix} -2 & -1 \end{bmatrix}$	$\begin{bmatrix} 2 \end{bmatrix}$	1	-1
"C4"	$\begin{bmatrix} -1 & 2 \end{bmatrix}$	$\begin{bmatrix} 1 \end{bmatrix}$	$\begin{bmatrix} -2 \end{bmatrix}$	1	-1
"D4"	$\begin{bmatrix} 2 & -1 \end{bmatrix}$	$\begin{bmatrix} 1 \end{bmatrix}$	$\begin{bmatrix} -2 \end{bmatrix}$	-1	1

## RHS

```
disp(T_MP_R(:,["param","gc","ori"]))
```

param	gc			ori		
"A1"	$\begin{bmatrix} 1 & -3 & 2 \end{bmatrix}$	$\begin{bmatrix} 3 \end{bmatrix}$	$\begin{bmatrix} -1 & -2 \end{bmatrix}$	1	-1	1
"B1"	$\begin{bmatrix} -1 & 3 & -2 \end{bmatrix}$	$\begin{bmatrix} -3 \end{bmatrix}$	$\begin{bmatrix} 1 & 2 \end{bmatrix}$	-1	1	-1
"C1"	$\begin{bmatrix} 2 & -3 \end{bmatrix}$	$\begin{bmatrix} 1 & 3 \end{bmatrix}$	$\begin{bmatrix} -1 & -2 \end{bmatrix}$	1	1	-1
"D1"	$\begin{bmatrix} -3 & 1 \end{bmatrix}$	$\begin{bmatrix} 3 & 2 \end{bmatrix}$	$\begin{bmatrix} -1 & -2 \end{bmatrix}$	-1	-1	1
"A2"	$\begin{bmatrix} 1 & -3 & 2 \end{bmatrix}$	$\begin{bmatrix} 3 \end{bmatrix}$	$\begin{bmatrix} -2 & -1 \end{bmatrix}$	-1	1	1
"B2"	$\begin{bmatrix} -1 & 3 & -2 \end{bmatrix}$	$\begin{bmatrix} -3 \end{bmatrix}$	$\begin{bmatrix} 2 & 1 \end{bmatrix}$	1	-1	-1
"C2"	$\begin{bmatrix} 2 & -3 \end{bmatrix}$	$\begin{bmatrix} 1 & 3 \end{bmatrix}$	$\begin{bmatrix} -2 & -1 \end{bmatrix}$	-1	-1	-1
"D2"	$\begin{bmatrix} -3 & 1 \end{bmatrix}$	$\begin{bmatrix} 3 & 2 \end{bmatrix}$	$\begin{bmatrix} -2 & -1 \end{bmatrix}$	1	1	1
"A3"	$\begin{bmatrix} 1 & -3 & 2 \end{bmatrix}$	$\begin{bmatrix} 3 \end{bmatrix}$	$\begin{bmatrix} -1 & -2 \end{bmatrix}$	1	-1	-1
"B3"	$\begin{bmatrix} -1 & 3 & -2 \end{bmatrix}$	$\begin{bmatrix} -3 \end{bmatrix}$	$\begin{bmatrix} 1 & 2 \end{bmatrix}$	-1	1	1
"C3"	$\begin{bmatrix} 2 & -3 \end{bmatrix}$	$\begin{bmatrix} 3 & 1 \end{bmatrix}$	$\begin{bmatrix} -1 & -2 \end{bmatrix}$	-1	1	1
"D3"	$\begin{bmatrix} -3 & 1 \end{bmatrix}$	$\begin{bmatrix} 2 & 3 \end{bmatrix}$	$\begin{bmatrix} -1 & -2 \end{bmatrix}$	-1	1	-1
"A4"	$\begin{bmatrix} 1 & -3 & 2 \end{bmatrix}$	$\begin{bmatrix} 3 \end{bmatrix}$	$\begin{bmatrix} -2 & -1 \end{bmatrix}$	-1	1	-1
"B4"	$\begin{bmatrix} -1 & 3 & -2 \end{bmatrix}$	$\begin{bmatrix} -3 \end{bmatrix}$	$\begin{bmatrix} 2 & 1 \end{bmatrix}$	1	-1	1
"C4"	$\begin{bmatrix} 2 & -3 \end{bmatrix}$	$\begin{bmatrix} 3 & 1 \end{bmatrix}$	$\begin{bmatrix} -2 & -1 \end{bmatrix}$	1	-1	1
"D4"	$\begin{bmatrix} -3 & 1 \end{bmatrix}$	$\begin{bmatrix} 2 & 3 \end{bmatrix}$	$\begin{bmatrix} -2 & -1 \end{bmatrix}$	1	-1	-1

## PS move



**Figure 2.15.** Pure sliding move ps-I – ps-IV.

```
load("PSmoveData.mat")
disp(T_PS_R(:,["param","gc","ori"]))
```

param	gc		ori	
"1"	{[1 2]}	{[-1 -2]}	1	-1
"2"	{[1 2]}	{[-1 -2]}	-1	1
"3"	{[1 2]}	{[-2 -1]}	1	-1
"4"	{[1 2]}	{[-2 -1]}	-1	1

```
disp(T_PS_L(:,["gc","ori"]))
```

gc		ori
{0×0 double}	{0×0 double}	1×0 double