Assessing Effects of Exposures to DDE and PCBs on Premature Delivery via Ordinal Logistic Regression

Raphael Morsomme Rihui Ou Alessandro Zito

Case Study 1 - Stat 723

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Overview

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Introduction

• Framework:

Dichlorodiphenyldichloroethylene (DDE) and Polychlorinated Biphenyls (PCBs) are chemicals that persist in the environment and get stored in fatty depositis in the human tissues.

⇒ Potential adverse effect on health

Question:

Is exposure to DDE and PBCs associated with a higher chance of premature delivery in pregnant women?

Pregnancy timeline

- **Dangerous preterm**: delivery at 34 weeks or before (when main organs are underdeveloped)
- Preterm: delivery beween 35 and 37 week
- At term: delivery after 37 weeks



Data

Data collected by 12 centers contained gestational age (in weeks) of the mother, the DDE and PCBs concentration, socio-economic info and scores (race, occupation, education, income), amount of triglycerides and cholesterol in blood and smoking status.

Preprocessing:

- Drop obs. with gestational age > 45 (the world record)
- Standardize and average levels of PCBs¹

$$PCB_i = rac{1}{11} \sum_{j=1}^{11} rac{PCB_{ij} - mean_i(PCB_{ij})}{sd_i(PCB_{ij})}$$

- Mean impute of occupation, education and income scores
- Aggregate race into race = 1 if white and race = 0 if non-white



¹This avoids the correlation between the PCBs. See the appendix ≥ → ⋅ ≥ → ≥ | ≥ ∞ < ∞

Data

Our dependent varible is:

$$\textit{gestgroup}_i = \begin{cases} 0 & \textit{if } \mathrm{Dangerous \; preterm} \\ 1 & \textit{if } \mathrm{Preterm} \\ 2 & \textit{if } \mathrm{At \; term} \end{cases}$$

- To account for triglyceredes and cholesterol, we introduce an adjusted measure for PCB and DDE by:
 - Computing total lipids using Phillips et al.(1989) and Bernert et al.(2007) forumula

$$lipid_i = 2.27 * cholesterol_i + triglycerides_i + 0.623$$

Setting²

$$adjDDE_i = \frac{DDE_i}{log(lipid_i)}$$
 $adjPCB_i = \frac{PCB_i}{log(lipid_i)}$

²The choice of the log comes from a Box-Cox analysis of the log-likelihood, as in Li, Longnecker and Dunson (2013)

EDA (I) - Exposures and gestational groups by race

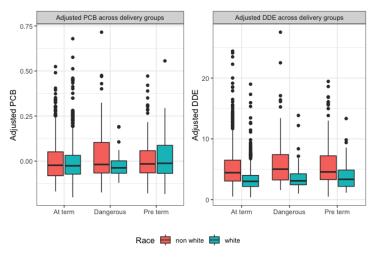


Figure: Relationship between delivery group and adjusted exposures, by race

EDA (II) - Exposure across centers

Model (I) - Ordinal Logistic Regression

After an AIC backward variable selection procedure, our final model is:

$$\begin{split} textrmlogit(P(\textit{gestgroup}_i \leq \textit{j})) &= \beta_{0j} - \eta_1 \textit{adjDDE}_i - \eta_2 \textit{adjPCB}_i \\ &- \eta_3 \textit{race}_i \\ &- \eta_4 \textit{adjDDE}_i * \textit{race}_i - \eta_4 \textit{adjDDE}_i * \textit{race}_i \\ &- \sum_{\textit{j=center}} \eta_{3,\textit{j}} \textit{center}_{\textit{j},\textit{i}} + \eta_4 \textit{smoke}_i \eta_4 \textit{adjDDE}_i \boldsymbol{\xi}^\mathsf{T} \boldsymbol{z}_i + \varepsilon \end{split}$$

where

- j = 0, 1, 2 is the outcome level
- DDE; and PCB; are the amount of DDE and PCB
- lipid_i measures the lipid deposit
- z_i is a set of covariates.

After an AIC backward , we determine that $z_i = (center_i, score_education_i)$ Model assumptions are checked in the appendix.



Model (II) - Bayesian Ordinal Logistic Regression

Results

Conclusions

Appendix (I) - More EDA

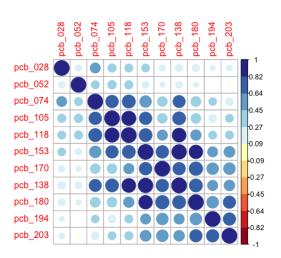


Figure: Correlation plot across PCBs

Model Checking

We can check the assumption of the (frequentist) ordinal logistic model by looking at the Surrogate residuals. If the model assumptions are correct, then the surrogate residuals R_S will have three properties:

- $E(R_S|X) = 0$
- $Var(R_S|X) = c$, the conditional variance of R_S is constant
- The emiprical distribution of R_S resembles an explicit distribution that is related to the link function $G^{-1}(\cdot)$. Specifically, $R_S \sim G(c + \int u dG(u))$.