#### Package demo

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Here is an example of how our package functions run. For our data set, we are using a "SGEMM GPU kernel performance Data Set," which measures the running times of a matrix-matrix product, given different parameter combinations.

Below, all 4 functions (calculating linear regression bootstrap, calculating coefficient confidence intervals, prediction intervals, and confidence intervals for sigma^2) are much faster with C++ than R. Overhead with functions such as map, apply, and reduce take much longer than when compared to C++ version that only uses RcppArmadillo and functions from std namespace. Use of syntactic sugar from Rcpp is minimized in the C++ functions.

```
library(devtools)
library(statatcfinal)
library(statatcfinal)
library(furrr)

set.seed(141)
dat = read_csv("sgemm_product.csv")
dat = dat[sample(241000, 1000),]
dat2 = dat[1:100,]

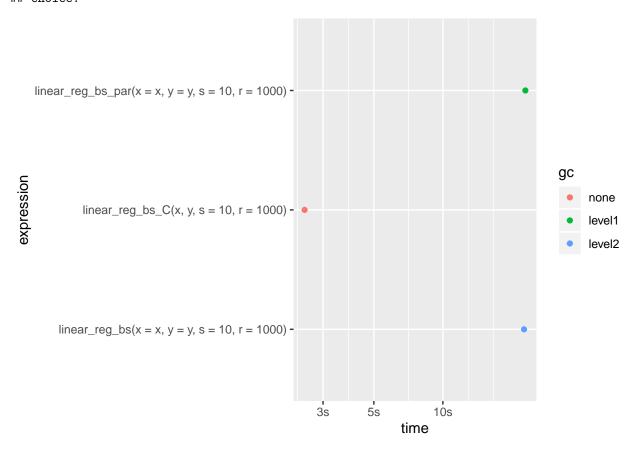
#We specifiy a specific column set
y = dat$Run1 (ms)
x = dat[,1:(ncol(dat)-4)]

#linear model objects
fit = linear_reg_bs_C(x, y, s = 10, r = 1000)
```

### Linear Regression with blb (n = 1000, p = 15, subsets = 10, and replications = 1000)

```
## Warning: Some expressions had a GC in every iteration; so filtering is disabled.
## # A tibble: 3 x 6
##
     expression
                                                           min median `itr/sec`
##
                                                        <bch:> <bch:>
     <bch:expr>
                                                                          <dbl>
## 1 linear_reg_bs(x = x, y = y, s = 10, r = 1000)
                                                        22.61s 22.61s
                                                                         0.0442
## 2 linear_reg_bs_par(x = x, y = y, s = 10, r = 1000) 22.92s 22.92s
                                                                         0.0436
## 3 linear_reg_bs_C(x, y, s = 10, r = 1000)
                                                         2.49s 2.49s
                                                                         0.401
## # ... with 2 more variables: mem_alloc <bch:byt>, `gc/sec` <dbl>
## Warning in f(...): The default behavior of beeswarm has changed in version
## 0.6.0. In versions <0.6.0, this plot would have been dodged on the y-axis. In
## versions >=0.6.0, grouponX=FALSE must be explicitly set to group on y-axis.
```

## Please set grouponX=TRUE/FALSE to avoid this warning and ensure proper axis
## choice.



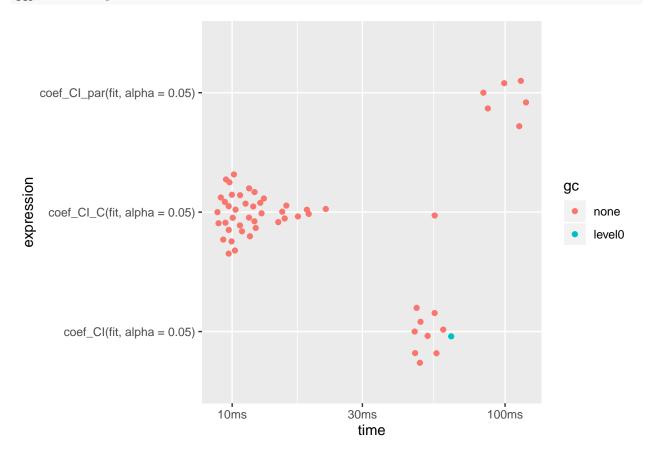
The C++ version is about 10 times faster than either of the R versions. The C++ version uses RcppArmadillo to multiply matrices as that was found to be the fastest version available. RcppArmadillo was generally faster than using multiplying matrices using std::inner\_product. The R parallel version took just as long as the R non-parallel version.

# 95~% Confidence Interval for Variable Coefficients (original dataset has 1000 replications and $10~{\rm subsets})$

```
coef_CI(fit, alpha = 0.05)
##
             Lower_Bounds
                             Estimates Upper_Bounds
## Intercept -250.9593638 -161.822787
                                          -77.756876
## MWG
                2.4803281
                              2.909166
                                            3.349526
## NWG
                2.3378785
                              2.785394
                                            3.245074
## KWG
                4.6214054
                              6.870881
                                            9.220991
## MDIMC
              -18.6137757
                            -15.942214
                                          -13.365062
## NDIMC
              -18.0645940
                            -15.529066
                                          -13.084430
## MDIMA
                0.8616486
                              2.773963
                                            4.808043
## NDIMB
               -0.1020447
                              1.983522
                                            4.069686
## KWI
                              5.744059
                                           10.709685
                0.8409772
## VWM
               -1.5499689
                              9.779875
                                           20.961781
                                           14.276281
## VWN
               -4.8347615
                              4.594360
```

```
## STRM
              -11.0345567
                             19.774674
                                          51.951853
## STRN
              -57.5970022 -24.403050
                                           9.056510
## SA
                0.2486218
                             28.977774
                                          58.002116
## SB
               24.4859861
                             57.913604
                                          92.355236
coef_CI_par(fit,alpha = 0.05)
##
             Lower Bounds
                             Estimates Upper_Bounds
## Intercept -250.9593638 -161.822787
                                         -77.756876
## MWG
                              2.909166
                                           3.349526
                2.4803281
## NWG
                2.3378785
                              2.785394
                                            3.245074
## KWG
                4.6214054
                              6.870881
                                            9.220991
## MDIMC
              -18.6137757
                           -15.942214
                                          -13.365062
## NDIMC
                                          -13.084430
              -18.0645940
                           -15.529066
## MDIMA
                0.8616486
                              2.773963
                                            4.808043
## NDIMB
               -0.1020447
                              1.983522
                                           4.069686
## KWI
                0.8409772
                              5.744059
                                          10.709685
## VWM
               -1.5499689
                              9.779875
                                          20.961781
## VWN
               -4.8347615
                              4.594360
                                          14.276281
## STRM
              -11.0345567
                             19.774674
                                          51.951853
## STRN
              -57.5970022
                            -24.403050
                                           9.056510
## SA
                0.2486218
                             28.977774
                                          58.002116
## SB
               24.4859861
                             57.913604
                                          92.355236
coef_CI_C(fit,alpha = 0.05)
             Lower_Bounds
                             Estimates Upper_Bounds
## Intercept -250.9291528 -161.822787
                                          -76.566608
## MWG
                2.4804299
                                            3.353727
                              2.909166
## NWG
                2.3379711
                              2.785394
                                            3.249154
## KWG
                4.6219064
                              6.870881
                                            9.246523
## MDIMC
              -18.6132246
                           -15.942214
                                          -13.333145
## NDIMC
              -18.0640532
                           -15.529066
                                         -13.067617
## MDIMA
                0.8620391
                              2.773963
                                           4.834013
## NDIMB
               -0.1017314
                              1.983522
                                           4.088236
## KWI
                0.8419045
                              5.744059
                                          10.754005
## VWM
               -1.5468762
                              9.779875
                                          21.047596
## VWN
               -4.8335146
                              4.594360
                                          14.337845
                             19.774674
## STRM
              -11.0248991
                                          52.324871
## STRN
              -57.5908069
                            -24.403050
                                           9.346352
## SA
                0.2563944
                             28.977774
                                          58.204637
## SB
               24.4928834
                             57.913604
                                          92.451715
(b1 = bench::mark(
  coef_CI(fit, alpha = 0.05),
  coef_CI_par(fit,alpha = 0.05),
  coef_CI_C(fit, alpha = 0.05),
  check = FALSE)
)
## # A tibble: 3 x 6
##
     expression
                                                 median `itr/sec` mem_alloc `gc/sec`
                                          min
     <bch:expr>
                                     <bch:tm> <bch:tm>
                                                            <dbl> <bch:byt>
                                                                                <dbl>
## 1 coef_CI(fit, alpha = 0.05)
                                                            19.5
                                                                      7.49MB
                                                                                 2.17
                                      46.65ms
                                                   49ms
## 2 coef_CI_par(fit, alpha = 0.05) 83.27ms
                                                  106ms
                                                             9.75
                                                                       7.8MB
                                                                                 0
## 3 coef_CI_C(fit, alpha = 0.05)
                                       8.83ms
                                                   11ms
                                                            76.5
                                                                      1.15MB
                                                                                 0
```



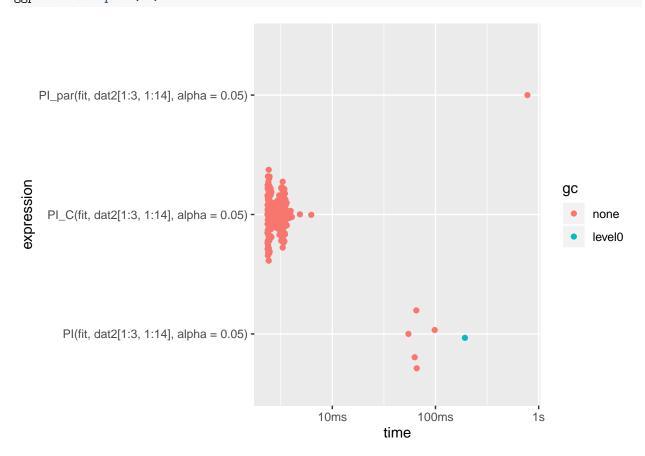


The C++ version was only about 5 times faster than the R version. The C++ uses 1/7 as much memory as the R version. Also note that the C++ version calculates the quantiles differently from the R version. Therefore, the lower and upper bounds are slightly different in the C++ and R versions.

# 95% Prediction Interval (with n=100 and p=14 (original dataset has 1000 replications and 10 subsets))

```
plan(multiprocess, workers = 4)
PI(fit, dat2[1:3, 1:14], alpha = 0.05)
##
        Lower_Bounds Estimates Upper_Bounds
## [1,]
           -119.5224 -64.28095
                                   -12.19813
## [2,]
            303.9097 373.82120
                                   446.12019
           -105.6873 -45.87250
## [3,]
                                    11.50187
PI_par(fit, dat2[1:3, 1:14], alpha = 0.05)
##
        Lower_Bounds Estimates Upper_Bounds
## [1,]
           -119.5224 -64.28095
                                   -12.19813
## [2,]
            303.9097 373.82120
                                   446.12019
## [3,]
           -105.6873 -45.87250
                                    11.50187
```

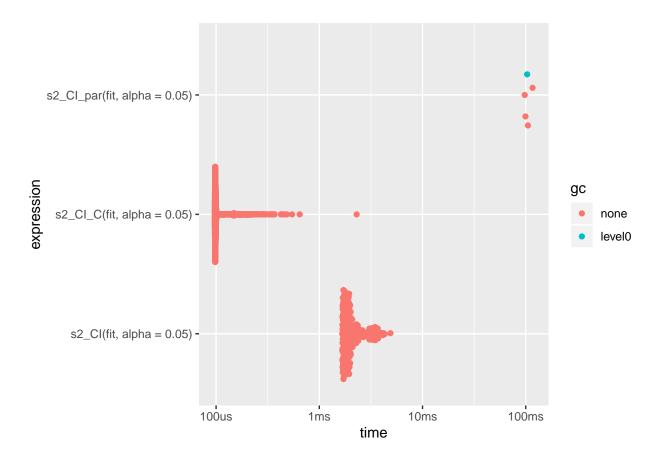
```
PI_C(fit, dat2[1:3, 1:14], alpha = 0.05)
        Lower_Bounds Estimates Upper_Bounds
           -119.5031 -64.28095
                                  -11.66223
## [1,]
## [2,]
            303.9193 373.82120
                                  446.62104
## [3,]
           -105.6698 -45.87250
                                   12.00876
(b2 = bench::mark(
 PI(fit, dat2[1:3, 1:14], alpha = 0.05),
  PI_par(fit, dat2[1:3, 1:14], alpha = 0.05),
 PI_C(fit, dat2[1:3, 1:14], alpha = 0.05),
  check = FALSE)
)
## # A tibble: 3 x 6
     expression
                                                           median `itr/sec`
                                                     min
     <bch:expr>
##
                                                                       <dbl>
                                                <bch:tm> <bch:tm>
## 1 PI(fit, dat2[1:3, 1:14], alpha = 0.05)
                                                 54.68ms 65.18ms
                                                                       14.4
## 2 PI par(fit, dat2[1:3, 1:14], alpha = 0.05) 778.54ms 778.54ms
                                                                        1.28
## 3 PI_C(fit, dat2[1:3, 1:14], alpha = 0.05)
                                                  2.35ms
                                                            2.91ms
                                                                      340.
## # ... with 2 more variables: mem_alloc <bch:byt>, `gc/sec` <dbl>
ggplot2::autoplot(b2)
```



The C++ version to calculate the 100 95% confidence intervals was more than 20 times faster than the R version. Again, the C++ and R confidence intervals are slightly difference due to calculating the quantiles differently.

#### 95 % Confindence Interval for Variance (original dataset has 1000 replications and 10 subsets)

```
s2_CI(fit, alpha = 0.05)
## Lower_Bound
                  Estimate Upper_Bound
      572738.9
                  718571.7
                               858566.8
s2_CI_par(fit, alpha = 0.05)
## Lower_Bound
                  Estimate Upper_Bound
      572738.9
                               858566.8
##
                  718571.7
s2_CI_C(fit, alpha = 0.05)
## Lower_Bound
                  Estimate Upper_Bound
      572781.4
                               859655.6
##
                  718571.7
(b3 = bench::mark(
  s2_CI(fit, alpha = 0.05),
  s2_CI_par(fit, alpha = 0.05),
  s2_CI_C(fit, alpha = 0.05),
  check = FALSE)
)
## # A tibble: 3 x 6
     expression
                                              median `itr/sec` mem_alloc `gc/sec`
##
                                        min
     <bch:expr>
                                                                              <dbl>
##
                                   <bch:tm> <bch:tm>
                                                          <dbl> <bch:byt>
## 1 s2_CI(fit, alpha = 0.05)
                                                                 118.12KB
                                                                              0
                                     1.67ms
                                              1.92ms
                                                         461.
## 2 s2_CI_par(fit, alpha = 0.05) 97.81ms 102.18ms
                                                           9.56
                                                                   2.53MB
                                                                               2.39
## 3 s2_CI_C(fit, alpha = 0.05)
                                     97.4us
                                              98.6us
                                                                   2.49KB
                                                        8910.
ggplot2::autoplot(b3)
```



The C++ version is about 19 times faster than the R version. The parallel version is not optimal for this case as it takes 100 times longer than the non-parallel R version. For some reason, the parallel version is not found to be faster than the non-parallel version for any of the 4 functions. But the C++ function is much faster anyways, so that is the one to use when trying to calculate these as fast as possible.