Introduction to Modern Regression and Predictive Modeling

Merlise Clyde

8/30/2017

► Instructor: Merlise Clyde

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► TAs:

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 - ► Eric Wang

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 - Github https://github.com/STA521-F17

Grading

Component	Percentage
Participation	5%
Homework	25%
Midterm 1	20%
Midterm 2	20%
Data Analysis Part I	15%
Data Analysis Part II	15%

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 - Individual contribution evaluated by peer assessment
 - You may help each other, but submitted work must be your own

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- 2 In-Class Midterms

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- ► Git + github

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 - R

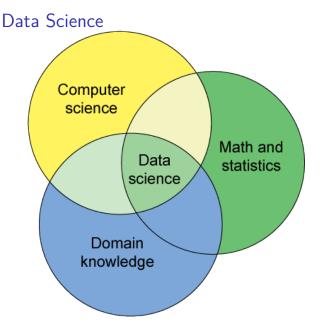
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- ► Complete the course survey (email link next week)



See (Bin Yu's IMS Presidential Address 2014)[http://bulletin.imstat.org/2014/10/ims-presidential-address-let-us-own-data-science/]

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 - Model Based Statistical Learning

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- ▶ interpretation of results for non-statisticians

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- Other Topics: Nonparametric Regression, Time Series, Neural Networks

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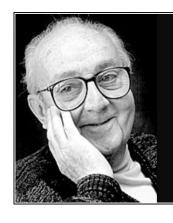
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Themes

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- understanding structure of data (relationships)
- ▶ Bayesian versus Frequentist ?

Tradeoffs...



All models are wrong, but some are useful.

— George Е.Р. Вох —

AZ QUOTES

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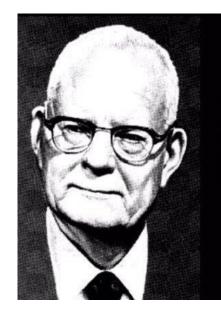
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uncertainty after seeing data

Got Data?



"Without data you're just another person with an opinion."

> W. Edwards Deming, Data Scientist

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- Bayesian methods sit on top of Frequentist Likelihood
- Important to understand advantages and problems of each perspective!

Statistical and Machine Learning?



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- ► EDA, Model Building, and Predictive Checking crucial!