



Department of Computer Science and Engineering (Data Science)

Experiment 4

(Greedy Algorithm)

Aim: Implementation of fractional Knapsack using greedy algorithm.

Theory:

Given a set of items, each with a weight and a value, determine a subset of items to include in a collection so that the total weight is less than or equal to a given limit and the total value is as large as possible.

The knapsack problem is in combinatorial optimization problem. It appears as a subproblem in many, more complex mathematical models of real-world problems. One general approach to difficult problems is to identify the most restrictive constraint, ignore the others, solve a knapsack problem, and somehow adjust the solution to satisfy the ignored constraints.

Applications:

In many cases of resource allocation along with some constraint, the problem can be derived in a similar way of Knapsack problem. Following is a set of example.

- Finding the least wasteful way to cut raw materials
- portfolio optimization
- Cutting stock problems

In this case, items can be broken into smaller pieces, hence the thief can select fractions of items.

According to the problem statement,

- There are n items in the store
- Weight of i^{th} item $w_i > 0$
- Profit for i^{th} item $p_i > 0$ and
- Capacity of the Knapsack is W
-

Pseudocode:

Greedy-Fractional-Knapsack ($w[1..n]$, $p[1..n]$, W)

for $i = 1$ to n

do $x[i] = 0$

weight = 0

for $i = 1$ to n

if weight + $w[i] \leq W$ then

$x[i] = 1$

weight = weight + $w[i]$



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else
    x[i] = (W - weight) / w[i]
    weight = W
    break
return x
  
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Complexity:

Time Complexity: $O(n \log n)$.

Example:

Problem: Consider the following instances of the fractional knapsack problem: $n = 3$, $M = 20$, $V = (24, 25, 15)$ and $W = (18, 15, 20)$ find the feasible solutions.

Solution:

Arrange items by decreasing order of profit density. Assume that items are labeled as $X = (I_1, I_2, I_3)$, have profit $V = \{24, 25, 15\}$ and weight $W = \{18, 15, 20\}$.

Item (x_i)	Value (v_i)	Weight (w_i)	$p_i = v_i / w_i$
I_2	25	15	1.67
I_1	24	18	1.33
I_3	15	20	0.75

Initialize, Weight of selected items, $SW = 0$,

Profit of selected items, $SP = 0$,

Set of selected items, $S = \{ \}$,

Here, Knapsack capacity $M = 20$.

Iteration 1 : $SW = (SW + w_2) = 0 + 15 = 15$

$SW \leq M$, so select I_2

$S = \{ I_2 \}$, $SW = 15$, $SP = 0 + 25 = 25$

Iteration 2 : $SW + w_1 > M$, so break down item I_1 .

The remaining capacity of the knapsack is 5 unit, so select only 5 units of item I_1 .

$\text{frac} = (M - SW) / W[i] = (20 - 15) / 18 = 5 / 18$



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$$S = \{ I_2, I_1 * 5/18 \}$$

$$SP = SP + v_1 * \text{frac} = 25 + (24 * (5/18)) = 25 + 6.67 = 31.67$$

$$SW = SW + w_1 * \text{frac} = 15 + (18 * (5/18)) = 15 + 5 = 20$$

The knapsack is full. Fractional Greedy algorithm selects items $\{I_2, I_1 * 5/18\}$, and it gives a profit of **31.67 units**.

Lab Assignment to Complete:

The capacity of the knapsack $W = 60$ and the list of provided items are shown in the following table –

Item	A	B	C	D
Profit	280	100	120	120
Weight	40	10	20	24

Solution:

Code:

Output: