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DWARKADAS J. SANGHVI COLLEGE OF ENGINEERING
(Autonomous College Affiliated to the University of Mumbai)
NAAC Accredited with "A" Grade (CGPA : 3.18)

Department of Computer Science and Engineering (Data Science)

Experiment 3

(Greedy Algorithm)

Aim: Implementation of Prims's & Kruskal's method.

Prim's algorithm:

Theory:

Prim's algorithm is a minimum spanning tree algorithm that takes a graph as input and finds the subset of the edges of that graph which

- form a tree that includes every vertex
- has the minimum sum of weights among all the trees that can be formed from the graph?

Algorithm:

Step 1:

- Randomly choose any vertex.
- The vertex connecting to the edge having least weight is usually selected.

Step 2:

- Find all the edges that connect the tree to new vertices.
- Find the least weight edge among those edges and include it in the existing tree.
- If including that edge creates a cycle, then reject that edge and look for the next least weight edge.

Step 3:

- Keep repeating step-02 until all the vertices are included and Minimum Spanning Tree (MST) is obtained.

Example:

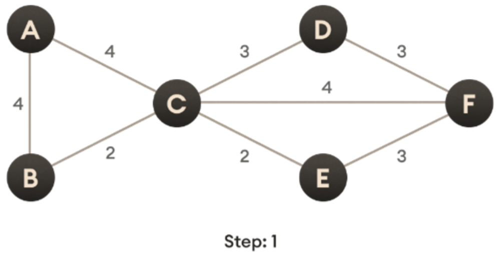

Figure 1. Start with a weighted graph

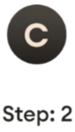

Figure 2.Choose a vertex

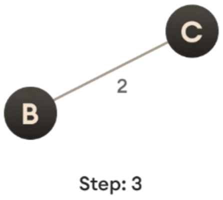

Figure 3.Choose the shortest edge from this vertex and add it

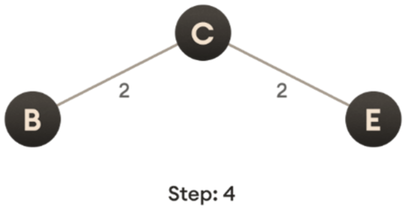

Figure 4.Choose the nearest vertex not yet in the solution

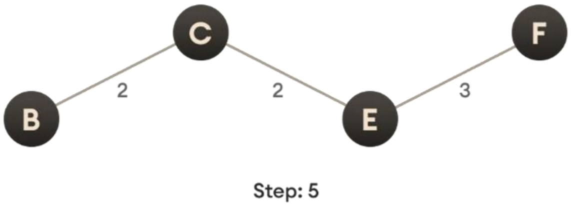

Figure 5.Choose the nearest edge not yet in the solution, if there are multiple choices, choose one at random

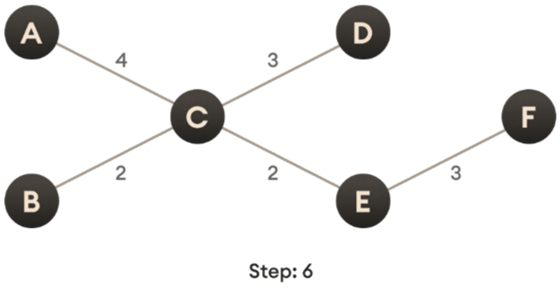

Figure 6.Repeat until you have a spanning tree

Complexity:

The time complexity of Prim's algorithm is O(E log V).

Kruskal's algorithm:

Theory:

Kruskal's algorithm is a minimum spanning tree algorithm that takes a graph as input and finds the subset of the edges of that graph which

- form a tree that includes every vertex
- has the minimum sum of weights among all the trees that can be formed from the graph?

Algorithm:

Step 1:

- Sort all the edges from low weight to high weight.

Step 2:

- Take the edge with the lowest weight and use it to connect the vertices of graph.
- If adding an edge creates a cycle, then reject that edge and go for the next least weight edge.

Step 3:

- Keep adding edges until all the vertices are connected and a Minimum Spanning Tree (MST) is obtained.

Example:

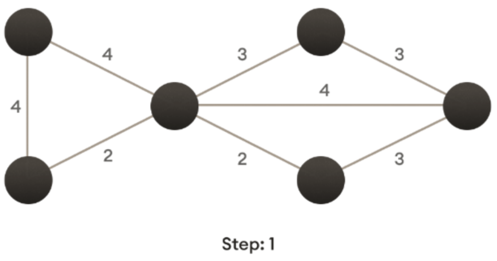

Figure 7. Start with a weighted graph

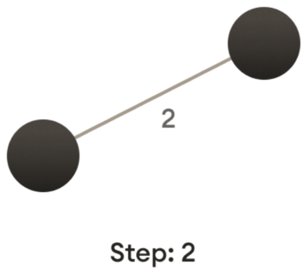

Figure 8. Choose the edge with the least weight, if there are more than 1, choose anyone

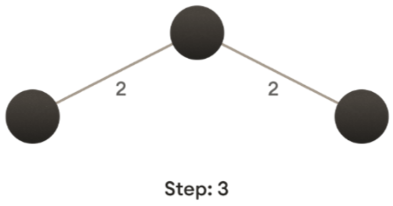

Figure 9. Choose the next shortest edge and add it

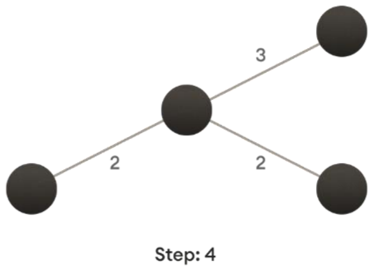

Figure 10. Choose the next shortest edge that doesn't create a cycle and add it

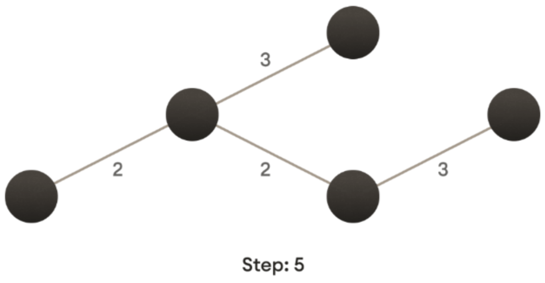

Figure 11. Choose the next shortest edge that doesn't create a cycle and add it

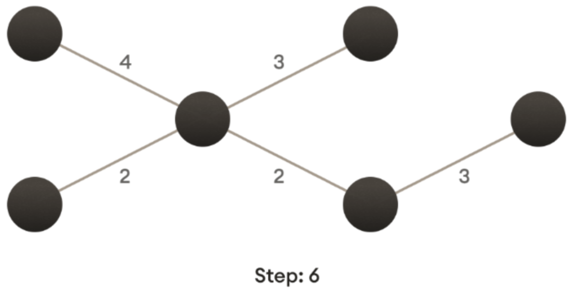

Figure 12.Repeat until you have a spanning tree

Complexity:

The time complexity Of Kruskal's Algorithm is: O(E log E).