

Regression and Other Stories: Ch 1.4 - 1.6

Building, interpreting, and checking regression models

The authors present four cycles for an iterative data analysis process:

1. Model Building:
2. Model Fitting:
3. Understanding model fits:
4. Criticism:

Classical and Bayesian Inference

Model fitting can be done in different ways... With any approach there are three considerations:

Information Information pertains to what

Assumptions The authors discuss three basic assumptions that underlay a regression model

Interpretation Classical (or frequentist) Inference: This approach summarize the data

The results and interpretation are based long-run expectations of the methods that are correct on average (unbiased) and confidence intervals that contain the true parameter the appropriate percent of the time (coverage).

Classical methods do tend to be conservative, in that strong statements are not make with *weak* data.

Bayesian Inference: This approach summarize the data

Results and interpretations are probabilistic

Bayesian inference uses additional information which can potentially give more reasonable results (using the prior to regularize the model),

Computing

Classical methods tend to use least-squares estimation (or maximum likelihood).

```
beer <- read_csv('http://math.montana.edu/ahoegh/Data/Brazil_cerveja.csv')
```

```
## Parsed with column specification:
## cols(
##   consumed = col_double(),
##   precip = col_double(),
##   max_tmp = col_double(),
##   weekend = col_double()
## )
```

```
lm_beer <- lm(consumed ~ max_tmp, data = beer)
summary(lm_beer)
```

```
##
## Call:
## lm(formula = consumed ~ max_tmp, data = beer)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -8.9116 -2.8451 -0.3342  2.3929  8.6191
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  7.97494    1.10459    7.22 3.07e-12 ***
## max_tmp      0.65485    0.04097   15.98 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.375 on 363 degrees of freedom
## Multiple R-squared:  0.413, Adjusted R-squared:  0.4114
## F-statistic: 255.4 on 1 and 363 DF, p-value: < 2.2e-16
```

The textbook authors (and your instructor), recommend using Bayesian inference for regression.

Furthermore, using Bayesian methods with *weakly informative* prior information enables stable estimates and simulation based inference, *but also can result (or approximately result) in frequentist solutions.*

```
stan_glm(consumed ~ max_tmp, data = beer, refresh = 0) %>% print()

## stan_glm
## family:      gaussian [identity]
## formula:      consumed ~ max_tmp
## observations: 365
## predictors:   2
## -----
##              Median MAD_SD
## (Intercept)  8.0      1.1
## max_tmp      0.7      0.0
##
## Auxiliary parameter(s):
##              Median MAD_SD
## sigma 3.4      0.1
##
## -----
## * For help interpreting the printed output see ?print.stanreg
## * For info on the priors used see ?prior_summary.stanreg
```