Regression and Other Stories: Regression Background

Regression methods have two purposes: prediction and comparison. Regression allows prediction of the distribution of the outcome or distributions of comparisons (sometimes called contrasts).

This section will focus on simulating fake data to understand models before fitting them to "non-fake" data.

Regression Models

As we have seen, a regression model can be written as

where y is the outcome variable, x is a predictor, β_0 and β_1 are coefficients that correspond to the linear relationship between y and x (slope and intercept, respectively), and ϵ is the error term.

Note ROS suggests interpreting β_0 and β_1 as a comparison not an **effect**. They suggest **effect** is reserved for causal inference.

- more predictors:
- non-linear model:
- non-additive models: interaction $y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_1 x_2 + \epsilon$
 - **Q** assume x_2 is binary and sketch the model fit for this interaction model
- generalized-linear models:
- non-parametric models: fit curves for the relationships between y and x.
- Multilevel (hierarchical) models: coefficients can vary by group (506)

Regression Models for Fake Data

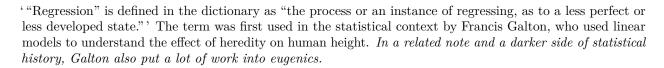
Activity:	${\bf Simulate}$	${\rm fake}$	data	and	fit	a	${\it regression}$	model	to	the dat	a.

1. Simulate Fake Data

- 2. Visualize Fake Data
- 3. Fit Model
- lm
- stan_glm()

- 4. Estimate comparison
- How to the estimates compare to the true values:
- What happens as n gets larger or smaller?

History of Regression



Predicting a child's height form parents height he noticed that tall parents tended to have children that were taller than average, but shorter than the parent. Similarly, short parents tended to have children that were shorter than average, but taller than the parent. Thus the people's heights **regressed** to the average heights.

The model from this data can be written as

$$y = 30 + .54x + error \tag{1}$$

$$y = 65.1 + .54(x - 65) + error \tag{2}$$

It might seem that the heights of the daughters would eventually collapse to 65 inches, but there is enough variability in the prediction (distribution of the predicted outcome) that the overall variation has stayed fairly constant. In other words, it is possible that a tall mother can have an even taller daughter.

This phenemenon (regression to the mean) can sometimes be confused with causality. The textbook talks about student test scores on a midterm and a final exam.