Capacitation

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Introduction

The effect of DMSO and ethanol is evaluated at concentrations from 0 up to 2% on spermatozoa capacitation (i.e., phosphotyrosines).

DMSO

Table 1: Data summary

Name	cap_dmso
Number of rows	25
Number of columns	3
Column type frequency:	
factor	1
numeric	2
Group variables	None

Variable type: factor

skim_variable	n_missing	$complete_rate$	ordered	n_unique	top_counts
donor	0	1	FALSE	5	1: 5, 2: 5, 3: 5, 4: 5

Variable type: numeric

skim_variable	n_missing comple	te_rat	emean	sd	p0	p25	p50	p75	p100	hist
conc	0	1	0.72	0.75	0.00	0.10	0.50	1.00	2.00	
capa	0	1	0.93	0.29	0.46	0.78	0.94	1.06	1.55	

There are five donors, no missing data.

```
table(cap_dmso$donor, as.factor(cap_dmso$conc))
```

```
0 0.1 0.5 1 2
1 1 1 1 1 1 1
2 1 1 1 1 1 1
3 1 1 1 1 1 1
4 1 1 1 1 1 1
```

The data are balanced with one observation for each concentration and each donor and no missing data.

```
cap_dmso_m1 <- lmer(capa ~ conc + (conc | donor), data = cap_dmso)</pre>
```

boundary (singular) fit: see help('isSingular')

```
summary(cap_dmso_m1)
```

Linear mixed model fit by REML. t-tests use Satterthwaite's method [lmerModLmerTest]

Formula: capa ~ conc + (conc | donor)

Data: cap_dmso

REML criterion at convergence: 9.7

```
Scaled residuals:
```

```
Min 1Q Median 3Q Max -1.76685 -0.49863 -0.02128 0.45054 1.77530
```

Random effects:

```
Groups Name Variance Std.Dev. Corr donor (Intercept) 0.0120077 0.10958 conc 0.0002396 0.01548 1.00 Residual 0.0604968 0.24596 Number of obs: 25, groups: donor, 5
```

boundary (singular) fit: see help('isSingular')

Fixed effects:

```
Estimate Std. Error df t value Pr(>|t|)

(Intercept) 1.04475 0.08469 5.57516 12.336 2.94e-05 ***

conc -0.15598 0.06770 17.57874 -2.304 0.0337 *

---

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Correlation of Fixed Effects:
    (Intr)

conc -0.510

optimizer (nloptwrap) convergence code: 0 (OK)
```

The fit is singular, due to a parameter evaluated at the boundary (correlation parameter between conc and donor is one in the random effect). The model is:

,

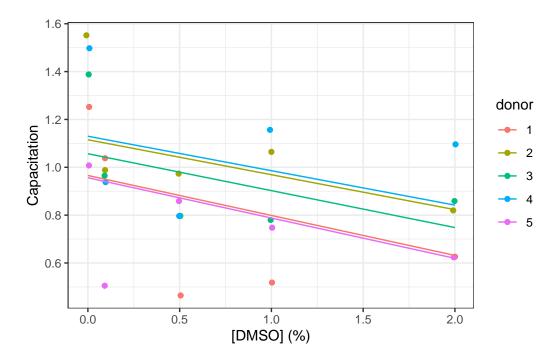
$$\operatorname{capa}_{i} \sim N\left(\alpha_{j[i]} + \beta_{1j[i]}(\operatorname{conc}), \sigma^{2}\right)$$

$$, \begin{pmatrix} \alpha_{j} \\ \beta_{1j} \end{pmatrix} \sim N\left(\begin{pmatrix} \mu_{\alpha_{j}} \\ \mu_{\beta_{1j}} \end{pmatrix}, \begin{pmatrix} \sigma_{\alpha_{j}}^{2} & \rho_{\alpha_{j}\beta_{1j}} \\ \rho_{\beta_{1j}\alpha_{j}} & \sigma_{\beta_{1j}}^{2} \end{pmatrix}\right), \text{ for donor } j = 1, \dots, J$$

$$(1)$$

Here is a plot of this model:

```
ggplot(data = cap_dmso) +
  geom_jitter(aes(x = conc, y = capa, col = donor), width = 0.01) +
  geom_line(aes(x = conc, y = fitted(cap_dmso_m1), col = donor)) +
  labs(x = "[DMSO] (%)", y = "Capacitation")
```



Slopes are all negative, suggesting a negative concentration effect. Data are rather widespread. Lines are rather parallel, and a simplification of the model should also deal with the singularity (only different intercepts for donor). Let's check it with a likelihood ratio test:

ANOVA-like table for random-effects: Single term deletions

ranova(cap_dmso_m1, reduce.terms = TRUE)

```
cap_dmso_m2 <- lmer(capa ~ conc + (1 | donor), data = cap_dmso)
anova(cap_dmso_m1, cap_dmso_m2, refit = FALSE) # Despite the name, it is indeed a LR test</pre>
```

Data: cap_dmso

Models: cap_dmso_m2: capa ~ conc + (1 | donor)

6 21.743 29.057 -4.8716

The likelihood ratio test (models *not* refitted using ML, not necessary because fixed effects are the same between the two models) does not detect significant differences between the full and simplified random effect term at $\alpha = 5\%$. We could thus use the simplest cap_dmso_m2 model with only a shift in the slope per donor. This model is:

,

cap_dmso_m1

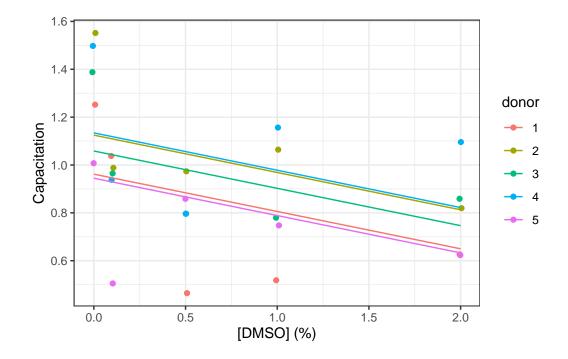
,
$$\begin{aligned} & \operatorname{capa}_i \sim N\left(\alpha_{j[i]} + \beta_1(\operatorname{conc}), \sigma^2\right) \\ & \alpha_j \sim N\left(\mu_{\alpha_j}, \sigma_{\alpha_j}^2\right), \text{ for donor } \mathbf{j} = 1, \dots, \mathbf{J} \end{aligned} \tag{2}$$

9.7433 0.035

0.9826

Here is a plot of this model:

```
ggplot(data = cap_dmso) +
  geom_jitter(aes(x = conc, y = capa, col = donor), width = 0.01) +
  geom_line(aes(x = conc, y = fitted(cap_dmso_m2), col = donor)) +
  labs(x = "[DMSO] (%)", y = "Capacitation")
```



Here is a summary of the final model:

```
summary(cap_dmso_m2)
Linear mixed model fit by REML. t-tests use Satterthwaite's method [
lmerModLmerTest]
Formula: capa ~ conc + (1 | donor)
   Data: cap_dmso
REML criterion at convergence: 9.8
Scaled residuals:
    Min
             1Q Median
                             3Q
                                    Max
-1.7214 -0.4981 -0.0374 0.4564 1.7331
Random effects:
 Groups
                      Variance Std.Dev.
 donor
          (Intercept) 0.01447 0.1203
 Residual
                      0.06070 0.2464
Number of obs: 25, groups: donor, 5
Fixed effects:
            Estimate Std. Error
                                      df t value Pr(>|t|)
                        0.08764 8.00119 11.921 2.25e-06 ***
(Intercept) 1.04475
            -0.15598
                        0.06746 19.00000 -2.312
                                                   0.0321 *
conc
                0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Signif. codes:
Correlation of Fixed Effects:
     (Intr)
conc -0.554
```

The t test indicates that conc is significantly different from zero at $\alpha = 5\%$, but not at $\alpha = 1\%$. Yet, t test is not the best one in the case of a mixed model like here. We prefer to rely on the 95% confidence interval calculated either on the profile, or via parametric bootstrap (and especially the later one):

```
confint(cap_dmso_m2, level = 0.95) # 95% CI based on profile
```

Computing profile confidence intervals ...

```
0.0000000 0.29941678
.sig01
.sigma
             0.1813240
                       0.33894333
(Intercept)
             0.8683698
                       1.22113067
conc
            -0.2912820 -0.02066896
  set.seed(52)
  # 1000x parameter bootstrap
  (cap_dmso_m2_conf <- confint(cap_dmso_m2, level = 0.95, method = "boot", nsim = 1000L))</pre>
Computing bootstrap confidence intervals ...
213 message(s): boundary (singular) fit: see help('isSingular')
                 2.5 %
                            97.5 %
.sig01
             0.0000000
                        0.25281969
```

About 1/5 of the bootstrapped models were singular. However, the 95%ICs calculated from profiles and using bootstrap do not differ much. So, we could trust these results. The slope conc significantly different to zero at $\alpha = 5\%$ because the 95% CIs do not contain zero (but it is very close to it at its minimum boundary).

Additional verifications

.sigma

conc

(Intercept)

We could double-check the significance of the slope conc by looking at a likelihood ratio test when dropping conc from the model:

```
drop.scope(terms(cap_dmso_m2))
[1] "conc"
    drop1(cap_dmso_m2, scope = "conc")
```

0.1656595

0.8774568

-0.2885403 -0.02125504

0.31286299

1.22378981

2.5 %

97.5 %

```
Single term deletions using Satterthwaite's method:
```

```
Model:
capa ~ conc + (1 | donor)
      Sum Sq Mean Sq NumDF DenDF F value Pr(>F)
conc 0.32454 0.32454
                         1
                              19 5.3465 0.03213 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
or:
  cap_dmso_m3 <- lmer(capa ~ 1 + (1 | donor), data = cap_dmso)</pre>
  anova(cap_dmso_m2, cap_dmso_m3, refit = TRUE)
refitting model(s) with ML (instead of REML)
Data: cap_dmso
Models:
cap_dmso_m3: capa ~ 1 + (1 | donor)
cap_dmso_m2: capa ~ conc + (1 | donor)
                           BIC logLik deviance Chisq Df Pr(>Chisq)
            npar
                    AIC
               3 13.643 17.300 -3.8215
                                         7.6429
cap_dmso_m3
               4 10.684 15.559 -1.3420
cap_dmso_m2
                                          2.6839 4.959 1
                                                             0.02596 *
___
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The model with a non zero slope is significantly different at α level 5% from a reference model using horizontal lines. There is thus a significant effect of DMSO concentration (confirmation of results obtained from 95% CI).

We also double-check convergence of the model by trying different optimisation engines (just to make sure). First, is there a singularity in the model?

```
isSingular(cap_dmso_m2)
```

[1] FALSE

... then, a report about the model convergence:

```
cap_dmso_m2_all <- allFit(cap_dmso_m2)</pre>
```

Loading required namespace: dfoptim

Loading required namespace: optimx

bobyqa : [OK] Nelder_Mead : [OK] nlminbwrap : [OK] nmkbw : [OK]

optimx.L-BFGS-B : [OK]

nloptwrap.NLOPT_LN_NELDERMEAD : [OK] nloptwrap.NLOPT_LN_BOBYQA : [OK]

summary(cap_dmso_m2_all)

\$which.OK

Nelder_Mead bobyqa TRUE TRUE nmkbw nlminbwrap TRUE TRUE optimx.L-BFGS-B nloptwrap.NLOPT_LN_NELDERMEAD

TRUE

nloptwrap.NLOPT_LN_BOBYQA TRUE

\$msgs

\$msgs\$bobyqa

NULL

\$msgs\$Nelder_Mead

NULL

\$msgs\$nlminbwrap

NULL

\$msgs\$nmkbw

NULL

\$msgs\$`optimx.L-BFGS-B`

NULL

 $\verb| msgs$nloptwrap.NLOPT_LN_NELDERMEAD| \\ NULL \\$

\$msgs\$nloptwrap.NLOPT_LN_BOBYQA
NULL

\$fixef

	(Intercept)	conc
bobyqa	1.04475	-0.1559755
Nelder_Mead	1.04475	-0.1559755
nlminbwrap	1.04475	-0.1559755
nmkbw	1.04475	-0.1559755
optimx.L-BFGS-B	1.04475	-0.1559755
${\tt nloptwrap.NLOPT_LN_NELDERMEAD}$	1.04475	-0.1559755
${\tt nloptwrap.NLOPT_LN_BOBYQA}$	1.04475	-0.1559755

\$11ik

bobyqa Nelder_Mead
-4.889164 -4.889164
nlminbwrap nmkbw
-4.889164 -4.889164
optimx.L-BFGS-B nloptwrap.NLOPT_LN_NELDERMEAD
-4.889164 -4.889164

nloptwrap.NLOPT_LN_BOBYQA -4.889164

\$sdcor

	donor.(Intercept)	sigma
bobyqa	0.1202798	0.2463765
Nelder_Mead	0.1202790	0.2463767
nlminbwrap	0.1202798	0.2463765
nmkbw	0.1202798	0.2463765
optimx.L-BFGS-B	0.1202798	0.2463765
${\tt nloptwrap.NLOPT_LN_NELDERMEAD}$	0.1202839	0.2463756
nloptwrap.NLOPT_LN_BOBYQA	0.1202798	0.2463765

\$theta

	donor.(Intercept)
bobyqa	0.4881950
Nelder_Mead	0.4881915
nlminbwrap	0.4881950
nmkbw	0.4881950

```
optimx.L-BFGS-B 0.4881953
nloptwrap.NLOPT_LN_NELDERMEAD 0.4882133
nloptwrap.NLOPT_LN_BOBYQA 0.4881950
```

\$times

	user.self	sys.self	elapsed	user.child	sys.child
bobyqa	0.035	0.000	0.035	0	0
Nelder_Mead	0.038	0.000	0.038	0	0
nlminbwrap	0.035	0.000	0.036	0	0
nmkbw	0.036	0.001	0.037	0	0
optimx.L-BFGS-B	0.182	0.000	0.182	0	0
nloptwrap.NLOPT_LN_NELDERMEAD	0.037	0.000	0.038	0	0
nloptwrap.NLOPT_LN_BOBYQA	0.036	0.000	0.036	0	0

\$feval

```
bobyqa Nelder_Mead

16 32

nlminbwrap nmkbw

NA NA

optimx.L-BFGS-B nloptwrap.NLOPT_LN_NELDERMEAD

14 28

nloptwrap.NLOPT_LN_BOBYQA

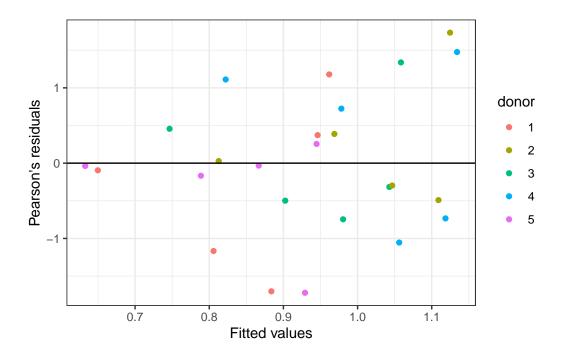
12
```

attr(,"class")
[1] "summary.allFit"

Analysis of the residuals

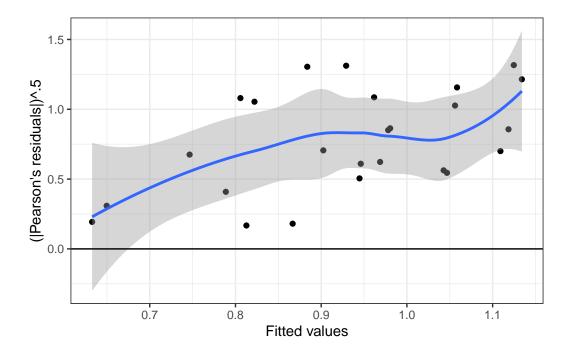
Let's check how the residuals distribute and if there is homoscedasticity.

```
cap_dmso <- fortify.merMod(cap_dmso_m2)
ggplot(data = cap_dmso, aes(x = .fitted, y = .scresid, col = donor)) +
    geom_point() +
    geom_hline(yintercept = 0) +
    labs(x = "Fitted values", y = "Pearson's residuals")</pre>
```



Residuals seem rather correctly distributed. Linearity is good here.

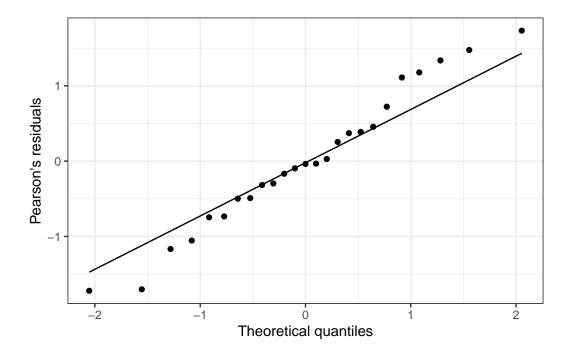
```
ggplot(data = cap_dmso, aes(x = .fitted, y = sqrt(abs(.scresid)))) +
    geom_point() +
    geom_smooth(method = "loess", formula = y ~ x) +
    geom_hline(yintercept = 0) +
    labs(x = "Fitted values", y = "(|Pearson's residuals|)^.5")
```



Homoscedasticity of the residuals does not seem to be matched here, but on a closer look, the lower variance for fitted values < 0.7 is due to having only two points in this area. So, we cannot conclude against homoscedasticity, since without these two points, the rest is OK. The amount of data is a little scarce here.

Note: according to Gauss-Markov theorem that indicates that linearity, random sample, non-collinearity between predictors, non-correlation between predictors and error term and homoscedasticity are the only requirements for our GLMM, we do not have to check it. Also the model is robust to departure of Normality, and none of the tests we made depend on a Normal distribution of the residuals (we said we don't trust z/t tests and replace them by likelihood ratio tests and parameterized bootstrapped confidence intervals). However, for completeness, here is the quantile-quantile plot of the residuals:

```
ggplot(data = cap_dmso, aes(sample = .scresid)) +
  geom_qq() +
  geom_qq_line() +
  labs(x = "Theoretical quantiles", y = "Pearson's residuals")
```



It appears not that bad. A Shapiro-Wilk test is not against Normality either:

```
shapiro.test(cap_dmso$.scresid)

Shapiro-Wilk normality test

data: cap_dmso$.scresid
W = 0.97655, p-value = 0.8094
```

Predictions

The model allows to calculate the drop in capacitation according to DMSO concentration from 0 to 2%.

```
cap_dmso_slope <- c(
  ci95_min = min(cap_dmso_m2_conf["conc", ]),
  estimate = fixef(cap_dmso_m2)[["conc"]],
  ci95_max = max(cap_dmso_m2_conf["conc", ]))
cap_dmso_slope</pre>
```

```
ci95_min estimate ci95_max
-0.28854026 -0.15597549 -0.02125504

#saveRDS(cap_dmso_slope, "../data/capacitation_DMSO_slope.rds")
```

Let's say we want to calculate the drop in total mobility for various DMSO concentrations between 0 and 2% if the total mobility of a sample without DMSO is 80%. The calculation is:

```
predict_with_ci <- function(conc, intercept = 1, slopes) {</pre>
    slopes_mat <- matrix(slopes, nrow = 1,</pre>
      dimnames = list(NULL, names(slopes)))
    data.frame(conc = conc, -intercept +
        (intercept + conc %*% slopes_mat))
  }
  dmso\_conc <- (0:20) / 10
  cap_dmso_lost <- predict_with_ci(dmso_conc, 1.1, cap_dmso_slope)</pre>
  cap_dmso_lost
  conc
           ci95_min
                       estimate
                                    ci95_max
   0.0 0.00000000 0.00000000
                                 0.00000000
1
2
   0.1 -0.02885403 -0.01559755 -0.002125504
3
   0.2 -0.05770805 -0.03119510 -0.004251007
   0.3 -0.08656208 -0.04679265 -0.006376511
5
   0.4 -0.11541610 -0.06239020 -0.008502014
6
   0.5 -0.14427013 -0.07798775 -0.010627518
7
   0.6 -0.17312416 -0.09358529 -0.012753021
8
   0.7 -0.20197818 -0.10918284 -0.014878525
   0.8 -0.23083221 -0.12478039 -0.017004028
10
  0.9 -0.25968623 -0.14037794 -0.019129532
   1.0 -0.28854026 -0.15597549 -0.021255035
   1.1 -0.31739428 -0.17157304 -0.023380539
13
   1.2 -0.34624831 -0.18717059 -0.025506042
14
   1.3 -0.37510234 -0.20276814 -0.027631546
   1.4 -0.40395636 -0.21836569 -0.029757049
15
16 1.5 -0.43281039 -0.23396324 -0.031882553
17
   1.6 -0.46166441 -0.24956079 -0.034008057
   1.7 -0.49051844 -0.26515834 -0.036133560
19
   1.8 -0.51937247 -0.28075588 -0.038259064
20
   1.9 -0.54822649 -0.29635343 -0.040384567
   2.0 -0.57708052 -0.31195098 -0.042510071
```

```
#saveRDS(cap_dmso_lost, "../data/capacitation_DMSO_lost.rds")
```

This is the lost in capacitation that the model predicts with 95%CIs.

Ethanol

Table 4: Data summary

Name	cap_etoh
Number of rows	25
Number of columns	3
Column type frequency:	
factor	1
numeric	2
Group variables	None

Variable type: factor

$skim_variable$	$n_{missing}$	$complete_rate$	ordered	n _unique	top_counts
donor	0	1	FALSE	5	1: 5, 2: 5, 3: 5, 4: 5

Variable type: numeric

skim_variable n	_missing comple	ete_rat	emean	sd	p0	p25	p50	p75	p100	hist
conc	0	1	0.72	0.75	0.00	0.10	0.50	1.00	2.00	
capa	0	1	1.04	0.29	0.24	0.88	1.02	1.24	1.57	

There are five donors, no missing data.

```
table(cap_etoh$donor, as.factor(cap_etoh$conc))
```

```
0 0.1 0.5 1 2
1 1 1 1 1 1 1
2 1 1 1 1 1 1
3 1 1 1 1 1 1
4 1 1 1 1 1 1
```

The data are balanced with one observation for each concentration and each donor and no missing data.

```
cap_etoh_m1 <- lmer(capa ~ conc + (conc | donor), data = cap_etoh)</pre>
boundary (singular) fit: see help('isSingular')
Warning: Model failed to converge with 1 negative eigenvalue: -4.6e+00
  summary(cap_etoh_m1)
Linear mixed model fit by REML. t-tests use Satterthwaite's method [
lmerModLmerTest]
Formula: capa ~ conc + (conc | donor)
   Data: cap_etoh
REML criterion at convergence: 11.2
Scaled residuals:
    Min
             1Q Median
                             3Q
                                    Max
-1.6871 -0.6063 0.0791 0.6660 1.6183
Random effects:
                      Variance Std.Dev. Corr
 Groups
          Name
 donor
          (Intercept) 0.000000 0.00000
                      0.008346 0.09136
          conc
                                         NaN
 Residual
                      0.067898 0.26057
```

```
Number of obs: 25, groups: donor, 5
Fixed effects:
            Estimate Std. Error
                                  df t value Pr(>|t|)
                                                    3e-12 ***
(Intercept) 1.14388 0.07317 18.86241 15.632
           -0.15010 0.08221 9.01039 -1.826
                                                    0.101
conc
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Correlation of Fixed Effects:
     (Intr)
conc -0.609
optimizer (nloptwrap) convergence code: 0 (OK)
boundary (singular) fit: see help('isSingular')
The fit is singular and the model failed to converge. We now try with a simplified random
term where only the intercept depends on donor, like for DMSO.
  cap_etoh_m2 <- lmer(capa ~ conc + (1 | donor), data = cap_etoh)</pre>
  summary(cap_etoh_m2)
Linear mixed model fit by REML. t-tests use Satterthwaite's method [
lmerModLmerTest]
Formula: capa ~ conc + (1 | donor)
   Data: cap_etoh
REML criterion at convergence: 11.6
Scaled residuals:
     Min
              1Q Median
                                 3Q
                                         Max
-2.07340 -0.63780 0.01602 0.73795 1.56525
Random effects:
 Groups
         Name
                     Variance Std.Dev.
 donor
          (Intercept) 0.004107 0.06409
 Residual
                      0.071961 0.26826
Number of obs: 25, groups: donor, 5
Fixed effects:
            Estimate Std. Error
                                      df t value Pr(>|t|)
```

(Intercept) 1.14388 0.08060 11.00773 14.192 2.02e-08 ***

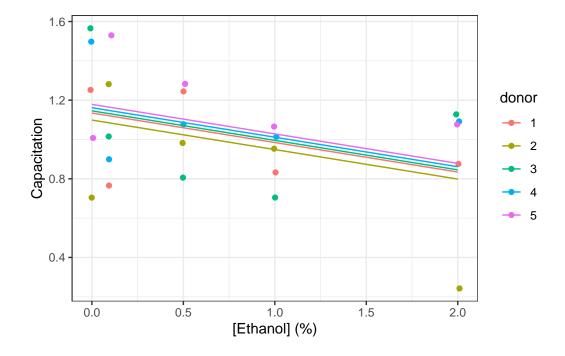
The simplified model fits well. According to t test, the slope is (just) not significantly different to zero at $\alpha = 5\%$. This model is:

,

,
$$\begin{aligned} & \operatorname{capa}_i \sim N\left(\alpha_{j[i]} + \beta_1(\operatorname{conc}), \sigma^2\right) \\ & \alpha_j \sim N\left(\mu_{\alpha_j}, \sigma_{\alpha_j}^2\right), \text{ for donor j} = 1, \dots, J \end{aligned} \tag{3}$$

Here is a plot of this model:

```
ggplot(data = cap_etoh) +
  geom_jitter(aes(x = conc, y = capa, col = donor), width = 0.01) +
  geom_line(aes(x = conc, y = fitted(cap_etoh_m2), col = donor)) +
  labs(x = "[Ethanol] (%)", y = "Capacitation")
```



Data are very widespread. Here, there seems to be less differences from one donor to the other. However, the random term **donor** in the model accounts for the repeated measures (same donor for different concentrations). Hence, this term *cannot* be dropped, even if it appears to be non significant. Otherwise, we will end up with a model that does not take correlation of observations for a the same donor into account and it would be a pseudo-replication error!

To check if the slope for conc'is different from zero, we prefer to rely on 95% confidence intervals, especially those calculated using parametric bootstrap:

```
confint(cap_etoh_m2, level = 0.95) # 95% CI based on profile
```

Computing profile confidence intervals ...

```
2.5 % 97.5 % .sig01 0.0000000 0.238410794 .sigma 0.1974261 0.357537791 (Intercept) 0.9850698 1.302680613 conc -0.2969104 -0.003292061
```

```
set.seed(874356)
# 1000x parameter bootstrap
(cap_etoh_m2_conf <- confint(cap_etoh_m2, level = 0.95,
    method = "boot", nsim = 1000L))</pre>
```

Computing bootstrap confidence intervals ...

```
429 message(s): boundary (singular) fit: see help('isSingular')
```

```
2.5 % 97.5 % .sig01 0.0000000 0.204865243 .sigma 0.1739216 0.345822810 (Intercept) 0.9945774 1.294731632 conc -0.2827724 -0.004787316
```

Here almost 1/2 of the bootstrapped samples led to singularity (probably because the slope conc'was very close to zero). However, the 95CIs are still similar to those calculated from the profile of our original model that was correctly fitted. The slope conc appears to be significantly different from zero at $\alpha = 5\%$ because the 95% CIs do not contain zero (but it is

very, very close to it at its minimum boundary). In this case, we should redo the analysis with a larger set of data to confirm or inform the slope is different from zero. Anyway, one could analyze the upper boundary of the 95%CI to determine if the effect might be problematic here or not. If not, it is not necessary to further investigate.

Additional verifications

We could double-check the significance of the slope conc by looking at a likelihood ratio test when dropping conc from the model:

```
drop.scope(terms(cap_etoh_m2))
[1] "conc"
  drop1(cap_etoh_m2, scope = "conc")
Single term deletions using Satterthwaite's method:
Model:
capa ~ conc + (1 | donor)
      Sum Sq Mean Sq NumDF DenDF F value Pr(>F)
conc 0.30056 0.30056 1
                              19 4.1766 0.0551 .
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
or:
  cap_etoh_m3 <- lmer(capa ~ 1 + (1 | donor), data = cap_etoh)</pre>
  anova(cap_etoh_m2, cap_etoh_m3, refit = TRUE)
refitting model(s) with ML (instead of REML)
Data: cap_etoh
Models:
cap_etoh_m3: capa ~ 1 + (1 | donor)
cap_etoh_m2: capa ~ conc + (1 | donor)
                           BIC logLik deviance Chisq Df Pr(>Chisq)
                    AIC
              3 14.272 17.928 -4.1359
                                         8.2718
cap_etoh_m3
```

The model with a non zero slope is just significantly different at α level 5% from a reference model using horizontal lines. There is thus a significant effect of ethanol concentration (confirmation of results obtained from 95% CI).

We also double-check convergence of the model by trying different optimisation engines (just to make sure). First, is there a singularity in the model?

```
isSingular(cap_etoh_m2)

[1] FALSE

... then, a report about the model convergence:
    cap_etoh_m2_all <- allFit(cap_etoh_m2)

bobyqa : [OK]
Nelder_Mead : [OK]
nlminbwrap :

boundary (singular) fit: see help('isSingular')

Warning: Model failed to converge with 1 negative eigenvalue: -9.0e+00

[OK]
nmkbw : [OK]
optimx.L-BFGS-B : [OK]
nloptwrap.NLOPT_LN_NELDERMEAD : [OK]
nloptwrap.NLOPT_LN_BOBYQA : [OK]

summary(cap_etoh_m2_all)</pre>
```

\$which.OK

bobyqa Nelder_Mead
TRUE TRUE

nlminbwrap nmkbw
TRUE TRUE

optimx.L-BFGS-B nloptwrap.NLOPT_LN_NELDERMEAD
TRUE TRUE

nloptwrap.NLOPT LN BOBYQA

 ${\tt nloptwrap.NLOPT_LN_BOBYQA} \\ {\tt TRUE}$

\$msgs

\$msgs\$bobyqa

NULL

\$msgs\$Nelder_Mead

NULL

\$msgs\$nlminbwrap

[1] "boundary (singular) fit: see help('isSingular')"

\$msgs\$nmkbw

NULL

\$msgs\$`optimx.L-BFGS-B`

NULL

\$msgs\$nloptwrap.NLOPT_LN_NELDERMEAD

NULL

\$msgs\$nloptwrap.NLOPT_LN_BOBYQA

NULL

\$fixef

	(Intercept)	conc
bobyqa	1.143875	-0.1501013
Nelder_Mead	1.143875	-0.1501013
nlminbwrap	1.143875	-0.1501013
nmkbw	1.143875	-0.1501013
optimx.L-BFGS-B	1.143875	-0.1501013
nloptwrap.NLOPT_LN_NELDERMEAD	1.143875	-0.1501013
nloptwrap.NLOPT_LN_BOBYQA	1.143875	-0.1501013

\$11ik

bobyqa	Nelder_Mead
-5.77876	-5.77876
nlminbwrap	nmkbw
-5.83370	-5.77876
optimx.L-BFGS-B	${\tt nloptwrap.NLOPT_LN_NELDERMEAD}$
-5.77876	-5.77876
${\tt nloptwrap.NLOPT_LN_BOBYQA}$	
-5.77876	

\$sdcor

	<pre>donor.(Intercept)</pre>	${\tt sigma}$
bobyqa	6.408808e-02	0.2682554
Nelder_Mead	6.408892e-02	0.2682553
nlminbwrap	6.052857e-07	0.2748318
nmkbw	6.408808e-02	0.2682554
optimx.L-BFGS-B	6.408784e-02	0.2682555
${\tt nloptwrap.NLOPT_LN_NELDERMEAD}$	6.409170e-02	0.2682548
nloptwrap.NLOPT_LN_BOBYQA	6.408808e-02	0.2682554

\$theta

	donor.(Intercept)
bobyqa	2.389069e-01
Nelder_Mead	2.389102e-01
nlminbwrap	2.202386e-06
nmkbw	2.389069e-01
optimx.L-BFGS-B	2.389060e-01
${\tt nloptwrap.NLOPT_LN_NELDERMEAD}$	2.389210e-01
nloptwrap.NLOPT_LN_BOBYQA	2.389069e-01

\$times

	user.self	sys.self	elapsed	user.child	sys.child
bobyqa	0.035	0.000	0.035	0	0
Nelder_Mead	0.040	0.000	0.041	0	0
nlminbwrap	0.034	0.000	0.034	0	0
nmkbw	0.035	0.000	0.036	0	0
optimx.L-BFGS-B	0.189	0.001	0.190	0	0
nloptwrap.NLOPT_LN_NELDERMEAD	0.038	0.000	0.038	0	0
${ t nloptwrap.NLOPT_LN_BOBYQA}$	0.038	0.000	0.039	0	0

\$feval

bobyqa Nelder_Mead 16 36

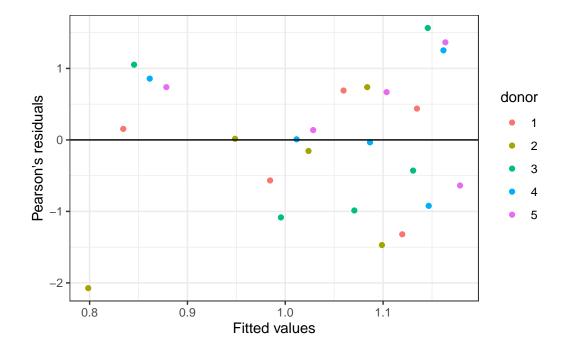
```
nlminbwrap nmkbw
NA NA
optimx.L-BFGS-B nloptwrap.NLOPT_LN_NELDERMEAD
24 31
nloptwrap.NLOPT_LN_BOBYQA
13
attr(,"class")
[1] "summary.allFit"
```

Only the nlminbwrap algorithm with default parameters was not able to fit the mode. For the other algorithms, the convergence towards the same solution suggests we got probably a global optimum.

Analysis of the residuals

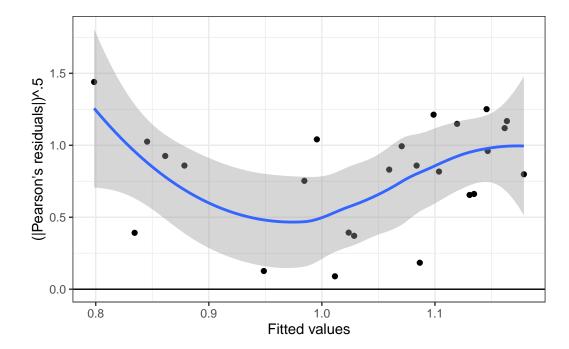
Let's check how the residuals distribute and if there is homoscedasticity.

```
cap_etoh <- fortify.merMod(cap_etoh_m2)
ggplot(data = cap_etoh, aes(x = .fitted, y = .scresid, col = donor)) +
    geom_point() +
    geom_hline(yintercept = 0) +
    labs(x = "Fitted values", y = "Pearson's residuals")</pre>
```



Residuals seem rather correctly distributed. Linearity is good here.

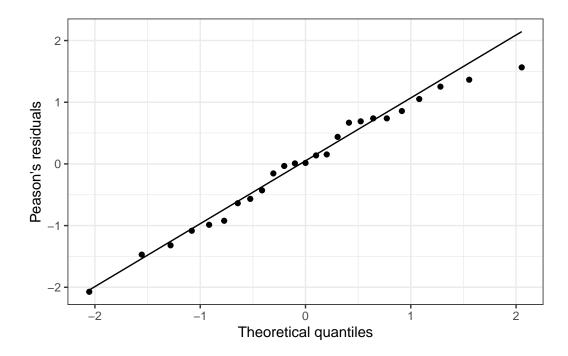
```
ggplot(data = cap_etoh, aes(x = .fitted, y = sqrt(abs(.scresid)))) +
    geom_point() +
    geom_smooth(method = "loess", formula = y ~ x) +
    geom_hline(yintercept = 0) +
    labs(x = "Fitted values", y = "(|Pearson's residuals|)^.5")
```



Homoscedasticity of the residuals does not seem too bad. The amount of data is a little scarce here for low fitted values < 0.95.

Note: according to Gauss-Markov theorem that indicates that linearity, random sample, non-collinearity between predictors, non-correlation between predictors and error term and homoscedasticity are the only requirements for our GLMM, we do not have to check it. Also the model is robust to departure of Normality, and none of the tests we made depend on a Normal distribution of the residuals (we said we don't trust z/t tests and replace them by likelihood ratio tests and parameterized bootstrapped confidence intervals). However, for completeness, here is the quantile-quantile plot of the residuals:

```
ggplot(data = cap_etoh, aes(sample = .scresid)) +
  geom_qq() +
  geom_qq_line() +
  labs(x = "Theoretical quantiles", y = "Peason's residuals")
```



It appears rather good. A Shapiro-Wilk test is not against Normality either:

```
Shapiro-Wilk normality test
data: cap_etoh$.scresid
W = 0.97416, p-value = 0.7508
```

shapiro.test(cap_etoh\$.scresid)

Predictions

The model allows to calculate the drop in capacitation according to ethanol concentration from 0 to 2%.

```
cap_etoh_slope <- c(
  ci95_min = min(cap_etoh_m2_conf["conc", ]),
  estimate = fixef(cap_etoh_m2)[["conc"]],
  ci95_max = max(cap_etoh_m2_conf["conc", ]))
cap_etoh_slope</pre>
```

```
ci95_min estimate ci95_max
-0.282772367 -0.150101260 -0.004787316

#saveRDS(cap_etoh_slope, "../data/capacitation_ETOH_slope.rds")
```

Let's say we want to calculate the drop in total mobility for various ethanol concentrations between 0 and 2% if the capacitation of a sample without ethanol is 1.1. The calculation is:

```
predict with ci <- function(conc, intercept = 1, slopes) {</pre>
    slopes_mat <- matrix(slopes, nrow = 1,</pre>
      dimnames = list(NULL, names(slopes)))
    data.frame(conc = conc, -intercept +
        (intercept + conc %*% slopes mat))
  }
  etoh_conc <- (0:20) / 10
  cap_etoh_lost <- predict_with_ci(etoh_conc, 1.1, cap_etoh_slope)</pre>
  cap_etoh_lost
  conc
           ci95_min
                       estimate
                                     ci95_max
   0.0 0.00000000 0.00000000 0.0000000000
1
2
   0.1 -0.02827724 -0.01501013 -0.0004787316
   0.2 -0.05655447 -0.03002025 -0.0009574632
3
   0.3 -0.08483171 -0.04503038 -0.0014361948
   0.4 -0.11310895 -0.06004050 -0.0019149264
   0.5 -0.14138618 -0.07505063 -0.0023936579
7
   0.6 -0.16966342 -0.09006076 -0.0028723895
   0.7 -0.19794066 -0.10507088 -0.0033511211
   0.8 -0.22621789 -0.12008101 -0.0038298527
10 0.9 -0.25449513 -0.13509113 -0.0043085843
11 1.0 -0.28277237 -0.15010126 -0.0047873159
12 1.1 -0.31104960 -0.16511139 -0.0052660475
   1.2 -0.33932684 -0.18012151 -0.0057447791
14 1.3 -0.36760408 -0.19513164 -0.0062235106
15
   1.4 -0.39588131 -0.21014176 -0.0067022422
16 1.5 -0.42415855 -0.22515189 -0.0071809738
17
  1.6 -0.45243579 -0.24016202 -0.0076597054
18 1.7 -0.48071302 -0.25517214 -0.0081384370
19 1.8 -0.50899026 -0.27018227 -0.0086171686
20 1.9 -0.53726750 -0.28519239 -0.0090959002
  2.0 -0.56554473 -0.30020252 -0.0095746318
```

```
#saveRDS(cap_etoh_lost, "../data/capacitation_ETOH_lost.rds")
```

This is the lost in capacitation that the model predicts with 95%CIs.

General informations

sessionInfo()

```
R version 4.1.3 (2022-03-10)
Platform: x86_64-apple-darwin17.0 (64-bit)
Running under: macOS Big Sur/Monterey 10.16
Matrix products: default
LAPACK: /Library/Frameworks/R.framework/Versions/4.1/Resources/lib/libRlapack.dylib
locale:
[1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8
attached base packages:
[1] stats
              graphics grDevices utils
                                             datasets methods
                                                                 base
other attached packages:
[1] ggplot2_3.3.5 lmerTest_3.1-3 lme4_1.1-29
                                                  Matrix_1.4-1
loaded via a namespace (and not attached):
 [1] tidyr_1.2.0
                          jsonlite_1.8.0
                                              splines_4.1.3
 [4] equatiomatic_0.3.1
                         shiny_1.7.1
                                              assertthat_0.2.1
 [7] highr_0.9
                         broom.mixed_0.2.9.4 cellranger_1.1.0
[10] yaml_2.3.5
                          globals_0.14.0
                                              numDeriv_2016.8-1.1
[13] pillar_1.7.0
                         backports_1.4.1
                                              lattice_0.20-45
[16] glue_1.6.2
                         digest_0.6.29
                                              promises_1.2.0.1
[19] minqa_1.2.4
                          colorspace_2.0-3
                                              dfoptim_2020.10-1
[22] htmltools_0.5.2
                         httpuv 1.6.5
                                              pkgconfig 2.0.3
[25] broom_0.8.0
                         listenv_0.8.0
                                              purrr_0.3.4
[28] xtable_1.8-4
                          scales_1.2.0
                                              later_1.3.0
[31] tibble_3.1.6
                         mgcv_1.8-40
                                              generics_0.1.2
[34] farver_2.1.0
                          ellipsis_0.3.2
                                              withr_2.5.0
[37] furrr_0.2.3
                         repr_1.1.4
                                              skimr_2.1.4
[40] cli_3.2.0
                         magrittr_2.0.3
                                              crayon_1.5.1
[43] readxl_1.4.0
                         mime_0.12
                                              evaluate_0.15
```

[46] fansi_1.0.3 [49] nlme_3.1-157 [52] tools_4.1.3 [55] munsell_0.5.0 [58] grid_4.1.3 [61] base64enc_0.1-3 [64] boot_1.3-28	future_1.24.0 MASS_7.3-56 lifecycle_1.0.1 compiler_4.1.3 nloptr_2.0.0 labeling_0.4.2 gtable_0.3.0	parallelly_1.31.0 forcats_0.5.1 stringr_1.4.0 rlang_1.0.2 rstudioapi_0.13 rmarkdown_2.13 codetools_0.2-18
[64] boot_1.3-28 [67] DBI_1.1.2	gtable_0.3.0 R6_2.5.1	knitr_1.38
[70] dplyr_1.0.8	optimx_2021-10.12	fastmap_1.1.0
[73] utf8_1.2.2 [76] Rcpp_1.0.8.3	stringi_1.7.6 vctrs_0.4.1	<pre>parallel_4.1.3 tidyselect_1.1.2</pre>
[79] xfun_0.30		