Total motility

Marie Bisconti, Philippe Grosjean & Elise Hennebert

Introduction

The effect of DMSO and ethanol is evaluated at concentrations from 0 up to 2% on spermatozoa total motility.

DMSO

Table 1: Data summary

Name Number of rows Number of columns	mt_dmso 40 5
Column type frequency: factor numeric	1 4
Group variables	None

Variable type: factor

skim_variable	n_missing	$complete_rate$	ordered	n_unique	top_counts
donor	0	1	FALSE	8	1: 5, 2: 5, 3: 5, 4: 5

Variable type: numeric

skim_variable	_missingcom	plete_ra	tmean	sd	p0	p25	p50	p75	p100	hist
conc	0	1	0.72	0.74	0.00	0.10	0.5	1.00	2.00	
motile	0	1	100.65	44.93	41.00	72.00	91.0	119.00	260.00	
total	0	1	131.20	56.45	54.00	92.00	124.5	150.50	301.00	
$motile_frac$	0	1	0.77	0.09	0.53	0.73	0.8	0.83	0.89	

There are eight donors, no missing data.

```
table(mt_dmso$donor, as.factor(mt_dmso$conc))
```

```
0 0.1 0.5 1 2
          1 1 1
1 1
      1
2 1
          1 1 1
      1
3 1
      1
          1 1 1
4 1
          1 1 1
5 1
      1
          1 1 1
6 1
          1 1 1
7 1
          1 1 1
8 1
          1 1 1
```

The data are balanced with one observation for each concentration and each donor and no missing data.

```
mt_dmso_m1 <- glmer(cbind(motile, total - motile) ~ conc + (conc | donor),
   data = mt_dmso, family = binomial(link = "logit"))
summary(mt_dmso_m1)</pre>
```

```
Generalized linear mixed model fit by maximum likelihood (Laplace
  Approximation) [glmerMod]
Family: binomial ( logit )
Formula: cbind(motile, total - motile) ~ conc + (conc | donor)
```

Data: mt_dmso

AIC BIC logLik deviance df.resid 314.1 322.6 -152.1 304.1 35

Scaled residuals:

Min 1Q Median 3Q Max -3.8305 -0.8161 0.0966 0.7369 5.0822

Random effects:

Groups Name Variance Std.Dev. Corr

donor (Intercept) 0.111404 0.3338

conc 0.007157 0.0846 0.02

Number of obs: 40, groups: donor, 8

Fixed effects:

Estimate Std. Error z value Pr(>|z|)

(Intercept) 1.39733 0.12833 10.89 < 2e-16 ***
conc -0.18586 0.05615 -3.31 0.000933 ***

Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1

Correlation of Fixed Effects:

(Intr)

conc -0.220

The model is:

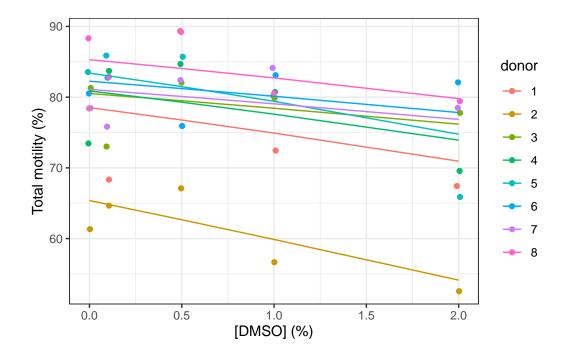
,

$$\begin{split} & \text{motile}_{i} \sim \text{Binomial}(n=1, \text{prob}_{\text{motile}=1} = \widehat{P}) \\ &, \log \left[\frac{\widehat{P}}{1 - \widehat{P}} \right] = \alpha_{j[i]} + \beta_{1j[i]}(\text{conc}) \\ & \left(\begin{array}{c} \alpha_{j} \\ \beta_{1j} \end{array} \right) \sim N \left(\left(\begin{array}{c} \mu_{\alpha_{j}} \\ \mu_{\beta_{1j}} \end{array} \right), \left(\begin{array}{cc} \sigma_{\alpha_{j}}^{2} & \rho_{\alpha_{j}\beta_{1j}} \\ \rho_{\beta_{1j}\alpha_{j}} & \sigma_{\beta_{1j}}^{2} \end{array} \right) \right), \text{ for donor j} = 1, \dots, J \end{split}$$

Here is a plot of this model:

```
ggplot(data = mt_dmso) +
  geom_jitter(aes(x = conc, y = motile_frac * 100, col = donor),
  width = 0.01) +
```

```
geom_line(aes(x = conc, y = fitted(mt_dmso_m1) * 100, col = donor)) + labs(x = "[DMSO] (%)", y = "Total motility (%)")
```



Generally, slopes are all negative, suggesting a negative concentration effect. Data are rather widespread. There are definitely shifts in the intercept per donor (different motility at [DMSO] = 0). Slopes seems not too different between donors (can the model be simplified?). Let's check it with a likelihood ratio test:

```
mt_dmso_m2 <- glmer(cbind(motile, total - motile) ~ conc + (1 | donor),
   data = mt_dmso, family = binomial(link = "logit"))
anova(mt_dmso_m1, mt_dmso_m2, refit = FALSE) # Despite the name, it is indeed a LR test</pre>
```

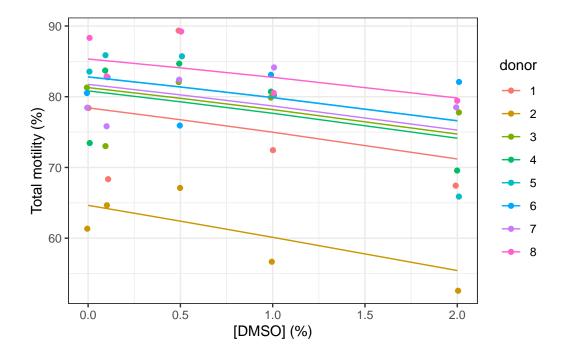
The likelihood ratio test does not detects significant differences between the full and simplified models at $\alpha = 5\%$. We could thus use the simplest mt_dmso_m2 model with only a shift in the slope per donor. This model is:

,

$$\begin{split} & \text{motile}_i \sim \text{Binomial}(n=1, \text{prob}_{\text{motile}=1} = \widehat{P}) \\ &, \log \left[\frac{\hat{P}}{1 - \hat{P}} \right] = \alpha_{j[i]} + \beta_1(\text{conc}) \\ & \qquad \qquad \alpha_j \sim N\left(\mu_{\alpha_j}, \sigma_{\alpha_j}^2\right), \, \text{for donor j} = 1, \dots, \text{J} \end{split} \tag{2}$$

Here is a plot of this model:

```
ggplot(data = mt_dmso) +
  geom_jitter(aes(x = conc, y = motile_frac * 100, col = donor),
    width = 0.01) +
  geom_line(aes(x = conc, y = fitted(mt_dmso_m2) * 100, col = donor)) +
  labs(x = "[DMSO] (%)", y = "Total motility (%)")
```



```
summary(mt_dmso_m2)
```

```
Generalized linear mixed model fit by maximum likelihood (Laplace
  Approximation) [glmerMod]
 Family: binomial (logit)
Formula: cbind(motile, total - motile) ~ conc + (1 | donor)
   Data: mt dmso
     AIC
              BIC
                    logLik deviance df.resid
   310.6
            315.7
                    -152.3
                              304.6
                                           37
Scaled residuals:
    Min
             1Q Median
                             3Q
                                    Max
-3.7957 -0.8682 0.0641 0.8505 5.0878
Random effects:
 Groups Name
                    Variance Std.Dev.
 donor (Intercept) 0.1166
                             0.3415
Number of obs: 40, groups: donor, 8
Fixed effects:
            Estimate Std. Error z value Pr(>|z|)
                        0.13047
(Intercept) 1.40292
                                 10.753
                                           <2e-16 ***
                                 -4.265
                                           2e-05 ***
conc
            -0.19271
                        0.04519
Signif. codes:
                0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Correlation of Fixed Effects:
     (Intr)
conc -0.256
```

The Z test indicates that conc is significantly different from zero at $\alpha = 5\%$. However, it is not the best test in the case of a mixed model like here. We prefer to rely on the 95% confidence interval calculated either on the profile, or via parametric bootstrap (and especially the later one):

```
confint(mt_dmso_m2, level = 0.95) # 95% CI based on profile
```

Computing profile confidence intervals ...

```
2.5 % 97.5 %
.sig01 0.2143841 0.6264441
(Intercept) 1.1208466 1.6907146
conc -0.2810892 -0.1038180
```

```
set.seed(8434)
# 1000x parameter bootstrap
(mt_dmso_m2_conf <- confint(mt_dmso_m2, level = 0.95,
    method = "boot", nsim = 1000L))</pre>
```

Computing bootstrap confidence intervals ...

2 warning(s): Model failed to converge: degenerate Hessian with 1 negative eigenvalues (and

```
2.5 % 97.5 %
.sig01 0.1220672 0.49749800
(Intercept) 1.1470026 1.66783797
conc -0.2800799 -0.09954095
```

Slope for conc is significantly different from zero at $\alpha = 5\%$ because the 95% CI does not contain zero.

Additional verifications

Check if there is not a overdispersion (in this case, a binomial generalized model would not be adequate), $Var(Y) = \varphi Np(1-p)$ with φ , the overdispersion coefficient that has to be close to zero. However, "overdispersion is not estimable (and hence practically irrelevant) for Bernoulli models (= binary data = binomial with N=1).", see glmmFAQ. Thus, it cannot be estimated here.

We could double-check the significance of the slope conc by looking at a likelihood ratio test when dropping conc from the model:

The model with conc is significantly different at α level 5% from a reference model that sets the slope conc = 0. There is thus a significant effect of DMSO concentration (confirmation of results obtained from 95% CI).

We also double-check convergence of the model by trying different optimisation engines (just to make sure). First, is there a singularity in the model?

```
isSingular(mt_dmso_m2)
```

[1] FALSE

... then, a report about the model convergence:

```
mt_dmso_m2_all <- allFit(mt_dmso_m2)</pre>
```

Loading required namespace: dfoptim

Loading required namespace: optimx

bobyqa : [OK] Nelder Mead :

Nelder_Mead : [OK]
nlminbwrap : [OK]
nmkbw : [OK]

optimx.L-BFGS-B : [OK]

nloptwrap.NLOPT_LN_NELDERMEAD : [OK]
nloptwrap.NLOPT_LN_BOBYQA : [OK]

```
summary(mt_dmso_m2_all)
```

\$which.OK

bobyqa Nelder_Mead
TRUE TRUE
nlminbwrap nmkbw
TRUE TRUE
optimx.L-BFGS-B nloptwrap.NLOPT_LN_NELDERMEAD

nloptwrap.NLOPT_LN_BOBYQA TRUE

\$msgs

\$msgs\$bobyqa

NULL

\$msgs\$Nelder_Mead

NULL

\$msgs\$nlminbwrap

NULL

\$msgs\$nmkbw

NULL

\$msgs\$`optimx.L-BFGS-B`

NULL

\$msgs\$nloptwrap.NLOPT_LN_NELDERMEAD

NULL

\$msgs\$nloptwrap.NLOPT_LN_BOBYQA

NULL

\$fixef

	(Intercept)	conc
bobyqa	1.402918	-0.1927083
Nelder_Mead	1.402924	-0.1927091
nlminbwrap	1.402918	-0.1927084
nmkbw	1.402896	-0.1927420
optimx.L-BFGS-B	1.402907	-0.1927069
nloptwrap.NLOPT_LN_NELDERMEAD	1.402879	-0.1927109
nloptwrap.NLOPT_LN_BOBYQA	1.402918	-0.1927070

\$11ik

bobyqa	Nelder_Mead
-152.2962	-152.2962
nlminbwrap	nmkbw
-152.2962	-152.2962
${\tt optimx.L-BFGS-B}$	${\tt nloptwrap.NLOPT_LN_NELDERMEAD}$
-152.2962	-152.2962
${\tt nloptwrap.NLOPT_LN_BOBYQA}$	
-152.2962	

\$sdcor

+5.4.0.1	
	<pre>donor.(Intercept)</pre>
bobyqa	0.3415152
Nelder_Mead	0.3415163
nlminbwrap	0.3415153
nmkbw	0.3415363
optimx.L-BFGS-B	0.3415439
${\tt nloptwrap.NLOPT_LN_NELDERMEAD}$	0.3415166
nloptwrap.NLOPT_LN_BOBYQA	0.3415171

\$theta

	donor.(Intercept)
bobyqa	0.3415152
Nelder_Mead	0.3415163
nlminbwrap	0.3415153
nmkbw	0.3415363
optimx.L-BFGS-B	0.3415439
nloptwrap.NLOPT_LN_NELDERMEAD	0.3415166
nloptwrap.NLOPT_LN_BOBYQA	0.3415171

\$times

	user.self	sys.self	elapsed	user.child	sys.child
bobyqa	0.049	0.001	0.050	0	0
Nelder_Mead	0.059	0.001	0.060	0	0
nlminbwrap	0.044	0.000	0.045	0	0
nmkbw	0.061	0.001	0.062	0	0
optimx.L-BFGS-B	0.346	0.001	0.346	0	0
nloptwrap.NLOPT_LN_NELDERMEAD	0.055	0.000	0.055	0	0
nloptwrap.NLOPT_LN_BOBYQA	0.040	0.000	0.040	0	0

\$feval

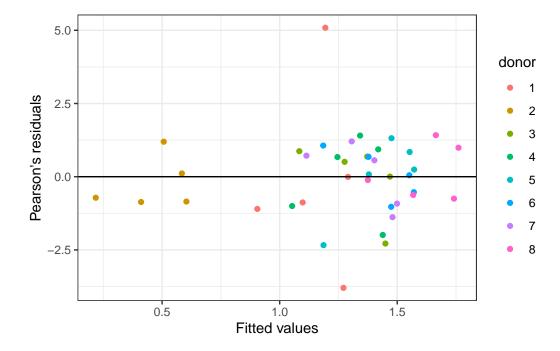
bobyqa Nelder_Mead 74 95

```
nlminbwrap nmkbw
NA 104
optimx.L-BFGS-B nloptwrap.NLOPT_LN_NELDERMEAD
14 88
nloptwrap.NLOPT_LN_BOBYQA
36
attr(,"class")
[1] "summary.allFit"
```

Analysis of the residuals

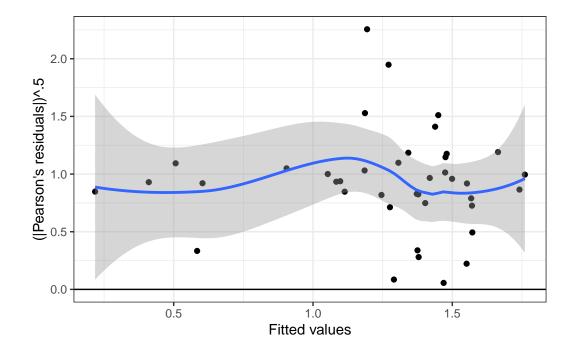
Let's check how the residuals distribute and if there is homoscedasticity.

```
mt_dmso <- fortify.merMod(mt_dmso_m2)
ggplot(data = mt_dmso, aes(x = .fitted, y = .scresid, col = donor)) +
    geom_point() +
    geom_hline(yintercept = 0) +
    labs(x = "Fitted values", y = "Pearson's residuals")</pre>
```



There is one extreme value, but otherwise, residuals seem rather correctly distributed. Linearity is good here.

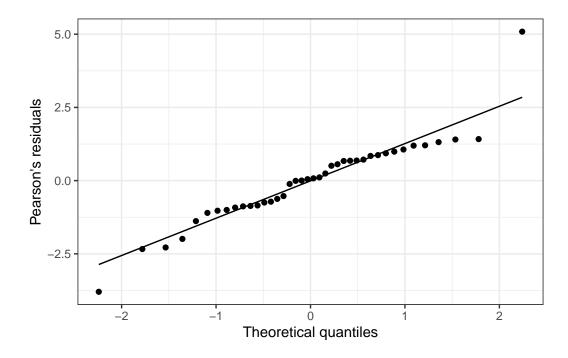
```
ggplot(data = mt_dmso, aes(x = .fitted, y = sqrt(abs(.scresid)))) +
  geom_point() +
  geom_smooth(method = "loess", formula = y ~ x) +
  geom_hline(yintercept = 0) +
  labs(x = "Fitted values", y = "(|Pearson's residuals|)^.5")
```



Homoscedasticity of the residuals seems here acceptable (the blue curve that is a loess smoothing in the data is relatively horizontal).

Note: according to Gauss-Markov theorem that indicates that linearity, random sample, non-collinearity between predictors, non-correlation between predictors and error term and homoscedasticity are the only requirements for our GLMM, we do not have to check it. Also the model is robust to departure of Normality, and none of the tests we made depend on a Normal distribution of the residuals (we said we don't trust \mathbf{z}/\mathbf{t} tests and replace them by likelihood ratio tests and parameterized bootstrapped confidence intervals). However, for completeness, here is the quantile-quantile plot of the residuals:

```
ggplot(data = mt_dmso, aes(sample = .scresid)) +
   geom_qq() +
   geom_qq_line() +
   labs(x = "Theoretical quantiles", y = "Pearson's residuals")
```



It appears not too bad, except for our extreme value that is clearly visible here at the top. A Shapiro-Wilk test does not confirm Normality, but we are pretty sure it is caused by the extreme value:

```
shapiro.test(mt_dmso$.scresid)
```

Shapiro-Wilk normality test

```
data: mt_dmso$.scresid
W = 0.91868, p-value = 0.007
```

Predictions

The model allows to calculate the drop in total mobility according to DMSO concentration from 0 to 2%. Note that an inverse logit transformation is required. Here is an example:

```
mt_dmso_slope <- c(
    ci95_min = min(mt_dmso_m2_conf["conc", ]),
    estimate = fixef(mt_dmso_m2)[["conc"]],
    ci95_max = max(mt_dmso_m2_conf["conc", ]))</pre>
```

Let's say we want to calculate the drop in total mobility for various DMSO concentrations between 0 and 2% if the total mobility of a sample without DMSO is 80%. The calculation is:

```
predict_logit <- function(conc, intercept = 1, slopes) {</pre>
    slopes_mat <- matrix(slopes, nrow = 1,</pre>
      dimnames = list(NULL, names(slopes)))
    data.frame(conc = conc, -intercept +
        boot::inv.logit(boot::logit(intercept) +
        conc %*% slopes mat))
  }
  dmso conc <- (0:20) / 10
  mt_dmso_lost <- predict_logit(dmso_conc, 0.8, mt_dmso_slope)</pre>
  mt_dmso_lost
            ci95_min
   conc
                         estimate
                                      ci95_max
   0.0 0.00000000 0.00000000 0.000000000
1
2
   0.1 -0.004518953 -0.003101179 -0.001597412
3
   0.2 -0.009113322 -0.006238047 -0.003204342
4
   0.3 -0.013783163 -0.009410633 -0.004820795
   0.4 -0.018528474 -0.012618950 -0.006446775
6
   0.5 -0.023349194 -0.015863000 -0.008082285
7
   0.6 -0.028245198 -0.019142771 -0.009727328
8
   0.7 -0.033216298 -0.022458236 -0.011381905
   0.8 -0.038262242 -0.025809357 -0.013046015
9
10 0.9 -0.043382709 -0.029196078 -0.014719660
11 1.0 -0.048577308 -0.032618332 -0.016402837
   1.1 -0.053845580 -0.036076035 -0.018095543
13 1.2 -0.059186994 -0.039569089 -0.019797777
14 1.3 -0.064600945 -0.043097380 -0.021509532
   1.4 -0.070086754 -0.046660779 -0.023230804
15
   1.5 -0.075643667 -0.050259141 -0.024961586
```

This is the lost in total mobility that the model predicts.

Ethanol

Table 4: Data summary

Name	mt_etoh
Number of rows	40
Number of columns	5
Column type frequency:	
factor	1
numeric	4
Group variables	None

Variable type: factor

$skim_variable$	$n_{missing}$	$complete_rate$	ordered	n_unique	top_counts
donor	0	1	FALSE	8	1: 5, 2: 5, 3: 5, 4: 5

Variable type: numeric

skim_variable	_missingcom	plete_ra	tmean	sd	p0	p25	p50	p75	p100	hist
conc	0	1	0.72	0.74	0.0	0.10	0.50	1.00	2.00	
motile	0	1	92.67	45.35	39.0	61.50	82.50	104.25	238.00	
total	0	1	127.20	56.93	66.0	87.00	117.00	140.25	301.00	
$motile_frac$	0	1	0.73	0.12	0.4	0.67	0.78	0.81	0.88	

There are also the same eight donors, no missing data.

```
table(mt_etoh$donor, as.factor(mt_etoh$conc))
```

```
0 0.1 0.5 1 2
1 1
      1
          1 1 1
2 1
          1 1 1
      1
3 1
          1 1 1
4 1
          1 1 1
5 1
      1
          1 1 1
6 1
      1
          1 1 1
7 1
          1 1 1
      1
8 1
          1 1 1
```

The data are balanced with one observation for each concentration and each donor and no missing data.

```
mt_etoh_m1 <- glmer(cbind(motile, total - motile) ~ conc + (conc | donor),
    data = mt_etoh, family = binomial(link = "logit"))
summary(mt_etoh_m1)</pre>
```

```
Generalized linear mixed model fit by maximum likelihood (Laplace
```

Approximation) [glmerMod]

Family: binomial (logit)

Formula: cbind(motile, total - motile) ~ conc + (conc | donor)

Data: mt_etoh

```
AIC BIC logLik deviance df.resid 320.3 328.7 -155.1 310.3 35
```

Scaled residuals:

Min 1Q Median 3Q Max

```
-4.9916 -0.7375 0.0028 0.9353 1.8933
```

```
Random effects:
```

Groups Name Variance Std.Dev. Corr donor (Intercept) 0.16977 0.4120 conc 0.02106 0.1451 -0.02

Number of obs: 40, groups: donor, 8

Fixed effects:

conc -0.163

The model is:

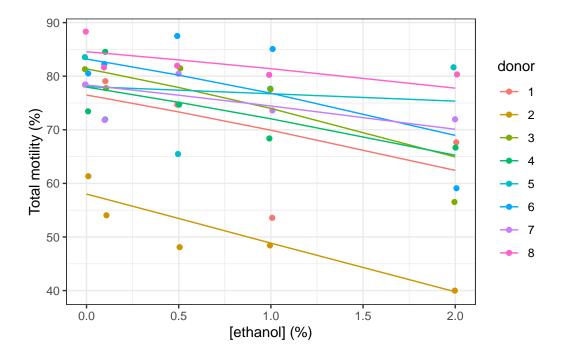
(Intr)

,

$$\begin{split} & \text{motile}_i \sim \text{Binomial}(n=1, \text{prob}_{\text{motile}=1} = \widehat{P}) \\ &, \log \left[\frac{\widehat{P}}{1 - \widehat{P}} \right] = \alpha_{j[i]} + \beta_{1j[i]}(\text{conc}) \\ &, \qquad \left(\begin{array}{c} \alpha_j \\ \beta_{1j} \end{array} \right) \sim N \left(\left(\begin{array}{c} \mu_{\alpha_j} \\ \mu_{\beta_{1j}} \end{array} \right), \left(\begin{array}{cc} \sigma_{\alpha_j}^2 & \rho_{\alpha_j\beta_{1j}} \\ \rho_{\beta_{1j}\alpha_j} & \sigma_{\beta_{1j}}^2 \end{array} \right) \right), \text{ for donor j} = 1, \dots, J \end{split}$$

Here is a plot of this model:

```
ggplot(data = mt_etoh) +
  geom_jitter(aes(x = conc, y = motile_frac * 100, col = donor),
    width = 0.01) +
  geom_line(aes(x = conc, y = fitted(mt_etoh_m1) * 100, col = donor)) +
  labs(x = "[ethanol] (%)", y = "Total motility (%)")
```



Generally, slopes are all negative, suggesting a negative concentration effect. Data are rather widespread. There are definitely shifts in the intercept per donor (different motility at [ethanol] = 0). Slopes seems more different between donors than for DMSO. However, we will also check if the model can be simplified using a likelihood ratio test:

```
mt_etoh_m2 <- glmer(cbind(motile, total - motile) ~ conc + (1 | donor),
   data = mt_etoh, family = binomial(link = "logit"))
anova(mt_etoh_m1, mt_etoh_m2, refit = FALSE) # Despite the name, it is indeed a LR test</pre>
```

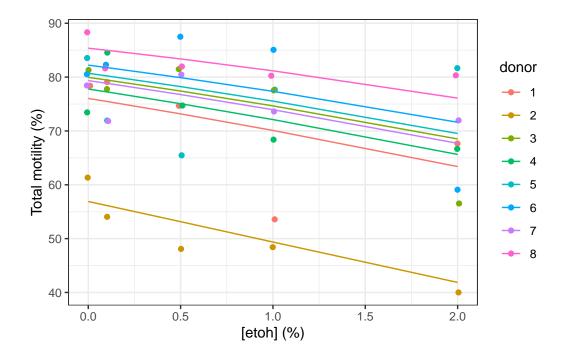
The likelihood ratio test does not detects significant differences between the full and simplified models at $\alpha = 5\%$. We could thus use the simplest mt_etoh_m2 model with only a shift in the slope per donor. This model is:

,

$$\begin{split} & \text{motile}_i \sim \text{Binomial}(n=1, \text{prob}_{\text{motile}=1} = \widehat{P}) \\ &, \log \left[\frac{\hat{P}}{1 - \hat{P}} \right] = \alpha_{j[i]} + \beta_1(\text{conc}) \\ & \qquad \qquad \alpha_j \sim N\left(\mu_{\alpha_j}, \sigma_{\alpha_j}^2\right), \, \text{for donor j} = 1, \dots, \text{J} \end{split} \tag{4}$$

Here is a plot of this model:

```
ggplot(data = mt_etoh) +
  geom_jitter(aes(x = conc, y = motile_frac * 100, col = donor),
    width = 0.01) +
  geom_line(aes(x = conc, y = fitted(mt_etoh_m2) * 100, col = donor)) +
  labs(x = "[etoh] (%)", y = "Total motility (%)")
```



```
summary(mt_etoh_m2)
```

```
Generalized linear mixed model fit by maximum likelihood (Laplace
  Approximation) [glmerMod]
Family: binomial ( logit )
Formula: cbind(motile, total - motile) ~ conc + (1 | donor)
```

```
Data: mt_etoh
```

```
AIC BIC logLik deviance df.resid 319.6 324.6 -156.8 313.6 37
```

Scaled residuals:

```
Min 1Q Median 3Q Max -5.0521 -0.5711 0.0252 0.9661 2.8884
```

Random effects:

```
Groups Name Variance Std.Dev. donor (Intercept) 0.1794 0.4236
Number of obs: 40, groups: donor, 8
```

Fixed effects:

The Z test indicates that conc is significantly different from zero at $\alpha=5\%$. However, it is not the best test in the case of a mixed model like here. We prefer to rely on the 95% confidence interval calculated either on the profile, or via parametric bootstrap (and especially the later one):

```
confint(mt_etoh_m2, level = 0.95) # 95% CI based on profile
```

Computing profile confidence intervals ...

```
2.5 % 97.5 % .sig01 0.2695168 0.7719890 (Intercept) 0.9261419 1.6176274 conc -0.3865530 -0.2192498
```

```
set.seed(535)
# 1000x parameter bootstrap
(mt_etoh_m2_conf <- confint(mt_etoh_m2, level = 0.95,
    method = "boot", nsim = 1000L))</pre>
```

Computing bootstrap confidence intervals ...

4 warning(s): Model failed to converge with max|grad| = 0.00611004 (tol = 0.002, component 1

```
2.5 % 97.5 % .sig01 0.1811891 0.6041279 (Intercept) 0.9728800 1.5769631 conc -0.3882783 -0.2237793
```

We had one model with singularity among the 1000, not a big problem (we may ignore this warning). Slope for conc is significantly different from zero at $\alpha = 5\%$ because the 95% CI does not contain zero.

Additional verifications

We could double-check the significance of the slope conc by looking at a likelihood ratio test when dropping conc from the model:

```
#drop1(mt_etoh_m2, scope = "conc")
  mt_etoh_m3 <- glmer(cbind(motile, total - motile) ~ 1 + (1 | donor),</pre>
    data = mt_etoh, family = binomial(link = "logit"))
  anova(mt_etoh_m2, mt_etoh_m3, refit = FALSE)
Data: mt_etoh
Models:
mt_etoh_m3: cbind(motile, total - motile) ~ 1 + (1 | donor)
mt_etoh_m2: cbind(motile, total - motile) ~ conc + (1 | donor)
                          BIC logLik deviance Chisq Df Pr(>Chisq)
                   AIC
mt_etoh_m3
              2 367.46 370.84 -181.73
                                        363.46
              3 319.58 324.65 -156.79 313.58 49.88 1 1.635e-12 ***
mt_etoh_m2
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The model with conc is significantly different at α level 5% from a reference model that sets the slope conc = 0. There is thus a significant effect of ethanol concentration (confirmation of results obtained from 95% CI).

We also double-check convergence of the model by trying different optimisation engines (just to make sure). First, is there a singularity in the model?

```
isSingular(mt_etoh_m2)
```

[1] FALSE

... then, a report about the model convergence:

```
mt_etoh_m2_all <- allFit(mt_etoh_m2)</pre>
```

bobyqa : [OK]

Nelder_Mead : [OK] nlminbwrap : [OK]

nmkbw : [OK]

optimx.L-BFGS-B : [OK]

nloptwrap.NLOPT_LN_NELDERMEAD : [OK] nloptwrap.NLOPT_LN_BOBYQA : [OK]

```
summary(mt_etoh_m2_all)
```

\$which.OK

bobyqa Nelder_Mead TRUE TRUE nlminbwrap nmkbw TRUE TRUE optimx.L-BFGS-B nloptwrap.NLOPT_LN_NELDERMEAD TRUE TRUE

nloptwrap.NLOPT_LN_BOBYQA

TRUE

\$msgs \$msgs\$bobyqa NULL

\$msgs\$Nelder_Mead
NULL

\$msgs\$nlminbwrap

NULL

\$msgs\$nmkbw

NULL

\$msgs\$`optimx.L-BFGS-B`

NULL

\$msgs\$nloptwrap.NLOPT_LN_NELDERMEAD

NULL

\$msgs\$nloptwrap.NLOPT_LN_BOBYQA

NULL

\$fixef

bobyqa(Intercept)concNelder_Mead1.269828-0.3029685nlminbwrap1.269826-0.3029668nmkbw1.269829-0.3029702optimx.L-BFGS-B1.269732-0.3029684nloptwrap.NLOPT_LN_NELDERMEAD1.269756-0.3029708nloptwrap.NLOPT_LN_BOBYQA1.269828-0.3029680

\$11ik

bobyqa Nelder_Mead
-156.7893 -156.7893
nlminbwrap nmkbw
-156.7893 -156.7893

optimx.L-BFGS-B nloptwrap.NLOPT_LN_NELDERMEAD -156.7893 -156.7893

 ${\tt nloptwrap.NLOPT_LN_BOBYQA}$

-156.7893

\$sdcor

donor.(Intercept)

bobyqa 0.4235709 Nelder_Mead 0.4235679

nlminbwrap	0.4235741
nmkbw	0.4235690
optimx.L-BFGS-B	0.4235601
nloptwrap.NLOPT_LN_NELDERMEAD	0.4235924
nloptwrap.NLOPT_LN_BOBYQA	0.4235698

\$theta

	donor.(Intercept)
bobyqa	0.4235709
Nelder_Mead	0.4235679
nlminbwrap	0.4235741
nmkbw	0.4235690
optimx.L-BFGS-B	0.4235601
${\tt nloptwrap.NLOPT_LN_NELDERMEAD}$	0.4235924
nloptwrap.NLOPT_LN_BOBYQA	0.4235698

\$times

	user.self	sys.self	elapsed	user.child	sys.child
bobyqa	0.044	0	0.044	0	0
Nelder_Mead	0.056	0	0.056	0	0
nlminbwrap	0.049	0	0.049	0	0
nmkbw	0.057	0	0.057	0	0
optimx.L-BFGS-B	0.344	0	0.345	0	0
nloptwrap.NLOPT_LN_NELDERMEAD	0.050	0	0.050	0	0
nloptwrap.NLOPT_LN_BOBYQA	0.039	0	0.039	0	0

\$feval

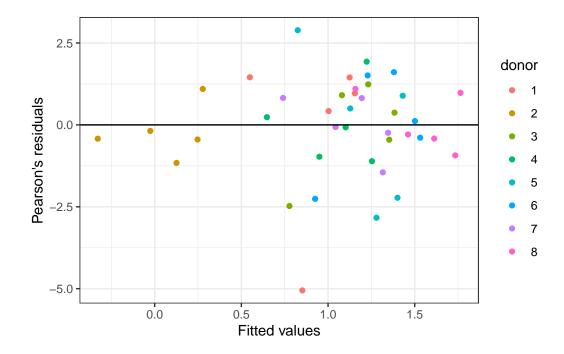
ead
88
kbw
100
ΞAD
92
1

attr(,"class")
[1] "summary.allFit"

Analysis of the residuals

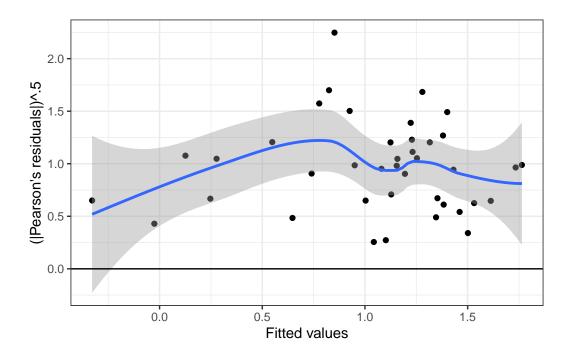
Let's check how the residuals distribute and if there is homoscedasticity.

```
mt_etoh <- fortify.merMod(mt_etoh_m2)
ggplot(data = mt_etoh, aes(x = .fitted, y = .scresid, col = donor)) +
    geom_point() +
    geom_hline(yintercept = 0) +
    labs(x = "Fitted values", y = "Pearson's residuals")</pre>
```



There is one extreme value (less extreme than for DMSO), but otherwise, residuals seem rather correctly distributed. Linearity is good here.

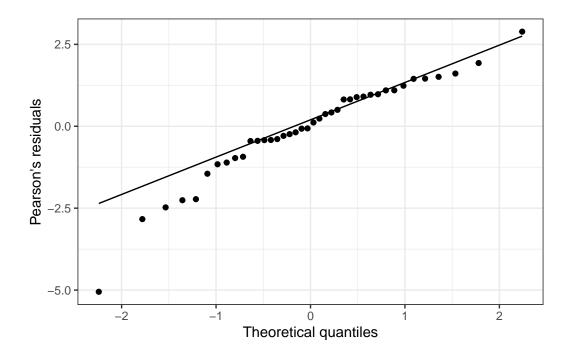
```
ggplot(data = mt_etoh, aes(x = .fitted, y = sqrt(abs(.scresid)))) +
  geom_point() +
  geom_smooth(method = "loess", formula = y ~ x) +
  geom_hline(yintercept = 0) +
  labs(x = "Fitted values", y = "(|Pearson's residuals|)^.5")
```



Homoscedasticity of the residuals seems here acceptable (the blue curve that is a loess smoothing in the data is relatively horizontal).

With the same remark as for DMSO, here is the quantile-quantile plot of the residuals:

```
ggplot(data = mt_etoh, aes(sample = .scresid)) +
  geom_qq() +
  geom_qq_line() +
  labs(x = "Theoretical quantiles", y = "Pearson's residuals")
```



It appears not too good. A Shapiro-Wilk test indicates mild non Normality (with caution because this test tends to be conservative):

```
shapiro.test(mt_etoh$.scresid)
```

Shapiro-Wilk normality test

```
data: mt_etoh$.scresid
W = 0.94028, p-value = 0.03534
```

Predictions

The model allows to calculate the drop in total mobility according to ethanol concentration from 0 to 2%. Note that an inverse logit transformation is required. Here is an example:

```
mt_etoh_slope <- c(
    ci95_min = min(mt_etoh_m2_conf["conc", ]),
    estimate = fixef(mt_etoh_m2)[["conc"]],
    ci95_max = max(mt_etoh_m2_conf["conc", ]))
mt_etoh_slope</pre>
```

```
ci95_min estimate ci95_max
-0.3882783 -0.3029708 -0.2237793

#saveRDS(mt_etoh_slope, "../data/motility_total_ETOH_slope.rds")
```

Let's say we want to calculate the drop in total mobility for various ethanol concentrations between 0 and 2% if the total mobility in a sample without ethanol is 80%. The calculation is:

```
predict_logit <- function(conc, intercept = 1, slopes) {</pre>
    slopes_mat <- matrix(slopes, nrow = 1,</pre>
      dimnames = list(NULL, names(slopes)))
    data.frame(conc = conc, -intercept +
      boot::inv.logit(boot::logit(intercept) +
      conc %*% slopes_mat))
  }
  etoh_conc <- (0:20) / 10
  mt_etoh_lost <- predict_logit(etoh_conc, 0.8, mt_etoh_slope)</pre>
  mt_etoh_lost
  conc
            ci95 min
                         estimate
                                      ci95 max
1
   0.0
        0.00000000 0.00000000 0.00000000
2
   0.1 -0.006284872 -0.004891619 -0.003604517
3
   0.2 -0.012714728 -0.009871491 -0.007257167
   0.3 -0.019289630 -0.014939680 -0.010957988
5
   0.4 -0.026009417 -0.020096167 -0.014706993
6
   0.5 -0.032873700 -0.025340853 -0.018504173
7
   0.6 -0.039881848 -0.030673549 -0.022349493
   0.7 -0.047032985 -0.036093983 -0.026242894
8
9
   0.8 -0.054325977 -0.041601787 -0.030184290
10 0.9 -0.061759427 -0.047196504 -0.034173569
   1.0 -0.069331667 -0.052877577 -0.038210591
   1.1 -0.077040754 -0.058644355 -0.042295190
   1.2 -0.084884466 -0.064496085 -0.046427171
14
   1.3 -0.092860294 -0.070431914 -0.050606312
15 1.4 -0.100965441 -0.076450885 -0.054832359
16 1.5 -0.109196822 -0.082551937 -0.059105030
17 1.6 -0.117551062 -0.088733904 -0.063424016
18
   1.7 -0.126024496 -0.094995513 -0.067788973
   1.8 -0.134613171 -0.101335385 -0.072199529
   1.9 -0.143312852 -0.107752031 -0.076655281
```

```
#saveRDS(mt_etoh_lost, "../data/motility_total_ETOH_lost.rds")
```

This is the lost in total mobility that the model predicts.

General informations

```
sessionInfo()
R version 4.1.3 (2022-03-10)
Platform: x86_64-apple-darwin17.0 (64-bit)
Running under: macOS Big Sur/Monterey 10.16
Matrix products: default
LAPACK: /Library/Frameworks/R.framework/Versions/4.1/Resources/lib/libRlapack.dylib
locale:
[1] en US.UTF-8/en US.UTF-8/en US.UTF-8/c/en US.UTF-8/en US.UTF-8
attached base packages:
[1] stats
              graphics grDevices utils
                                             datasets methods
                                                                 hase
other attached packages:
[1] ggplot2_3.3.5 lme4_1.1-29
                                Matrix_1.4-1
loaded via a namespace (and not attached):
 [1] tidyr_1.2.0
                         jsonlite_1.8.0
                                              splines_4.1.3
 [4] equatiomatic_0.3.1 shiny_1.7.1
                                              assertthat_0.2.1
 [7] highr_0.9
                         broom.mixed_0.2.9.4 cellranger_1.1.0
[10] yaml_2.3.5
                                              numDeriv_2016.8-1.1
                         globals_0.14.0
[13] pillar_1.7.0
                         backports 1.4.1
                                              lattice 0.20-45
[16] glue_1.6.2
                         digest_0.6.29
                                              promises_1.2.0.1
[19] minqa_1.2.4
                         colorspace_2.0-3
                                              dfoptim_2020.10-1
[22] htmltools_0.5.2
                         httpuv_1.6.5
                                              pkgconfig_2.0.3
[25] broom_0.8.0
                         listenv_0.8.0
                                              purrr_0.3.4
[28] xtable_1.8-4
                         scales_1.2.0
                                              later_1.3.0
[31] tibble_3.1.6
                         mgcv_1.8-40
                                              generics_0.1.2
[34] farver_2.1.0
                         ellipsis_0.3.2
                                              withr_2.5.0
[37] furrr_0.2.3
                         repr_1.1.4
                                              skimr_2.1.4
```

[40] cli_3.2.0	magrittr_2.0.3	crayon_1.5.1
[43] readxl_1.4.0	mime_0.12	evaluate_0.15
[46] fansi_1.0.3	future_1.24.0	parallelly_1.31.0
[49] nlme_3.1-157	MASS_7.3-56	forcats_0.5.1
[52] tools_4.1.3	lifecycle_1.0.1	stringr_1.4.0
[55] munsell_0.5.0	compiler_4.1.3	rlang_1.0.2
[58] grid_4.1.3	nloptr_2.0.0	rstudioapi_0.13
[61] base64enc_0.1-3	labeling_0.4.2	rmarkdown_2.13
[64] boot_1.3-28	gtable_0.3.0	codetools_0.2-18
[67] DBI_1.1.2	R6_2.5.1	knitr_1.38
[70] dplyr_1.0.8	optimx_2021-10.12	fastmap_1.1.0
[73] utf8_1.2.2	stringi_1.7.6	parallel_4.1.3
[76] Rcpp_1.0.8.3	vctrs_0.4.1	tidyselect_1.1.2
[79] xfun_0.30		