

# 6<sup>th</sup> Grade Competition and Solutions

Math Competition 2006 22 October 2006

1. To get ready for a math competition, Kevin buys a pencil for fifty cents, a ruler for one dollar, and graph paper for thirty dollars. How much money does Kevin spend?

**Answer: \$31.50**

Add the three costs, lining up decimal points:

$$\begin{array}{r} \$0.50 \\ \$1.00 \\ +\$30.00 \\ \hline \$31.50 \end{array}$$

2. Mrs. Stone makes 20 telephone calls each day. How many telephone calls does she make in the month of January?

**Answer: 620**

There are 31 days in January, and she makes 20 calls on each of these days, so she makes a total of  $31 \cdot 20 = 620$  phone calls in January.

3. When the band The Beatles first formed, they had 1 fan. This fan told 3 other people about The Beatles. Each of these 3 people told 3 other people about The Beatles. As a result, how many people in total knew about The Beatles?

**Answer: 13**

First one person knew, then an additional three people knew, then for each of these three people, an additional three people knew:  $1 + 3 + 3 \cdot 3 = 13$ .

4. Jan gives away 10 muffins out of every 12 that she bakes. If Jan bakes 60 muffins, how many does she give away?

**Answer: 50**

$$(60 \div 12) \cdot 10 = 50.$$

5. Every time Joey visits Monica and Chandler's apartment, he steals one more food item than he did the last time. If he visits once every day for a week, and steals 3 items the first day, how many food items does he steal in the week?

**Answer: 42**

On the first day Joey steals 3 items, on the second he steals 4 items, and so on, until on the seventh day he steals 9 items. Add these all together:  $3 + 4 + 5 + 6 + 7 + 8 + 9 = 42$ . This can also be computed by using the formula  $1 + 2 + \cdots + n = \frac{n(n+1)}{2}$ :  $\frac{9 \cdot 10}{2} - 2 - 1 = 45 - 3 = 42$ .

6. Donald has twice as many books as Kevin. Kevin has 4 times as many books as Watson. Watson has 6 books. How many books do Donald, Kevin, and Watson have in total?

**Answer: 78**

Watson has 6 books, so Kevin has  $4 \cdot 6 = 24$  books and Donald has  $2 \cdot 24 = 48$  books. In total they have  $6 + 24 + 48 = 78$  books.

7. Find the product of the even multiples of 5 that are greater than 1 and less than 49.

**Answer: 240000**

The even multiples of 5 between 1 and 49 are simply the multiples of 10: 10, 20, 30, and 40.  
 $10 \cdot 20 \cdot 30 \cdot 40 = 240,000$ .

8. How many perfect squares are there between 2 and 140?

**Answer: 10**

The perfect squares between 2 and 140 are  $2^2 = 4, 3^2 = 9, \dots, 11^2 = 121$ . So there are  $11 - 2 + 1 = 10$ .

9. Compute  $(1 + 2 + 3 + \dots + 98 + 99) \div (.01 + .02 + .03 + \dots + .98 + .99)$ .

**Answer: 100**

Note that multiplying each term in the divisor by 100 yields  $1 + 2 + 3 + \dots + 98 + 99$ . So the dividend is 100 times the divisor; thus the quotient is 100.

10. The sum of the ages of Sam and Cara is 30. Sam is 4 years younger than Cara. How old is Cara?

**Answer: 17**

Guess-and-check solves this problem fairly quickly. Alternately, let  $x$  be Sam's age and  $y$  be Cara's age, in years. From the problem,  $x + y = 30$  and  $y - 4 = x$ . Substituting  $x = y - 4$  into the first equation yields  $y - 4 + y = 30 \Rightarrow 2y - 4 = 30 \Rightarrow 2y = 34 \Rightarrow y = 17$ .

11. Find the probability that a randomly chosen positive whole number less than or equal to 90 is a multiple of 17.

**Answer:  $\frac{1}{18}$**

The positive multiples of 17 less than or equal to 90 are 17, 34, 51, 68, and 85. There are 5 such numbers out of a total 90. Thus the answer is  $\frac{5}{90}$ , or  $\frac{1}{18}$ .

12. Sixteen teams compete in a soccer tournament. Each game, one team wins and one team loses, and the losing team is eliminated. How many games must be played so that only one team remains undefeated?

**Answer: 15**

Fifteen teams must be eliminated, and it takes one game to eliminate one team, so 15 games must be played.

13. The hypotenuse of a right triangle has length 10, and one of the legs has length 6. What is the area of the triangle?

**Answer: 24**

By the Pythagorean Theorem,  $a^2 + b^2 = c^2$ , where  $a$  and  $b$  are the lengths of the legs of a right triangle and  $c$  is the length of the hypotenuse. So the remaining leg of the triangle has length  $\sqrt{10^2 - 6^2} = \sqrt{64} = 8$ . The lengths of the legs are the base and height of the triangle. Since area equals one-half of the base times the height, the area of the triangle is  $\frac{6 \cdot 8}{2} = 24$ .

14. Jen took pictures of exactly 40 birds. Exactly 30 of the birds were blue, and exactly 15 of the birds were male. How many of the birds were both blue and male?

**Answer: 5**

Adding together the number of blue birds plus the number of male birds counts the birds that are both blue and male twice. The total number of birds equals the number of blue (but not male) birds plus the number of male (but not blue) birds plus the number of blue male birds. So the number of blue male birds is the sum of the number of blue birds and the number of male birds minus the total number of birds:  $30 + 15 - 40 = 5$ . This uses the principle of inclusion-exclusion.

15. 9 is 15% of what number?

**Answer: 60**

Divide 9 by 15%:  $9 \div 0.15 = 60$ .

16. Connie took a test with 25 questions. For every question she got right, she earned 4 points, and for every question she got wrong, she lost 1 point. She answered every question, and got a score of 80. How many questions did she get right?

**Answer: 21**

Guess-and-check can be used to solve this problem. Alternately, let  $c$  be the number of questions Connie got right. Then she got  $25 - c$  questions wrong. So her score is  $4c - (25 - c) = 5c - 25 = 80$ . Solve for  $c$ :  $5c = 105 \Rightarrow c = 21$ .

17. Ian and Rob are having a barbecue. Ian goes to Shoprite and buys 62 ounces of meat. Rob goes to Pathmark and buys 82 ounces of meat. In total, how many *pounds* of meat did Ian and Rob buy? (There are 16 ounces in one pound.)

**Answer: 9**

Together they bought  $62 + 82 = 144$  ounces of meat. Since one pound is equivalent to 16 ounces, they bought  $144 \div 16 = 9$  pounds of meat.

18. In 4 ponds, there are 33 ducks. For any arrangement of ducks in these ponds, you can find at least one pond with at least  $n$  ducks. What is the largest possible value of  $n$ ?

**Answer: 9**

This is an application of the Pigeonhole Principle, with 33 “pigeons” (ducks) in 4 “holes” (ponds). Since  $33 \div 4 = 8.25$ , we round up to get the answer of 9.

19. Vincent likes to mix different types of soda. He buys one liter of cola for \$2.00, one liter of lemon-lime soda for \$1.50, and 2 liters of orange soda for a total of \$3.50. If he mixes these all together, what is the price per liter of the mixture?

**Answer: \$1.75**

The total cost is  $\$2.00 + \$1.50 + \$3.50 = \$7.00$ . There are four liters of the mixture. So the price per liter is  $\$7.00 \div 4 = \$1.75$ .

20. How many 2-digit whole numbers contain the digit 2 exactly once?

**Answer: 17**

The 2-digit numbers that contain the digit 2 exactly once are 12, 20, 21, 23, 24, 25, 26, 27, 28, 29, 32, 42, 52, 62, 72, 82, and 92. There are 17 of them. This can also be seen by noting that either the first digit must be 2 or the second digit must be 2. If the first digit is 2, there are 9 options for the second digit, making 9 numbers. If the second digit is 2, there are 8 options for the first digit (it cannot be 0 or 2), making 8 numbers. So there are  $9 + 8 = 17$  in total.

21. Christine can sing 120 notes every minute, while Rachel can sing 180 notes every minute. If Christine and Rachel begin singing at the same time, how long, *in seconds*, will it take for their combined note total to equal 1080 notes?

**Answer: 216**

Together they sing  $120 + 180 = 300$  notes every minute. So it takes 1080 notes  $\cdot \frac{1 \text{ minute}}{300 \text{ notes}} = 3.6$  minutes for them to sing 1080 notes. Convert this to seconds:  $3.6 \text{ minutes} \cdot 60 \frac{\text{seconds}}{\text{minute}} = 216$  seconds. This uses dimensional analysis: multiplying a given quantity by a ratio so that its unit cancels out and you are left with a different unit.

22. Farmer John wants to buy fencing for the perimeter of his rectangular field. The length of the field is 17 meters and the area of the field is 119 square meters. Given that fencing costs 10 cents per meter, how much money will Farmer John have to spend?

**Answer: \$4.80**

Since the area of a rectangle equals its length times its width, its width equals its area divided by its length. Thus the width of Farmer John's field is  $119 \div 17 = 7$  meters. The perimeter of the field is then  $17 + 17 + 7 + 7 = 48$  meters. So Farmer John must buy 48 meters of fencing at 10 cents per meter, for a total cost of  $48 \cdot 10 = 480$  cents, or \$4.80.

23. Sally has 7 coins, which together make 72 cents. Each coin is a penny, nickel, dime or quarter. How many dimes does Sally have?

**Answer: 1**

Sally must have 2 pennies, since every other coin has a cent value that is a multiple of 5. If her other 5 coins are all dimes, she would only have 52 cents, so she must have at least one quarter. If her other 4 coins are all dimes, she would only have  $25 + 40 + 2 = 67$  cents, so she must have at least two quarters. If her other 3 coins are all dimes, she would have  $50 + 30 + 2 = 82$  cents, which is too much, so at least one coin must be a nickel. This would yield  $50 + 20 + 5 + 2 = 77$  cents, which is still too much, so two coins must be nickels. Thus she has 2 pennies, 2 quarters, 2 nickels, and 1 dime ( $2 \cdot 1 + 2 \cdot 25 + 2 \cdot 5 + 1 \cdot 10 = 72$ ).

24. What is the number halfway between  $\frac{1}{13}$  and  $\frac{1}{9}$ ?

**Answer:  $\frac{11}{117}$**

Find the arithmetic mean of the two fractions. Add the two fractions:  $\frac{1}{9} + \frac{1}{13} = \frac{13+9}{9 \cdot 13} = \frac{22}{117}$ . Divide this sum by 2 to yield  $\frac{11}{117}$ .

25. What is the positive difference between the sum of the first fifteen positive even numbers and the sum of the first fifteen positive odd numbers?

**Answer: 15**

The first fifteen positive even numbers are  $2, 4, \dots, 28$  and the first fifteen odd positive numbers are  $1, 3, \dots, 27$ . The desired difference is then  $(2 + 4 + \dots + 28) - (1 + 3 + \dots + 27)$ . By associativity, this equals  $(2 - 1) + (4 - 3) + \dots + (28 - 27) = 1 + 1 + \dots + 1$ , where there are fifteen 1's in the final expression. So the difference equals 15.

26. One issue of Math Magazine, which is published once per month, costs \$5. A yearlong subscription costs \$50, while a set of 10 yearlong subscriptions costs \$404. How much do I save per issue if I buy one set of 10 yearlong subscriptions and two additional yearlong subscriptions, rather than buying one magazine per month individually for the same time period?

**Answer: \$1.50**

My set of 12 subscriptions costs \$504, and contains  $12 \cdot 12 = 144$  issues. This is a value of  $\$504 \div 144 = \$3.50$  per issue. Subtract this from the monthly price of \$5 per issue to obtain \$1.50.

27. My initials are the first letter of my first name followed by the first letter of my last name. How many possible sets of initials could I have? (There are 26 letters.)

**Answer: 676**

There are 26 possibilities for the first letter of my first name and 26 possibilities for the first letter of my last name. So there are  $26 \cdot 26 = 676$  possibilities for my set of initials.

28. Let  $N = 20 \cdot 30 \cdot 50 \cdot 70 \cdot 90 \cdot 110 \cdot 130$ . What is the smallest prime number that is not a factor of  $N$ ?

**Answer: 17**

From the expression given for  $N$  in the problem, it can be seen that  $N = 2 \cdot 3 \cdot 5 \cdot 7 \cdot 9 \cdot 11 \cdot 13 \cdot 10^7$ . So the first six prime numbers 2, 3, 5, 7, 11 and 13 are all factors of  $N$ , while 17 - the next prime - is not.

29. The average (arithmetic mean) of five numbers in a list is 35. The average of the first two numbers is 26. What is the average of the last three numbers?

**Answer: 41**

The sum of all the numbers in the list is  $5 \cdot 35 = 175$ . The sum of the first two numbers is  $2 \cdot 26 = 52$ , so the sum of the last three numbers is  $175 - 52 = 123$ . The average of these numbers is  $123 \div 3 = 41$ .

30. If the length, width, and height of a box (rectangular prism) are all doubled, by how many times is the volume of the box increased?

**Answer: 8**

Since volume = length  $\cdot$  width  $\cdot$  height, the increased volume is  $2l \cdot 2w \cdot 2h = 8lwh = 8v$ , where  $l, w, h$  and  $v$  represent the original length, width, height, and volume, respectively.

31. Eddy scored 4 free throws out of the 13 free throws he has taken. How many consecutive shots must he now score in order to achieve a shooting percentage (free throws scored out of total free throws taken) of 50%?

**Answer: 5**

Add one more free throw scored and one more free throw taken until the number taken is twice the number scored:  $\frac{5}{14}, \frac{6}{15}, \frac{7}{16}, \frac{8}{17}, \frac{9}{18}$ . 9 is half of 18, so if he scores the next  $9 - 4 = 5$  consecutive free throws, he will have a shooting percentage of 50%.

Alternately, let  $x$  be the number of consecutive shots he scores after the first 13 free throws. We want  $\frac{4+x}{13+x} = \frac{1}{2}$ . Solve for  $x$ :  $2(4+x) = 13+x \Rightarrow 8+2x = 13+x \Rightarrow x = 5$ .

32. How many lines of symmetry does a regular dodecagon (a polygon with 12 sides) have?

**Answer: 12**

Since 12 is even, the lines of symmetry will either join two opposite vertices through the center, or join the midpoints of 2 opposite sides through the center. There are 6 of the first type and 6 of the second type, making 12 total.

33. If a box of donuts is marked down 20% from its original price of \$5, then marked back up 20% from the sale price, how much does this box of donuts cost now?

**Answer: \$4.80**

Taking 20% off is the same as multiplying by  $1 - 0.20 = 0.80$ , so a 20% reduction off \$5 brings the price to  $0.80 \cdot \$5 = \$4$ . Marking this up by 20% is the same as multiplying by 1.20, giving the desired result  $1.20 \cdot \$4 = \$4.80$ .

34. On planet Penev, the symbol  $\left\{ - \right\}$  is defined as follows:  $\left\{ \frac{x}{y} \right\} = (-1)^{x+y}$ . Compute  $\left\{ \frac{2}{4} \right\}$ .

**Answer: 1**

From the given definition,  $\left\{ \frac{2}{4} \right\} = (-1)^{2+4} = (-1)^6 = 1$ , since 6 is even.

35. Three ducks - Duck 1, Duck 2, and Duck 3 - are sitting in a row. Duck 1 quacks once every six minutes. Duck 2 quacks once every nine minutes. Duck 3 quacks once every fifteen minutes. Given that all three ducks quack at 1:00 PM, when is the next time they will all simultaneously quack? ("Simultaneously" means at the same time.)

**Answer: 2:30 PM**

Find the least common multiple of the times between quacks: the least common multiple of 6, 9, and 15 is 90 ( $2 \cdot 3 \cdot 3 \cdot 5$ ). So all three ducks quack simultaneously every 90 minutes. Since they all quack at 1:00 PM, the next time they all quack is 90 minutes later, or 2:30 PM.

36. The angle measures of *acute* triangle  $ABC$  are all positive whole numbers. If  $m\angle A = 50^\circ$ , what is the smallest possible measure, in degrees, of  $\angle B$ ?

**Answer: 41**

The sum of the three internal angles of a triangle is  $180^\circ$ . So  $m\angle B + m\angle C = 180^\circ - m\angle A = 180^\circ - 50^\circ = 130^\circ$ . The measure of  $\angle B$  is smallest when  $\angle C$  is largest. Since  $\triangle ABC$  is acute, each angle measures less than  $90^\circ$ , so the maximum value for the measure of  $\angle C$  is  $89^\circ$ . Thus the smallest value for the measure of  $\angle B$  is  $130^\circ - 89^\circ = 41^\circ$ .

37. Three children at a time can play jacks. For 30 minutes, 5 children take turns playing jacks so that each child plays for the same amount of time. How many total minutes does each child play jacks?

**Answer: 18**

Since three children at a time play for 30 minutes, there are  $3 \cdot 30 = 90$  total minutes spent playing jacks. This is divided equally among the five children, so each child plays for  $90 \div 5 = 18$  minutes.

38. A *palindrome* is a number that reads the same left-to-right as right-to-left. For example, 1234321 is a palindrome. How many palindromes between 1000 and 9999 are divisible by 5?

**Answer: 10**

Note that any multiple of 5 ends in 0 or 5, so a palindrome must end in 5 (since the first digit cannot be 0). Hence palindromes between 1000 and 9999 divisible by 5 are of the form  $5xx5$ , where  $x$  is any digit. Since there are 10 possibilities for  $x$ , there are 10 palindromes between 1000 and 9999 that are divisible by 5.

39. Dan runs at a speed of  $1.1\pi$  miles per hour. How long, in hours, does it take Dan to run 2.75 times around a circle with radius 1 mile?

**Answer: 5**

The circumference of a circle equals  $2\pi r$ , where  $r$  is the circle's radius. So the circle in the problem has circumference  $2\pi \cdot 1 = 2\pi$  miles. Running around it 2.75 times is thus  $2.75 \cdot 2\pi = 5.5\pi$  miles. Since distance=rate·time, time=distance÷rate and Dan's time is  $5.5\pi \text{ miles} \div 1.1\pi \text{ miles/hour} = 5 \text{ hours}$ .

40. To complete his meal, James must select 3 different side dishes and one drink. There are 6 available different side dishes and 4 available drinks. The order in which James selects the side dishes and drinks does not matter. How many different meals can James select?

**Answer: 80**

James can select  $\binom{6}{3} = \frac{6!}{3!3!} = \frac{6 \cdot 5 \cdot 4}{3 \cdot 2 \cdot 1} = 20$  different combinations of side dishes. For each of these combinations of side dishes, he has four choices of drink, for a total of  $4 \cdot 20 = 80$  different meals. Note:  $\binom{n}{k}$ , read " $n$  choose  $k$ ," denotes the expression for the number of ways to choose  $k$  elements from a set of  $n$  elements. It is equal to  $\frac{n!}{k!(n-k)!}$ .

41. Compute  $\left(\sqrt{2^3}\right)^{\frac{4}{3}}$ .

**Answer: 4**

Taking a square root is equivalent to raising to the  $\frac{1}{2}$  power:  $\sqrt{2^3} = (2^3)^{\frac{1}{2}}$ . Using the rules of exponents, we see that  $\left((2^3)^{\frac{1}{2}}\right)^{\frac{4}{3}} = 2^{3 \cdot \frac{1}{2} \cdot \frac{4}{3}} = 2^2 = 4$ .

42. Dr. Mayers raises chickens and rabbits in his classroom. He counts 450 total animals, and 1050 total legs on the animals. Each chicken has 2 legs, while each rabbit has 4 legs. How many rabbits does Dr. Mayers have?

**Answer: 75**

Let the number of chickens be  $c$  and the number of rabbits be  $r$ . From the given information,  $r + c = 450$  and  $4r + 2c = 1050$ . Multiplying the first equation by 2 and subtracting it from the second yields  $2r = 150$ . Therefore  $r = 75$ .

Note: This problem can also be solved without using any algebra. The classic method is to first assume that all the animals are chickens, and then switch in a rabbit for a chicken until the leg number becomes 1050.

43. Aaron and John have a 300-square-foot lawn. It takes Aaron 30 minutes to mow the lawn alone, and it takes John 20 minutes to mow the lawn alone. If Aaron and John work together to mow the lawn at the same time, how long, in minutes, will it take them to mow it?

**Answer: 12**

Aaron mows at a rate of  $\frac{300sqft}{30min} = 10\frac{sqft}{min}$ , and John mows at a rate of  $\frac{300sqft}{20min} = 15\frac{sqft}{min}$ . Together they mow at a rate of  $10 + 15 = 25\frac{sqft}{min}$ . So they mow the 300-square-foot lawn in  $\frac{300sqft}{25sqft/min} = 12$  minutes.

44. Four different numbers  $A, B, C$  and  $D$  are chosen from the set

$$\{-4, -\frac{3}{2}, -1, 0, \frac{5}{8}, 1, 4, 7\}.$$

What is the smallest possible value of the sum  $\frac{A}{B} + \frac{C}{D}$ ?

**Answer:  $-\frac{67}{5}$**

The sum is smallest when both fractions are negative and as far from zero as possible. This occurs when the two fractions are  $\frac{7}{-1}$  and  $\frac{-4}{5/8}$ , which sum to  $-\frac{67}{5}$ .

45. Richard plays darts on a circular dartboard that is made up of two concentric circles (two circles with the same center but different sizes). Getting a bulls-eye means hitting anywhere in the inner circle, which has radius 2 inches. The outer circle has radius 3 inches. Richard always hits the dartboard, but does not always get a bulls-eye. If Richard has an equal chance of hitting each point on the dartboard, what is the probability that Richard gets a bulls-eye in his next shot?

**Answer:  $\frac{4}{9}$**

The area of a circle is  $\pi r^2$ , where  $r$  is the circle's radius. Since the probability of hitting each point is equal, divide the bulls-eye area by the total area:  $\frac{\pi \cdot 2^2}{\pi \cdot 3^2} = \frac{4}{9}$ .

46. In the game of Gaussball, there are two ways to score points: a regular goal, worth 3 points; and a Gauss goal, worth 4 points. What is the greatest whole number that cannot be earned as a score in a game of Gaussball?

**Answer: 5**

A score of 6 is possible by scoring two regular goals. One regular goal and one Gauss goal earn a score of 7, and two Gauss goals earn a score of 8. Any greater whole number can be earned as a score by earning 6, 7 or 8 points and then scoring some number of regular goals. So every whole number greater than or equal to 6 can be earned as a score in Gaussball, while 5 cannot.

47. What is the units digit of  $8^{22}$ ?

**Answer: 4**

When finding the units digits of successive powers of 8, it is only necessary to multiply the preceding units digit by 8.  $8^1 = 8$  and  $8^2 = 64$ , so the units digit of  $8^3$  is the units digit of  $4 \cdot 8 = 32$ , which is 2. The units digit of  $8^4$  is then 6, and the units digit of  $8^5$  is 8. Since we have only been multiplying by 8 and now the units digit 8 has repeated, we have a repeating pattern of units digits: 8, 4, 2, 6. Since this pattern consists of 4 terms, and 20 is a multiple of 4, the units digit of  $8^{22}$  is the same as the units digit of  $8^2$ , which is 4.

48. Dr. Crane gave her class five homework assignments. Arthur only did three of these assignments. Dr. Crane picks two assignments at random to check, out of the five she gave. What is the

probability that Arthur has done both of the assignments that Dr. Crane checks?

**Answer:**  $\frac{3}{10}$

For the first assignment that Dr. Crane checks, there is a  $\frac{3}{5}$  chance that Arthur has done it. If Arthur has done this assignment, then there are four remaining assignments Dr. Crane could check, and Arthur has done two of them, so there is a  $\frac{3}{5} \cdot \frac{2}{4} = \frac{6}{20} = \frac{3}{10}$  chance Arthur has done both assignments.

49. A cylindrical container of internal radius 2 inches and internal volume  $32\pi$  cubic inches is  $\frac{3}{4}$  filled with water. What is the maximum number of cylindrical disks of radius 2 inches and height  $\frac{3}{5}$  inch that can be added to the container without letting the water overflow?

**Answer:** 3

The radius of each disk is the same as the radius of the container, so we are only concerned with the heights. The container is a cylinder, so the formula  $V = \pi r^2 h$  applies; solving for  $h$  gives a height of 8 inches. Because it is  $\frac{3}{4}$  filled, the water is at a height of  $\frac{3}{4} \cdot 8 = 6$  inches. Adding 3 disks will increase the water level to 7.8 inches, but adding 4 will cause the water level to exceed 8 inches, overflowing the container.

50. Jimbo, Jun, Jay, Jacob, Janine and Jenna are standing in a line with their backs to a wall. How many different orders could they be standing in so that Jenna and Jimbo are standing next to each other?

**Answer:** 240

Since Jenna and Jimbo must be next to each other, we can treat them for the moment as one unit. Thus we have five units to line up, which can be done in  $5! = 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 120$  ways. Since Jenna and Jimbo can switch places with each other, multiply this number by two:  $2 \cdot 120 = 240$ .