

1. Assume 4 positive integers  $a, b, c$ ,  $a \neq b$  and  $b \neq c$ . Please prove for 3 numbers  $a^3b - ab^3$ ,  $b^3c - bc^3$ ,  $c^3a - ca^3$ , one of them is divisible by 10.
2. Please prove: for whole number  $a$ , it is not divisible by 2 and 3, then  $24 \mid (a^2 - 1)$ .
3. Numbers  $p$  and  $q$  are prime, and are bigger than 3, please prove  $24 \mid (p^2 - q^2)$ .
4.  $36x + 83y = 1$ . If  $x$  and  $y$  are integers, please find  $x$  and  $y$ .