

1.  $f(x) = ax^2 + bx + c$ , where  $a, b, c$  are known integers. For odd number  $m$ ,  $am^2 + bm + c$  is odd number and  $c$  is also odd number. Please prove for  $ax^2 + bx + c = 0$ ,  $x$  would not be an odd number.
2.  $a, b, c, d$  are 4 natural numbers, and  $a + b + c + d = 1989$ , please prove  $a^3 + b^3 + c^3 + d^3$  are not even number.
3.  $a, b$  are two integers and  $b$  would not equal 0. If integer  $q$ , then  $a = b * q$ , then we can say  $a$  is divisible by  $b$ , written as  $b|a$ . Now we know  $7|(13x + 8y)$ , please prove  $7|(9x + 5y)$ .
4. We know  $m$  and  $n$  are odd numbers. When  $4|k$ , please prove  $8|(m^k - n^k)$ .