复利和退休计划管理 (401K, 403b, 457 plans)

李春贵

#### invitation Only

# 复利和我们的401K退休计划



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温习小学数学和复利知识



活学活用复利知识和理论



研究退休计划稳步增长规律



掌握积累三百万退休金秘诀



避免财务管理金融投资误区



Group: 明尼苏达财务和投资 规划研究



#### 财务规划和金融投资及管理的八个方面

#### Budget Planning & Debt Management & Emergency Fund



3 to 6 mo. expense

#### Real Estate/Mortgage

Mortgage Planning Tax Planning on Investment Property



#### **Education fund**

How to Max Out Financial Aid? Where to save? – 529?



#### Retirement plan

Growth/Safety/Longevity
How to create a Pension



#### Investment

Balance: Risk, Return, Liquidity



#### Tax

Tax now? Tax Later? Tax Free?



#### **Family Protection**

People: Health/Disability/Life/LTC Asset: Market Risk/Legal/Tax



#### **Estate Planning**

Minor Children, Probate, Estate Tax Will & Trust & POA



#### 金融投资需要关注的要点

- ❖投资回报Market Return
- ❖市场风险Market Risk
- ❖投资税务责任Investment Tax
- ❖灵活性Flexibility
- ❖流动性Liquidity
- ❖投资者行为和纪律性Investor Behavior and discipline

### 金融规划的目的:不确定性----->确定性

未来 不确定 性

- •市场风险
- •未来税率
- 退休的时机
- •账户提取率
- •人的寿命
- •人的健康

确定性

- 保本投资
- 保证免税投资
- 保证的永续收入
- <mark>保证</mark>的长期护理 保护

#### 我们推荐的理念和原则

We encourage each family and every individual to have a financial plan in day one, encourage each family to review and update this financial plan in each of the family's milestones. We emphasize creating a **disciplined** and **active** (in opposite to **inactive** or **reactive**) financial plan with **sound, solid, effective** processes for all 8 sectors.

我们鼓励每一个家庭每一位朋友都在你开始工作学习的第一天,就建立一个金融计划, 鼓励在人生中每一个里程碑重新评价和更新这个金融计划。我们着重于鼓励需要的朋友们建立一个有纪律性的积极的(反对前极的或者反应性)的金融计划。在这个计划中我们可以帮助在八大块儿中的每一块都建立强有力的,实在在的,有效的行事规则和方法来有效地管理个人和家庭的财务。

#### 退休计划的五个投资基本法则

- ◆早投 (Invest earlier)
- ❖分散 (Diversification)
- ❖定投 (Dollar cost averaging)
- ❖长期 (Time in the market not timing the market)
- ❖保本 (Downside protection)

#### 投资基本法则 - 早投 赶早不赶晚

Interest Problems are word problems that use formula for calculating Interests as well as future values:

- Simple Interest and future value
- Compound Interest and future value
- Continuously Compounded Interest and future value

In Finance, compounding is the process by which an asset's earnings, from either capital gains or interest, are reinvested to generate additional earnings over time.

#### Interest Formulas

#### Simple Interest Formula

#### I = Prt

I = Interest
P = Principal (Initial Value)
r = Interest Rate
t = time (years)

#### Continuously Compounded Interest

$$A = Pe^{rt}$$

A = Future Value
P = Principal (Initial Value)
r = Interest Rate
t = time

#### **Compound Interest Formula**

$$A = P\left(1 + \frac{r}{n}\right)^{nt}$$

A = Future Value
P = Principal (Initial Value)
r = Interest Rate
n = number of times
compounded in one "t"
t = time

- Simple interest is applied only to the principal and not any accumulated interest.
- Compound interest is interest accruing on the principal and previously applied interest.
- The effect of compound interest depends on how frequently it is applied.
- For bonds, the bond equivalent yield is the expected annual return.
- Continuously compounding returns scale over multiple periods.
- Interest compounding at its highest frequency is said to be compounding continuously.

### Simple Interest and Future Value

### Simple Interest Problem Example:

John wants to have an interest income of \$3,000 a year. How much must he invest for one year at 8%?

### Simple Interest Problem Example:

John wants to have an interest income of \$3,000 a year. How much must he invest for one year at 8%?

```
Step 1: Write down the formula I = prt
Step 2: Plug in the values 3000 = p \times 0.08 \times 1
3000 = 0.08p
p = 37,500
```

Answer: He must invest \$37,500

# Compound Interest and Future Value

## Current Deposit Rates for 08/26/2023 - 09/01/2023

#### **Savings Accounts:**

Annual Percentage Yields (APYs) and Interest Rates shown are offered on accounts accepted by the Bank and effective for the dates shown above, unless otherwise noted. Interest Rates are subject to change without notice. Interest is compounded daily and paid monthly. Interest is calculated and accrued daily based on the daily collected balances in the account. Accrued interest is considered to be earned and will be paid only when the total interest accrued reaches \$0.01 or more.

From https://www.wellsfargo.com/savings-cds/rates/

# Compound Interest Problem Example:

Scott wants to invest \$1000 for 1 year. At Bank A, his investment will collect 3% interest compounded daily while at Bank B, his investment will collect 3.50% interest compounded monthly. Which bank offers a better return? How much more will he receive by choosing that bank over the other?

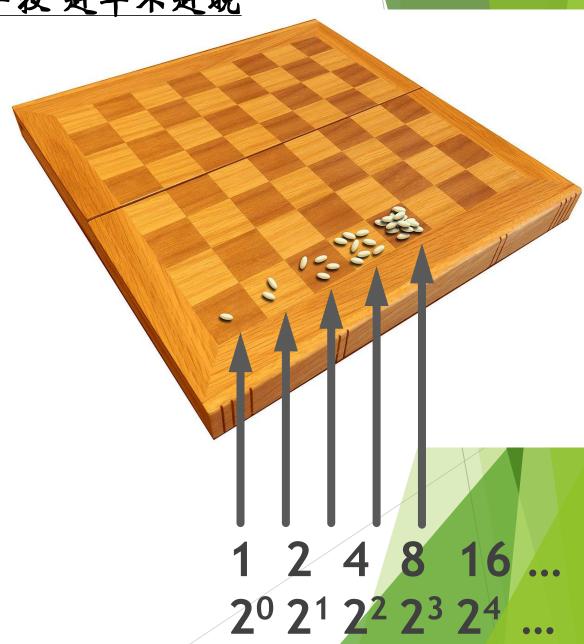
# Compound Interest Problem Example:

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Bank B, \$5.12

The inventor of chess (in some tellings Sessa, an ancient Indian Minister, year 1256) request his ruler give him wheat according to the wheat and chessboard problem. The ruler laughs it off as a meager prize for a brilliant invention, only to have court treasurers report the unexpectedly huge number of wheat grains would outstrip the ruler's resources.

投资基本法则 - 早投 赶早不赶晚



# Would you rather have a million dollars or a penny on day 1, doubled every day until day 30?

2<sup>30</sup>-1=1,073,741,823 Cents

Or: over 10 million dollars



Day 5 **2**<sup>5</sup>

Day 10 **2**<sup>10</sup>

Day 11.3 211.3

### What does a fish feel in the

the fish is totally happy: < 25% covered

> 25% covered

Seriously concerned: > 50% covered

Dead 100% covered

Day 1	Day 2	Day 3	Day 4	Day 5	Day 6	Day 7	Day 8	Day 9	Day 10	Day 11	Day 11 7 AM
				=)		=					××



An example of compounding working against us: COVID-19

# Exercise: Folding papers

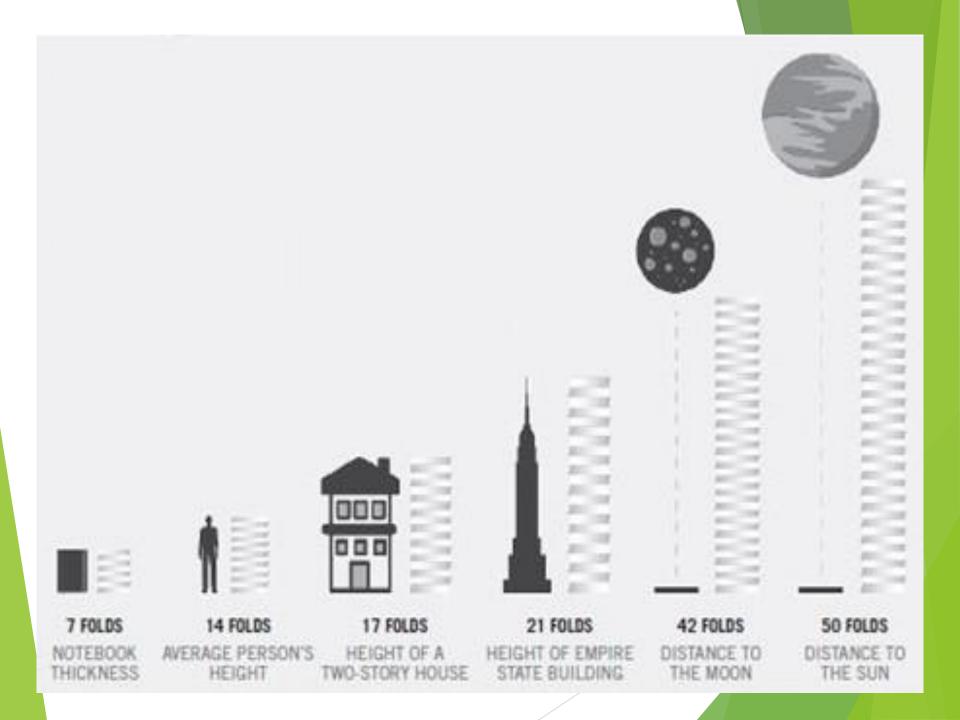
The thickness of a standard printing paper is about 0.1mm. Fold it once and it will be 0.2mm thick. If fold it again, it will be 0.4mm thick. Keeping folding it:

Times of Folding	The thickness of the Folded Paper
0	
1	
2	
7	
14	
21	
42	
50	

# Exercise: Folding papers

The thickness of a standard printing paper is about 0.1mm. Fold it once and it will be 0.2mm thick. If fold it again, it will be 0.4mm thick. Keeping folding it:

Times of Folding	The thickness of the Folded Paper	<b>2</b> ×
0	0.1mm	$0.1 \times 2^{0}$
1	0.2mm	$0.1 \times 2^{1}$
2	0.4mm	$0.1 \times 2^2$
7	128mm	$0.1 \times 2^7$
14	1638.4mm = 1.63m	0.1 x 2 <sup>14</sup>
21	209715.2mm = 2,097m	$0.1 \times 2^{21}$
42	4.4 x 10 <sup>10</sup> m	0.1 x 2 <sup>42</sup>
50	1.1 x 10 <sup>13</sup> m	$0.1 \times 2^{50}$



#### **Exercise:**

Calculate \$1's worth at age 65 if investing the \$1 at ages 20, 25, 30, 35, 40, 45, 50, 55

Starting Age of the \$1 Investment	Ending Age of the \$1 Investment	The Worth of \$1 Investment At Ending Age
20	65	
25	65	
30	65	
35	65	
40	65	
45	65	
50	65	
55	65	

Starting Age of the \$1 Investment	Ending Age of the \$1 Investment	The Worth of \$1 Investment At Ending Age
20	65	\$13.76
25	65	\$10.29
30	65	\$7.69
35	65	\$5.74
40	65	\$4.29
45	65	\$3.21
50	65	\$2.40
55	65	\$1.79

#### Start early / Make your retirement savings work hard for you



For illustrative purposes only. Assumes a 6% return.

# Have you started saving or investing?

## Compounding Problem:

John invested \$2,000 each year from year 2011 for first 8 years of a 40-year period with an annual compound rate of 10%. Kevin started to invest \$2,000 a year from 2019 with the same rate and he has planned to continue to do that until 2050. Who will earn more by the end of year 2050? By how much?

Year	Early Contribution	Funding Year-End Value	Late Contribution	Funding Year-End Value	Continu	al Funding Year-End Value
1	\$2,000	\$2,200	\$0	\$0	\$2,000	\$2,200
2	\$2,000	\$4,620	\$0	\$0	\$2,000	\$4,620
3	\$2,000	\$7,282	\$0	\$0	\$2,000	\$7,282
4	\$2,000	\$10,210	\$0	\$0	\$2,000	\$10,210
	\$2,000	\$13,431	\$0	\$0	\$2,000	\$13,431
6	\$2,000	\$16,974	\$0	\$0	\$2,000	\$16,974
5 6 7	\$2,000	\$20,871	\$0	\$0	\$2,000	\$20,871
	\$2,000	\$25,158	\$0	\$0	\$2,000	\$25,158
8	\$0	\$27,674	\$2,000	\$2,200	\$2,000	\$29,874
10	\$0	\$30,441	\$2,000	\$4,620	\$2,000	\$35,061
11	\$0	\$33,485	\$2,000	\$7,282	\$2,000	\$40,767
12	\$0	\$36,834	\$2,000	\$10,210	\$2,000	\$47,044
13	\$0	\$40,517	\$2,000	\$13,431	\$2,000	\$53,948
14	\$0	\$44,569	\$2,000	\$16,974	\$2,000	\$61,643
15	\$0	\$49,026	\$2,000	\$20,871	\$2,000	\$69,897
16	\$0	\$53,929	\$2,000	\$25,158	\$2,000	\$79,087
17	\$0	\$59,322	\$2,000	\$29,874	\$2,000	\$89,196
18	\$0	\$65,254	\$2,000	\$35,061	\$2,000	\$100,316
19	\$0	\$71,779	\$2,000	\$40,767	\$2,000	\$112,548
20	\$0	\$78,957	\$2,000	\$47,044	\$2,000	\$126,003
21	\$0	\$86,853	\$2,000	\$53,948	\$2,000	\$140,803
22	\$0	\$95,583	\$2,000	\$61,643	\$2,000	\$157,083
23	\$0	\$105,092	\$2,000	\$69,897	\$2,000	\$174,991
24	\$0	\$115,601	\$2,000	\$79,087	\$2,000	\$194,690
25	\$0	\$127,161	\$2,000	\$89,196	\$2,000	\$216,359
26	\$0	\$139,877	\$2,000	\$100,316	\$2,000	\$240,195
27	\$0	\$153,865	\$2,000	\$112,548	\$2,000	\$266,415
28	\$0	\$169,252	\$2,000	\$126,003	\$2,000	\$295,257
29	\$0	\$186,177	\$2,000	\$140,803	\$2,000	\$326,983
30	\$0	\$204,795	\$2,000	\$157,083	\$2,000	\$361,881
31	\$0	\$225,275	\$2,000	\$174,991	\$2,000	\$400,269
32	\$0	\$247,803	\$2,000	\$194,690	\$2,000	\$442,496
33	\$0	\$272,583	\$2,000	\$216,359	\$2,000	\$488,741
34	\$0	\$299,841	\$2,000	\$240,195	\$2,000	\$539,615
35	\$0	\$329,825	\$2,000	\$266,415	\$2,000	\$595,576
36	\$0	\$362,808	\$2,000	\$295,257	\$2,000	\$657,134
37	\$0	\$399,089	\$2,000	\$326,983	\$2,000	\$724,847
38	\$0	\$438,998	\$2,000	\$361,881	\$2,000	\$799,332
39	\$0	\$482,898	\$2,000	\$400,269	\$2,000	\$881,265
40	\$0	\$531,188	\$2,000	\$442,496	\$2,000	\$971,339
Investment		\$16,000		\$64,000	5.	\$80,000
Earnings	I	\$515.188		\$374,496		\$891,339

1       12000       13,200         2       12000       27,720         3       12000       43,692         4       12000       61,261         5       12000       80,587         6       12000       101,846         7       12000       125,231         8       12000       150,954         9       12000       179,249         10       12000       210,374         11       231,411       254,553         13       280,008         14       308,009         15       338,809         16       372,690         17       409,959         18       450,955         19       496,051         20       545,656         21       600,222         22       660,244         23       726,268         24       798,895         25       878,784         26       966,663         27       1,063,329         28       1,169,662         29       1,286,628			
2       12000       27,720         3       12000       43,692         4       12000       61,261         5       12000       80,587         6       12000       101,846         7       12000       125,231         8       12000       179,249         10       12000       210,374         11       231,411         12       254,553         13       280,008         14       308,009         15       338,809         16       372,690         17       409,959         18       450,955         19       496,051         20       545,656         21       600,222         22       660,244         23       726,268         24       798,895         25       878,784         26       966,663         27       1,063,329         28       1,169,662         29       1,286,628	Years	Principle	Deferred Growth
3       12000       43,692         4       12000       61,261         5       12000       101,846         7       12000       125,231         8       12000       150,954         9       12000       179,249         10       12000       210,374         11       231,411         12       254,553         13       280,008         14       308,009         15       338,809         16       372,690         17       409,959         18       450,955         19       496,051         20       545,656         21       600,222         22       660,244         23       726,268         24       798,895         25       878,784         26       966,663         27       1,063,329         28       1,169,662         29       1,286,628	1	12000	13,200
4       12000       61,261         5       12000       80,587         6       12000       101,846         7       12000       125,231         8       12000       150,954         9       12000       179,249         10       12000       210,374         11       231,411         12       254,553         13       280,008         14       308,009         15       338,809         16       372,690         17       409,959         18       450,955         19       496,051         20       545,656         21       600,222         22       660,244         23       726,268         24       798,895         25       878,784         26       966,663         27       1,063,329         28       1,169,662         29       1,286,628	2	12000	27,720
5       12000       80,587         6       12000       101,846         7       12000       125,231         8       12000       150,954         9       12000       179,249         10       12000       210,374         11       231,411         12       254,553         13       280,008         14       308,009         15       338,809         16       372,690         17       409,959         18       450,955         19       496,051         20       545,656         21       600,222         22       660,244         23       726,268         24       798,895         25       878,784         26       966,663         27       1,063,329         28       1,169,662         29       1,286,628	3	12000	43,692
6 12000 101,846 7 12000 125,231 8 12000 150,954 9 12000 179,249 10 12000 210,374 11 231,411 12 254,553 13 280,008 14 308,009 15 338,809 16 372,690 17 409,959 18 450,955 19 496,051 20 545,656 21 600,222 22 660,244 23 726,268 24 798,895 25 878,784 26 966,663 27 1,063,329 28 1,169,662 29 1,286,628	4	12000	61,261
7       12000       125,231         8       12000       150,954         9       12000       179,249         10       12000       210,374         11       231,411         12       254,553         13       280,008         14       308,009         15       338,809         16       372,690         17       409,959         18       450,955         19       496,051         20       545,656         21       600,222         22       660,244         23       726,268         24       798,895         25       878,784         26       966,663         27       1,063,329         28       1,169,662         29       1,286,628	5	12000	80,587
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10       12000       210,374         11       231,411         12       254,553         13       280,008         14       308,009         15       338,809         16       372,690         17       409,959         18       450,955         19       496,051         20       545,656         21       600,222         22       660,244         23       726,268         24       798,895         25       878,784         26       966,663         27       1,063,329         28       1,169,662         29       1,286,628	8	12000	150,954
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12       254,553         13       280,008         14       308,009         15       338,809         16       372,690         17       409,959         18       450,955         19       496,051         20       545,656         21       600,222         22       660,244         23       726,268         24       798,895         25       878,784         26       966,663         27       1,063,329         28       1,169,662         29       1,286,628	10	12000	210,374
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14       308,009         15       338,809         16       372,690         17       409,959         18       450,955         19       496,051         20       545,656         21       600,222         22       660,244         23       726,268         24       798,895         25       878,784         26       966,663         27       1,063,329         28       1,169,662         29       1,286,628	12		254,553
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16       372,690         17       409,959         18       450,955         19       496,051         20       545,656         21       600,222         22       660,244         23       726,268         24       798,895         25       878,784         26       966,663         27       1,063,329         28       1,169,662         29       1,286,628	14		308,009
17       409,959         18       450,955         19       496,051         20       545,656         21       600,222         22       660,244         23       726,268         24       798,895         25       878,784         26       966,663         27       1,063,329         28       1,169,662         29       1,286,628	15		338,809
18       450,955         19       496,051         20       545,656         21       600,222         22       660,244         23       726,268         24       798,895         25       878,784         26       966,663         27       1,063,329         28       1,169,662         29       1,286,628	16		372,690
19       496,051         20       545,656         21       600,222         22       660,244         23       726,268         24       798,895         25       878,784         26       966,663         27       1,063,329         28       1,169,662         29       1,286,628	17		409,959
20     545,656       21     600,222       22     660,244       23     726,268       24     798,895       25     878,784       26     966,663       27     1,063,329       28     1,169,662       29     1,286,628	18		450,955
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23       726,268         24       798,895         25       878,784         26       966,663         27       1,063,329         28       1,169,662         29       1,286,628	21		600,222
24     798,895       25     878,784       26     966,663       27     1,063,329       28     1,169,662       29     1,286,628	22		660,244
25 878,784 26 966,663 27 1,063,329 28 1,169,662 29 1,286,628	23		726,268
26     966,663       27     1,063,329       28     1,169,662       29     1,286,628	24		798,895
27     1,063,329       28     1,169,662       29     1,286,628	25		878,784
28 1,169,662 29 1,286,628	26		966,663
29 1,286,628	27		1,063,329
	28		1,169,662
4 445 004	29		1,286,628
30 1,415,291	30		1,415,291

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Years	Principle	Deferred Growth
1	12000	13,200
2	12000	27,720
3	12000	43,692
4	12000	61,261
5	12000	80,587
6	12000	101,846
7	12000	125,231
8	12000	150,954
9	12000	179,249
10	12000	210,374
11	12000	244,611
12	12000	282,273
13	12000	323,700
14	12000	369,270
15	12000	419,397
16	12000	474,536
17	12000	535,190
18	12000	601,909
19	12000	675,300
20	12000	756,030
21		831,633
22		914,796
23		1,006,276
24		1,106,904
25		1,217,594
26		1,339,353
27		1,473,289
28		1,620,617
29		1,782,679
30		1,960,947

Years	Principle	Deferred Growth
1	12000	13,200
2	12000	27,720
3	12000	43,692
4	12000	61,261
5	12000	80,587
6	12000	101,846
7	12000	125,231
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17	12000	535,190
18	12000	601,909
19	12000	675,300
20	12000	756,030
21	12000	844,833
22	12000	942,516
23	12000	1,049,968
24	12000	1,168,165
25	12000	1,298,181
26	12000	1,441,199
27	12000	1,598,519
28	12000	1,771,571
29	12000	1,961,928
30	12000	2,171,321

# When to start investing matters!!!

纯利润

第一个十年: \$1,295,291

第二个十年: \$425,656

第三个十年: \$90,374

Assumptions: Same annual return of 10% (not guaranteed)

My wealth has come from a combination of living in America, some lucky genes, and compound interest.

Warren Buffett – The Giving Pledge, 2010. www.givingpledge.org

Years	Principle	Deferred Growth	
1	12000	13,200	
2	12000	27,720	
3	12000	43,692	
4	12000	61,261	
5	12000	80,587	
6	12000	101,846	
7	12000	125,231	
8	12000	150,954	
9	12000	179,249	
10	12000	210,374	
11		231,411	
	allowing only low annual		

contributions

Only saving low amount yearly

18	450,955
19	496,051
20	545,656
21	600,222
22	660,244
23	726,268
24	798,895
25	878,784
26	966,663
27	1,063,329
28	1,169,662
29	1,286,628
30	1,415,291

Years	Principle	Deferred Growth
1	40000	44,000
2	40000	92,400
3	40000	145,640
4		160,204
5		176,224
6		193,847
7		213,232
8		234,555
9		258,010
10		283,811
11		312,192

#### Accounts allowing only high annual contributions

#### Saving in higher amount vearly

	<u>amoun</u>	<u>L VEALLY</u>
18		608,374
19		669,212
20		736,133
21		809,746
22		890,721
23		979,793
24		1,077,772
25		1,185,550
26		1,304,105
27		1,434,515
28		1,577,967
29		1,735,763
30		1,909,340

The amount of initial investment matters!!!

Assumptions: Same total principle \$120K, Same annual return of 10% (not guaranteed) With compounding, how many years would it take for your money to double?

## Rule of 72

•Divide 72 by the interest rate to estimate the number of years it takes for your money to double.

$$FV = PV \cdot (1+i)^{n}$$

$$4\% \quad Age \quad 6\% \quad Age \quad 8\% \quad Age \quad 12\%$$

$$29 \quad \$10,000 \quad 29 \quad \$10,000 \quad 35 \quad \$10,000 \quad 47 \quad \$20,000 \quad 41 \quad \$20,000 \quad 47 \quad \$40,000 \quad 47 \quad \$40,000 \quad 53 \quad \$80,000 \quad 65 \quad \$80,000 \quad 65 \quad \$160,000 \quad 65 \quad \$220,000 \quad 65 \quad \$220,000 \quad 65 \quad \$220,000 \quad 65 \quad 8220,000 \quad 820,000 \quad 820,$$

<sup>\*</sup> All figures are for illustrative purposes only and do not reflect an actual investment in any product. They do not reflect the performance risks, expenses or charges associated with any actual investment. Past performance is not an indication of future performance. The Rule of 72 is a mathematical concept that approximates the number of years it would take to double the principal at a constant rate of return. The performance of investments fluctuates over time, and as a result, the actual time it will take an investment to double in value cannot be predicted with any certainty. Additionally, there are no guarantees that any investment or savings program can out-pace inflation.

## Rule of 72

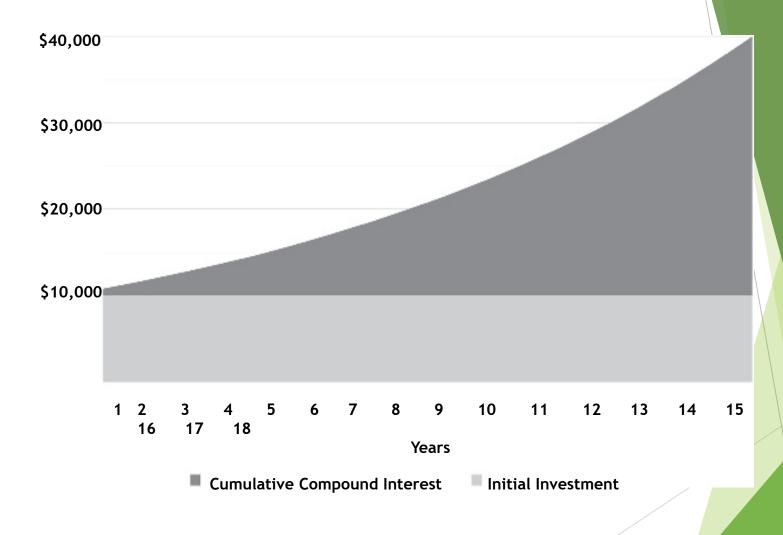
•Divide 72 by the interest rate to estimate the number of years it takes for your money to double.

<sup>\*</sup> All figures are for illustrative purposes only and do not reflect an actual investment in any product. They do not reflect the performance risks, expenses or charges associated with any actual investment. Past performance is not an indication of future performance. The Rule of 72 is a mathematical concept that approximates the number of years it would take to double the principal at a constant rate of return. The performance of investments fluctuates over time, and as a result, the actual time it will take an investment to double in value cannot be predicted with any certainty. Additionally, there are no guarantees that any investment or savings program can out-pace inflation.

## "The Rule of 72":

Simply assume a reasonable rate of return for planning purposes (between 7 percent and 9 percent over a multidecade time period) and divide 72 by that rate. This calculates the period of time it would take for your money to double.

Note: The Rule of 72 is an approximation. The equation is  $2 = 1 \times (1 + Rate of Return)^{Y}$ , where Y is the time to double.



GROWTH OF \$10,000 INVESTMENT WITH AN 8 PERCENT RETURN: IN I T I A L
INVESTMENT VERSUS CUMULATI V E COMPOUND I NTEREST

Warren Buffett says, "Life is like a snowball. The important thing is finding wet snow and a long hill":

- The wet snow is the interest you reinvest to pick up even more interest as you roll along.
- The long hill is the multiple decades you give yourself if you start saving early.

The formula for compound interest is:

$$A = P (1 + r/n)^{nt}$$

#### Where:

A = the future value of the investment/loan, including interest

P = the principal investment amount (the initial deposit or loan amount)

r = the annual interest rate or return

n = the number of times that interest is compounded per unit t

t = the time the money is invested or borrowed for



# Compounding Summary

- \* T, when to invest matters.
- P, the amount of initial investment matters.
- \* R, the interest or return rate matters.



# Compounding Summary

- It could be your BEST friend (wealth/business)
- It could be your WORST enemy (tax/COVID)
- Compounding Power comes at late stage
- How to manage life/study/investment?
- Understand its power and make use of it
- Success is not far away

# 投资基本法则 - 分散

\$100.000

## 投资基本法则 - 分散



#### Investment is compounded for 25 years

The hypothetical rates of returns shown are assumed on a \$100,000 investment compounded for 25 years. These figures are for illustrative purposes only and do not represent the past for future performance of any actival investments. Sources: Stocks, Bonds, Bills, and Inflation 1999 Yearbook, Ibbotson Associates, Inc., Based on copyright works by Ibbotson and Singuefield. All rights reserved. There's no assurance that a diversified portfolio will achieve a better return than a

#### 投资基本法则 - 分散



The hypothetical rates of returns shown are assumed on a \$100,000 investment compounded for 25 years. These figures are for illustrative purposes only and do not represent the past or future performance of any actual investments. Sources: Stocks, Blands, Bills, and Inflation 1997 (earbook, Ibbotson Associates, Inc., Based on conviction works by Ibbotson and Singuistical, All included the return than a conviction of the past of the pas

### 资产种类分散

																2008	- 2022
2008	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018	2019	2020	2021	2022	YTD	Ann.	Vol.
Fixed		RSITe	RETA	RETE	Secali		REITE	Secol	EM	Cash	Large	Sex add		Com dty	Large	Large	RESTR
Income 5.2%	Equity	27.9%	83%	19.7%	Cap 38.6%	28.0%	2.6%	21.3%	Equity	1.8%	Cap 31.5%	Cap 20.0%		16,1%	Cap 18.4%	Cap 8.8%	23.4%
9.2%	79.0%		- Industrial		Name and Address of the Owner, where the Owner, which is the	100000	The same of the sa	and the last of		- Contract	31.5%			10,179	Name and Address of the Owner, where the Owner, which the	100000000000000000000000000000000000000	
Cash	High Yield	Small	Fixed Income	High Yield	Large	Cap	Cao	High	Equity	Fixed Income	PERTS	Equity 1	Cap	Cash	DM Equity	Cap	Small Cap
1.8%	59.4%	26.9%	7.8%	19.6%	32.4%	13.7%	1.4%	14.3%	25.8%	0.0%	28.7%	18.7%	28.7%	1.5%	10.8%	7.2%	23.2%
Asset	DM	BA	High	EM .	CMI	Fixed	Fixed	Large	Large		Sim all	Large	Name of the last	Hgh	Small		BM .
Alloc.	Equity		Yield		Equity	Incom e	Incom e	Сар	Сар	RETS	Cap	Cap	Comdty.	Yield	Cap		
-25,4%	32.5%		3.1%		23.3%	6.0%	0.5%	12.0%	21.8%		25.5%	18.4%	27.1%	-12.7%	8.7%		
Hgh	RETS	Com dty.	Large	DM	Asset	Asset	Cash	Com dty.	Sm all	High	DM	Asset	Small	Fixed	Asset	Asset	Comdty.
Yield		Com aty.	Cap	Equity	Allgo.	Allec.		Com aty.	Cap	Yield	Equity	Affec.	Cap	Incom e	Alloc.	Alloc.	Comaty.
-26.95	25.0%	16.8%	2.1%	17.9%	14/9%	5.2%	0.0%	11.8%	14,6%	4.1%	22.7%	10.6%	14.8%	-13.0%	8.1%	6.1%	20.2%
5m all	Small	Large	Cash	Sm all	#gh	Small	DM	EM	Asset	Large	Asset	DM	Asset	Asset	High	High	DM
Cap	Сар	Cep		Cep	Yield	Cep	Equity		Allon	Cap	Alloc.	Equity	Alloc.	Alfoc.	Yield	Yield	Equity
-53.8%	27.2%	15.1%	0.1%	16.3%	7.3%	4.9%	-0.4%	111,6%	14.6%	-14%	19.5%	8.3%	13.5%	-13.9%	6.5%	5,4%	29.0%
Com dty.	Large	High	Asset	Large	REITA	Cash	Apset	REITS	High	Alloc.	1000	Fixed	DM	DM		Fixed	Large
-35.6%	Cap 16.5%	Yield 14.8%	0.7%	Cap 16.0%	2.9%	0.0%	Allec.	1.05	Yield 10.4%	-5.8%	10.9%	7.5%	Equity 11.8%	-14.0%	Equity	income 2.7%	Cap 17.7%
					237				10.4	-	COAS-SAC		-		1000	DM	
Cap	Alloc.	Allec.	Sm all Cap	ANGC.	Cash	High Yield	High Yield	Asset	REITS	Cap	High Yield	High Yield	Yield	Large Cap	Cash	Equity	High Yield
-37.0%	25.0%	13.3%	42%	12.2%	0.016	0.0%	-2.7%	8.3%	8.7%	-11.0%	12.6%	7.0%	1.0%	-18.1%	3.2%	2.5%	13.0%
	-	DM	CM	Fixed	Fixed	TM	Sm all	Fixed	Fixed	Annual Vision	Fixed			22		EM	Asset
RETH	Com dty.	Equity	Equity	Incom e	Income	Equity	Cep	Income	Income	Comdty.	Income	Cash	Cash	Equity			Alloc.
-37.7%	18.9%	9.2%	-11.7%	4.2%	-2.0%	1.8%	4.4%	2.6%	3.5%	-11.2%	8.7%	0.5%	0.0%	-10.7%			12.4%
DM	Fixed	Fixed	Com dty.	Cash	EM	DM	EM	DM	Com dty.	DM	Com dty.	Com dty.	Fixed	Sm all	Fixed	Cash	Fixed
Equity	Incom e	Income	Description of	R to the last	Equity	Equity		Equity		Equity		Comitaty.	Income	Cap	Income	Section .	Incom e
-45,1%	5.9%	6.5%	-13.3%	0.1%	-23%	-4.5%	-14.6%	1.5%	1.7%	-13.4%	7.7%	-3.1%	-1.5%	-20.4%	1.3%	0.6%	4.2%
224	Cash	Cash		Com dty.	Com dty.	Comdty.	Com dty.	Cash	Cash		Cash			RESTA	Comdty.	Com dty.	Cash
Equity								A 200	A 000		2.00						0.000
-53.2%	0.1%	0.1%	48.2%	-1.1%	-9.5%	-17.0%	-24.7%	0.3%	0.8%	-14.2%	2.2%	4.1%	-22%	-24.9%	-3.0%	-2.6%	0.4%

Source: Bloomberg, FactSet, MSCI, NAREIT, Russell, Standard & Poor's, J.P. Morgan Asset Management.

Source: Bloomberg, Exciset, MSCI, NARCIT, Russell, Standard & Poor's, J.P. Morgan Asset Management. Large cap: SAP 500, Small cap: Russell 2000, EM Equity: MSCI EAFE, EM Equity: MSCI EAFE, Comdry, Bloomberg Commodity Index, High Yield: Bloomberg Global HY Index, Fixed Income: Bloomberg US Aggregate, REITs: NAREIT Equity REIT Index, Cash: Bloomberg 1-3m Treasury. The "Asset Allocation" portfolio assumes the following weights: 25% in the SSP 500, 10% in the Russell 2000, 15% in the MSCI EAFE, 5% in the MSCI EME, 25% in the Bloomberg Global High Yield Index, 5% in the Bloomberg Global High Yield Index purposes only. Past performance is not indicative of future returns.

Guide to the Markets - U.S. Data are as of August 29, 2023.

J.P.Morgan ASSET MANAGEMENT

## 投资基本法则 - 定投

Dollar-cost averaging is a mathematical concept for periodic investing based on a long-term fluctuating market. Dollar-cost averaging does not assure a profit and does not protect against a loss in declining markets. Because of fluctuating prices, investors should consider their ability to continue purchases through periods of both high and low price levels. These are hypothetical examples for illustrative purposes only, and do not reflect the actual investment in any product.

#### Dollar-cost averaging in a rising market

- Assumes an investment of
- Accumulated units
- Average Share Price
- Liquidation value

\$200 per month

85

\$15.00

#### Dollar-cost averaging in a fluctuating market

- Assumes an investment of
- Accumulated units
- Average Share Price
- Liquidation value

\$200 per month

170

\$7.67



#### Dollar-cost averaging in a declining market

- Assumes an investment of
- Accumulated units
- Average Share Price
- Liquidation value

\$200 per month 535

\$4.83

\$4.65



## 投资基本法则-定投

Dollar-cost averaging is a mathematical concept for periodic investing based on a long-term fluctuating market. Dollar-cost averaging does not assure a profit and does not protect against a loss in declining markets. Because of fluctuating prices, investors should consider their ability to continue purchases through periods of both high and low price levels. These are hypothetical examples for illustrative purposes only, and do not reflect the actual investment in

#### Dollar-cost averaging in a rising market

Assumes an investment of

Accumulated units

Average Share Price

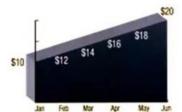
Liquidation value

\$200 per month

85

\$15.00

\$1,700 (85 x \$20)



#### Dollar-cost averaging in a fluctuating market

Assumes an investment of

Accumulated units

Average Share Price

Liquidation value

\$200 per month

170 \$7.67

535

\$4.83

\$1,700 (170 x \$10)



#### Dollar-cost averaging in a declining market \$200 per month

Assumes an investment of

Accumulated units

Average Share Price

Liquidation value

\$2,140 (535 x \$4)



# 投资基本法则 - 定投

Month	Y	Market	<b>Principle</b>	Shares	Cash Value
0	0.00	10.0	1000	100	
1	1.50	11.5	1000	87	20.0
2	2.60	12.6	1000	79	18.0
3	3.00	13.0	1000	77	16.0
4	2.60	12.6	1000	79	
5	1.50	11.5	1000	87	14.0
6	0.00	10.0	1000	100	9 12.0 7 10.0
7	-1.50	8.5	1000	118	<b>10.0</b>
8	-2.60	7.4	1000	135	8.0 But 10.0
9	-3.00	7.0	1000	143	6.0
10	-2.60	7.4	1000	135	4.0
11	-1.50	8.5	1000	118	
12	0.00	10.0	1000	100	2.0
					0.0
	Degree c	of	Total	Ending	0 5 10 15 Month
F	Fluctuatio	on	Principle	Value	Monut
	3		13000	13579	

# 投资基本法则 - 定投

Month	Y	Market	<b>Principle</b>	Shares	Cash Value	
0	0.00	10.0	1000	100		
1	3.00	13.0	1000	77	20.0	
2	5.20	15.2	1000	66	18.0	
3	6.00	16.0	1000	63	16.0	
4	5.20	15.2	1000	66	*	
5	3.00	13.0	1000	77	14.0	
6	0.00	10.0	1000	100	12.0 10.0 8.0	
7	-3.00	7.0	1000	143	₹ 10.0	
8	-5.20	4.8	1000	208	¥ 8.0	
9	-6.00	4.0	1000	250	6.0	
10	-5.20	4.8	1000	208	4.0	
11	-3.00	7.0	1000	143	X1693	
12	0.00	10.0	1000	100	2.0	
					0.0	
1	Degree o	of	Total	Ending	0 5 10 Month	15
F	Fluctuation	on	Principle	Value	Month	
	6		13000	16000		

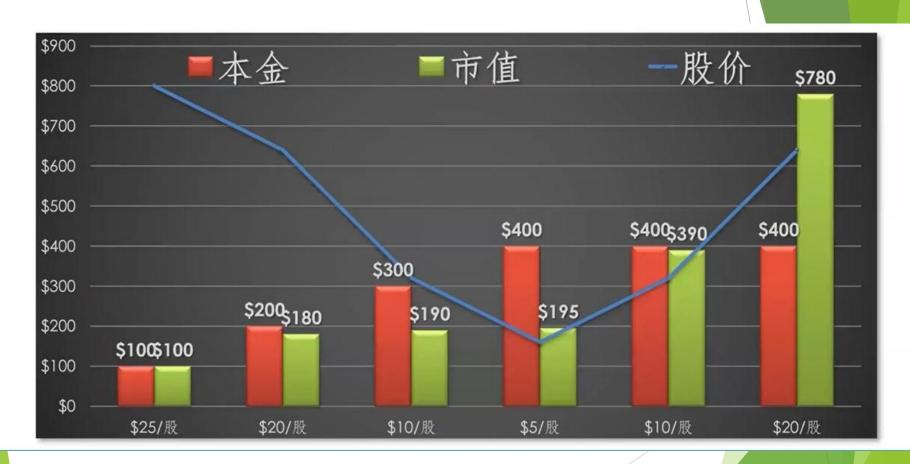
## 投资基本法则-定投

Month	Y	Market	<b>Principle</b>	Shares	Cash Value
0	0.00	10.0	1000	100	
1	4.50	14.5	1000	69	20.0
2	7.79	17.8	1000	56	18.0
3	9.00	19.0	1000	53	16.0
4	7.79	17.8	1000	56	
5	4.50	14.5	1000	69	14.0
6	0.00	10.0	1000	100	12.0 And 10.0 8.0 8.0
7	-4.50	5.5	1000	182	\$ 10.0
8	-7.79	2.2	1000	453	8.0
9	-9.00	1.0	1000	1000	6.0
10	-7.79	2.2	1000	453	4.0
11	-4.50	5.5	1000	182	
12	0.00	10.0	1000	100	2.0
					0.0
Γ	Degree c	of	Total	Ending	0 5 10 15 Month
F	Fluctuatio	on	Principle	Value	Month
	9		13000	28733	

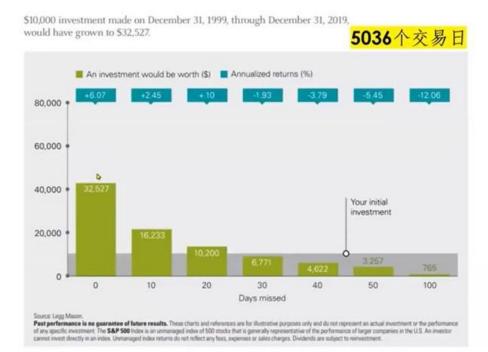
## 投资基本法则-定投



## 投资基本法则 - 定投



## 投资基本法则-长期



### 投资基本法则-长期



#### Best Days Come Near the Worst

Despite 2008 being in the center of the Great Recession, it had 8 of the 20 best price return days for the S&P 500 since 1928.

September 2008							
1	2	3	4	5			
8	9	10	11	12			
15	16	17	18	19			
22	23	24	25	26			
29	30						

		1	2	3
6	7	8	9	10
13	14	15	16	17
20	21	22	23	24
27	28	29	30	31

12%	
5% -5%	
000	

November 2008								
3	4	5	6	7				
10	11	12	13	14				
17	18	19	20	21				
24	25	26	27	28				

December 2008							
1	2	3	4	5			
8	9	10	11	12			
15	16	17	18	19			
22	23	24	25	26			
29	30	31					

## 投资基本法则-长期

Worst-d	ay investments (mar	ket highs)	Best-day investments (market lows)			
Date of market high	Cumulative investment <sup>2</sup>	Value on 12/31	Date of market low	Cumulative investment <sup>2</sup>	Value on 12/31	
5/21/01	\$10,000	\$9,229	9/21/01	\$10,000	\$11,409	
3/19/02	20,000	16,174	10/9/02	20,000	21,119	
12/31/03	30,000	30,457	3/11/03	30,000	40,492	
12/28/04	40,000	43,478	10/25/04	40,000	55,440	
3/4/05	50,000	57,060	4/20/05	50,000	70,546	
12/27/06	60,000	76,227	1/20/06	60,000	93,355	
10/9/07	70,000	90,340	3/5/07	70,000	109,934	
5/2/08	80,000	65,874	11/20/08	80,000	83,667	
12/30/09	90,000	93,888	3/9/09	90,000	122,620	
12/29/10	100,000	114,261	7/2/10	100,000	148,368	
4/29/11	110,000	121,690	10/3/11	110,000	157,459	
10/5/12	120,000	150,966	6/4/12	120,000	193,845	
12/31/13	130,000	210,342	1/8/13	130,000	270,244	
12/26/14	140,000	246,073	2/3/14	140,000	315,325	
5/19/15	150,000	252,422	8/25/15	150,000	322,095	
12/20/16	160,000	299,700	2/11/16	160,000	382,335	
12/28/17	170,000	369,376	1/19/17	170,000	470,271	
10/3/18	180,000	354,813	12/24/18	180,000	451,216	
12/27/19	190,000	452,496	1/3/19	190,000	575,506	
12/31/20	200,000	529,276	3/23/20	200,000	676,524	

Every year, for the past 20 years, he's invested \$10,000 in ICA

## 投资基本法则-长期

Date	Action	Symbol	Quantity	Price	Amount
4/3/2025	1	BAC	500		
4/4/2025	· '	BAC	1,000		
4/8/2025	<u> </u>	BAC	500		
4/8/2025		BAC	500		
4/8/2025		BAC	1,000		
4/9/2025		BAC	499		
4/9/2025		BAC	1	\$37.42	
4/9/2025	Sell	BAC	500	\$37.19	\$18,594.40
4/9/2025	Sell	BAC	500	\$36.27	\$18,131.92
4/9/2025	Buy	BAC	500	\$33.45	(\$16,722.50)
4/10/2025	Sell	ВАС	500	\$35.71	\$17,854.66
4/10/2025	Sell	BAC	500	\$35.24	\$17,619.48
4/10/2025	Buy	ВАС	500	\$34.78	(\$17,387.50)
4/10/2025	Buy	ВАС	500	\$35.10	(\$17,549.05)
4/10/2025	Buy	ВАС	500	\$35.60	(\$17,798.97
4/14/2025	Sell	BAC	500	\$36.78	\$18,389.41
4/15/2025	Sell	ВАС	500	\$38.35	\$19,174.39
4/16/2025	Buy	ВАС	500	\$37.00	(\$18,500.00)
4/16/2025	Buy	ВАС	500	\$37.33	(\$18,664.95
4/17/2025	Sell	ВАС	500	\$37.75	\$18,876.20
4/21/2025	Buy	BAC	500	\$36.86	(\$18,428.15)
4/22/2025	Sell	ВАС	500	\$38.12	\$19,060.84
4/22/2025	Sell	ВАС	500	\$37.94	\$18,966.89
Total					\$9,039.00
				87130	10.37%

#### 投资基本法则-长期



#### 投资基本法则-长期



#### 退休计划的五个投资基本法则

- ◆早投 (Invest earlier) --- by compounding rules, 尽可能多投
- ❖分散 (Diversification)
- ◆定投 (Dollar cost averaging) --- not timing the market
- ❖长期 (Time in the market not timing the market) --- 不随市场变化
- ◆保本 (Downside protection)

9:51





Account overview

Balance >

\$1,855,293.36

As of 5/17/2025

Rate of return >

+14.87% (Annualized)

5/17/2022 to 5/17/2025

- Started from June 2004
- ❖ To 2012, invested full amount allowed + employer match
- From 2012 to 2023, invested \$15,000 annually + employer match

#### Formula:

$$P = d * ((1 + r/k)^{(Nk)} - 1) / (r/k)$$

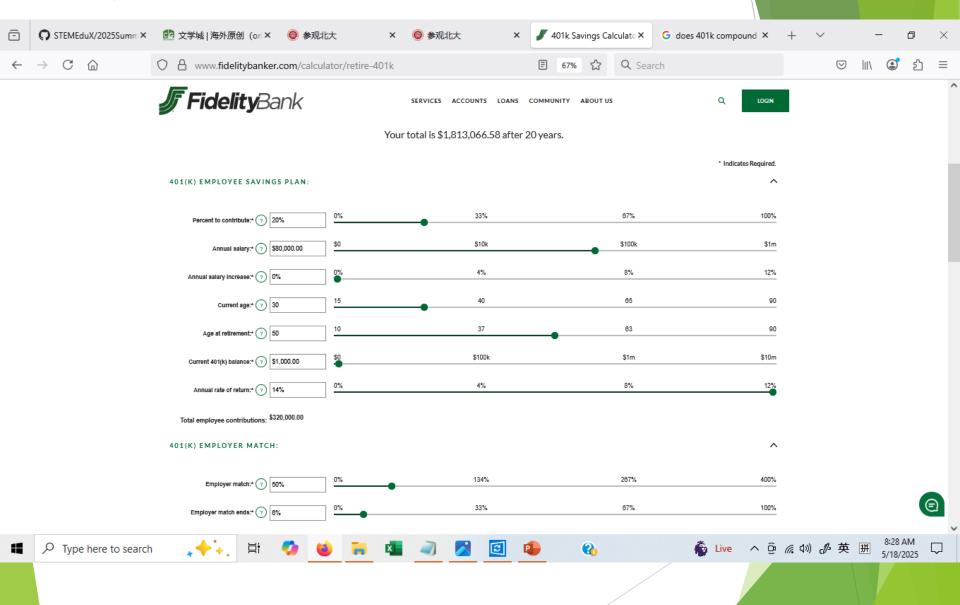
Where: P = Final balance after N years, d = Regular contribution (annual), r = Annual interest rate, k = Number of compounding periods per year, and N = Number of years.

### Example:

Let's say you contribute \$5,000 annually, expect an 8% annual return, and plan to invest for 20 years. Assuming annual compounding (k=1):

 $P = 5000 * ((1 + 0.08)^20 - 1) / 0.08$  $P \approx $327,331.70$ 

https://www.fidelitybanker.com/calculator/retire-401k



Year	Employee Contribution	Employer Contribution	Total Contribution	Catch Up Contribution (Age 50+)		
2024	\$23,000	\$46,000	\$69,000	\$7,500		
2023	\$22,500	\$43,500	\$66,000	\$7,500		
2022	\$20,500	\$40,500	\$61,000	\$6,500		
2021	\$19,500	\$38,500	\$58,000	\$6,500		
2020	\$19,500	\$37,500	\$57,000	\$6,500		
2019	\$19,000	\$37,000	\$56,000	\$6,000		
2018	\$18,500	\$36,500	\$55,000	\$6,000		
2017	\$18,000	\$36,000	\$54,000	\$6,000		
2016	\$18,000	\$35,000	\$53,000	\$6,000		
2015	\$18,000	\$35,000	\$53,000	\$5,500		
2014	\$17,500	\$34,500	\$52,000	\$5,500		
2013	\$17,000	\$34,000	\$51,000	\$5,500		
2012	\$17,000	\$33,000	\$50,000	\$5,500		
2011 - 2009	\$16,500	\$32,500	\$49,000	\$5,500		
2008	\$15,500	\$30,500	\$46,000	\$5,000		
2007	\$15,500	\$29,500	\$45,000	\$5,000		
2006	\$15,000	\$29,000	\$44,000	\$5,000		
2005	\$14,000	\$28,000	\$42,000	\$4,000		
2004	\$13,000	\$28,000	\$41,000	\$3,000		

Calendar Year	DB 415(b)(1)(A)	DC 415(c)(1)(A)	Maximum Deferral						Highly Compensated Definition Limits Under IRC 414(q)	Annust Comp Lim <b>i</b> t	Taxable	
			401(k) & 402(g)(1)	Over 50 Catch-up Contribution	60-63 Catch-up Contribution	403(b)	SIMPLE	SIMPLE Over 50 Catch-up Contribution	457	(1)(8)	401(a)(17), 404(l), 408(k)(3)(C)	Wage Base
2025	280,000	70,000	23,500	7,500	11,250	23,500	16,500	3,500	23,500	160,000	350,000	176,600
2024	275,000	69,000	23,000	7,500	n/a	23,000	16,000	3,500	23,000	155,000	345,000	168,600
2023	265,000	66,000	22,500	7,500	n/a	22,500	15,500	3,500	22,500	150,000	330,000	160,200
2022	245,000	61,000	20,500	6,500	n/a	20,500	14,000	3,000	20,500	135,000	305,000	147,000
2021	230,000	58,000	19,500	6,500	n/a	19,500	13,500	3,000	19,500	130,000	290,000	142,800
2020	230,000	57,000	19,500	6,500	n/a	19,500	13,500	3,000	19,500	130,000	285,000	137,700
2019	225,000	56,000	19,000	6,000	n/a	19,000	13,000	3,000	19,000	125,000	280,000	132,900
2018	220,000	55,000	18,500	6,000	n/a	18,500	12,500	3,000	18,500	120,000	275,000	128,400

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Account overview

Balance >

\$1,855,293.36

As of 5/17/2025

Rate of return >

+14.87% (Annualized)

5/17/2022 to 5/17/2025

- Started from June 2004
- ❖ To 2012, invested full amount allowed + employer match
- From 2012 to 2023, invested \$15,000 annually + employer match

- ❖401K投资与家庭住房MORTGAGE投资的 关系
- ❖401K投资与股票投资的关系
- ❖401K投资与其它如房地产投资的关系
- ❖小企业,餐馆,个人企业LLC如何制定退 休计划

# 我们的办公室



哥伦比亚, 马里兰



兰辛,密歇根



盖城, 马里兰



都柏林, 俄亥俄



达拉斯, 德州



泰森, 弗吉尼亚



尔湾, 加州



迈阿密, 佛罗里达



底特律, 密歇根



明尼唐卡, 明尼苏达

# 您的三大福利

#### 1. 免费家庭全盘财务和税务规划分析

- · 理清财务状况, 发现规划盲区
- ・ 从六个方面(风险控制, 税务规划, 家庭保护, 子女教育, 退休养老, 财富传承) 给出具体建议

#### 2. 注册成我们的学员(\$125注册费)

- · 终身免费的财商教育,分享理财师内部资料,系统的学习如何做好家庭财务规划
- · 终身免费财务咨询, 共享团队理财师, 税务师, 律师资源
- 需要实名注册,无犯罪破产记录

#### 3. 加入北极星团队

- ・世界500强金融服务平台支持,全牌照,独立理财师支持
- · 时间投入灵活,可兼职开始
- 共同普及财商知识,服务广大中产阶级

# Q&A?

