```
clear;
clc;
m=500; % Number of observations, feel free to change around
n=5; % Number of features, feel free to change around
Feature scaling = 1; % 0 for NO feature scaling, 1 for feature scaling
% Fixed offset (random), scaling the cofficients by 10, feel free to change
beta0=10*rand():
% Coefficients of functional relationship, randomly generated
beta coeff = 10*rand(n,1); % Scaling the cofficients by 10, feel free to change
% Random initiation of x-matrix (m observations with n features);
x multiplier = 20;
x = x multiplier*rand(m,n);
% Magnitudes of scaled x-matrix affect the convergence of algorithm
% Feature scaling may have to be enabled for large x-multipler
if (Feature scaling==1)
    x = x/\max(\max(x));
end;
```

```
\% Functional relationship between y and x; \% The exact exponents of x's are randomly generated i.e. p is a random variable \% Random noise added to the y vector;
```

$$y = \beta_0 + \sum_{i=1}^n \beta_i x_i^p + \varepsilon$$
 (noise)

```
y = beta0+(x.^{(0.8+0.9*rand()))*beta_coeff+10*rand();
```

```
% Define X and theta (linear regression coefficient) vectors;
% X is just x matrix appended with a first column of 1's for gradient descient run;
% Theta is (n+1) vector with a theta0 at the beginning
X = [ones(m,1) x];
theta = zeros(n+1,1);
```

```
% Number of iterations for Gradient Descent and 'Learning Rate'
num_iter = 10000; % Feel free to experiment with this number
alpha = 0.01; % Feel free to experiment with this rate
J_history = zeros(num_iter,1); % Error vector initialization;
```

```
% GradientDescent loop (and computing the cost function)
%-----
for i = 1:num_iter
    h = X*theta; % Hypothesis function, inner product of X and theta;
    er = h-y; % error (difference of hypothesis and actual observation);
    er_sqr = er.^2; % error squared
```

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^{2}$$

 $J = (1/(2*m))*sum(er_sqr); % mean-squared-error (with a 1/2 factor)$

$$\theta_j := \theta_j - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}). x_j^{(i)}$$

```
% Partial derivative of J(theta) with respect to theta
theta_change = (alpha/m)*(X'*(h-y));
theta = theta-theta_change; % Update theta vector

%Book-keeping of errors for plotting
iter = i;
J_history(iter) = J;
end;
```

```
% Generate predicted values from the final theta vector and compute R^2-statistic y_hat = theta(1)+x*(theta(2:n+1));

SSE = sum((y-y_hat).^2);

SSTO = sum((y-mean(y)).^2);

r_squared = 1 - (SSE/SSTO);
```

```
% Result and comparison
beta0; % Actual functional offset
beta_coeff; % Actual functional coefficients
theta; % Final linear regression coefficients
J_history(num_iter-1); % Show the last element of the MSE vector
regression_coeff = theta(2:n+1);
% Table of actual functional coefficients and regression coefficients, side-by-side
t_coeff = table(beta_coeff, regression_coeff);
```

```
% Plots (this section will be totally commented out)
%----
% Scatter plot of y-actual and y-predicted;
% works for x-dimensions > 1 since it will not be possible
% to plot standard x-y scatter and linear regression line for x > 1 dimension
%scatter (1:length(x),y); hold on; scatter(1:length(x),y_hat, 'filled');
%hold off;
%hist(y-y_hat,50); % Residuals histogram, adjust number of bins for a decent plot
%scatter(x,y); hold on; plot(x, y_hat); % this is for 1-dimensional x vector only
```