

Name: \_\_\_\_\_

Student ID: \_\_\_\_\_

- Please avoid all unethical behaviors (e.g., looking at others' solutions, asking others), as this will result in a grade of zero in the quiz.
- The exam is worth 12 points (which would be later 8% of the final grade), and total duration of the exam is 10 minutes.

1. **True/False (6 points)** Write "T" if True and "F" if False.

- (a) (1 point) \_\_\_\_ **F** \_\_\_\_ Population is a subset of the sample and we do inference for the sample quantities.
- (b) (1 point) \_\_\_\_ **T** \_\_\_\_ The value of the estimator will change from sample to sample.
- (c) (1 point) \_\_\_\_ **F** \_\_\_\_ For a continuous random variable we can calculate the probability for any specific value.
- (d) (1 point) \_\_\_\_ **F** \_\_\_\_ For a discrete random variable we must need a density function.
- (e) (1 point) \_\_\_\_ **F** \_\_\_\_ Inferential Statistics is just explaining the data and we don't make any conclusion regarding the population.
- (f) (1 point) \_\_\_\_ **T** \_\_\_\_ For Bernoulli distribution we have only one parameter.

2. **Short Questions (6 points)**

- (a) (3 points) If we have random variable  $X$  that represents height (in feet) of the EWU students, how do you interpret, following quantities:  $\mathbb{E}(X) = 4.5$  and  $\mathbb{P}(4.5 < X < 6) = .60$

**Solution:**

If  $X$  is a random variable representing height of the EWU students, the the expected height  $\mathbb{E}(X) = 4.5$  feet means average height of all EWU students is 4.5 feet.  $\mathbb{P}(4.5 < X < 6) = .60$  means the probability that the height of a random students is between 4.5 and 6 feet is 0.60. More concretely this means, if we randomly select 100 students from EWU, then the height of the 60 students will fall between 4.5 and 6 feet (this is the classical interpretation of probability!)

- (b) (3 points) If we assume height is normally distributed then, then for a sample size of 6 students, propose an estimator for the population mean, then also assuming i.i.d. what is the distribution of the sample means.

**Solution:**

If we assume height is normally distributed, this means  $X \sim \mathcal{N}(\mu, \sigma^2)$ . In this case if our target parameter is the population mean  $\mathbb{E}(X) = \mu$ , then the sample mean  $\bar{X}$  is a "good" estimator for the population mean. Note in this case,  $\bar{X}$  is a random quantity.

The theory suggests (in particular look at the Theorem 1.2 of Chapter 1), if the population is normal, then the sample mean  $\bar{X}$  is also normally distributed, and  $\bar{X} \sim \mathcal{N}(\mu, \frac{\sigma^2}{n})$ .

Since we know the population mean  $\mathbb{E}(X) = \mu = 4.5$  and  $\mathbb{V}(X) = \sigma^2 = 8$ , in this case,  $\bar{X} \sim \mathcal{N}(4.5, \frac{8}{6})$