

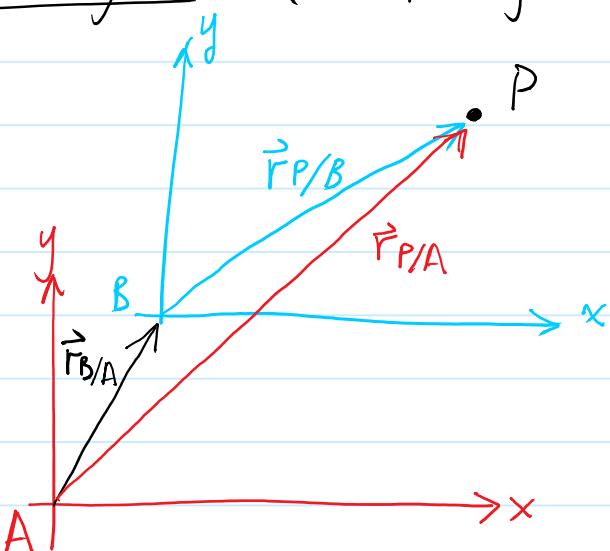
# Lecture 2 : Newton's Law I.

P.I.

Outline: - Relative motion , Reference frame

- Newton's Laws
- Inertial frame
- Apparent weight

Reference frame ( choice of coordinate system)



$\vec{r}_{P/A}$ : position of P  
observed by / relative to A

$\vec{r}_{P/B}$ : position of P

According to vector addition rule:

$$\vec{r}_{P/A} = \underbrace{\vec{r}_{P/B}}_{\text{Contract.}} + \vec{r}_{B/A}$$

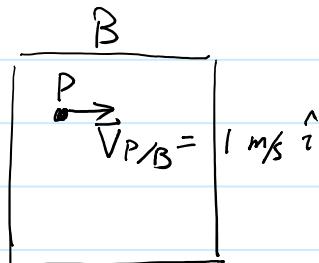
or  $\vec{r}_{P/B} = \vec{r}_{P/A} - \vec{r}_{B/A}$

relative to same observer

Taking time derivatives:

$$\vec{v}_{P/A} = \vec{v}_{P/B} + \vec{v}_{B/A} \quad \text{or} \quad \vec{v}_{P/B} = \vec{v}_{P/A} - \vec{v}_{B/A}$$

$$\vec{a}_{P/A} = \vec{a}_{P/B} + \vec{a}_{B/A} \quad \text{or} \quad \vec{a}_{P/B} = \vec{a}_{P/A} - \vec{a}_{B/A}$$

Example

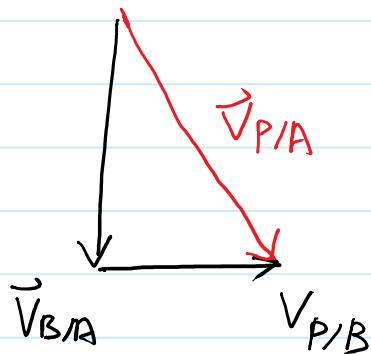
B: train

P: Person in the train

$$\downarrow \vec{v}_{B/A} = 100 \text{ m/s} (-\hat{j})$$

Velocity of P observed by A:

$$\vec{v}_{P/A} = \vec{v}_{P/B} + \vec{v}_{B/A} = -100\hat{j} + 1\hat{i} = \hat{i} + 100\hat{j}.$$

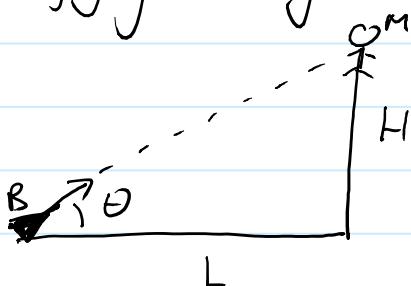


Review on monkey &amp; hunter.

at  $t=0$ , monkey sees the bullet flying directly towards it.

$$\therefore \tan \theta = \frac{H}{L}$$

What is the trajectory of the bullet in the monkey's point of view afterwards?

 $\Rightarrow$  what is  $\vec{v}_{B/M}(t)$  ?

According to Lecture 1, the trajectories are found relative to a stationary observer, say the ground ( $G$ ).

$$\vec{V}_{B/G} = V_0 \cos \theta \hat{i} + (V_0 \sin \theta - gt) \hat{j}$$

$$\vec{V}_{M/G} = \vec{0} \hat{i} + (-gt) \hat{j} \quad (\text{velocity for free fall})$$

$$\Rightarrow \vec{V}_{B/M} = \vec{V}_{B/G} - \vec{V}_{M/G}$$

$$= V_0 \cos \theta \hat{i} + V_0 \sin \theta \hat{j}$$

$$= \vec{V}_0 \quad (\text{constant})$$

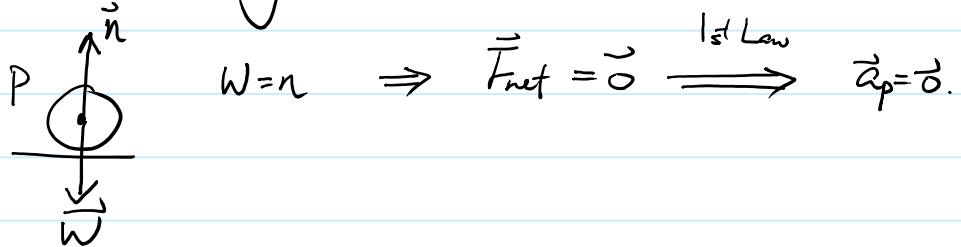
$\Rightarrow$  The falling monkey sees the bullet is flying in a straight line towards it all the time.

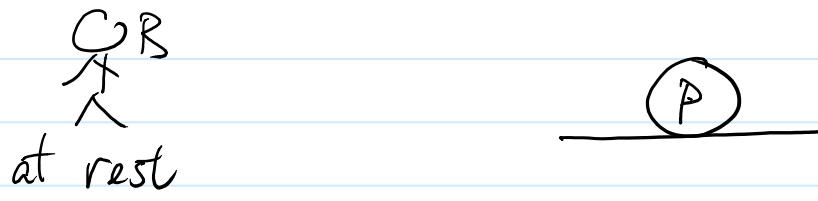
### Inertia      1st Law

$$\text{"} \vec{F}_{\text{net}} = \sum \vec{F}_i = \vec{0} \Leftrightarrow \text{uniform motion, } \vec{a} = \vec{0} \text{"}$$

1st Law is not true for all reference frame. why?

Consider a ball being at rest on the floor.





$$\vec{a}_{P/B} = \vec{0} \quad \checkmark \quad 1st \text{ Law ok!}$$

$$\frac{\text{Object } A}{\text{Object } B} \rightarrow \vec{v}_{A/B}$$

P

$$\vec{v}_{P/A} = \vec{v}_{P/B} + \vec{v}_{B/A} = \vec{v}_{P/B} - \vec{v}_{A/B}$$

$$\Rightarrow \vec{a}_{P/A} = \vec{a}_{P/B} - \vec{a}_{A/B}$$

Case (a) : A is moving in uniform motion relative to B.

$$\Rightarrow \vec{a}_{A/B} = \vec{0}$$

$$\Rightarrow \vec{a}_{P/A} = \vec{0} \quad \checkmark \quad 1st \text{ Law ok!}$$

Case (b) : A has non zero acc. relative to B.

$$\Rightarrow \vec{a}_{A/B} \neq \vec{0}$$

$$\Rightarrow \vec{a}_{P/A} \neq \vec{0} \quad \text{but} \quad \vec{F}_{\text{net on } P} = \vec{0}$$

$\Rightarrow$  1st Law is violated.

Let's define the reference frame where Newton's 1st Law is valid as an inertial frame.

Newton's 1st Law (& 2<sup>nd</sup> Law) does not hold in a reference frame (A) which has acc. relative to an inertial frame (B).

We call those frame a non-inertial frame.

Newton's 1st and 2nd Law apply only in inertial frame

How to find inertial frame?

- an observer with no net forces acting on it is an inertial frame.
- an observer moves in uniform motion relative to an inertial observer.

## Newton's 2nd Law.

$$\vec{F}_{\text{net}} = m \vec{a} \Rightarrow |\vec{a}| = \frac{|F|}{m}$$

↑  
effect

cause  
mass  
"laziness"

---

$$\text{SI unit: } 1 \text{ Newton} = 1 \text{ N} = 1 \text{ kg m s}^{-2}$$

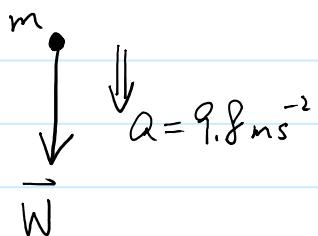
Why is weight =  $mg$ ?

Weight = gravitation attraction due to the Earth.

On surface of the Earth, we observe that

every free falling object falls at  $a = 9.8 \text{ m s}^{-2}$ .

Since no forces beside gravity is acting on the object, according to 2nd Law.



$$\vec{F}_{\text{net}} = m \vec{a}$$

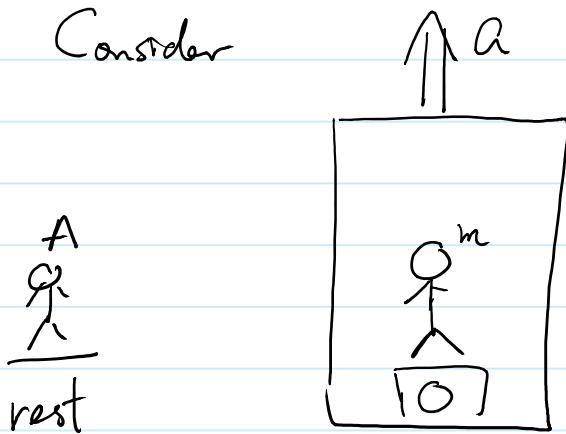
$\downarrow$

$$W = m g$$

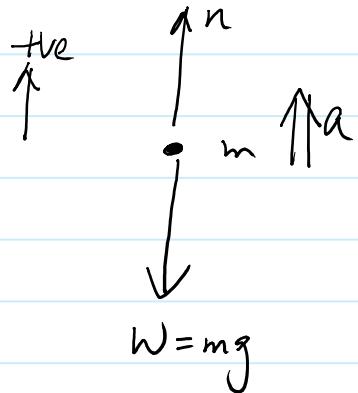
$\downarrow$  from kinematics.

## Application

Consider



## Free Body Diagram



$$F = ma$$

acc of the lift and the person

$$\underbrace{n - w}_{\text{causes}} = \underbrace{m a}_{\text{effect}}$$

$\Rightarrow n - mg = ma$

acceleration relative  
a stationary object

$$n = m(a+g) > mg = w$$

Reading is larger than actual weight.

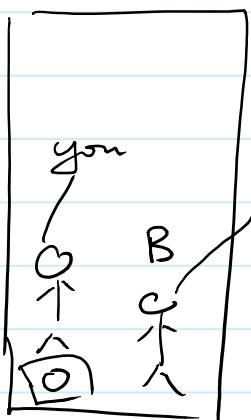
Apparent weight = mass  $\times$  relative acc. to some  
non-inertial frame  
(e.g. the lift)

Suppose  $m = 50 \text{ kg}$ ,  $g = 10 \text{ m s}^{-2}$  and  $a = 1 \text{ m s}^{-2}$

$$\Rightarrow n = 50 \cdot 11 = 550 \text{ N}$$

$\Rightarrow$  Reading on the scale  $\sim 55 \text{ kg}$

Consider someone (B) inside the lift and he/she wants to apply Newton's 2<sup>nd</sup> Law on you.



In B's mind

- There are gravity and normal force acting on this guy (you).

$$\Rightarrow F_{\text{net}} = n - W$$

- But this guy is at rest.  
Newton's Law says:

$$\Rightarrow \vec{a} = \vec{0}$$

$$F_{\text{net}} = m a$$

$$n - W = m \cdot 0$$

$$\Rightarrow n = W = mg$$

not  $m(g+a)$  in last calculation.

Since the reading on the scale is 55 kg, he must be 55 kg.

But you are only 50 kg. What's wrong?