

# NEWTON'S LAWS OF MOTION I

Intended Learning Outcomes – after this lecture you will learn:

1. the concept of frame of reference and relative velocity
2. to use the Newton's three laws of motion to solve problems.
3. the concept of inertial frame of reference.
4. the meanings of apparent weight and weightlessness.

Textbook Reference: Ch 3.5, 4, 5.1, 5.2

**Reference frame** – An observer making observation/measurement forms a reference frame. e.g.

**Reference Frame A**

1<sup>st</sup> observer A,  
standing still on the  
platform

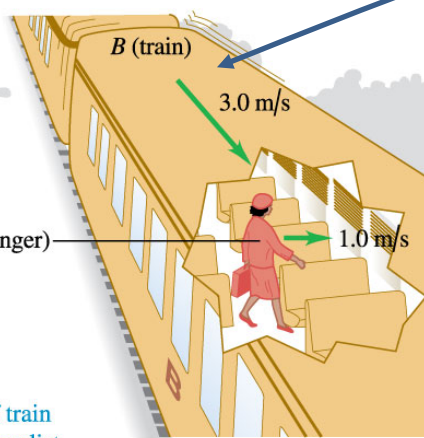
(a)



A (cyclist)

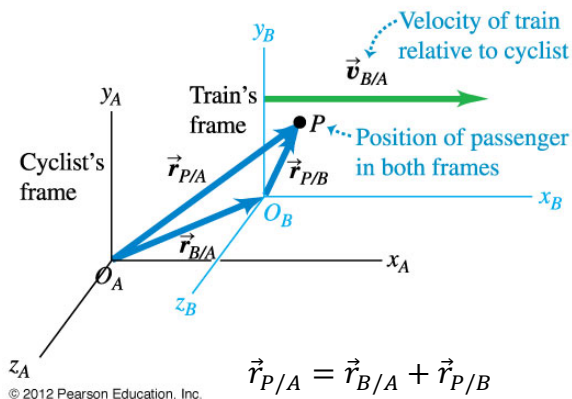
**Reference Frame B**

2<sup>nd</sup> observer B,  
sitting still inside  
the train



P (passenger)

(b)



$$\vec{r}_{P/A} = \vec{r}_{B/A} + \vec{r}_{P/B}$$

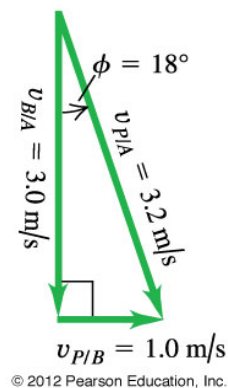
$$\Rightarrow \vec{v}_{P/A} = \vec{v}_{B/A} + \vec{v}_{P/B}$$

velocity of P  
measured in  
frame A

velocity of  
frame B  
measured in

velocity of P  
measured in  
frame B

(c) Relative velocities  
(seen from above)



## Newton's first law of motion

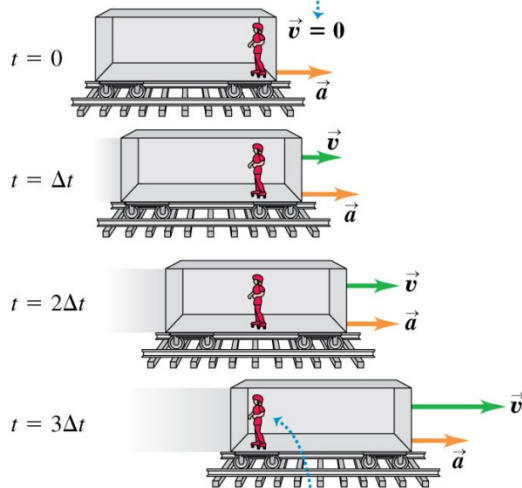
A body acted on by no net force moves with constant velocity

$$\sum \vec{F} = 0 \text{ body in equilibrium}$$

⚠ may be moving

### Inertial Frame of Reference

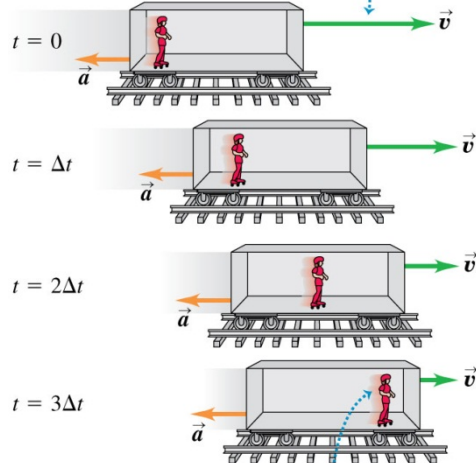
(a) Initially, you and the vehicle are at rest.



You tend to remain at rest as the vehicle accelerates around you.

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(b) Initially, you and the vehicle are in motion.



You tend to continue moving with constant velocity as the vehicle slows down around you.

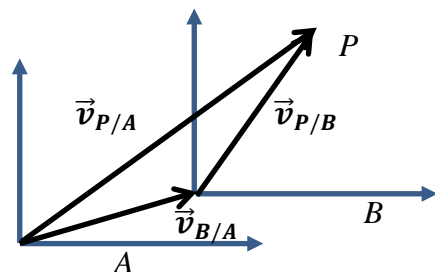
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Passenger (in roller skate) accelerates inside the train, but net force is zero. Violate Newton's first law?? The train is not an inertial frame.

**Definition:** a frame of reference in which Newton's first law is valid is called an inertial frame

Note: 1. Is the earth an inertial frame? Only approximately

2. Given an inertial frame A,



$$\vec{v}_{P/A} = \vec{v}_{P/B} + \vec{v}_{B/A}$$

no net force

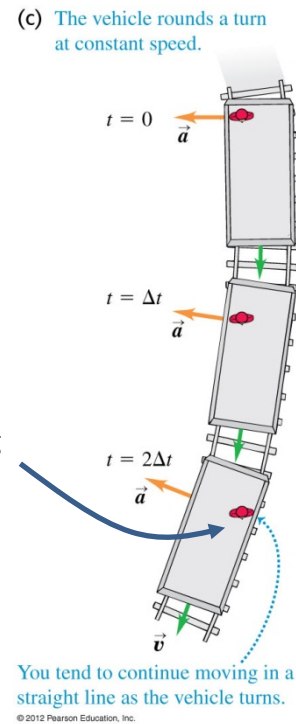
$\Rightarrow \vec{v}_{P/A}$  constant

$\Rightarrow \vec{v}_{P/B}$  constant provided  $\vec{v}_{B/A}$  constant

any frame B moving with constant  $\vec{v}_{B/A}$  (can be zero) is also an inertial frame

⚠ In a non-inertial frame of reference, may feel like being acted on by a (non-existing) force.

feel like a force pushing you aside



**Question:** In which of the following situations is there zero net force on the body?

- an airplane flying due north at a steady speed and at a constant altitude, assuming that the earth is flat and is an inertial frame;
- a car driving straight up a hill with constant slope at constant speed;
- a hawk circling at constant speed and constant height above an open field;
- a box with slick, frictionless surfaces in the back of a truck as the truck accelerates forward on a level road at constant acceleration.

**Answer:** see inverted text on P. 135 of textbook

**Demonstration:** Relative motion



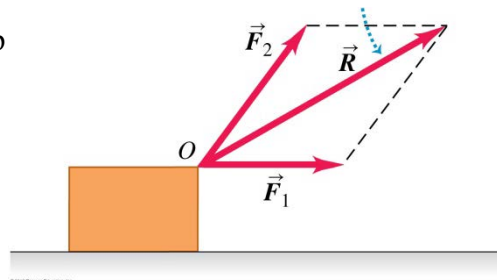
## Superposition of forces

Forces are vectors and can be added up

$\vec{R}$  is called the net or resultant force

The SI unit of force is newton,


$$1 \text{ N} = 1 \text{ kg m/s}^2$$



## Newton's second law

If a *net* external force acts on a body, the body accelerates according to

$$\Sigma \vec{F} = m\vec{a}$$

 inertial mass – how reluctant the body is to change its velocity

⚠ Make sure  $\Sigma \vec{F}$  is the net force, see **Demonstration: fan car**



**Question:** Suppose an astronaut landed on a planet where  $g = 19.6 \text{ m/s}^2$ . Compared to earth, it would be (easier / harder / just as easy) for her to walk around. It would be (easier / harder / just as easy) for her to catch a ball that is moving horizontally at 12 m/s.

**Answer:** see inverted text on P. 143 of textbook

## Newton's third law of motion

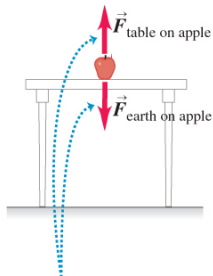
If body *A* exerts a force on body *B* (an “action”), then body *B* exerts a force on body *A* (a “reaction”). These two forces have the same magnitude but are opposite in direction. These two forces act on different bodies.

**Question:** Since action and reaction are equal and opposite, should they cancel each other?

### Example 4.9 P. 144

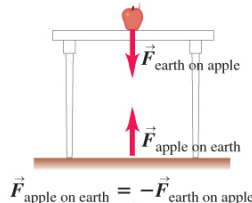
Action and reaction forces acting on an apple sitting on a table

(a) The forces acting on the apple



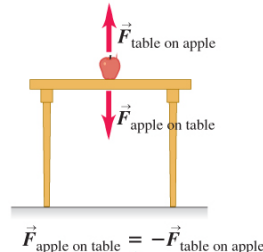
The two forces on the apple *cannot* be an action–reaction pair because they act on the same object.

(b) The action–reaction pair for the interaction between the apple and the earth

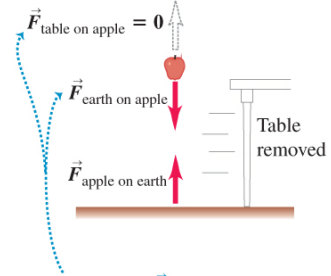


An action–reaction pair is a mutual interaction between two objects. The two forces act on two *different* objects.

(c) The action–reaction pair for the interaction between the apple and the table



(d) We eliminate the force of the table on the apple.



When we remove the table,  $\vec{F}_{\text{table on apple}}$  becomes zero but  $\vec{F}_{\text{earth on apple}}$  is unchanged. Hence these forces (which act on the same object) *cannot* be an action–reaction pair.

**Question:** The buoyance force experienced by a scuba diver is one half of an action–reaction pair. What force is the other half of this pair?

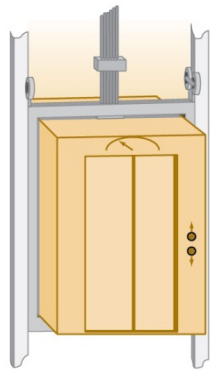
- a) the weight of the diver;
- b) the forward thrust force;
- c) the backward drag force;
- d) the downward force that the swimmer exerts on the water.

### Example 5.8 and 5.9 P. 164: Tension in an elevator cable

An elevator, mass 800 kg, moving downwards at 10.0 m/s

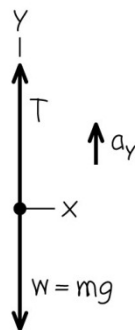
If it comes to a stop in a distance of 25.0 m

(a) Descending elevator



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(b) Free-body diagram for elevator



To find deceleration  $a_y$

$$v_y^2 = v_{0y}^2 + 2a_y(y - y_0)$$

$\nearrow$  0 m/s       $\uparrow$  -10.0 m/s       $\uparrow$  -25.0 m

$$\Rightarrow a_y = 2.00 \text{ m/s}^2$$

Tension in the cable

$$\sum F_y = T - w = ma_y$$

$$\Rightarrow T = m(g + a_y) = 9440 \text{ N}$$

### Apparent weight and weightlessness

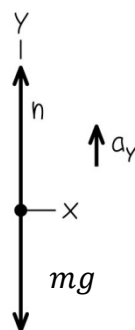
A person standing on a scale in an elevator, reading of the scale is  $n$

(a) Woman in a descending elevator



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(b) Free-body diagram for woman



$$\sum F_y = n - mg = ma_y$$

$$\Rightarrow n = m(g + a_y) \text{ apparent weight of the person}$$

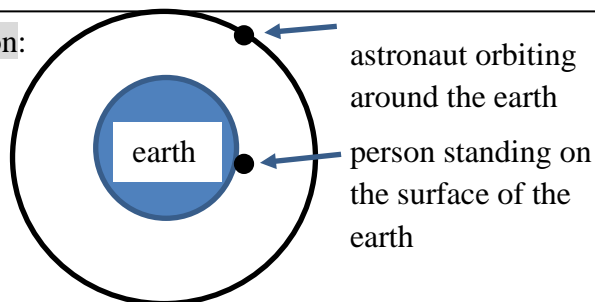
What if free falling, i.e.,  $a_y = -g$ ?

$$n = 0 \text{ apparent weightlessness}$$

Her feet effectively lose contact with the floor

**Question:** One of your very clever classmates says, "If your elevator has a broken cable and is falling freely to the ground, you can save yourself by jumping up at the instant the elevator hits the ground." Will this work?

**Question:**



Both are under the gravitational attraction of the earth. Why does the person have weight but the astronaut is weightless?

## Clicker Questions:

Q3.12



The pilot of a light airplane with an airspeed of 200 km/h wants to fly due west. There is a strong wind of 120 km/h blowing from the north.

If the pilot points the nose of the airplane north of west so that her ground track is due west, what will be her ground speed?

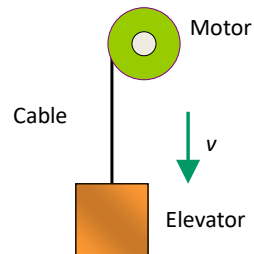
- A. 80 km/h
- B. 120 km/h
- C. 160 km/h
- D. 180 km/h
- E. It would be impossible to fly due west in this situation.

Q4.6



An elevator is being lowered at constant speed by a steel cable attached to an electric motor. There is no air resistance, nor is there any friction between the elevator and the walls of the elevator shaft.

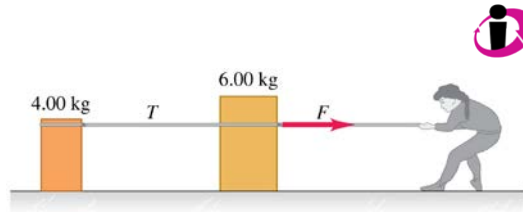
The upward force exerted on the elevator by the cable has the same magnitude as the force of gravity on the elevator, but points in the opposite direction. Why?



- A. Newton's first law
- B. Newton's second law
- C. Newton's third law

Q4.12

A woman pulls on a 6.00-kg crate, which in turn is connected to a 4.00-kg crate by a light rope. It is given that both crates have non-zero accelerations and the light rope remains taut.

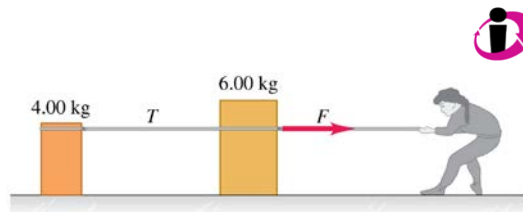


Compared to the 6.00-kg crate, the lighter 4.00-kg crate

- A. is subjected to the same net force and has the same acceleration.
- B. is subjected to a smaller net force and has the same acceleration.
- C. is subjected to the same net force and has a smaller acceleration.
- D. is subjected to a smaller net force and has a smaller acceleration.
- E. none of the above

Q4.14

A woman pulls on a 6.00-kg crate, which in turn is connected to a 4.00-kg crate by a light rope. It is given that both crates have non-zero accelerations and the light rope remains taut.



- A. the 6.00-kg crate exerts more force on the 4.00-kg crate than the 4.00-kg crate exerts on the 6.00-kg crate.
- B. the 6.00-kg crate exerts less force on the 4.00-kg crate than the 4.00-kg crate exerts on the 6.00-kg crate.
- C. the 6.00-kg crate exerts as much force on the 4.00-kg crate as the 4.00-kg crate exerts on the 6.00-kg crate.

Ans: Q3.12) C, Q4.6) A, Q4.12) B, Q4.14) C



# Isaac Newton

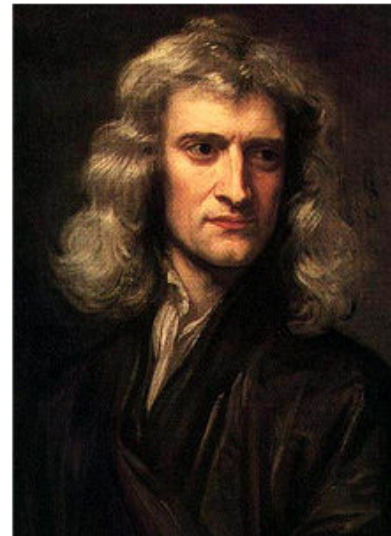
From Wikipedia, the free encyclopedia

**Sir Isaac Newton** PRS MP (25 December 1642 – 20 March 1727 [NS: 4 January 1643 – 31 March 1727])<sup>[1]</sup> was an English physicist, mathematician, astronomer, natural philosopher, alchemist and theologian, who has been "considered by many to be the greatest and most influential scientist who ever lived."<sup>[7]</sup> His monograph *Philosophiæ Naturalis Principia Mathematica*, published in 1687, lays the foundations for most of classical mechanics. In this work, Newton described universal gravitation and the three laws of motion, which dominated the scientific view of the physical universe for the next three centuries. Newton showed that the motions of objects on Earth and of celestial bodies are governed by the same set of natural laws, by demonstrating the consistency between Kepler's laws of planetary motion and his theory of gravitation, thus removing the last doubts about heliocentrism and advancing the Scientific Revolution.

The *Principia* is generally considered to be one of the most important scientific books ever written, due, independently, to the specific physical laws the work successfully described, and for the style of the work, which assisted in setting standards for scientific publication down to the present time. Newton built the first practical reflecting telescope<sup>[8]</sup> and developed a theory of colour based on the observation that a prism decomposes white light into the many colours that form the visible spectrum. He also formulated an empirical law of cooling and studied the speed of sound. In mathematics, Newton shares the credit with Gottfried Leibniz for the development of differential and integral calculus. He also demonstrated the generalised binomial theorem, developed Newton's method for approximating the roots of a function, and contributed to the study of power series.

Newton, although an unorthodox Christian, was deeply religious, and wrote more on Biblical hermeneutics and occult studies than on science and mathematics. Newton secretly rejected Trinitarianism, and feared being accused of refusing holy orders.<sup>[9]</sup>

## Sir Isaac Newton



Godfrey Kneller's 1689 portrait of Isaac Newton (age 46)

<b>Born</b>	25 December 1642 [NS: 4 January 1643] <sup>[1]</sup> Woolsthorpe-by-Colsterworth Lincolnshire, England
<b>Died</b>	20 March 1727 (aged 84) [NS: 31 March 1727] <sup>[1]</sup> Kensington, Middlesex, England
<b>Residence</b>	England
<b>Nationality</b>	English
<b>Fields</b>	Physics, mathematics, astronomy, natural philosophy, alchemy, Christian theology
<b>Institutions</b>	University of Cambridge Royal Society Royal Mint
<b>Alma mater</b>	Trinity College, Cambridge
<b>Academic advisors</b>	Isaac Barrow <sup>[2]</sup> Benjamin Pulleyn <sup>[3]</sup> <sup>[4]</sup>
<b>Notable students</b>	Roger Cotes William Whiston

For more information see [http://en.wikipedia.org/wiki/Isaac\\_Newton](http://en.wikipedia.org/wiki/Isaac_Newton)