

# Temperature and Heat.

What is temperature,  $T$ ? (in our perspective)

$T$  quantifies physical properties of matter consists of numerous particles / molecules.

$T \longleftrightarrow$  state  
characterised by macroscopic  
quantities: Pressure, Volume, resistance...

e.g. thermometer:

$T \longleftrightarrow$  Volume of liquid.  $T \uparrow V \uparrow$ .

Resistor in circuit

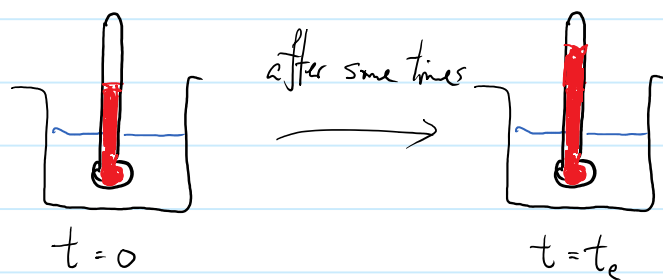
$T \longleftrightarrow$  resistance.  $T \uparrow R \uparrow$

## Thermal Equilibrium.

Thermal contact — energy transfer is allowed between two systems

When the states of two thermally contacting systems remain unchanged, the systems are called <sup>being</sup> in thermal equilibrium.

e.g. a thermometer in water

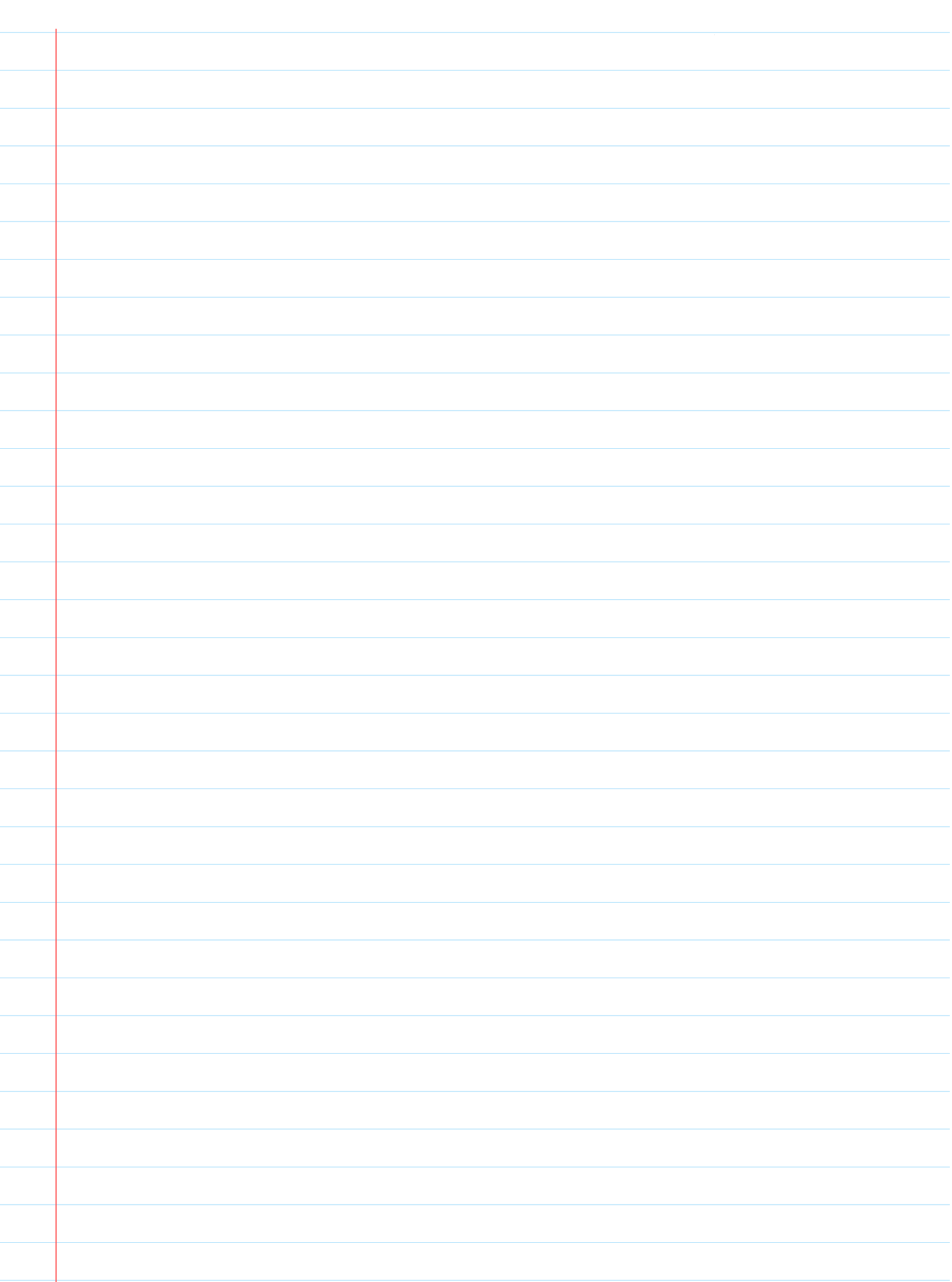


no more changes.

$\Rightarrow$  Thermometer & water  
are in thermal equilibrium.

$\Downarrow$   
we also say that

they have the same Temperature!



Thermal Equilibrium = same temperature.

## Zero-th Law of Thermodynamics

If A & B are each in thermal equilibrium with C,  
then A & B are in thermal equilibrium with each other.

## Different units/scales of temperature.

Fahrenheit ( $T_F$ )	Celsius ( $T_C$ )	Kelvin ( $T$ )
• Freezing point of water $32^\circ\text{F}$	• Freezing point of water $0^\circ\text{C}$	• Lowest possible temp. $0\text{ K}$
• Boiling point of water $212^\circ\text{F}$	• Boiling point of water $100^\circ\text{C}$	• Triple pt. of water $273.16\text{ K } (=0.01^\circ\text{C})$ @ $p = 0.006\text{ atm.}$
• human body temp. $\sim 96^\circ\text{F}$	• human body temp. $\sim 37.5^\circ\text{C}$	
set to fit human body temp.	set to fit water freezing & boiling pt.	most objective scale (more in Lecture 23-24)

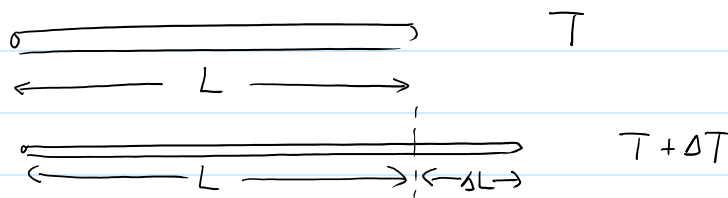
Conversion:

$$T_F = \frac{9}{5} T_C + 32$$

$$T_C = T - 273.15\text{ K}$$

# Thermal Expansion

Linear expansion



$$\text{fractional change} = \frac{\Delta L}{L} \propto \Delta T$$

$$\Rightarrow \frac{\Delta L}{L} = \alpha \Delta T \xrightarrow{\text{infinitesimal change}} \frac{dL}{L} = \alpha dT$$

↑  
coefficient of linear expansion.

e.g.  $\alpha_{\text{Aluminium}} = 2.4 \times 10^{-5} \text{ K}^{-1}$

$\alpha_{\text{glass}} = 0.4 \times 10^{-5} \text{ K}^{-1}$

open cold jar lid  $\Rightarrow$  warm the lid.  
lid expands more than glass.



Volume expansion.



$$\frac{\Delta V}{V} = \beta \Delta T \rightarrow \frac{dV}{V} = \beta dT$$

e.g.  $V = L^3$  (cube)  $\Rightarrow \frac{dV}{V} = \frac{1}{L^3} 3L^2 dL = 3 \frac{dL}{L} = 3\alpha dT \equiv \beta dT$

$\underline{\beta = 3\alpha}$

Heat = energy transfer due to temperature difference. (instead of work)

Heat and temperature change

Heat  $\Delta Q > 0$  if Heat enters to the system

$\Delta Q < 0$  if Heat exits from the system

for any object

$$\underline{\Delta Q = C_{\text{bulk}} \Delta T}$$

$C_{\text{bulk}}$  = heat capacity of the object, which can be a mixture of different materials (bulk)

for single material

$$\underline{\Delta Q = m c \Delta T}, \quad c = \text{specific heat of the material}$$

e.g. water  $c_w \sim 4200 \text{ J/kg}\cdot\text{K}$

for gas

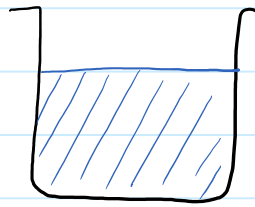
$$\underline{\Delta Q = n C_{\text{mol}} \Delta T}, \quad C_{\text{mol}} = \text{molar heat capacity}$$

Latent Heat - Amount of heat per one unit of mass

to change the substance from one phase to another.  
e.g. gas, liquid, solid...

- During the phase change/transition,  $\Delta T = 0$   
e.g. vapourization, freezing...

Example.



Water

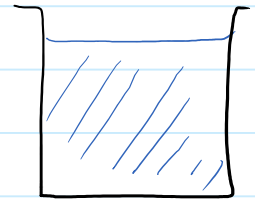
$$m_w = 0.25 \text{ kg}$$
$$T_w = 25^\circ \text{C}$$

+



Ice

$$m_I = ?$$
$$T_I = -20^\circ \text{C}$$



Water

$$T_f = 0^\circ \text{C}$$

Find  $m_I$ .

Assuming the process occurs in a thermal insulator.

$$\Delta Q_{\text{sys}} = 0$$

$$\Delta Q_{\text{water}} + \Delta Q_{\text{ice}} = 0$$

$$\Delta Q_{\text{water}} = m_w c_w \Delta T = m_w c_w (T_f - T_w)$$

$$\Delta Q_{\text{ice}} = \Delta Q_{\text{melting}} + \Delta Q_{T_I \rightarrow T_f}$$
$$= +m_I L_{\text{fusion}} + m_I c_I (T_f - T_I)$$

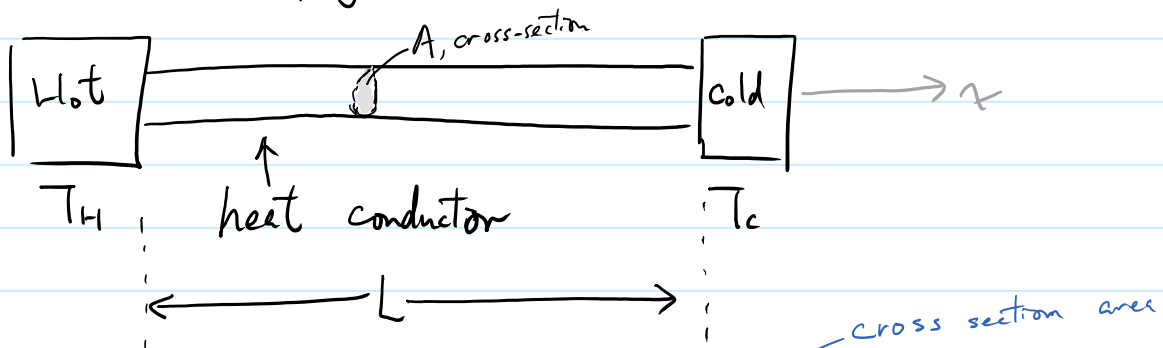
↑  
Ice absorbs  
energy in  
melting

$$\Rightarrow m_I = \frac{m_w c_w (T_f - T_w)}{c_I (T_f - T_I) + L_{\text{fusion}}}$$

# Mechanism of Heat Transfer

Conduction, Convection & Radiation

Conduction (physical contact.)



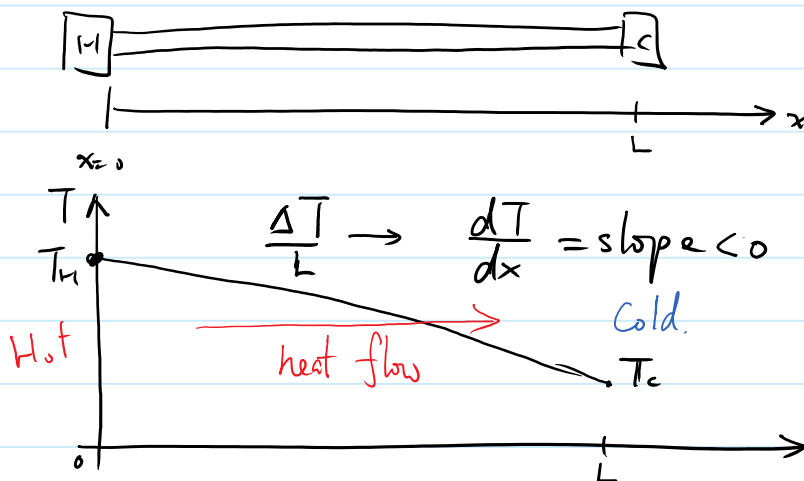
Heat flow per unit time =  $H = \frac{k A (T_H - T_C)}{L}$   
(unit: W)

Annotations:  $k$  is Thermal conductivity (material dependence),  $\frac{W}{mK}$ .  $L$  is length of conductor.

Thermal conductivity (material dependence),  $\frac{W}{mK}$ .

$\frac{T_H - T_C}{L} = \frac{\Delta T}{L}$  = Temp. gradient, diff. in Temp. over distance

Consider temperature as a function of  $x$ .

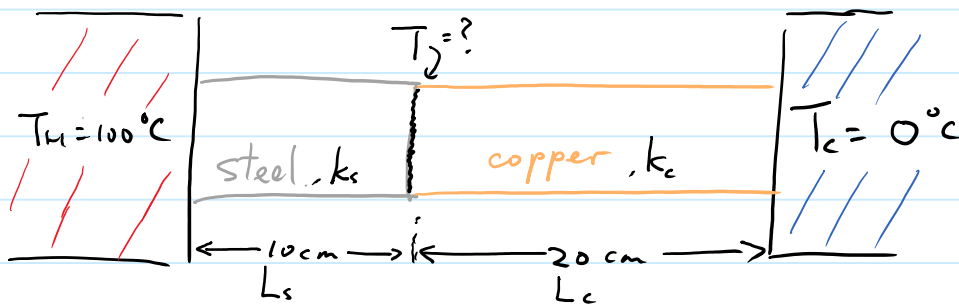


Since  $\frac{dT}{dx}$  is opposite to the direction of the heat flow,

$H \propto -\frac{dT}{dx}$

Define  $H > 0$  when heat flow to  $+x$ ,  $H = -kA \frac{dT}{dx}$

Example. conducting heat with two materials.



$$k_s = 50.2 \text{ W/mK} \quad , \quad k_c = 385.0 \text{ W/mK}$$

Find  $T$ .

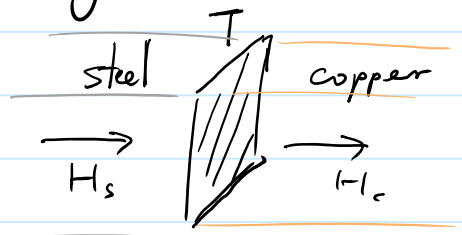
$$\text{Heat flow along the steel} = H_s = k_s A \frac{T_h - T}{L_s}$$

$$\text{Heat flow along the copper} = H_c = k_c A \frac{T - T_c}{L_c}$$

At steady state,  $H_s = H_c$  otherwise there is net heat flowing in or away at the boundary.

$$\Rightarrow H_s = H_c$$

$$\Rightarrow \frac{k_s (T_h - T)}{L_s} = \frac{k_c (T - T_c)}{L_c}$$

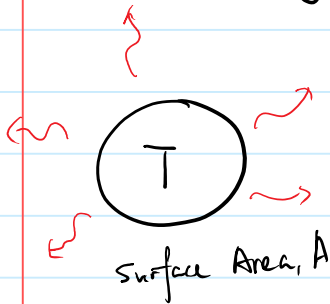


$$\Rightarrow T = 20.7^\circ\text{C}$$



## Radiation

Any body ( $T > 0 \text{ K}$ ) radiates energy.



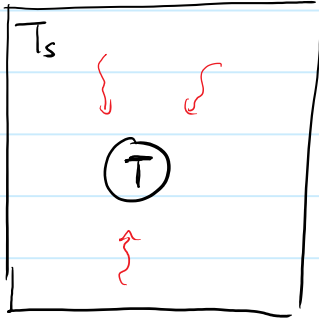
Radiation Power

$$H_{\text{rad}} = A e \sigma T^4 \quad [\text{W}]$$

$$\begin{aligned} \sigma &= \text{Stefan-Boltzmann Constant (universal)} \\ &= 5.6704 \times 10^{-8} \text{ W/m}^2/\text{K}^4 \end{aligned}$$

$$e = \text{emissivity of object. } 0 \leq e \leq 1$$

$$A = \text{Total surface area.}$$



The environment surrounding ( $T_s$ ) the object also radiates. The object will absorb the radiation according to.

$$H_{\text{abs}} = A e \sigma T_s^4$$

⇒ The net heat flow due to radiation is

$$H_{\text{net}} = H_{\text{rad}} - H_{\text{abs}} = A e \sigma (T^4 - T_s^4)$$

Human body at  $T = 30^\circ\text{C}$  with surface area  $1.2 \text{ m}^2$  and emissivity  $e \approx 1$  surrounded by temperature  $20^\circ\text{C}$ .

$$\begin{aligned} H_{\text{net}} &= A e \sigma (T^4 - T_s^4) \\ &= (1.2)(1)(5.67 \times 10^{-8}) \cdot (303^4 - 293^4) \\ &= 72 \text{ W} \end{aligned}$$

ie. the human needs to generate 72 W to keep the body temp.