1. HKDSE MATH CORE 2019 Past Paper I Q1

Make h the subject of the formula 9(h+6k) = 7h + 8. (3 marks)

2. HKDSE MATH CORE 2019 Past Paper I Q2 Simplify
$$\frac{3}{7x-6} - \frac{2}{5x-4}$$
. (3 marks)

3. HKDSE MATH CORE 2019 Past Paper I Q3

The length and the breadth of a rectangle are 24 cm and (13 + r) cm respectively. If the length of a diagonal of the rectangle is (17-3r) cm, find r. (3 marks)

4. HKDSE MATH CORE 2019 Past Paper I Q4 Factorize

- (a) $4m^2 9$,
- (b) $2m^2n + 7mn 15n$.
- (c) $4m^2 9 2m^2n 7mn + 15n$.

(4 marks)

5. HKDSE MATH CORE 2019 Past Paper I Q5

A wallet is sold at a discount of 25% on its marked price. The selling price of the wallet is \$690.

- (a) Find the marked price of the wallet.
- (b) After selling the wallet, the percentage profit is 15%. Find the cost of the wallet.

(4 marks)

6. HKDSE MATH CORE 2019 Past Paper I Q6

- (a) Solve the inequality $\frac{7x+26}{4} \le 2(3x-1)$.
- (b) Find the number of integers satisfying both inequalities $\frac{7x+26}{4} \le 2(3x-1)$ and $45-5x \ge 0$

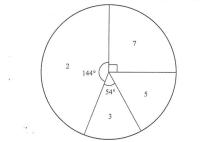
(4 marks)

7. HKDSE MATH CORE 2019 Past Paper I Q7

In a playground, the ratio of the number of adults to the number of children is 13:6. If 9 adults and 24 children enter the playground, then the ratio of the number of adults to the number of children is 8:7. Find the original number of adults in the playground.

(4 marks)

The pie chart below shows the distribution of the numbers of rings owned by the girls in a group.



Distribution of the numbers of rings owned by the girls in the group

- (a) Write down the mode of the distribution.
- (b) Find the mean of the distribution.
- (c) If a girl is randomly selected from the group, find the probability that the selected girl owns more than 3 rings.

(5 marks)

9. HKDSE MATH CORE 2019 Past Paper I Q9

The sum of the volumes of two spheres is 324π cm³. The radius of the larger sphere is equal to the diameter of the smaller sphere. Express, in terms of π ,

- (a) The volume of the larger sphere;
- (b) The sum of the surface areas of the two spheres.

(5 marks)

10. HKDSE MATH CORE 2019 Past Paper I Q10

It is given that h(x) is partly constant and partly varies as x. Suppose that h(-2) = -96 and h(5) = 72.

- (a) Find h(x). (3 marks)
- (b) Solve the equation $h(x) = 3x^2$. (2 marks)

11. HKDSE MATH CORE 2019 Past Paper I Q11

Let p(X) be a cubic polynomial. When p(x) is divided by x-1, the remainder is 50. When p(X) is divided by x+2, the remainder is -52. It is given that p(x) is divisible by $2x^2+9x+14$.

- (a) Find the quotient when p(X) is divided by $2x^2 + 9x + 14$. (3 marks)
- (b) How many rational roots does the equation have? Explain your answer. (3 marks)

The stem-and-leaf diagram below shows the distribution of the results (in seconds) of some boys in a 400 m race. It is given that the inter-quartile range of the distribution is 8 seconds.

Stem (tens)	Leaf (units)
5	a
6	$0\ 0\ 3\ c\ c\ 8\ 9\ 9\ 9$
7	$\begin{bmatrix} a \\ 0 & 0 & 3 & c & c & 8 & 9 & 9 & 9 \\ 0 & 1 & 1 & 1 & 2 & 2 & 5 & 6 & 9 \end{bmatrix}$
8	$\mid b \mid$

(a) Find c.

(2 marks)

- (b) It is given that the range of the distribution exceeds 34 seconds and the mean of the distribution is 69 seconds. Find
 - (i) a and b,
 - (ii) the least possible standard deviation of the distribution.

(6 marks)

13. HKDSE MATH CORE 2019 Past Paper I Q13

In Figure 1, O is the centre of circle ABCDE. AC is a diameter of the circle. BD and OC intersect at the point F. It is given that $\angle AED = 115^{\circ}$.

(a) Find $\angle CBF$.

(3 marks)

(b) Suppose that BC//OD and OB = 18 cm. Is the perimeter of the sector OBC less than 60 cm? Explain your answer.

(5 marks)

14. HKDSE MATH CORE 2019 Past Paper I Q14

In Figure 2, ABCD is a square. It is given that E is a point lying on AD. BD and CE intersect at the point F. Let G be a point such that BG//EC and CG//DB.

- (a) Prove that
 - (i) $\triangle BCG \equiv \triangle CBF$,
 - (ii) $\triangle BCF \sim \triangle DEF$.

(4 marks)

- (b) Suppose that $\angle BCF = \angle BGC$.
 - (i) Let BC = l. Express DF in terms of l.
 - (ii) Someone claims that AE > DF. Do you agree? Explain your answer.

(4 marks)

There are 21 boys and 11 girls in a class. If 5 students are selected from the class to form a committee consisting of at least 1 boy, how many different committees can be formed? (3 marks)

16. HKDSE MATH CORE 2019 Past Paper I Q16

Let α and β be real numbers such that $\begin{cases} \beta = 5\alpha - 18 \\ \beta = \alpha^2 - 13\alpha + 63 \end{cases}$.

- (a) Find α and β . (2 marks)
- (b) The 1st term and the 2nd term of an arithmetic sequence are $\log \alpha$ and $\log \beta$ respectively. Find the least value of n such that the sum of the first n terms of the sequence is greater than 888.

 (4 mark)

17. HKDSE MATH CORE 2019 Past Paper I Q17

- (a) Let a and p be the area and the perimeter of $\triangle CDE$ respectively. Denote the radius of the inscribed circle of $\triangle CDE$ by r. Prove that pr=2a.

 (2 marks)
- (b) The coordinates of the points H and K are (9,12) and (14,0) respectively. Let P be a moving point in the rectangular coordinate plane such that the perpendicular distance from P to OH is equal to the perpendicular distance from P to HK, where O is the origin. Denote the locus of P by Γ .
 - (i) Describe the geometric relationship between Γ and $\triangle OHK$.
 - (ii) Using (a), find the equation of Γ .

(5 marks)

18. HKDSE MATH CORE 2019 Past Paper I Q18

Figure 3 shows a tetrahedron ABCD. Let P be a point lying on AD such that BP is perpendicular to AD. A craftsman finds that AC = AD = CD = 13 cm, BC = 8 cm, BD = 12 cm and $\angle ABD = 72^{\circ}$.

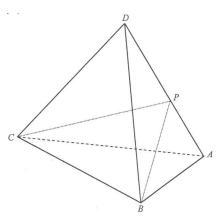


Figure 3

- (a) Find
 - (i) $\angle BAD$,
 - (ii) CP.
 - (5 marks)
- (b) TThe craftsman claims that $\angle BPC$ is the angle between the face ABD and the face ACD. Is the claim correct? Explain your answer. (2 marks)

Let $f(x) = \frac{1}{1+k}(x^2 + (6k-2)x + (9k+25))$, where k is a positive constant. Denote the point (4,33) by F.

- (a) Prove that the graph of y = f(x) passes through F.

 (1 mark)
- (b) The graph of y = g(x) is obtained by reflecting the graph of y = f(x) with respect to the y-axis and then translating the resulting graph upwards by 4 units. Let U be the vertex of the graph of y = g(x). Denote the origin by O.
 - (i) Using the method of completing the square, express the coordinates of U in terms of k.
 - (ii) Find k such that the area of the circle passing through F, O and U is the least.
 - (iii) For any positive constant k, the graph of y = g(x) passes through the same point G. Let V be the vertex of the graph of y = g(x) such that the area of the circle passing through F, O and V is the least. Are F, G, O and V concyclic? Explain your answer.

(11 marks)