1. HKDSE MATH CORE 2016 Past Paper I Q1

Simplify $\frac{(x^8y^7)^2}{x^5y^{-6}}$ and express your answer with positive indices. (3 marks)

2. HKDSE MATH CORE 2016 Past Paper I Q2

Make x the subject of the formula Ax = (4x + B)C. (3 marks)

3. HKDSE MATH CORE 2016 Past Paper I Q3

Simplify
$$\frac{2}{4x-5} + \frac{3}{1-6x}.$$
 (3 marks)

4. HKDSE MATH CORE 2016 Past Paper I Q4

Factorize

- (a) 5m 10n,
- (b) $m^2 + mn 6n^2$,
- (c) $m^2 + mn 6n^2 5m + 10n$.

(4 marks)

5. HKDSE MATH CORE 2016 Past Paper I Q5

In a recreation club, there are 180 members and the number of male members in 40% more than the number of female members. Find the difference of the number of male members and the number of female members.

(4 marks)

6. HKDSE MATH CORE 2016 Past Paper I Q6

Consider the compound inequality

$$x + 6 < 6(x + 11)$$
 or $x < -5 \dots (*)$.

- (a) Solve (*).
- (b) Write down the greatest negative integer satisfying (*).

(4 marks)

7. HKDSE MATH CORE 2016 Past Paper I Q7

In a polar coordinate system, O is the pole. The polar coordinates of the points A and B are $(12,75^{\circ})$ and $(12,135^{\circ})$ respectively.

(a) Find $\angle APB$.

- (b) Find the perimeter of $\triangle AOB$.
- (c) Write down the number of folds of rotational symmetry of $\triangle AOB$.

It is given that f(x) is the sum of two parts, one part varies as x and the other part varies as x^2 . Suppose that f(3) = 48 and f(9) = 198.

- (a) Find f(x).
- (b) Solve the equation f(x) = 90.

(5 marks)

9. HKDSE MATH CORE 2016 Past Paper I Q9

The frequency distribution table and the cumulative frequency distribution table below show the distribution of the heights of the plants in a garden.

Height (m)	Frequency
0.1 - 0.3	a
0.4 - 0.6	4
0.7 - 0.9	b
1.0 - 1.2	c
1.3 - 1.5	15
1.6 - 1.8	3

Height less than(m)	Cumulative frequency
0.35	2
0.65	x
0.95	13
1.25	y
1.55	37
1.85	z

- (a) Find x, y and z.
- (b) If a plant is randomly selected from the garden, find the probability that the height of the selected plant is less than 1.25 m but not less than 0.65 m.

(5 marks)

10. HKDSE MATH CORE 2016 Past Paper I Q10

The coordinates of the points A and B are (5,7) and (13,1) respectively. Let P be a moving point in the rectangular coordinate plane such that P is equidistant from A and B. Denote the locus of P by Γ .

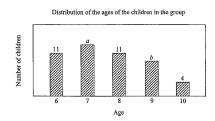
- (a) Find the equation of Γ . (4 marks)
- (b) Γ intersects the x-axis and the y-axis at H and K respectively. Denote the origin by O. Let C be the circle which passes through O, H and K. Someone claims that the circumference of C exceeds 30. Is the claim correct? Explain your answer.
 (3 marks)

11. HKDSE MATH CORE 2016 Past Paper I Q11

An inverted right circular conical vessel contains some milk. The vessel is held vertically. The depth of milk in the vessel is 12 cm. Peter then pours 444π cm³ of milk into the vessel without overflowing. He now finds that the depth of milk in the vessel is 16 cm.

- (a) Express the final volume of milk in the vessel in terms of π . (3 marks)
- (b) Peter claims that the final area of the wet curved surface of the vessel is at least 800 cm².
 Do you agree? Explain your answer.
 (3 marks)

The bar chart below shows the distribution of the ages of the children in a group, where a > 11 and 4 < b < 10. The median of the ages in the group is 7.5.

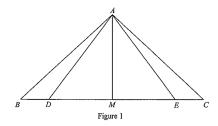


- (a) Find a and b. (3 marks)
- (b) Four more children now join the group. It is found that the ages of these four children are all different and the range of the ages of the children in the group remains unchanged. Find
 - (i) the greatest possible median of the ages of the children in the group,
 - (ii) the least possible mean of the ages of the children in the group.

(4 marks)

13. HKDSE MATH CORE 2016 Past Paper I Q13

In Figure 1, ABC is a triangle. D, E and M are points lying on BC such that BD = CE, $\angle ADC = \angle AEB$ and DM = EM.



- (a) Prove that $\triangle ACD \equiv \triangle ABE$. (2 marks)
- (b) Suppose that AD=15 cm, BD=7 cm and DE=18 cm.
 - (i) Find AM.
 - (ii) Is $\triangle ABE$ a right-angled triangle? Explain your answer.
 - (5 marks)

Let $p(x) = 6x^4 + 7x^3 + ax^2 + bx + c$, where a, b and c are constants. When p(x) is divided by x + 2 and when p(x) is divided by x - 2, the two remainders are equal. It is given that $p(x) = (lx^2 + 5x + 8)(2x^2 + mx + n)$, where l, m and n are constants.

- (a) Find l, m and n. (5 marks)
- (b) How many real roots does the equation p(x) = 0 have? Explain your answer. (5 marks)

15. HKDSE MATH CORE 2016 Past Paper I Q15

If 4 boys and 5 girls randomly form a queue, find the probability that no boys are next to each other in the queue.

(3 marks)

16. HKDSE MATH CORE 2016 Past Paper I Q16

In a test, the mean of the distribution of the scores of a class of students is 61 marks. The standard scores of Albert and Mary are -2.6 and 1.4 respectively. Albert gets 22 marks. A student claims that the range of the distribution is at most 59 marks. Is the claim correct? Explain your answer. (3 marks)

17. HKDSE MATH CORE 2016 Past Paper I Q17

The 1st term and the 38th term of an arithmetic sequence are 666 and 555 respectively. Find

- (a) the common difference of the sequence, (2 marks)
- (b) the greatest value of n such that the sum of the first n terms of the sequence is positive.

 (3 marks)

18. HKDSE MATH CORE 2016 Past Paper I Q18

Let
$$f(x) = \frac{-1}{3}x^2 + 12x - 121$$
.

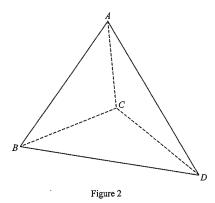
- (a) Using the method of completing the square, find the coordinates of the vertex of the graph of y = f(x).

 (2 marks)
- (b) The graph of y = g(x) is obtained by translating the graph of y = f(x) vertically. If the graph of y = g(x) touches the x-axis, find g(x).

 (2 marks)
- (c) Under a transformation, f(x) is changed to $\frac{-1}{3}x^2 12x 121$. Describe the geometric meaning of the transformation.

 (2 marks)

Figure 2 shows a geometric model ABCD in the form of tetrahedron. It is given that $\angle BAD = 86^{\circ}$, $\angle CBD = 43^{\circ}$, AB = 10 cm, AC = 6 cm, BC = 8 cm and BD = 15 cm.



- (a) Find $\angle BAD$ and CD. (4 marks)
- (b) A craftsman claims that the angle between AB and the face BCD is $\angle ABC$. Do you agree? Explain your answer. (2 marks)

20. HKDSE MATH CORE 2016 Past Paper I Q20

 $\triangle OPQ$ is an obtuse-angled triangle. Denote the in-centre and the circumcentre of $\triangle OPQ$ by I and J respectively. It is given that P, I and J are collinear.

- (a) Prove that OP = PQ. (3 marks)
- (b) A rectangular coordinate system is introduced so that the coordinates of O and Q are (0,0) and (40,30) respectively while the y-coordinate of P is 19. Let C be the circle which passes through O, P and Q.
 - (i) Find the equation of C.
 - (ii) Let L_1 and L_2 be two tangents to C such that the slope of each tangent is $\frac{3}{4}$ and the y-intercept of L_1 is greater than that of L_2 . L_1 cuts the x-axis and the y-axis at S and T respectively while L_2 cuts the x-axis and the y-axis at U and V respectively. Someone claims that the area of the trapezium STUV exceeds 17 000. Is the claim correct? Explain your answer.

(9 marks)