| Pape | r I | Solution | Marks | Remarks |
|------|---|--|-----------|--|
| 1. | $\frac{(x^8y^7)^2}{x^5y^{-6}}$ | ************************************** | | |
| | $=\frac{x^{16}y^{14}}{x^5y^{-6}}$ | | 1M | for $(ab)^m = a^m b^m$ or $(a^m)^n = a^{mn}$ |
| | $=x^{16-5}y^{14-(-6)}$ | * : | 1M | for $\frac{c^p}{c^q} = c^{p-q}$ or $\frac{c^p}{c^q} = \frac{1}{c^{q-p}}$ |
| | $=x^{11}y^{20}$ | | 1A (3) | |
| | | | | , s |
| | Ax = (4x + B)C $Ax = 4Cx + BC$ | | 1M | |
| | Ax - 4Cx = BC $(A - 4C)x = BC$ | | 1M | for putting x on one side |
| | $x = \frac{BC}{A - 4C}$ | | 1A | or equivalent |
| | Ax = (4x + B)C $A = 4x + B$ | | 1M | |
| | $\frac{A}{C}x = 4x + B$ $\frac{A}{C}x - 4x = B$ | | 1M | for putting x on one side |
| | $\left(\frac{A}{C} - 4\right)x = B$ | | | |
| | $\left(\frac{A-4C}{C}\right)x = B$ BC | | | 6 72 |
| | $x = \frac{BC}{A - 4C}$ | | 1A | or equivalent |
| | | | (3) | |
| 3. | $\frac{2}{4x-5} + \frac{3}{1-6x}$ | | | |
| | $=\frac{2(1-6x)+3(4x-5)}{(4x-5)(1-6x)}$ | | 1M | |
| | $=\frac{2-12x+12x-15}{(4x-5)(1-6x)}$ -13 | | 1M | 11 |
| | $-\frac{(4x-5)(1-6x)}{13}$ | | 1A | or equivalent |
| | $-\frac{1}{(4x-5)(6x-1)}$ | | (3) | |
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| | | | | ii. |
| | | 44 | | |

| | | Solution | Marks | Remarks |
|----|--|--|-----------------|---|
| 4. | (a) | 5m - 10n $= 5(m - 2n)$ | 1A | |
| | (b) | $m^2 + mn - 6n^2$ $= (m+3n)(m-2n)$ | 1A | |
| | (c) | $m^{2} + mn - 6n^{2} - 5m + 10n$ $= m^{2} + mn - 6n^{2} - (5m - 10n)$ $= (m + 3n)(m - 2n) - 5(m - 2n)$ $= (m - 2n)(m + 3n - 5)$ | 1M 1A (4) | for using the results of (a) and (b) or equivalent |
| | | | | |
| 5. | $\begin{cases} x - x \\ x = x \\ \text{So, } x \\ \text{Solv} \end{cases}$ | x and y be the number of male members and the number of female abers respectively. y = 180 y = (1+40%)y we have $1.4y + y = 180$. Fing, we have $y = 75$ and $x = 105$. | }1A+1A 1M | for getting a linear equation in x or y only |
| | mem | s, the difference of the number of male members and the number of female libers is 30. x be the number of male members. | 1A | $\int 1A \text{ for } x = (1 + 40\%)y$ |
| | Solv Note | (1+40%)(180-x) ring, we have $x=105$. e that $105-(180-105)=30$. s, the difference of the number of male members and the number of female | 1A+1A+1M | $\begin{cases} + 1A \text{ for } y = 180 - x \\ + 1M \text{ for a linear equation in one unknow} \end{cases}$ |
| | | ibers is 30. | 1A | |
| | | the difference of the number of male members and the number of female members $(180)(40\%)$ $(100\% + (100\% + 40\%))$ | 1A+1A+1M 1A | \[\begin{cases} 1A for numerator + 1A for denominator + 1M for fraction \end{cases} |
| | $\frac{180}{2}$ $d = $ Thus | d be the difference of the number of male members and number of female members. $\frac{d}{dt} = \left(\frac{180 - d}{2}\right)(1 + 40\%)$ 30 s, the difference of the number of male members and the number of female members is 30. | 1A+1A+1M 1A | $\begin{cases} 1A \text{ for } \frac{180+d}{2} \text{ or } \frac{180-d}{2} \\ +1A \text{ for } \left(\frac{180-d}{2}\right)(1+40\%) \\ +1M \text{ for a linear equation in one unknow} \end{cases}$ |
| | | | (4) | |
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| | | Solution | Marks | Remarks |
|----|-----|--|-----------------|-----------------------------|
| 6. | (a) | x+6 < 6(x+11) $x+6 < 6x+66$ $x-6x < 66-6$ $-5x < 60$ $x > -12$ | 1M 1A | for putting x on one side |
| | | Therefore, we have $x > -12$ or $x \le -5$. Thus, the solutions of (*) are all real numbers. | 1A | |
| | (b) | -1 | 1A (4) | |
| | | | | |
| 7. | (a) | $\angle AOB$ $= 135^{\circ} - 75^{\circ}$ $= 60^{\circ}$ | 1A | |
| | (b) | Since $AO = BO$, we have $\angle OAB = \angle OBA$. Note that $\angle OAB + \angle OBA + 60^\circ = 180^\circ$. Therefore, we have $\angle OAB = \angle OBA = 60^\circ$. So, $\triangle AOB$ is an equilateral triangle. The perimeter of $\triangle AOB$ = 3(12) | 1M | can be absorbed |
| | (c) | = 36 3 | 1A 1A (4) | |
| 8. | (a) | Let $f(x) = hx + kx^2$, where h and k are non-zero constants. | 1A | ė) |
| | | So, we have $3h+9k=48$ and $9h+81k=198$. Solving, we have $h=13$ and $k=1$. Thus, we have $f(x) = 13x + x^2$. | 1M 1A | for either substitution |
| | (b) | $f(x) = 90$ $13x + x^{2} = 90$ $x^{2} + 13x - 90 = 0$ $(x - 5)(x + 18) = 0$ $x = 5 \text{ or } x = -18$ | 1M 1A (5) | |
| | | 46 | | |

| | Solution | Marks | Remarks |
|-----|---------------------------------|---------|------------------------------------|
| (a) | x | | |
| | =2+4 | | |
| | = 6 | 1A | |
| | | | |
| | y 27 15 | | |
| | = 37 - 15 = 22 | 1A | |
| | == lala | IA | |
| | Z | | |
| | = 37 + 3 | | |
| | = 40 | 1A | |
| (b) | The required probability | | |
| (0) | | No. 201 | v-x |
| | $=\frac{22-6}{40}$ | 1M | for $\frac{y-x}{z}$ |
| | 2 | | |
| | $=\frac{2}{5}$ | 1A | 0.4 |
| | 3 | | |
| | Note that $b = 7$ and $c = 9$. | | |
| | The required probability | | 2 |
| | $=\frac{7+9}{1}$ | 1M | for $\frac{b+c}{z}$ |
| | 40 | | Z |
| | $=\frac{2}{5}$ | 1A | 0.4 |
| | 5 | | |
| | Note that $a = 2$. | | |
| | The required probability | | ga . |
| | 10-2-1-15-3 | | z-a-4-15-3 |
| | $=\frac{40-2-4-13-3}{40}$ | 1M | for $\frac{z - a - 4 - 15 - 3}{z}$ |
| | | 1.4 | |
| | $=\frac{2}{5}$ | 1A | 0.4 |
| | | (5) | |
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| | Solution | Marks | Remarks |
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|). (a) | Let (x, y) be the coordinates of P . $\sqrt{(x-5)^2 + (y-7)^2} = \sqrt{(x-13)^2 + (y-1)^2}$ 4x-3y-24=0 Thus, the equation of Γ is $4x-3y-24=0$. | 1M 1A | or equivalent |
| | The slope of AB $= \frac{7-1}{5-13}$ $= \frac{-3}{4}$ The slope of Γ $= \frac{4}{3}$ The mid-point of AB $= \left(\frac{5+13}{2}, \frac{7+1}{2}\right)$ $= (9, 4)$ Therefore, the equation of Γ is $y-4=\frac{4}{3}(x-9)$. | 1M | |
| | Thus, the equation of Γ is $4x-3y-24=0$. | 1A | or equivalent |
| (b) | Putting $y=0$ in $4x-3y-24=0$, we have $x=6$. So, the coordinates of H are $(6,0)$. Putting $x=0$ in $4x-3y-24=0$, we have $y=-8$. Therefore, the coordinates of K are $(0,-8)$. | 1M | either one |
| | The diameter of C = HK = $\sqrt{(6-0)^2 + (0-(-8))^2}$ = 10 | | |
| | The circumference of C = 10π ≈ 31.41592654 | 1M | *************************************** |
| | > 30 Thus, the claim is correct. | 1A (3) | f.t. |
| | | | -53 |
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| | Solution | Marks | Remarks |
|-------|---|-------|---------------------------------------|
| . (a) | Let $V \text{ cm}^3$ be the final volume of milk in the vessel. | | |
| | $\frac{V-444\pi}{V} = \left(\frac{12}{16}\right)^3$ | 1M+1A | 1M for $\left(\frac{12}{16}\right)^3$ |
| | | | $\left(\frac{1}{16}\right)$ |
| | $V = 768 \pi$ Thus, the final volume of milk in the vessel is $768 \pi \text{ cm}^3$. | 1A | * |
| | | | |
| | Let $V \text{ cm}^3$ and $r \text{ cm}$ be the final volume of milk and the final radius of the surface of milk in the vessel respectively. | | |
| | $V = \frac{1}{3}\pi r^2 (16)$ | | * |
| | 3 (12)2 | | ž |
| | $V - 444\pi = \frac{1}{3}\pi \left(\frac{12r}{16}\right)^2 (12)$ | | |
| | So, we have $V - 444\pi = \frac{1}{3}\pi \left(\frac{12}{16}\right)^2 \left(\frac{3V}{16\pi}\right)$ (12). | 1M+1A | 1M for eliminating r^2 |
| | Solving, we have $V = 768\pi$. | 1A | |
| | Thus, the final volume of milk in the vessel is $768\pi \text{ cm}^3$. | IA. | 1 |
| | | (3) | |
| (b) | Let r cm be the final radius of the surface of milk in the vessel. | | 9 |
| | $\frac{1}{3}\pi r^2(16) = 768\pi$ | 1M | |
| | r = 12 | | |
| | The final area of the wet curved surface of the vessel | | |
| | $= \pi (12)\sqrt{12^2 + 16^2}$ | 1M | |
| | $=240\pi$ | | |
| | $\approx 753.9822369 \text{ cm}^2$ | | |
| | < 800 cm ² Thus, the claim is disagreed. | 1A | f.t. |
| | Thus, the claim is disagreed. | (3) | 1.1. |
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| | | | Solution | Marks | Remarks |
|------|-----|------------|---|--------------|--|
| 2. (| (a) | <i>a</i> = | a = 11 + b + 4 b + 4 that $a > 11$ and $4 < b < 10$. | 1M | f. <u>u</u> |
| | | | s, we have $\begin{cases} a = 12 \\ b = 8 \end{cases}$ or $\begin{cases} a = 13 \\ b = 9 \end{cases}$. | 1A+1A (3) | 1A for one pair + 1A for all |
| (| (b) | (i) | The median is the greatest when the ages of these four children are 7, 8, 9 and 10. The greatest possible median of the ages of the children in the group = 8 | 1M 1A | |
| | | (ii) | The mean is the least when the ages of these four children are 6 , 7 , 8 and 9 . By (a), there are two cases. | 1M | , |
| | | | Case 1: $a = 12$ and $b = 8$ The mean of the ages of the children in the group $= \frac{12(6) + 13(7) + 12(8) + 9(9) + 4(10)}{12 + 13 + 12 + 9 + 4}$ $= 7.6$ | , | e e |
| | | | Case 2: $a = 13$ and $b = 9$ The mean of the ages of the children in the group $= \frac{12(6) + 14(7) + 12(8) + 10(9) + 4(10)}{12 + 14 + 12 + 10 + 4}$ ≈ 7.615384615 | | |
| | | | Thus, the least possible mean of the ages of the children in the group is 7.6 . | 1A (4) | f.t. |
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| | Soluti | on | Marks | Remarks |
|-----|--|--|-------|--------------|
| (a) | In $\triangle ACD$ and $\triangle ABE$, | | | |
| (4) | $\angle ADC = \angle AEB$ | (given) | | |
| | AD = AE | (sides opp. equal ∠s) | | |
| | CE = BD | (given) | | |
| | CE - BD CE + DE = BD + DE | (given) | | |
| | CD = BE | | | |
| | $\triangle ACD \cong \triangle ABE$ | (SAS) | | |
| | | | | |
| | Marking Scheme: Case I Any correct proof w | ith correct reasons | | |
| | Case 2 Any correct proof w | ithout reasons | 1 | |
| | Case 2 Thiy contect proof w | mout reasons. | (2) | |
| | | | | |
| (b) | 13. A | m and $\angle AMD = \angle AME = 90^{\circ}$. | | |
| | AM | | | |
| | $=\sqrt{AD^2-DM^2}$ | | 1M | |
| | $=\sqrt{15^2-9^2}$ | | | |
| | $=\sqrt{144}$ | | | |
| | $= \sqrt{144}$ $= 12 \text{ cm}$ | | 1A | |
| | - 12 OH | | 1 111 | |
| | (ii) AB^2 | | | |
| | $=AM^2 + BM^2$ | | | |
| | $= 144 + (7+9)^2$ | | | |
| | = 400 | | | |
| | By (a), we have $AE = AD$ | -15 cm | 1M | |
| | $AB^2 + AE^2$ | _ 15 cm . | 1111 | |
| | $AB^2 + AE^2$ = $400 + 15^2$ | | | |
| | $= 400 + 15^{-}$ = 625 | | 1 | F |
| | $= (7+18)^2$ | | | |
| | | | | |
| | $= (BD + DE)^2$ | | | |
| | $=BE^2$ | | 1M | |
| | Thus, $\triangle ABE$ is a right-an | igled triangle. | 1A | f.t. |
| | | | (5) | |
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| | Solution | Marks | Remarks |
|---------|---|--------------|------------|
| 14. (a) | Note that $p(2) = 152 + 4a + 2b + c$ and $p(-2) = 40 + 4a - 2b + c$. Since $p(2) = p(-2)$, we have $b = -28$. | 1M | |
| | By comparing the coefficients of x^4 , we have $l=3$. Note that the coefficients of x^3 and x in the expansion of | 1A | |
| | $(3x^2 + 5x + 8)(2x^2 + mx + n)$ are $3m + 10$ and $8m + 5n$ respectively. | | |
| | So, we have $3m+10=7$ and $8m+5n=-28$. | 1M | |
| | Solving, we have $m = -1$ and $n = -4$. | 1A+1A (5) | - |
| (b) | p(x) = 0 | | |
| | $(3x^2 + 5x + 8)(2x^2 - x - 4) = 0$ (by (a)) | | |
| | $3x^2 + 5x + 8 = 0$ or $2x^2 - x - 4 = 0$ | - | |
| | $5^2 - 4(3)(8)$ | 1M . | |
| | = -71 | 1A | |
| | < 0 So, the quadratic equation $3x^2 + 5x + 8 = 0$ does not have real roots. | 13.4.14 | either one |
| | | 1M+1A | either one |
| | $(-1)^2 - 4(2)(-4)$ = 33 | | either one |
| | > 0 | | |
| | Therefore, the quadratic equation $2x^2 - x - 4 = 0$ has 2 real roots. | | |
| | Hence, the equation $(3x^2 + 5x + 8)(2x^2 - x - 4) = 0$ has 2 real roots. | | |
| | Thus, the equation $p(x) = 0$ has 2 real roots. | 1A | f.t. |
| | | (5) | |
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| - | Solution | Marks | Remarks |
|----|---|-----------|-----------------------------------|
| 5. | The required probability | | |
| | $=\frac{C_4^6}{4!5!}$ | 13.6.13.6 | 13.66 1 |
| | $=\frac{1}{(4+5)!}$ | 1M+1M | 1M for denominator + 1M for 4! |
| | 43 200 | | |
| | $=\frac{43\ 200}{362\ 880}$ | | |
| | | | 992 SQ192 S |
| | $=\frac{5}{42}$ | 1A | r.t. 0.119 |
| | | | |
| | The required probability | | |
| | $=\frac{4!5!+4!5!(4)(2)+4!5!(3)}{(4+5)!}$ | 1M+1M | 1M for denominator + 1M for 4! |
| | | | |
| | $=\frac{43\ 200}{}$ | | |
| | 362 880 | | |
| | $=\frac{5}{42}$ | 1A | r.t. 0.119 |
| | 42 | 171 | 1.6. 0.117 |
| 1 | The complex described the | | |
| | The required probability | | |
| | $= \left(\frac{4}{4}\right)\left(\frac{3}{3}\right)\left(\frac{2}{2}\right)\left(\frac{1}{1}\right)\left(\frac{5}{9}\right)\left(\frac{4}{8}\right)\left(\frac{3}{7}\right)\left(\frac{2}{6}\right)\left(\frac{1}{5}\right)(1+(4)(2)+3+3)$ | 1M+1M | 1M for denominator |
| | | | + 1M for (4)(3)(2)(1)(5)(4)(3)(2) |
| | $=\frac{43200}{362000}$ | | |
| | 362 880 | | 25 |
| | $=\frac{5}{42}$ | 1A | r.t. 0.119 |
| 1 | 42 | | |
| | | (3) | |
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| | 8 | | |
| _ | Yes and the first of the first | | |
| | Let σ marks be the standard deviation of the distribution. | | |
| | $\frac{22-61}{2} = -2.6$ | 1M | |
| | σ $\sigma = 15$ | | - |
| | 0 = 15 | | either one |
| | The score of Mary | | l |
| | $=61+1.4\sigma$ | | |
| | =61+1.4(15) | | |
| | = 82 marks | 1A | |
| | • | 171 | |
| | The difference of the score of Mary and the score of Albert | | |
| | =82-22 | | 15 |
| | = 60 marks | | |
| | > 59 marks | | 10 |
| | * | | 9 |
| | Note that the range of the distribution is at least the difference of the score of | | |
| | Mary and the score of Albert. | | |
| | Therefore, the range of the distribution exceeds 59 marks. | | |
| | Thus, the claim is incorrect. | 1A | f.t. |
| | | (3) | |
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| Let d be the common difference of the sequence. | | 8 | |
|--|--|--|---|
| 555 = 666 + (38 - 1)d | | 1M | |
| d = -3 | | 1A | |
| The common difference of the sequence | | - | |
| $=\frac{555-666}{}$ | | 1M | |
| | | | |
| = -3 | | (2) | |
| | | | |
| $\frac{n}{2}(2(666) + (n-1)(-3)) > 0$ | | 1M+1A | |
| | | | |
| | | | |
| 0 < n < 445 | | | |
| Thus, the greatest value of n is 444. | | 1A | |
| | | (3) | (8) |
| | | | |
| * | | | |
| | | | |
| f(x) | | | |
| | | | |
| $=\frac{1}{3}x^2+12x-121$ | | | |
| $=\frac{-1}{3}(x^2-36x)-121$ | | | |
| $=\frac{-1}{x}(x^2-36x+18^2-18^2)-121$ | | 1M | |
| ~ | | | |
| $=\frac{1}{3}(x-18)^2-13$ | | | |
| Thus, the coordinates of the vertex are $(18, -13)$. | | 1A | |
| | | (2) | |
| g(x) | | * | .= |
| | | 1M | Ø |
| | | | -1 $x^2 + 12x + 108$ |
| $=\frac{3}{3}(x-16)$ | | 1A | accept $\frac{-1}{3}x^2 + 12x - 108$ |
| | | (2) | |
| Note that $\frac{-1}{x^2} + \frac{-1}{x^2} + \frac{-1}{x^2} + \frac{-1}{x^2} = \frac{-1}{x^2} + \frac{-1}{x^2} = \frac{-1}{x^2} + \frac{-1}{$ | | | |
| <u> </u> | | 44.44 | 1 4 6 0 1 4 6 11 |
| Thus, the transformation is the reflection with respect to the y -axis. | | IA+IA | 1A for reflection + 1A for all correct |
| Note that $\frac{-1}{x^2} x^2 - 12x - 121 = f(x+36)$ | | | |
| | | 1 1 1 1 1 | 1 A few two policies + 1 A few all correct |
| Thus, the transformation is the lettward translation of 50 units. | | (2) | 1A for translation + 1A for all correct |
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| | | | × |
| | | | |
| 54 | | | |
| | $555 = 666 + (38 - 1)d$ $d = -3$ The common difference of the sequence $= \frac{555 - 666}{38 - 1}$ $= -3$ $\frac{n}{2}(2(666) + (n - 1)(-3)) > 0$ $1335n - 3n^2 > 0$ $n(n - 445) < 0$ $0 < n < 445$ Thus, the greatest value of n is 444. $f(x)$ $= \frac{-1}{3}x^2 + 12x - 121$ $= \frac{-1}{3}(x^2 - 36x) - 121$ $= \frac{-1}{3}(x^2 - 36x + 18^2 - 18^2) - 121$ $= \frac{-1}{3}(x - 18)^2 - 13$ Thus, the coordinates of the vertex are $(18, -13)$. $g(x)$ $= f(x) + 13$ $= \frac{-1}{3}(x - 18)^2$ Note that $\frac{-1}{3}x^2 - 12x - 121 = f(-x)$. Thus, the transformation is the reflection with respect to the y -axis. Note that $\frac{-1}{3}x^2 - 12x - 121 = f(x + 36)$. Thus, the transformation is the leftward translation of 36 units. | $555 = 666 + (38 - 1)d$ $d = -3$ The common difference of the sequence $= \frac{555 - 666}{38 - 1}$ $= -3$ $\frac{n}{2}(2(666) + (n - 1)(-3)) > 0$ $1335n - 3n^2 > 0$ $n(n - 445) < 0$ $0 < n < 445$ Thus, the greatest value of n is 444. $f(x)$ $= \frac{-1}{3}(x^2 - 36x) - 121$ $= \frac{-1}{3}(x^2 - 36x + 18^2 - 18^2) - 121$ $= \frac{-1}{3}(x - 18)^2 - 13$ Thus, the coordinates of the vertex are $(18, -13)$. $g(x)$ $= f(x) + 13$ $= \frac{-1}{3}(x - 18)^2$ Note that $\frac{-1}{3}x^2 - 12x - 121 = f(-x)$. Thus, the transformation is the reflection with respect to the y -axis. Note that $\frac{-1}{3}x^2 - 12x - 121 = f(x + 36)$. Thus, the transformation is the leftward translation of 36 units. | $ \frac{555 = 666 + (38-1)d}{d = -3} \qquad 1M \\ 1A $ The common difference of the sequence $ \frac{555 - 666}{38-1} = 1M \\ = -3 $ $ \frac{n}{2}(2(666) + (n-1)(-3)) > 0 $ $ 1335n - 3n^2 > 0 \\ n(n - 445) < 0 \\ 0 < n < 445 $ Thus, the greatest value of n is 444. $ \frac{1A}{3} = \frac{1}{3}(x^2 - 36x + 18^2 - 18^2) - 121 $ $ \frac{-1}{3}(x - 18)^2 - 13 $ Thus, the coordinates of the vertex are $(18, -13)$. $ \frac{1A}{3} = \frac{1}{3}(x - 18)^2 - 13 $ Thus, the transformation is the reflection with respect to the y -axis. $ \frac{1A + 1A}{3} = \frac{1}{3}(x - 18) + 13 = \frac{1}{3}(x - 18)^2 $ Thus, the transformation is the leftward translation of 36 units. $ \frac{1A + 1A}{3} = \frac{1}{3}(x - 18) + 13 = \frac{1}{3}(x - 18) + 14 = \frac$ |

| | Solution | Marks | Remarks |
|-----|--|-----------|--------------|
| (a) | By sine formula, $ \frac{AB}{\sin \angle ADB} = \frac{BD}{\sin \angle BAD} $ $ \frac{10}{\sin \angle ADB} = \frac{15}{\sin 86^{\circ}} $ $ \angle ADB \approx 41.68560132^{\circ} \text{ or } \angle ADB \approx 138.3143987^{\circ} \text{ (rejected)} $ $ \angle ABD = 180^{\circ} - \angle BAD - \angle ADB $ | 1M | 5 |
| | $\angle ABD \approx 52.31439868^{\circ}$ $\angle ABD \approx 52.3^{\circ}$ | 1A | r.t. 52.3° |
| | By cosine formula, $CD^2 = BC^2 + BD^2 - 2(BC)(BD)\cos \angle CBD$ | 1M | |
| | $CD^2 \approx 8^2 + 15^2 - 2(8)(15)\cos 43^\circ$ $CD \approx 10.65246974$ $CD \approx 10.7 \text{ cm}$ | 1A (4) | r.t. 10.7 cm |
| (b) | Since $AC^2 + BC^2 = AB^2$, we have $\angle ACB = 90^\circ$. | | |
| | By cosine formula, $AD^2 = AB^2 + BD^2 - 2(AB)(BD)\cos \angle ABD$ $AD^2 \approx 10^2 + 15^2 - 2(10)(15)\cos 52.31439868^\circ$ $AD \approx 11.89964475$ | | , |
| | By cosine formula, $AD^{2} = AC^{2} + CD^{2} - 2(AC)(CD)\cos \angle ACD$ $\cos \angle ACD \approx \frac{6^{2} + (10.65246974)^{2} - (11.89964475)^{2}}{2(6)(10.65246794)}$ $\angle ACD \approx 86.46867599^{\circ}$ | | * |
| | So, $\angle ACD$ is not a right angle. Hence, the angle between AB and the face BCD is not $\angle ABC$. Thus, the claim is disagreed. | 1M 1A | f.t. |
| | Since $AC^2 + BC^2 = AB^2$, we have $\angle ACB = 90^\circ$. | | |
| | By cosine formula, $AD^{2} = AB^{2} + BD^{2} - 2(AB)(BD) \cos \angle ABD$ $AD^{2} \approx 10^{2} + 15^{2} - 2(10)(15) \cos 52.31439868^{\circ}$ $AD^{2} \approx 141.6015451$ | 25 | = |
| | $AC^2 + CD^2 \approx 6^2 + (10.65246974)^2$ $AC^2 + CD^2 \approx 149.4751116$ | | |
| | Hence, we have $AD^2 \neq AC^2 + CD^2$. So, $\angle ACD$ is not a right angle. Hence, the angle between AB and the face BCD is not $\angle ABC$. Thus, the claim is disagreed. | 1M | f.t. |

| THE RESERVE OF THE PERSON NAMED IN | Solution | | Marks | Remarks |
|------------------------------------|---|--|-------|---------|
| Note | Note that J is the centre of the circle OPQ . | | | |
| | $\angle IPO = \angle IPQ$ (in-centre of Δ) | | | |
| | Also note that P , I and J are collinear. | | | |
| | $\angle JPO = \angle JPQ$ | | | |
| | =JP | (radii) | | |
| | $OP = \angle JPO$ | (base ∠s, isos. △) | | |
| | =JQ | (radii) | | |
| | $PQ = \angle JQP$ | (base ∠s, isos. Δ) | | |
| | $OP = \angle JQP$ | (0000 220, 1000. 23) | | |
| | = JP | (common side) | | |
| | $OP \cong \Delta JQP$ | (AAS) | | |
| | s, we have $OP = PQ$. | (corr. sides, ≅∆s) | | |
| 1110 | s, we have '01 - 1 g . | (6011. 51405, =23) | | |
| Note | e that J is the centre of the ci | | | |
| ∠II | $PO = \angle IPQ$ | (in-centre of Δ) | | |
| Also | o note that P , I and J are constant. | ollinear. | | |
| $\angle JI$ | $PO = \angle JPQ$ | 0 | | |
| JP : | =JQ | (radii) | | |
| $\angle J_{\zeta}$ | $QP = \angle JPQ$ | (base ∠s, isos. △) | | |
| | $= \angle JPO$ | 18 | | |
| 2/1 | $POQ = \angle PJQ$ | (∠at centre twice∠at circumference) | | |
| | $=180^{\circ} - \angle JPQ - \angle JQP$ | $(\angle sum of \Delta)$ | | |
| | $=180^{\circ} - \angle JPQ - \angle JPO$ | | | |
| | $= \angle POQ + \angle OQP$ | $(\angle sum of \Delta)$ | | |
| $\angle P$ | $OQ = \angle OQP$ | | | |
| Thu | s, we have $OP = PQ$. | (sides opp. equal ∠s) | | |
| DT. | 1 7 1 1 01 | | | |
| | e that J is the centre of the ci | 77. | | |
| | $PO = \angle IPQ$ | (in-centre of Δ) | | |
| F | o note that P , I and J are constant. | ollinear. | | |
| | $PO = \angle JPQ$ | / 111 \ | | |
| 1000 | = JP | (radii) | | |
| | $OP = \angle JPO$ | (base \angle s, isos. \triangle) | | |
| | =JQ | (radii) | | |
| | $PQ = \angle JQP$ | (base ∠s, isos. ∆) | | |
| | $OP = \angle JQP$ | / III \ | | |
| | =JQ | (radii) | | |
| | $OQ = \angle JQO$ | (base ∠s, isos. ∆) | | |
| | $OP - \angle JOQ = \angle JQP - \angle JQC$ |) | | |
| | $OQ = \angle OQP$ | | | |
| Thu | s, we have $OP = PQ$. | (sides opp. equal ∠s) | | |
| Th. Ar | 11 . G.1 | | | |
| | arking Scheme: | h correct reasons | 3 2 | |
| 11 6 | Case 1 Any correct proof with correct reasons. Case 2 Any correct proof without reasons. | | | |
| | Case 3 Incomplete proof with any one correct step and one correct reason. | | | |
| Ca | | | (2) | |
| Ca | | | (3) | |
| Ca | | а | (3) | |
| Ca | | в | (3) | |
| Ca | | in the second se | (3) | |

| | Solution | Marks | Remarks |
|---------|---|----------------|--|
| (b) (i) | Let $(h, 19)$ be the coordinates of P . By (a), we have $h^2 + 19^2 = (40 - h)^2 + (30 - 19)^2$. Solving, we have $h = 17$. | 1M | |
| | Let $x^2 + y^2 + Dx + Ey + F = 0$ be the equation of C . Since C passes through the origin, we have $F = 0$. So, we have $17D + 19E + 650 = 0$ and $40D + 30E + 2500 = 0$. Solving, we have $D = -112$ and $E = 66$. Thus, the equation of C is $x^2 + y^2 - 112x + 66y = 0$. | 1A 1M 1A | for either one $(x-56)^2 + (y+33)^2 = 65^2$ |
| (ii) | Note that the equations of L_1 and L_2 are in the form | | |
| | $y = \frac{3}{4}x + c$, where c is a constant. | | |
| | Putting $y = \frac{3}{4}x + c$ in $x^2 + y^2 - 112x + 66y = 0$, we have | | |
| | $x^{2} + \left(\frac{3}{4}x + c\right)^{2} - 112x + 66\left(\frac{3}{4}x + c\right) = 0$. | 1M | |
| | $25x^2 + (24c - 1000)x + 16c^2 + 1056c = 0$ | | |
| | Since L_1 and L_2 are tangents to C , we have | | |
| | $(24c-1000)^2 - 4(25)(16c^2 + 1056c) = 0.$ | 1M | |
| | $16c^2 + 2400c - 15625 = 0$ | | |
| | (4c - 25)(4c + 625) = 0 -625 | | |
| | $c = \frac{25}{4}$ or $c = \frac{-625}{4}$ | | |
| | Therefore, the equations of L_1 and L_2 are | | |
| | $y = \frac{3}{4}x + \frac{25}{4}$ and $y = \frac{3}{4}x - \frac{625}{4}$ respectively. | 1M | for either one |
| | Note that the coordinates of S , T , U and V are $\left(\frac{-25}{3}, 0\right)$, | | ÷ |
| | $\left(0, \frac{25}{4}\right)$, $\left(\frac{625}{3}, 0\right)$ and $\left(0, \frac{-625}{4}\right)$ respectively. | | |
| | The area of the trapezium $STUV$ $= \frac{1}{2} \left(\left(\frac{625}{3} \right) \left(\frac{625}{4} \right) + \left(\frac{625}{4} \right) \left(\frac{25}{3} \right) + \left(\frac{25}{3} \right) \left(\frac{25}{4} \right) + \left(\frac{25}{4} \right) \left(\frac{625}{3} \right) \right)$ $= \frac{105 625}{6}$ | 1M | $\frac{2(65)}{2} \left(\sqrt{\left(\frac{625}{3}\right)^2 + \left(\frac{-625}{4}\right)^2} + \sqrt{\left(\frac{-25}{3}\right)^2 + \left(\frac{25}{4}\right)^2} \right)$ |
| | ≈ 17.604.16667 | | |
| | > 17 000 Thus, the claim is correct. | 1A (9) | f.t. |
| | | | |
| | 9 | | |
| | | | |
| | | | |

Paper 2

| Question No. | Key | Question No. | Key |
|--------------|--------|--------------|--------|
| 1. | A (47) | 26. | B (37) |
| 2. | A(81) | 27. | C (56) |
| 3. | D (65) | 28. | C (58) |
| 4. | C (87) | 29. | B (69) |
| 5. | A (80) | 30. | B (76) |
| 6. | B (76) | 31. | C (61) |
| 7. | A (62) | 32. | D (40) |
| 8. | C (82) | 33. | A (43) |
| 9. | D (46) | 34. | B (38) |
| 10. | C (69) | 35. | D (47) |
| 11. | D (81) | 36. | B (35) |
| 12. | D (67) | 37. | A (46) |
| 13. | A (81) | 38. | B (49) |
| 14. | C (92) | 39. | A (35) |
| 15. | B (45) | 40. | D (38) |
| 16. | D (80) | 41. | C (45) |
| 17. | A (55) | 42. | A (55) |
| 18. | C (79) | 43. | D (51) |
| 19. | A (59) | 44. | B (52) |
| 20. | C (51) | 45. | C (50) |
| 19 | D (55) | | |
| 21. | B (57) | | |
| 22. | D (54) | | |
| 23. | A (82) | | |
| 24. | B (64) | | |
| 25. | D (35) | | |

Note: Figures in brackets indicate the percentages of candidates choosing the correct answers.