

## Op-Amp Introduction.

- Op-amps (amplifiers/buffers in general) are drawn as a triangle in a circuit schematic. - They are nearly ideal.

- Two inputs:

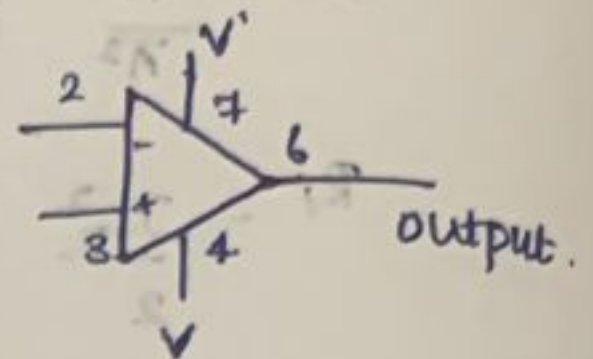
Inverting and Non-Inverting.

- One output.

- Also power connections. [no explicit ground].

2  $\rightarrow$  inverting terminal (input)

3  $\rightarrow$  non-inverting (positive) terminal (input)



- There will be divot on pin-1. end.

The ideal op-amp.

Characteristics.

- It has a infinite voltage gain.

- means diff. b/w the positive terminal and negative terminal is amplified by 200,000.

[which transistor used as op-amp].

- Infinite input impedance.

- no current flow into input  $\rightarrow 10^{12} \Omega$  for FET input op-amp.

- It has a zero output impedance.

current max. (usually 5-25 mA).

- Infinitely fast (infinite bandwidth).

- in truth, limited to few MHz range.

- Slew rate limited to  $0.5 \rightarrow 20 \text{ V}/\mu\text{s}$ .

op-amp without feedback.

The internal op-amp formula:  $V_{out} = A(V_+ - V_-)$

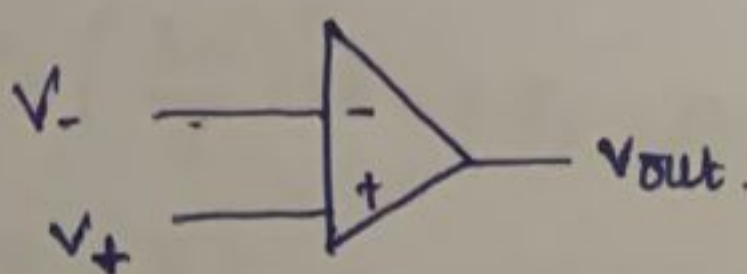
$\rightarrow$  symbol  $\Rightarrow A$ .

$$V_{out} = \text{gain} \times (V_+ - V_-) \Rightarrow V_{out} = A \times (V_+ - V_-)$$

$\therefore V_+$  is greater than  $V_-$  so, output  $\rightarrow +ve$ .

if,  $V_-$  greater than  $V_+$ , the output  $\rightarrow -ve$ .

Max & min. voltage is fixed (+15 & -15 resp.).



A gain of 200,000, device is useless. Practically.



## OP-AMP Characteristics.

**Slew Rate:** Maximum rate of change of output voltage vs time.

Let the signal be a sine wave  $v(t) = k \sin 2\pi ft$ .

The rate of change of signal w.r.t time is  $\frac{dv}{dt} = 2\pi f k \cos 2\pi ft$

Max. rate of change  $\frac{dv}{dt} = 2\pi f k$

$$\text{slew rate required} = \boxed{2\pi f_{\max} V_p}$$

$f_{\max}$  is the highest signal frequency and  $V_p$  is the maximum output voltage required to be supported by the op-amp.

Ex: 1. An op-amp having a <sup>1</sup>slew rate of  $SR = 2 \text{ V/}\mu\text{s}$ , what is the maximum closed-loop voltage gain that can be used when the input signal varies by  $0.5 \text{ V}$  in  $10 \mu\text{s}$ ?

Soln: For voltage gain  $A$ ,  $V_o = AV_i \Rightarrow \frac{\Delta V_o}{\Delta t} = A \frac{\Delta V_i}{\Delta t}$

$$\Rightarrow A = \frac{\frac{\Delta V_o}{\Delta t}}{\frac{\Delta V_i}{\Delta t}} = \frac{SR}{\frac{\Delta V_i}{\Delta t}} = \frac{2}{0.5/10} = 40.$$



common mode rejection

- The common signal is rejected while the difference of the signals is amplified.
- Noise is common to both inputs, and hence is attenuated via the differential connections.
- This feature is known as common mode rejection ratio (CMRR).
- Ideally CMRR should be infinite.

$$CMRR = A_d / A_c$$

$$CMRR (dB) = 20 \log_{10} (A_d / A_c)$$

It is a measure of how well the op-amp suppresses the ideal signals.

Problem 1: An op-amp with a differential gain of  $A_d = 4000$  is supplied with input voltages of  $V_{i1} = 150 \mu V$  and  $V_{i2} = 140 \mu V$ .

The output voltage is given by

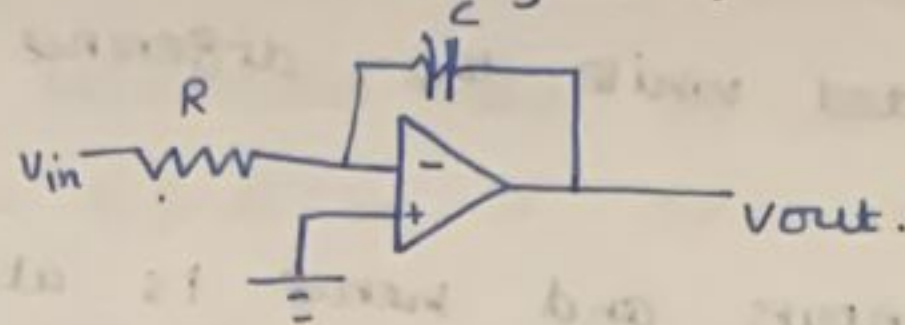
$$V_o = A_d V_d + A_c V_c = A_d V_d \left( 1 + \frac{A_c V_c}{A_d V_d} \right) \Rightarrow V_o = A_d V_d \left( 1 + \frac{1}{CMRR} \frac{V_c}{V_d} \right)$$

a.  $CMRR = 100$

$$V_o = A_d V_d \left( 1 + \frac{1}{CMRR} \frac{V_c}{V_d} \right) = 4000 \times 10$$



Low pass filter (integrator)



$$I_f = V_{in}/R, \text{ so } C \cdot dV \text{ cap } / dt = V_{in}/R.$$

$$i = \frac{V_{in}}{R} = \frac{dQ}{dt} = \frac{C dV_o}{dt} \quad Q = CV_o$$

$$dV_o = \frac{V_{in}}{RC} dt.$$

$$V_o = \frac{1}{RC} \int V_{in} dt.$$

Subtractor - Differencing Amplifier:

The non-Inverting input:

$$V_{node} = \frac{V^+ R_2}{(R_1 + R_2)}$$

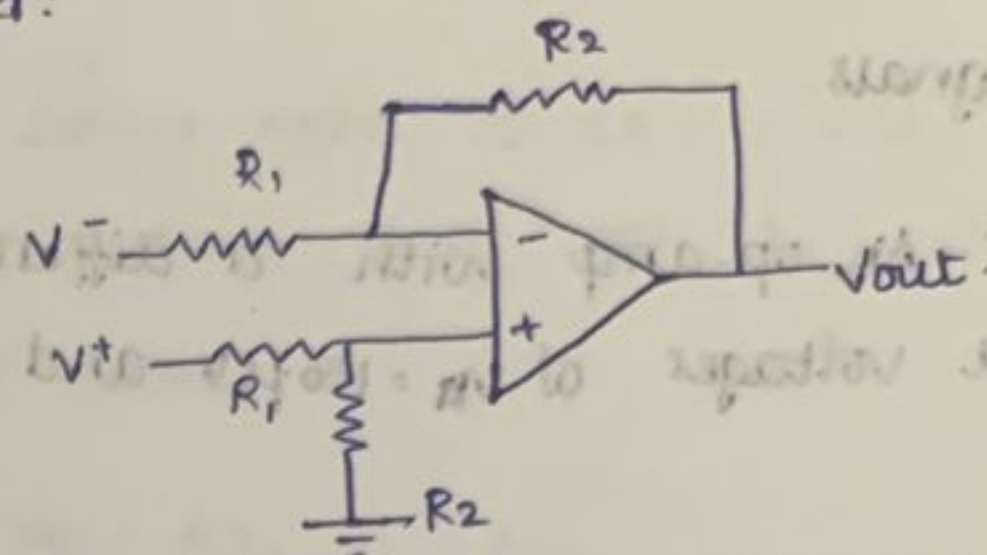
$$\text{So } I_f = (V^- - V_{node}) / R_1$$

$$V_{out} = V_{node} - I_f R_2$$

$$= V^+ (1 + R_2/R_1) (R_2 / (R_1 + R_2)) - V^- (R_2/R_1)$$

$$\text{So, } V_{out} = \left( \frac{R_2}{R_1} \right) (V^+ - V^-).$$

↳ voltage gain



Differential mode operation.

$$V_o = A_d V_i$$

↳ differential.  
↳ gain

$$[V_o = A_d V_i]$$

$A_d$  typically very large.

Common mode operation:

$$V_o = A_c V_i$$

$$A_c \ll A_d$$

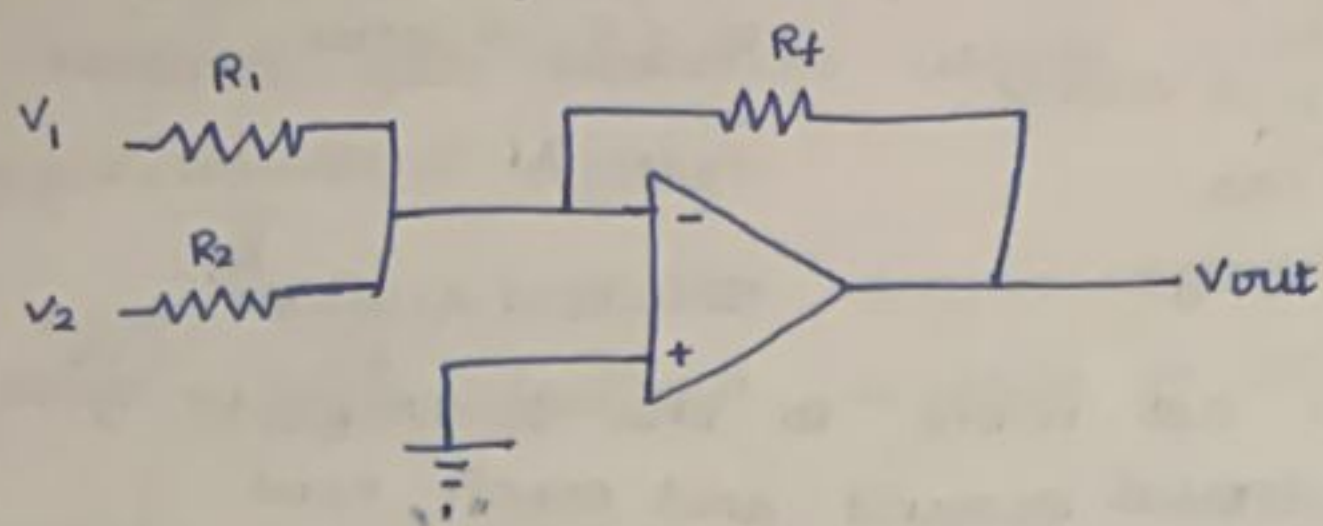
$$\text{output voltage} = V_o = A_d V_d + A_c V_c$$

$$V_d = (V_{i1} - V_{i2}), \quad V_c = (V_{i1} + V_{i2}) / 2$$

$$A_d \gg A_c,$$



## Summing Amplifiers:



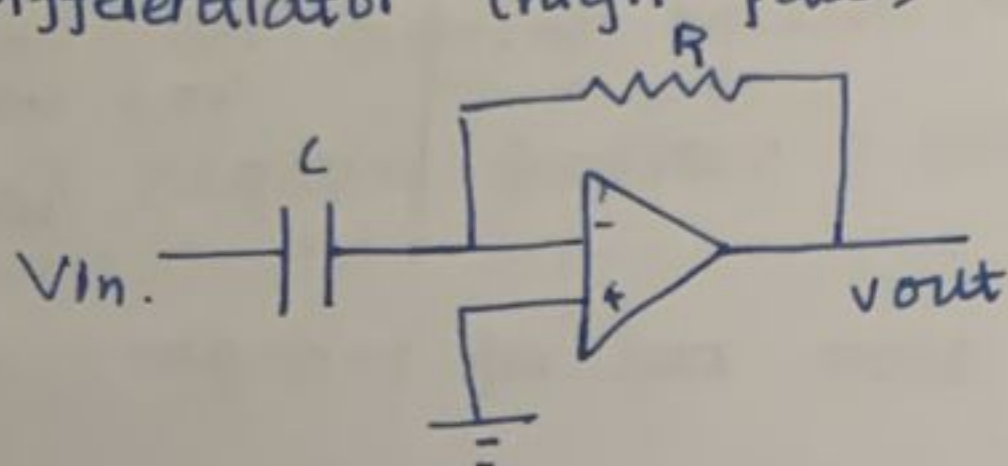
inverting input still held at virtual ground.

$I_1$  and  $I_2$  are added together to run through  $R_f$ .

$$V_{out} = R_f \times (V_1/R_1 + V_2/R_2)$$

If  $R_2 = R_1$  we get a sum proportional to  $(V_1 + V_2)$ .

## Differentiator (high-pass)



$$Q = CV \quad I_{cap} = \frac{dQ}{dt} = C \cdot dV/dt$$

$$\text{Thus, } V_{out} = -I_{cap} R = -RC \cdot dV/dt$$

- If signal is  $v_o \sin \omega t$ ,  $V_{out} = -v_o RC \omega \cos \omega t$

- the  $\omega$ -dependence means higher frequencies amplified more.

$$i = \frac{dQ}{dt} = C \frac{dV_{in}}{dt}$$

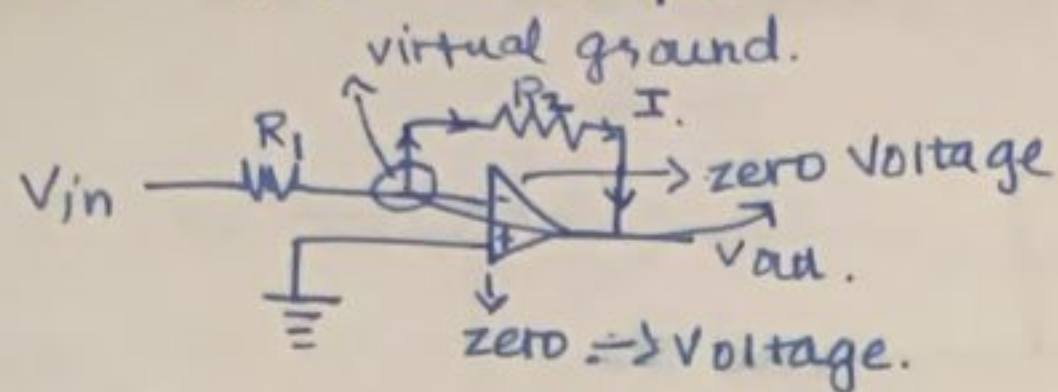
$$V_{in} = \sin \omega t$$

$$i = \frac{V_o}{R} = C \frac{dV_{in}}{dt}$$

$$V_o = -RC \cdot \frac{dV_{in}}{dt}$$



## Inverting amplifier example:



$R_1$  &  $R_2 \rightarrow$  series.

$$I \text{ in } R_1 \rightarrow \frac{0 - V_{in}}{R_1} = -\frac{V_{in}}{R_1}$$

$$I \text{ in } R_2 \rightarrow \frac{v_{out} - 0}{R_2} = \frac{v_{out}}{R_2}$$

current will not move to the opamp, it goes through the virtual ground and reach  $v_{out}$ .

inverting  $\rightarrow$  positive input.

$\Downarrow$   
negative output.

$$v_{out} = 0 - v_{in} \times (R_2 / R_1)$$

$$= -v_{in} (R_2 / R_1)$$

We amplify  $v_{in}$  by factor  $-R_2 / R_1$ .

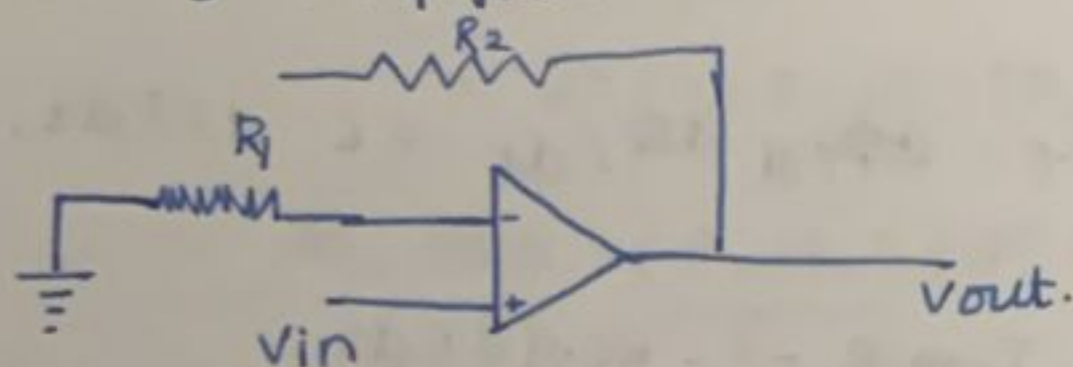
$$\therefore V_o = -\frac{R_2}{R_1} v_{in}$$

$$V_o = \text{Gain } v_{in}$$

$$\therefore \text{gain} = \left( -\frac{R_2}{R_1} \right)$$

$\downarrow$   
inverting.

## Non-inverting Amplifier.



$v_{in}$  in positive terminal.

$$R_1 \text{ is } I = v_{in} / R_1$$

$$R_2 \text{ is } I, R_2 = v_{in} \times (R_2 / R_1)$$

$$v_{out} = v_{in} + v_{in} \times (R_2 / R_1) = v_{in} \times (1 + R_2 / R_1)$$

$$\left[ \begin{array}{l} v_{in} = v_o \frac{R_1}{R_1 + R_2} \Rightarrow v_o = \left( \frac{R_1 + R_2}{R_1} \right) v_{in} \\ \therefore v_o = \left( 1 + \frac{R_2}{R_1} \right) v_{in} \end{array} \right]$$

current is sourced from op-amp output. in the above example.



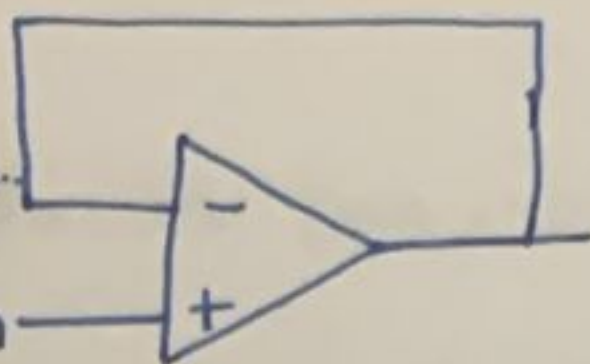
Infinite gain in negative feedback

• Infinite gain would be useless except in the self-regulated negative feedback regime.

positive feedback  $\rightarrow$  runaway or oscillation  $\rightarrow$  very bad.

negative feedback  $\rightarrow$  leads to stability.

output to  
inverting  
terminal.



negative feedback loop

• output ~~negative~~ greater than  $V_{in}$  - negative

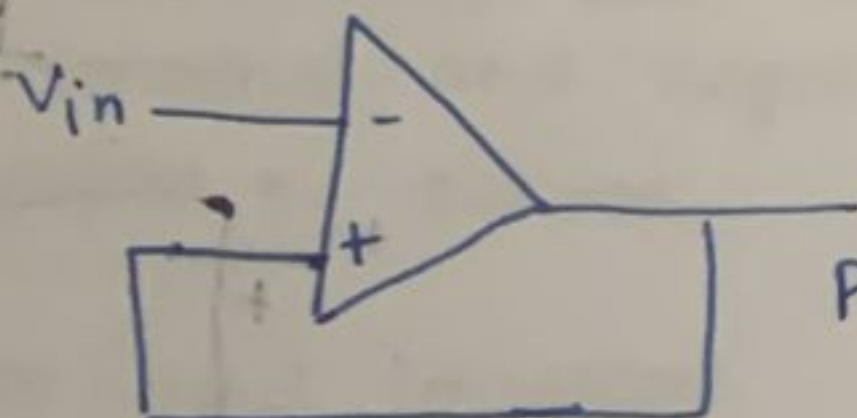
• output less than  $V_{in} \rightarrow$  positive

$$V_o = A(V_{in}^+ - V_{in}^-)$$

- If we give to positive feedback, the output will shoot the extreme saturation value.

- negative feedback  $\rightarrow$  oscillated b/w positive and negative.

- negative feedback make it self-working.



positive feedback: BAD.

Makes the positive terminal even more positive.

System will immediately "rail" at the supply voltage.

Op-amp rules:

configured in any negative feedback arrangement:

- The inputs to the op-amp ~~output~~ draw or source no current.

- The op-amp output will do whatever it can to make the voltage difference b/w the two inputs zero.

[one terminal is always grounding].



