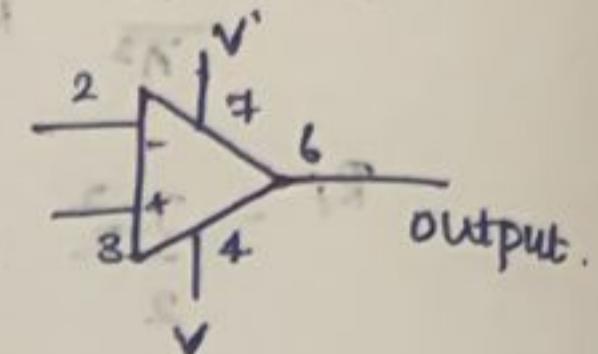


OP-Amp Introduction.

- Op-amps (amplifiers / buffers in general), are drawn as a triangle in a circuit schematic. - They are nearly ideal.
- Two inputs:
 - Inverting and Non-inverting.
- One output.
- Also power connections. [no explicit ground].

2 → inverting terminal (input)

3 → non-inverting (positive) terminal (input)



- There will be divot on pin-1 end.

The ideal op-amp.

Characteristics.

- It has a infinite voltage gain.

- means diff. b/w the positive terminal and negative terminal is amplified by 200,000.

[which transistor used as op-amp].

- Infinite input impedance.

- no current flow into input $\rightarrow 10^{12} \Omega$ for FET input op-amp.

- It has a zero output impedance.

current max. (usually 5-25 mA).

- Infinitely fast (infinite bandwidth).

- in truth, limited to few MHz range.

- Slew rate limited to $0.5 \text{ to } 20 \text{ V/}\mu\text{s}$.

Op-amp without feedback.

The internal op-amp formula:

\rightarrow symbol $\Rightarrow A$.

$$V_{out} = \text{gain} \times (V_+ - V_-) \Rightarrow V_{out} = A \times (V_+ - V_-)$$

$\therefore V_+$ is greater than V_- so, output $\rightarrow +ve$.

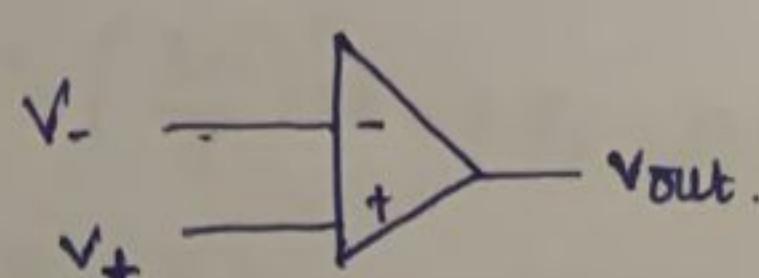
if, V_- greater than V_+ , the output $\rightarrow -ve$.

Max & min.

voltage is

fixed ($+15$ &

-15 resp.).



A gain of 200,000, device is useless. Practically.

OP-AMP Characteristics.

Slew Rate: Maximum rate of change of output voltage vs time.

Let the signal be a sine wave $v(t) = k \sin 2\pi ft$.

The rate of change of signal w.r.t time is $\frac{dv}{dt} = 2\pi f k \cos 2\pi ft$

$$\text{Max. rate of change } \frac{dv}{dt} = 2\pi f k$$

$$\text{Slew rate required} = \boxed{2\pi f_{\max} V_p}$$

f_{\max} is the highest signal frequency and V_p is the maximum output voltage required to be supported by the op-amp.

Ex:1. An op-amp having a slew rate of $SR = 2 \text{ V/s}$, what is the maximum closed-loop voltage gain that can be used when the input signal varies by 0.5 V in 10s ?

$$\underline{\text{Soln}}: \text{For voltage gain } A, V_o = AV_i \Rightarrow \frac{\Delta V_o}{\Delta t} = A \frac{\Delta V_i}{\Delta t}$$

$$\Rightarrow A = \frac{\frac{\Delta V_o}{\Delta t}}{\frac{\Delta V_i}{\Delta t}} = \frac{\frac{SR}{\Delta V_i}}{\frac{\Delta t}{\Delta t}} = \frac{2}{0.5 / 10} = 40.$$

common mode rejection

- The common signal is rejected while the difference of the ^{singal} _{V_d} is amplified.
- Noise is common to both inputs, and hence is attenuated via the differential connections.
- This feature is known as common mode rejection ratio (CMRR).
- Ideally CMRR should be infinite.

$$CMRR = A_d / A_c$$

$$CMRR (\text{dB}) = 20 \log_{10} (A_d / A_c)$$

It is a measure of how well the op-amp suppresses the ideal signals.

Problem 1: An op-amp with a differential gain of $A_d = 4000$ is supplied with input voltages of $v_{in} = 150 \mu\text{V}$ and $v_{d} = 40 \mu\text{V}$.

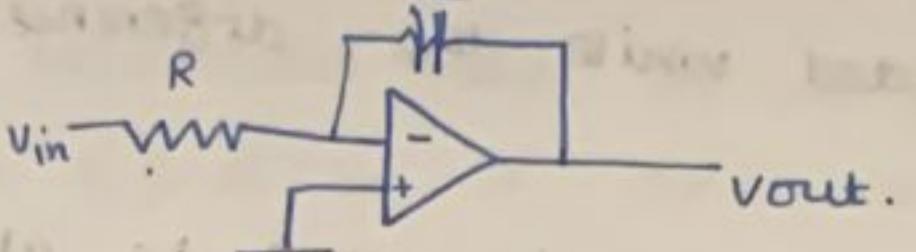
The output voltage is given by

$$v_o = A_d v_d + A_c v_c = A_d v_d \left(1 + \frac{A_c v_c}{A_d v_d} \right) \Rightarrow v_o = A_d v_d \left(1 + \frac{1}{CMRR} \frac{v_c}{v_d} \right)$$

a. $CMRR = 100$

$$v_o = A_d v_d \left(1 + \frac{1}{100} \frac{v_c}{v_d} \right) = 4000 \times 10^{-6} \times 40 \times 10^{-6} \times 100 = 16 \mu\text{V}$$

Low pass filter (integrator)



$$I_f = V_{in}/R, \text{ so } C \cdot dV \text{ cap } / dt = V_{in}/R.$$

$$i = \frac{V_{in}}{R^3} \quad i = \frac{dQ}{dt} = \frac{C dV_o}{dt} \quad Q = C V_o$$

$$dV_o = \frac{V_{in}}{CR} dt.$$

$$V_o = \frac{1}{RC} \int V_{in} dt.$$

Subtractor - Differentiating Amplifier:

The non-inverting input:

$$V_{node} = \frac{V^+ R_2}{(R_1 + R_2)}$$

$$\text{So } I_f = (V^- - V_{node}) / R_1$$

$$V_{out} = V_{node} - I_f R_2$$

$$= V^+ (1 + R_2/R_1) [R_2 / (R_1 + R_2)] - V^- (R_2/R_1)$$

$$\text{So, } V_{out} = \frac{(R_2/R_1)(V^+ - V^-)}{1 + R_2/R_1}$$

$\xrightarrow{\text{voltage gain}}$

Differential mode operation:

$$V_o = Ad(V_i) \quad \begin{matrix} \nearrow \text{differential} \\ \downarrow \text{gain} \end{matrix} \quad \left(\frac{\Delta V}{\Delta V} \right) \quad [V_o = Ad(V_i)]$$

Ad typically very large.

Common mode operation:

$$V_o = A_c V_i$$

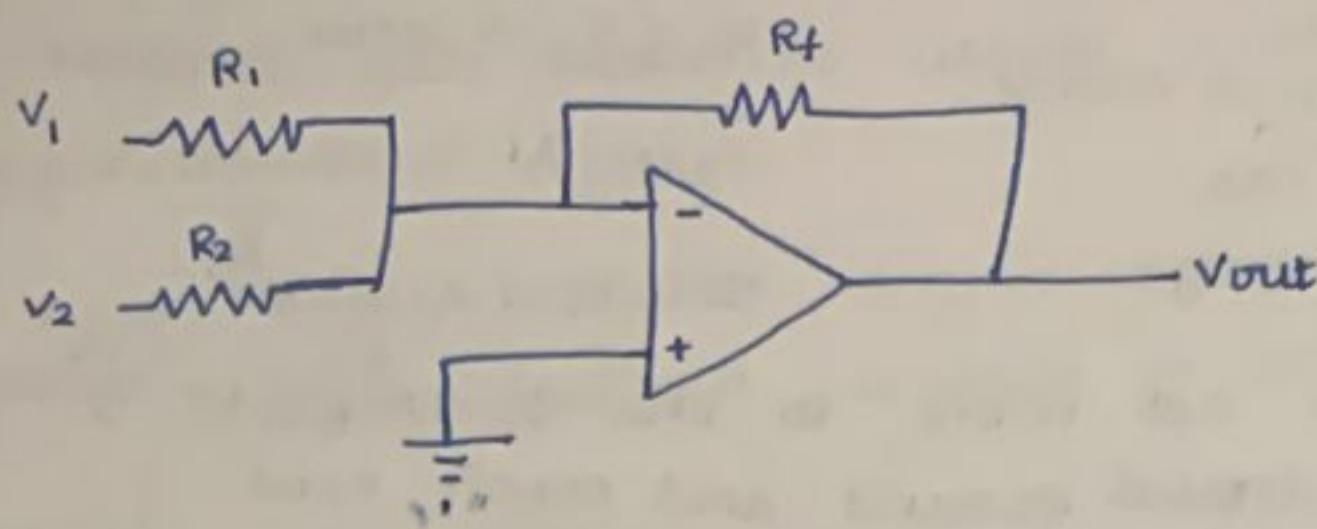
$$A_c \ll Ad$$

$$\text{output voltage } V_o = Ad V_d + A_c V_c$$

$$V_d = (V_{i1} - V_{i2}), V_c = (V_{i1} + V_{i2})/2$$

$$Ad \gg A_c$$

Summing Amplifiers:



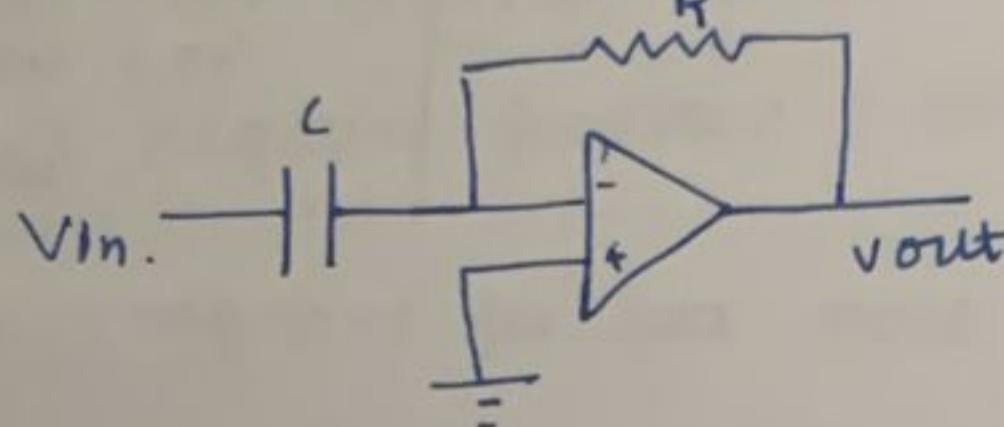
inverting input still held at virtual ground.

I_1 and I_2 are added together to run through R_f .

$$V_{out} = R_f \times (v_1/R_1 + v_2/R_2)$$

If $R_2 = R_1$ we get a sum proportional to $(v_1 + v_2)$.

Differentiator (high-pass)



$$Q = CV \quad I_{cap} = \frac{dQ}{dt} \quad dQ/dt = C \cdot dV/dt.$$

$$\text{Thus, } V_{out} = -I_{cap} R = -RC \cdot dV/dt.$$

-If signal is $v_0 \sin \omega t$, $V_{out} = -v_0 R C \omega \cos \omega t$

-the ω -dependence means higher frequencies amplified more.

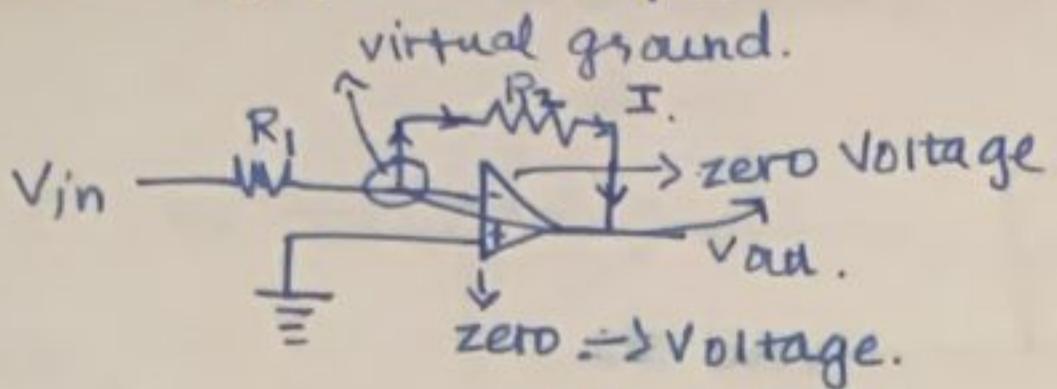
$$i = \frac{-dQ}{dt} = C \frac{dV_{in}}{dt}$$

$$V_{in} = \sin \omega t$$

$$i = \frac{V_0}{R} = C \frac{dV_{in}}{dt}$$

$$V_0 = -RC \cdot \frac{dV_{in}}{dt}$$

Inverting amplifier example:



current will not move to the opamp, it goes through the virtual ground and reach V_{out} .

$R_1 \& R_2 \rightarrow$ series.

$$I \text{ in } R_1 \rightarrow 0 - V_{in} = -\frac{V_{in}}{R_1}$$

$$I \text{ in } R_2 \rightarrow \frac{V_{out} - 0}{R_2} = \frac{V_{out}}{R_2}$$

Inverting \rightarrow positive input.

\Downarrow
negative output.

$$V_{out} = 0 - V_{in} \times (R_2 / R_1)$$

$$= -V_{in} (R_2 / R_1)$$

We amplify V_{in} by factor

$$-R_2 / R_1$$

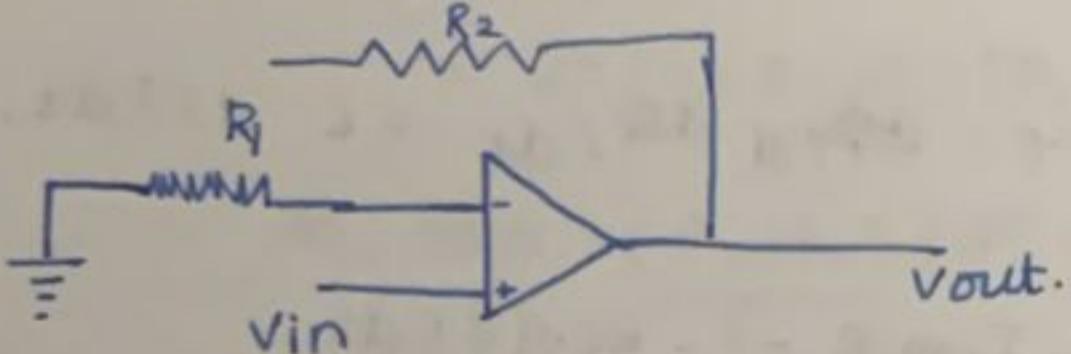
$$\therefore V_o = -\frac{R_2}{R_1} V_{in}$$

$$V_o = \text{Gain } V_{in}$$

$$\therefore \text{Gain} = \frac{-R_2}{R_1}$$

inverting.

Non-inverting Amplifier.



V_{in} in positive terminal.

$$R_1 \text{ is } I = V_{in} / R_1$$

$$R_2 \text{ is } I, R_2 = V_{in} \times (R_2 / R_1)$$

$$V_{out} = V_{in} + V_{in} \times (R_2 / R_1) = V_{in} \times (1 + R_2 / R_1)$$

$$\left[\begin{array}{l} \cancel{R_2} V_{in} = V_o \frac{R_1}{R_1 + R_2} \Rightarrow V_o = \left(\frac{R_1 + R_2}{R_2} \right) V_{in} \\ \therefore V_o = \left(1 + \frac{R_2}{R_1} \right) V_{in} \end{array} \right]$$

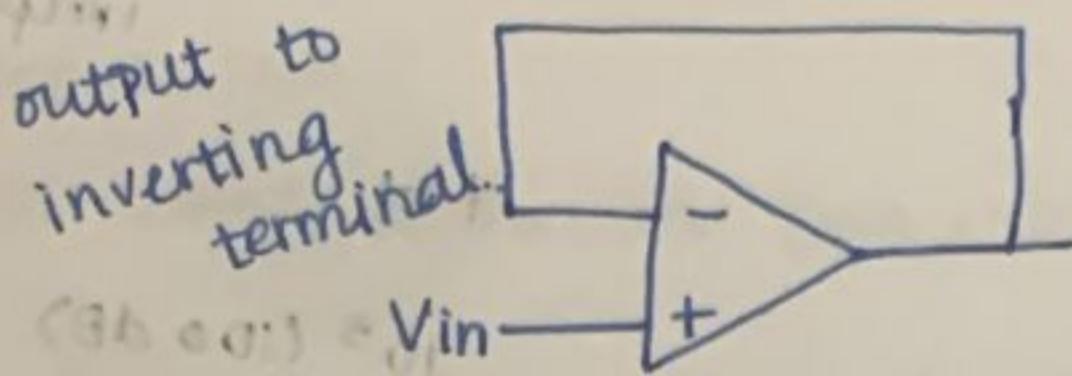
current is sourced from op-amp output. in the above example.

infinite gain in negative feedback

- infinite gain would be useless except in the self-regulated negative feedback regime.

positive feedback \rightarrow runaway or oscillation \rightarrow very bad.

negative feedback \rightarrow leads to stability.



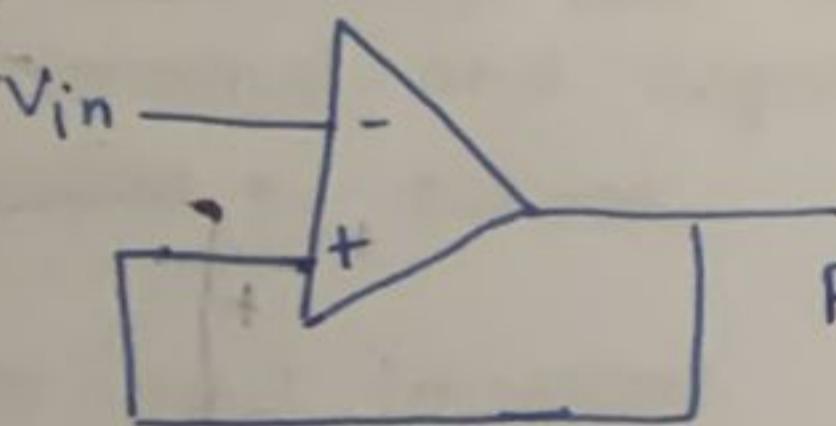
negative feedback loop

- output negative greater than V_{in} - negative
- output less than V_{in} \rightarrow positive

- If we give to positive feedback, the output will shoot the extreme saturation value.

- negative feedback \rightarrow oscillated b/w positive and negative.

- negative feedback make it self-working.



positive feedback: BAD.

Makes the positive terminal even more positive. System will immediately "rail" at the supply voltage.

Op-amp rules:

configured in any negative feedback arrangement:

- The inputs to the op-amp must draw or source no current.
- The op-amp output will do whatever it can to make the voltage difference b/w the two inputs zero.

[one terminal is always grounding].

• The external resistance are much larger than R_o and much smaller than R_i [Assume: $R_i \rightarrow \infty$, $R_o \rightarrow 0$]

Ideal op-amp \rightarrow Input is ∞ .

Amt. of current flow through the op-amp is zero, but it is flowing outside.
 \downarrow
 coz of ∞ input impedance.

Parameter Ideal OP-amp

$+V_1$

A_v ∞

10^5 (100 dB)

R_i ∞

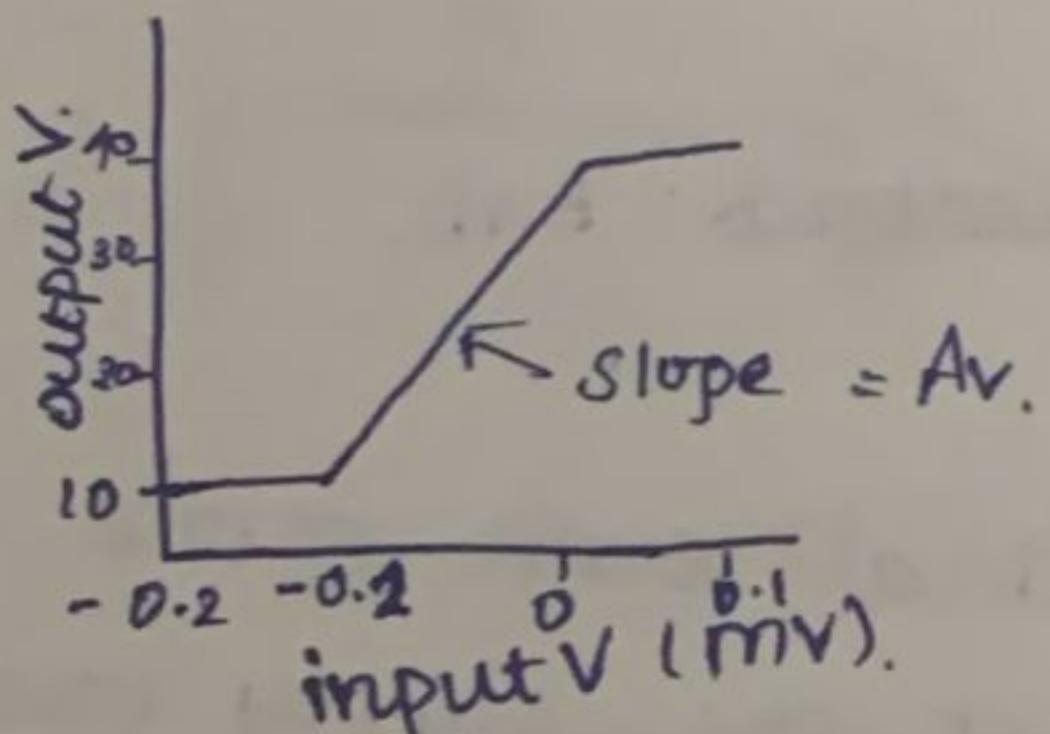
$2M\Omega$

R_o 0

$+5\Omega$

V_{cc} and V_{ee} \downarrow pin \downarrow pin } \rightarrow supply voltage. block diagrams.

Graph:



i.e., v_+ as $\frac{1}{1}$
 v_- as $\frac{1}{0.0001}$.

v_+ is 1.0001 } $\rightarrow 10V$.
 v_- is 1.

