Number Theory Resources

Number Theory

Shafayater Blog: [Link]
 This is a great website for learning. Try to spend time on this website to learn new topics.
 forthright48.com: [Link]
 This website almost covers all topics of number theory.
 www.progkriya.org: [Link]
 Number Theory: [Link]

N.B: Take your time to understand these topics. Feel free to discuss with your friend if you do not understand anything clearly.

1.Seive(): Finding primes in a range

```
//seive().cpp
#include<bits/stdc++.h>
using namespace std;
#define mx 10000010
bool flag[mx];
int primes[mx];
int seive(int n)
    int sq=sqrt(n);
    flag[1]=1;
    for(int i=4;i<=n;i+=2)flag[i]=1;</pre>
    for(int i=3;i<=sq;i+=2){</pre>
        if(flag[i] == 0){
            for(int j=2*i;j<=n;j+=i)</pre>
                flag[j]=1;
        }
    }
    int count=0;
    cout<<"Number of primes in the range of 1 to N: ";</pre>
    for(int i=1;i<=n;i++){</pre>
        if(flag[i]==0)count++;
    }
    cout<<count<<endl;</pre>
```

```
return count;
}
int main()
{
    int n;
    while(1){
        cin>>n;
        seive(n);
    }
}
// if N 100 Total Primes: 25
// if N 1000 Total Primes: 168
// if N 1000000 Total Primes: 78498
```

2. Number of divisor of a number N.

```
//NumberOfDivisors.cpp
#include<bits/stdc++.h>
using namespace std;
#define mx 10000010
bool flag[mx];
int primes[mx];
int seive(int n)
    int sq=sqrt(n);
    flag[1]=1;
    for(int i=4;i<=n;i+=2)flag[i]=1;</pre>
    for(int i=3;i<=sq;i+=2){</pre>
        if(flag[i]==0){
            for(int j=2*i;j<=n;j+=i)</pre>
               flag[j]=1;
       }
    }
    int count=0;
    for(int i=1;i<=n;i++){</pre>
        if(flag[i]==0){
           primes[count++]=i;
       }
    }
}
int divisor (int n)
    int sq=sqrt(n), sum=1;
    for(int i=0;primes[i]<=sq;i++){</pre>
        if(n%primes[i] == 0){
```

```
int count=0;
           while(n%primes[i]==0){
               n/=primes[i];
               count++;
           //cout<<pre><<pre>fi]<<<' '<<count<<endl;</pre>
           sum=sum*(count+1);
       }
   }
   if(n>1){
       sum=sum*2;
   return sum;
}
int main()
{
   seive(100000);
   int n;
   while(cin>>n){
        cout<<"Number of divisor of "<<n<<" are: "<<divisor(n)<<endl;;</pre>
   }
}
// 5 No Of divisor:2
// 8 No Of divisor:4
// 100 No Of divisor:9
// 568 No Of divisor:8
// 48 No Of divisor:10
```

2.Sum of divisor of a number N.

```
//SumOfDivisors.cpp
#include<bits/stdc++.h>
using namespace std;
#define mx 10000010
bool flag[mx];
int primes[mx];
int seive(int n)
{
    int sq=sqrt(n);
    flag[1]=1;
    for(int i=4;i<=n;i+=2)flag[i]=1;</pre>
    for(int i=3;i<=sq;i+=2){</pre>
        if(flag[i]==0){
            for(int j=2*i;j<=n;j+=i)</pre>
               flag[j]=1;
       }
    }
```

```
int count=0;
   for(int i=1;i<=n;i++){</pre>
       if(flag[i]==0){
           primes[count++]=i;
       }
   }
}
int divisor_sum (int n)
   int sq=sqrt(n), sum=1, p=1,s;
   for(int i=0;primes[i] <= sq; i++){</pre>
       if(n%primes[i] == 0){
           p=1;
           while(n%primes[i]==0){
               n/=primes[i];
               p*=primes[i];
           }
           p*=primes[i];
           sum*=(p-1)/(primes[i]-1);
       }
   }
   if(n>1){
       p=n*n;
       s=(p-1)/(n-1);
       sum=sum*s;
   }
   return sum;
}
int main()
{
   seive(100000);
   int n;
   while(cin>>n){
       cout<<"Sum of divisor of "<<n<<" are: "<<divisor_sum(n)<<endl;;</pre>
   }
}
// 48 Sum of Of divisor:124
//72 Sum of Of divisor:195
```