

Access Control Matrix

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- Special Rights
 - Principle of Attenuation of Privilege

Overview

- State of a system

It is the collection of the current values of all memory locations, all secondary storage, all registers and other components of the system.

- Protection state of a system

- The subset of this collection that deals with protection.
- Describes current settings, values of system relevant to protection.

Access Control Matrix (ACM)

- ACM
 - Describes protection state precisely.
 - Matrix describing rights of subjects.
 - State transitions change elements of matrix.
- P - The set of possible protection states.
- $Q \subseteq P$ – Those states in which the system is authorized to reside.
- $(P - Q)$ – System is not secure.

Description

Objects (entities)

Subjects

	o_1	\dots	o_m	s_1	\dots	s_n
s_1						
s_2						
\dots						
s_n						

- Subjects $S = \{ s_1, \dots, s_n \}$
- Objects $O = \{ o_1, \dots, o_m \}$
- Rights $R = \{ r_1, \dots, r_k \}$
- Entries $A[s_i, o_j] \subseteq R$
- $A[s_i, o_j] = \{ r_x, \dots, r_y \}$
means subject s_i has rights
 r_x, \dots, r_y over object o_j

Example 1

- Processes p, q
- Files f, g
- Rights r, w, a, e

	f	g	p	q
p	rwe	r	rwe	w
q	a	re	r	rwe

Example 2

- Procedures *inc_ctr*, *dec_ctr*, *manage*
- Variable *counter*
- Rights $+$, $-$, *call*

	<i>counter</i>	<i>inc_ctr</i>	<i>dec_ctr</i>	<i>manage</i>
<i>inc_ctr</i>	$+$			
<i>dec_ctr</i>	$-$			
<i>manage</i>		<i>call</i>	<i>call</i>	<i>call</i>

Boolean Expression Evaluation

- ACM controls access to database fields
 - Subjects have attributes.
 - Verbs define type of access.
 - Rules associated with objects, verb pair.
- Subject attempts to access object
 - Rule for object, verb evaluated, grants or denies access.

Example

- Subject Annie
 - Attributes role (artist), groups (creative)
- Verb Paint
 - Default 0 (deny unless explicitly granted)
- Object Picture
 - Rule:
Paint: ‘artist’ in subject.role and
‘creative’ in subject.groups and
 $\text{time.hour} \geq 0$ and $\text{time.hour} < 5$

ACM at 3AM and 10AM

At 3AM, time condition met; ACM is:

... picture ...

...	annie	...			
			paint		

At 10AM, time condition not met; ACM is:

... picture ...

...	annie	...			

Access Control By History

- Assume that the database contains N records.
- Users query the database about sets of records C ; this set is the *query set*.
- The goal of attackers is to obtain a statistic for an individual record.
- The *query-set-overlap control* is a prevention mechanism that answers queries only when the size of the intersection of the query set and each previous query set is smaller than some parameter.

History

Database: Set=2

Name	Position	Age	Salary
Alice	Teacher	45	\$40,000
Bob	Aide	20	\$20,000
Cathy	Principal	37	\$60,000
Dilbert	Teacher	50	\$50,000
Eve	Teacher	33	\$50,000

Queries:

1. $\text{sum}(\text{salary}, \text{"Position = Teacher"}) = 140,000$
2. $\text{sum}(\text{salary}, \text{"Age < 40 \& Position = Teacher"})$
3. $\text{sum}(\text{salary}, \text{"Age > 40 \& Position = Teacher"})$ should not be answered (deduce Eve's salary)

ACM of Database Queries

$O_i = \{\text{Union of the objects referenced in query } i\}$

$F(O_i) = \{\text{read}\} \quad |O_i| > 1$

$F(O_i) = \emptyset \quad \text{otherwise}$

Element of the matrix $A[s, o] = F(O_i \cap \{o\})$ for query i ,
where $1 \leq i$ and $O_0 = \emptyset$

C1: $A[\text{asker}, (\text{Alice}, \text{Dilbert}, \text{Eve})] = \{\text{read}\} \quad \text{and} \quad |O_1| = 3$

C2: $A[\text{asker}, \text{Eve}] = \{\text{read}\} \quad \text{and} \quad |O_2| = 1$

C3: $A[\text{asker}, (\text{Alice}, \text{Dilbert})] = \emptyset \quad \text{and} \quad |O_3| = 2$

ACM of Database Queries

$O_i = \{\text{objects referenced in query } i\}$

$F(o_i) = \{\text{read}\}$ for o_j in O_i , if $|\cup_{j=1,\dots,i} O_j| > 1$

$F(o_i) = \emptyset$ for $o_j \in O_i$, otherwise

1. $O_1 = \{\text{Alice, Dilbert, Eve}\}$ and no previous query set,
so:

$A[\text{asker, Alice}] = f(\text{Alice}) = \{\text{read}\}$

$A[\text{asker, Dilbert}] = f(\text{Dilbert}) = \{\text{read}\}$

$A[\text{asker, Eve}] = f(\text{Eve}) = \{\text{read}\}$

and query can be answered.

But Query 2

From last slide:

$F(o_i) = \{ \text{read} \}$ for o_j in O_i , if $|\cup_{j=1,\dots,i} O_j| > 1$

$F(o_i) = \emptyset$ for o_j in O_i , otherwise

2. $O_2 = \{ \text{Alice, Dilbert} \}$ but $|O_2 \cap O_1| = 2$ so

$A[\text{asker, Alice}] = f(\text{Alice}) = \emptyset$

$A[\text{asker, Dilbert}] = f(\text{Dilbert}) = \emptyset$

and query cannot be answered.

State Transitions

- Change the protection state of system
- $\mid-$ represents transition
 - $X_i \mid-_{\tau} X_{i+1}$: command τ moves system from state X_i to X_{i+1}
 - $X_i \mid-^* X_{i+1}$: a sequence of commands moves system from state X_i to X_{i+1}
- Commands often called *transformation procedures*

Primitive Operations

- **create subject s ; create object o**
 - Creates new row, column in ACM; creates new column in ACM
- **destroy subject s ; destroy object o**
 - Deletes row, column from ACM; deletes column from ACM
- **enter r into $A[s, o]$**
 - Adds r rights for subject s over object o
- **delete r from $A[s, o]$**
 - Removes r rights from subject s over object o

Create Subject

- Precondition: $s \notin S$
- Primitive command: **create subject s**
- Postconditions:
 - $S' = S \cup \{ s \}, O' = O \cup \{ s \}$
 - $(\forall y \in O')[a'[s, y] = \emptyset], (\forall x \in S')[a'[x, s] = \emptyset]$
 - $(\forall x \in S)(\forall y \in O)[a'[x, y] = a[x, y]]$

Create Object

- Precondition: $o \notin O$
- Primitive command: **create object** o
- Postconditions:
 - $S' = S, O' = O \cup \{ o \}$
 - $(\forall x \in S')[a'[x, o] = \emptyset]$
 - $(\forall x \in S)(\forall y \in O)[a'[x, y] = a[x, y]]$

Add Right

- Precondition: $s \in S, o \in O$
- Primitive command: enter r into $a[s, o]$
- Postconditions:
 - $S' = S, O' = O$
 - $a'[s, o] = a[s, o] \cup \{ r \}$
 - $(\forall x \in S')(\forall y \in O' - \{ o \}) [a'[x, y] = a[x, y]]$
 - $(\forall x \in S' - \{ s \})(\forall y \in O') [a'[x, y] = a[x, y]]$

Delete Right

- Precondition: $s \in S, o \in O$
- Primitive command: **delete r from $a[s, o]$**
- Postconditions:
 - $S' = S, O' = O$
 - $a'[s, o] = a[s, o] - \{ r \}$
 - $(\forall x \in S')(\forall y \in O' - \{ o \}) [a'[x, y] = a[x, y]]$
 - $(\forall x \in S' - \{ s \})(\forall y \in O') [a'[x, y] = a[x, y]]$

Destroy Subject

- Precondition: $s \in S$
- Primitive command: **destroy subject s**
- Postconditions:
 - $S' = S - \{ s \}, O' = O - \{ s \}$
 - $(\forall y \in O')[a'[s, y] = \emptyset], (\forall x \in S')[a'[x, s] = \emptyset]$
 - $(\forall x \in S')(\forall y \in O') [a'[x, y] = a[x, y]]$

Destroy Object

- Precondition: $o \in O$
- Primitive command: **destroy object o**
- Postconditions:
 - $S' = S, O' = O - \{ o \}$
 - $(\forall x \in S')[a'[x, o] = \emptyset]$
 - $(\forall x \in S')(\forall y \in O') [a'[x, y] = a[x, y]]$

Creating File

- Process p creates file f with owner r and w permission

```
command create•file( $p$ ,  $f$ )  
    create object  $f$ ;  
    enter own into  $A[p, f]$ ;  
    enter  $r$  into  $A[p, f]$ ;  
    enter  $w$  into  $A[p, f]$ ;  
end
```

Mono-Operational Commands

- Make process p the owner of file g

```
command make • owner( $p$ ,  $g$ )  
    enter own into  $A[p, g]$ ;  
end
```

- Mono-operational command
 - Single primitive operation in this command

Conditional Commands

- Let p give q r rights over f , if p owns f
command $grant \cdot read \cdot file \cdot 1(p, f, q)$
 if own **in** $A[p, f]$
 then
 enter r **into** $A[q, f];$
 end
- Mono-conditional command
 - Single condition in this command

Multiple Conditions

- Let p give q r and w rights over f , if p owns f and p has c rights over q

```
command grant.read.file.2( $p$ ,  $f$ ,  $q$ )  
    if own in  $A[p, f]$  and  $c$  in  $A[p, q]$   
    then  
        enter  $r$  into  $A[q, f]$  ;  
        enter  $w$  into  $A[q, f]$  ;  
end
```

Copy Right

- Allows possessor to give rights to another
- Often attached to a right, so only applies to that right
 - r is read right that cannot be copied
 - rc is read right that can be copied
- Is copy flag copied when giving r rights?
 - Depends on model, instantiation of model

Own Right

- Usually allows possessor to change entries in ACM column
 - So owner of object can add, delete rights for others
 - May depend on what system allows
 - Can't give rights to specific (set of) users
 - Can't pass copy flag to specific (set of) users

Attenuation of Privilege

- Principle says you can't give rights you do not possess
 - Restricts addition of rights within a system
 - Usually *ignored* for owner
 - Why? Owner gives himself/herself rights, gives them to others, deletes his/her rights.

Key Points

- Access control matrix simplest abstraction mechanism for representing protection state.
- Transitions alter protection state.
- 6 primitive operations alter matrix
 - Transitions can be expressed as commands composed of these operations and, possibly, conditions.