Template for XCPC

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1 Compile

1.1 Fast I/O

```
#include <bits/stdc++.h>
  #define init(x) memset (x,0,sizeof (x))
  #define INF 0x3f3f3f3f
  #define pii pair <int,int>
  using i64 = long long;
  using u64 = unsigned long long;
  using LD = long double;
  using namespace std;
  const int MAX = 1e5 + 5;
  const int MOD = 1e9 + 7;
  char s[200];
  inline int read ();
  inline void output ();
  int main ()
       //freopen (".in","r",stdin);
//freopen (".out","w",stdout);
       return 0;
   inline int read ()
       int s = 0; int f = 1;
       char ch = getchar ();
       while ((ch < '0' || ch > '9') && ch != EOF)
           if (ch == '-') f = -1:
           ch = getchar ();
       while (ch >= '0' && ch <= '9')
           s = s * 10 + ch - '0';
           ch = getchar ();
       return s * f;
   }
  inline void output (int x)
       if (x < 0) putchar ('-');</pre>
       x = (x > 0) ? x : -x;
       int cnt = 0;
       while (x)
           s[cnt++] = x \% 10 + 0;
           x /= 10;
       while (cnt) putchar (s[--cnt]);
   }
1.2 Run.bash
   #!/bin/bash
   g++ -std=c++17 -02 -Wall "$1" -o main
   ./main < in.txt > out.txt
1.3 Run.ps1
  # Set-ExecutionPolicy -Scope Process -ExecutionPolicy Bypass
  # new file : 'type nul > filename.cpp'
  # run : '.\run.ps1 filename.cpp'
```

g++ -std=c++17 -02 -Wall \$args[0] -o main
cat in.txt | .\main | Out-File -FilePath out.txt

2 Graph

2.1 Diameter of a Tree

```
template <typename T>
class Diameter
    int n,p;
    vector <T> dis;
    vector <vector <pair <int,T>>> ve;
    void dfs (int u,int fa)
        for (const auto& [v,w] : ve[u])
            if (v == fa) continue;
            dis[v] = dis[u] + w;
            if (dis[v] > dis[p]) p = v;
            dfs (v,u);
        }
    }
    public:
    Diameter (int n) : n(n), ve(n + 1) {}
    void add (int u,int v,T w = 1) {ve[u].push_back ({v,w});ve[v].push_back ({u,w})
       });}
    T calc ()
        dis.assign (n + 1,0);
        p = 1; dfs (1,0);
        dis[p] = 0; dfs (p,0);
        return dis[p];
    }
};
```

2.2 Centroid of a Tree

```
class Centroid
{
    int n;
   vector <int> sz,w,cen;
   vector <vector <int>>> ve;
    void dfs (int u,int fa)
        sz[u] = 1; w[u] = 0;
        for (auto v : ve[u])
            if (v == fa) continue;
            dfs (v,u);
            sz[u] += sz[v];
            w[u] = max (w[u], sz[v]);
        w[u] = max (w[u], n - sz[u]);
        if (w[u] <= n / 2) cen.push_back (u);</pre>
   }
   Centroid (int n): n(n), ve (n + 1), sz (n + 1), w (n + 1) {}
   void add (int u,int v) {ve[u].push_back (v);ve[v].push_back (u);}
   auto calc ()
        cen.clear ();
        dfs (1, 0);
        sort (cen.begin (),cen.end ());
        return cen;
    }
```

};

2.3 Minimum Spanning Tree

2.3.1 Prim

```
template <typename T>
   class MST
   {
       int n;T ans;
       vector <int> vis;vector <vector <int>> g;vector <T> dis;
       public :
       MST (int n) : n (n), vis (n + 1,0),g (n + 1, vector <int> (n + 1, INF)), dis (n +
            1,INF) {dis[1] = ans = 0; vis[1] = 1;}
       void add (int u,int v,T w) \{g[u][v] = g[v][u] = w;\}
       T calc ()
       {
           for (int i = 2;i <= n;++i) dis[i] = g[1][i];</pre>
           for (int i = 1; i < n; ++i)
               int k = 0;
               for (int j = 1; j <= n; ++j)
                    if (!vis[j] && dis[j] < dis[k]) k = j;</pre>
               vis[k] = 1;
               ans += dis[k];
               for (int j = 1; j <= n; ++j)
                    if (!vis[j] && g[k][j] < dis[j]) dis[j] = g[k][j];</pre>
           }
           return ans;
       }
  };
2.3.2 Kruskal
   template <typename T>
  class MST
       int n,m,e_cnt,cnt;T ans;
       struct node {int u,v;T w;};
       vector <int> fa; vector <node> g;
       public:
       MST (int n, int m) : n (n), m(m), fa (n + 1,0), g (m + 1) {cnt = e_cnt = ans =
           0;}
       void add (int u,int v,int w) \{g[++e\_cnt].u = u,g[e\_cnt].v = v,g[e\_cnt].w = w
          ;}
       int getfa (int u) {return fa[u] == u ? u : fa[u] = getfa (fa[u]);}
       T calc ()
           sort (g.begin (),g.end (),[] (auto &x,auto &y) {return } x.w < y.w;});
           for (int i = 1; i \le n; ++i) fa[i] = i;
           for (int i = 1; cnt < n && i <= m; ++i)
               int dx = getfa (g[i].u),dy = getfa (g[i].v);
               if (dx == dy) continue;
               ans += g[i].w;fa[dx] = dy;++cnt;
           return ans;
       }
  };
2.4 LCA
   class LCA
   {
```

```
static constexpr int lg = 20;
       int n;
       vector <int> dep;
       vector <vector <int>> f,ve;
       public:
       LCA (int n): n (n), ve (n + 1), dep (n + 1), f (n + 1, vector \langle int \rangle (lg + 1,0))
       void add (int u,int v) {ve[u].push_back (v);ve[v].push_back (u);}
       void pre (int u,int fa)
           f[u][0] = fa; dep[u] = dep[fa] + 1;
           for (int i = 0; i < lg; ++i) f[u][i + 1] = f[f[u][i]][i];
           for (auto v : ve[u])
               if (v != fa) pre (v,u);
       int query (int u,int v)
           if (dep[u] < dep[v]) swap (u,v);
           for (int i = lg;~i;--i)
               if (dep[f[u][i]] >= dep[v]) u = f[u][i];
               if (u == v) return u;
           for (int i = lg; ~i; --i)
               if (f[u][i] != f[v][i]) u = f[u][i], v = f[v][i];
           return f[u][0];
  };
2.5 Topological Sorting
   class Topo
   {
       int n;
       vector <int> deg;
       vector <vector <int>> ve;
       public:
       Topo (int n): n (n), ve (n + 1), deg (n + 1, 0) {}
       void add (int u,int v)
           ve[u].push_back (v);
           ++deg[v];
       vector <int> calc ()
           queue <int> q;
           vector <int> lst;
           for (int i = 1; i <= n; ++i)
               if (!deg[i]) q.push (i);
           while (!q.empty ())
               int u = q.front();q.pop();
               lst.push_back (u);
               for (auto v : ve[u])
               {
                   --deg[v];
                   if (!deg[v]) q.push (v);
               }
           }
           return lst;
       }
  };
```

2.6 Shortest Path

2.6.1 Dijstrka

```
class dijkstra
       int n,m,cnt;
       vector <int> head, to, nxt, val, vis;
       vector <1l> dis;
       public:
       dijkstra (int n,int m) :
           n (n), m (m), vis (n + 1, 0), head (n + 1, 0), dis (n + 1, INF),
           to (2 * m + 1,0), nxt (2 * m + 1,0), val (2 * m + 1,0) {cnt = 0;}
       void add (int u,int v,int w)
       {
           to[++cnt] = v;val[cnt] = w;nxt[cnt] = head[u];head[u] = cnt;
           to[++cnt] = u;val[cnt] = w;nxt[cnt] = head[v];head[v] = cnt;
       }
       auto calc (int s)
       {
           priority_queue <pii> q;
           for (int i = 1; i \le n; ++i) vis[i] = 0, dis[i] = INF;
           q.push ({0,s});
           dis[s] = 0;
           while (!q.empty ())
               int u = q.top ().second;q.pop ();
               if (vis[u]) continue;
               vis[u] = 1;
               for (int i = head[u];i;i = nxt[i])
               {
                   int v = to[i];
                   if (dis[v] > dis[u] + val[i])
                        dis[v] = dis[u] + val[i];
                        q.push ({-dis[v],v});
                   }
               }
           }
           return dis;
       }
  };
2.6.2 SPFA
   class SPFA
       int n,m,cnt;
       vector <int> head, to, nxt, val, vis, times;
       vector <1l> dis;
       public:
       SPFA (int n, int m) :
           n (n), m (m), times (n + 1,0), vis (n + 1,0), head (n + 1,0), dis (n + 1,INF),
           to (2 * m + 1,0), nxt (2 * m + 1,0), val (2 * m + 1,0) {cnt = 0;}
       void add (int u,int v,int w)
       {
           to[++cnt] = v;val[cnt] = w;nxt[cnt] = head[u];head[u] = cnt;
           to[++cnt] = u;val[cnt] = w;nxt[cnt] = head[v];head[v] = cnt;
       auto calc (int s)
           queue <int> q;
           for (int i = 1;i <= n;++i) vis[i] = 0,dis[i] = INF;</pre>
           dis[s] = 0, vis[s] = 1; q.push(s);
```

```
while (!q.empty())
               int u = q.front ();
               q.pop(), vis[u] = 0;
               for (int i = head[u];i;i = nxt[i])
                   int v = to[i];
                   if (dis[v] > dis[u] + val[i])
                       dis[v] = dis[u] + val[i];
                       times[v] = times[u] + 1;
                       if (times[v] >= n) return {-1};//Negative Cycle
                       if (!vis[v]) q.push (v),vis[v] = 1;
               }
           }
           return dis;
       }
  };
2.7 DCC
   class DCC
   {
       public:
       struct Edge {int to,nxt;};
       vector <Edge> G;
       vector <int> head,dfn,low,col;
       vector <bool> cut;
       stack <int> stk;
       int cnt,cct,n;
       void init (int nn = 0)
           G.assign (2,{0,0});
           n = nn; head.assign (n + 1,0);
       void dfs (int u, int f = -1)
            dfn[u] = low[u] = ++cnt;
           int ch = 0;
           for (int i = head[u];i;i = G[i].nxt)
           if (i != f)
           {
               int v = G[i].to;
               if (dfn[v] < dfn[u]) stk.push (i >> 1);
               if (!dfn[v])
               {
                   dfs (v,i ^ 1);++ch;
                   low[u] = min (low[u],low[v]);
                   if (low[v] >= dfn[u])
                   {
                       int I = 0;
                       ++cct;cut[u] = true;
                       do
                       {
                            assert (!stk.empty ());
                            I = stk.top ();stk.pop ();
                            col[I] = cct;
                       while (I !=(i >> 1));
                   }
               }
               else if (dfn[v] < low[u]) low[u] = dfn[v];</pre>
           }
```

```
if (f == -1 && ch == 1) cut[u] = false;
      }
      void tarjan ()
       {
           cnt = cct = 0;
           col.assign (G.size () >> 1,0);
           dfn.assign (n + 1,0);
           low.assign (n + 1,0);
           cut.assign (n + 1, false);
           while (!stk.empty ()) stk.pop ();
           for (int i = 1; i \le n; ++i) if (!dfn[i]) dfs (i);
      }
      void insert (int u,int v)
       {
           G.push_back (\{v,head[u]\});head[u] = G.size () - 1;
           G.push_back( \{u,head[v]\});head[v] = G.size() - 1;
      void insert (vector <vector <int>> &G1)
           for (unsigned u = 1; u < G1.size ();++u)
               for (int v : G1[u]) insert (u,v);
       bool operator [] (const int &x) const {return cut[x];}
   };
2.8 Tarjan
   class Tarjan
   {
       int n,m,cnt,times,scc_cnt;
      vector <int> head, to, nxt, low, scc, dfn;
       stack <int> s;
      void tarjan (int u)
           low[u] = dfn[u] = ++times;
           s.push (u);
           for (int i = head[u];i;i = nxt[i])
               int v = to[i];
               if (!dfn[v])
               {
                   tarjan (v);
                   low[u] = min (low[u],low[v]);
               else if (!scc[v]) low[u] = min (low[u],dfn[v]);
           if (low[u] == dfn[u])
               ++scc_cnt;
               while (1)
               {
                   int x = s.top(); s.pop();
                   scc[x] = scc_cnt;
                   if (x == u) break;
               }
           }
      public:
       Tarjan (int n,int m) :
           n (n), m (m), head (n + 1,0), low (n + 1,0), dfn (n + 1,0), scc (n + 1,0),
           to (2 * m + 1,0), nxt (2 * m + 1,0) \{cnt = times = scc_cnt = 0;\}
      void add (int u,int v) // Note that the bidirectional edges
           to[++cnt] = v;nxt[cnt] = head[u];head[u] = cnt;
```

```
to[++cnt] = u;nxt[cnt] = head[v];head[v] = cnt;
       }
       auto calc ()
       {
           for (int i = 1; i \le n; ++i)
               if (!dfn[i]) tarjan (i);
           return scc;
       }
   };
2.9 Bipartite Graph Matchings
   class Matching
       int l,r;//the number of left/right side points
       vector <vector <int>> ve;
       vector <int> vis,op;
       bool dfs (int u)
       {
           for (auto v : ve[u])
               if (vis[v]) continue;
               vis[v] = 1;
               if (!op[v] || dfs (op[v])) {op[v] = u;return true;}
           return false;
       }
       public:
       Matching (int 1, int r) : 1 (1), r (r), vis (r + 1, 0), op (r + 1, 0), ve (1 + 1) {}
       void add (int u,int v) {ve[u].push_back (v);}
       int calc ()
           int ans = 0;
           for (int i = 1; i <= 1; ++i)
               vis.assign (r + 1,0);
               if (dfs (i)) ++ans;
           }
           return ans;
       }
   };
2.10 Flow
2.10.1 Edmonds-Karp
   template <typename T>
   class EK
   {
       int n,m,s,t,cnt;
       vector <int> head, to, nxt, vis, pre, edge;
       vector <T> val;
       bool bfs ()
       {
           queue <T> q;
           for (int i = 1; i \le n; ++i) vis[i] = 0, pre[i] = edge[i] = -1;
           vis[s] = 1;q.push(s);
           while (!q.empty ())
               int u = q.front ();q.pop ();
               for (int i = head[u];i;i = nxt[i])
               {
                   int v = to[i];
```

if (!vis[v] && val[i])

```
{
                       pre[v] = u;edge[v] = i;vis[v] = 1;
                        q.push (v);
                        if (v == t) return 1;
                   }
               }
           }
           return 0;
       }
       public :
       EK (int n,int m,int s,int t) :
           n (n), m (m), s (s), t (t),
           vis (n + 1,0), head (n + 1,0), pre (n + 1,-1), edge (n + 1,-1),
           to (m + 1,0), nxt (m + 1,0), val (m + 1,0) {cnt = 1;}
       void add (int u,int v,T w)
           to[++cnt] = v;val[cnt] = w;nxt[cnt] = head[u];head[u] = cnt;
           to[++cnt] = u;val[cnt] = 0;nxt[cnt] = head[v];head[v] = cnt;
       T calc ()
           T ans = 0;
           while (bfs ())
               T mn = INF;
               for (int i = t;i != s;i = pre[i]) mn = min (mn, val[edge[i]]);
               for (int i = t;i != s;i = pre[i]) val[edge[i]] -= mn,val[edge[i] ^ 1]
                    += mn;
               ans += mn;
           }
           return ans;
       }
  };
2.10.2 Dinic
   template <typename T>
   class Dinic
       int n,m,s,t,cnt;
       vector <int> head, to, nxt, cur, dep;
       vector <T> val;
       int bfs ()
           for (int i = 0;i <= n;++i) dep[i] = 0,cur[i] = head[i];</pre>
           queue <int> q;
           q.push(s), dep[s] = 1;
           while (!q.empty ())
               int u = q.front ();q.pop ();
               for (int i = head[u];i;i = nxt[i])
               {
                   int v = to[i];
                   if (val[i] && !dep[v]) q.push (v),dep[v] = dep[u] + 1;
               }
           }
           return dep[t];
       T dfs (int u,int t,T flow)
           if (u == t) return flow;
           T ans = 0;
           for (int &i = cur[u];i && ans < flow;i = nxt[i])</pre>
           {
```

```
int v = to[i];
            if (val[i] \&\& dep[v] == dep[u] + 1)
                int x = dfs (v,t,min (val[i], flow - ans));
                if (x) val[i] -= x,val[i ^ 1] += x,ans += x;
        if (ans < flow) dep[u] = -1;
        return ans;
    }
    public :
    Dinic (int n,int m,int s,int t) :
        n (n), m (m), s (s), t (t),
        head (n + 1,0), cur (n + 1,0), dep (n + 1,0),
        to (m + 1,0), nxt (m + 1,0), val (m + 1,0) {cnt = 1;}
    void add (int u,int v,T w)
    {
        to[++cnt] = v;val[cnt] = w;nxt[cnt] = head[u];head[u] = cnt;
        to[++cnt] = u;val[cnt] = 0;nxt[cnt] = head[v];head[v] = cnt;
    }
    T calc ()
        T ans = 0;
        while (bfs ())
            while ((x = dfs (s,t,INF))) ans += x;
        return ans;
    }
};
```

3 Data Structure

- 3.1 Segment Tree
- 3.2 Fenwick Tree
- 3.3 Heavy-Light Decomposition
- 3.4 Splay Tree
- 3.5 Sparse Table
- 3.6 Persistent Data Structure
- 3.7 Linear-Basis

```
template <typename T>
class Basis
{
    int n, lg;
    vector <T> p,ex,nw;vector <vector <int>> id;
    Basis (int n, int lg): n (n), lg (lg), p (lg + 1,0), nw (lg + 1,0), id (lg + 1)
    void modify (T x,int idx)
        vector \langle int \rangle cur (n + 1,0); cur[idx] = 1;
        for (int i = lg;~i;--i)
             if (!((111 << i) & x)) continue;</pre>
             if (!p[i]) {p[i] = x;id[i] = cur;break;}
             else
             {
                 x ^= p[i];
                 for (int j = 1; j <= n;++j) cur[j] ^= id[i][j];</pre>
        }
    }
    T get_max ()
        T ans = 0;
        for (int i = lg; ~i; --i)
             if ((ans ^ p[i]) > ans) ans ^= p[i];
        return ans;
    }
    T get_min ()
        T ans = 0; int cnt = 0;
        for (int i = 0; i \le lg; ++i) cnt += p[i] > 0;
        if (cnt < n) return 0;</pre>
        for (int i = 0; i \le lg; ++i)
             if (p[i] > 0) return p[i];
    }
    void change ()
        for (int i = 0;i <= lg;++i) nw[i] = p[i];</pre>
        for (int i = 0; i \leftarrow lg; ++i)
             for (int j = i - 1; ~j; --j)
                 if (nw[i] >> j & 1) nw[i] ^= nw[j];
        for (int i = 0; i \leftarrow lg; ++i)
             if (nw[i]) ex.push_back (i);
    T get_min_k (T k)
```

```
{
         int sz = (int)ex.size ();
         if (sz < n) --k; // element 0
if (k > (111 << sz) - 1) return -1;</pre>
         T ans = 0;
         for (int j = 0; j < sz; ++j)
             if (k >> j & 1) ans ^= nw[ex[j]];
         return ans;
    }
    bool find (T x)
         for (int i = lg;~i;--i)
              if (!(x >> i & 1)) continue;
              if (!p[i]) return false;
              x ^= p[i];
         }
         return true;
    }
    vector \langle int \rangle getid (T x) // if find (x) == 1
         vector \langle int \rangle res (n + 1, 0);
         for (int i = lg; \tilde{i}; --i)
              if (!(x >> i \& 1)) continue;
              for (int j = 1; j <= n; ++j) res[j] ^= id[i][j];</pre>
         return res;
    }
};
```

4 Math

4.1 Subset Enumeration

```
for (int S = 1; S < (1 << n); ++S)
for (int S0 = S; S0; S0 = (S0 - 1) & S)
```

4.2 Elementary Arithmetic Bucket

```
template <typename T, int MOD = 1000000007>
class Z
{
   Tx;
   Z < T, MOD > qpow (Z x, T y)
        Z < T, MOD > res (1);
        while (y)
            if (y & 1) res *= x;
            x *= x;
            y >>= 1;
        return res;
   public :
   Z() : x(0) {}
   Z (T x) : x (x) {}
   T get () {return x;}
   Z & operator = (T o) {x = o % MOD; return *this;}
   Z & operator += (Z o) {x = (x + o.x + MOD) % MOD; return *this;}
   Z & operator -= (Z o) {x = (x - o.x + MOD) % MOD; return *this;}
   Z & operator *= (Z o) {x = 111 * o.x * x % MOD; return *this;}
   Z & operator \hat{}= (Z \circ) \{x = qpow (x,o.x).x; return *this; \}
   Z & operator \neq (Z o) {*this *= o ^ (MOD - 2); return *this;}
    Z & operator \%=(Z \circ) \{x = x \% \circ .x; return *this; \}
    friend Z operator + (Z x, Z y) {return x += y;}
    friend Z operator - (Z x,Z y) {return x -= y;}
    friend Z operator * (Z x,Z y) {return x *= y;}
    friend Z operator / (Z x, Z y) \{ return x /= y; \}
    friend Z operator ^ (Z x,Z y) {return x ^= y;}
    friend Z operator % (Z x,Z y) {return x %= y;}
    friend bool operator == (Z x,Z y) {return x.x == y.x;}
    friend bool operator != (Z x,Z y) {return x.x != y.x;}
    friend istream& operator >> (istream& is, Z& o) {T val;is >> val;o = Z(val);
        return is;}
    friend ostream& operator << (ostream &os, const Z &z) {return os << z.x;}
};
```

4.3 Combination

```
template <typename T,int MOD = 1000000007>
class COM
{
   int n;
   vector <Z <T,MOD>> fac,inv;
   public :
    COM (int n) : n (n),fac (2 * n + 2),inv (2 * n + 2)
   {
      fac[0] = inv[0] = inv[1] = 1;
      for (int i = 1;i <= 2 * n;++i) fac[i] = fac[i - 1] * i;
      inv[2 * n] = fac[2 * n] ^ (MOD - 2);
      for (int i = 2 * n - 1;i > 0;--i) inv[i] = inv[i + 1] * (i + 1);
}
```

```
Z <T,MOD> f (int x) {return fac[x];}
       Z <T,MOD> inv_f (int x) {return inv[x];}
       Z <T,MOD> comb (int x,int y)
           if (y < 0 \mid | y > x) return 0;
           else return fac[x] * inv[x - y] * inv[y];
       Z <T,MOD> arr (int x,int y)
           if (y > x) return 0;
           else return fac[x] * inv[x - y];
       Z < T, MOD > catalan (int x) {return comb (2 * x,x) / (x + 1);}
4.4 The Sieve of Primes & Euler's Totient Function & Möbius Function
   class Prime
   {
       int mx;
       vector <int> p,phi,mu;
       void pre ()
           vector \langle int \rangle fl (mx + 1,0);
           phi[1] = mu[1] = 1;
           for (int i = 2; i \le mx; ++i)
               if (!fl[i]) p.push_back (i),phi[i] = i - 1,mu[i] = -1;
               for (auto v : p)
               {
                    if (i * v > mx) break;
                    fl[i * v] = 1;
                    if (i % v == 0) {phi[i * v] = phi[i] * v,mu[i * v] = 0;break;}
                    phi[i * v] = phi[i] * (v - 1);mu[i * v] = -mu[i];
               }
           }
       }
       public :
       Prime (int mx): mx (mx), phi (mx + 1,0), mu (mx + 1,0) {pre ();}
       auto get_prime () {return p;}
       auto get_phi () {return phi;}
       auto get_mu () {return mu;}
  };
4.5 Exgcd
  11 exgcd (11 a,11 b,11 &x,11 &y)
       if (!b) {x = 1;y = 0;return a;}
       11 d = exgcd (b, (a \% b + b) \% b, y, x);
       y -= a / b * x;
       return d;
   }
4.6 CRT
   11 CRT ()
       //ans \% a[i] = b[i] if gcd (a[i],a[j]) = 1
       11 \text{ sum} = 1, \text{ans} = 0;
       for (int i = 1; i \le n; ++i) sum *= a[i];
       for (int i = 1; i \le n; ++i)
```

11 x,y,tmp = sum / a[i];

```
exgcd (tmp,a[i],x,y);
ans = (ans + tmp * x * b[i]) % sum;
return (ans + sum) % sum;
```

}

if (op == -1) {for (auto &x : a) x /= n;}

vector <double> conv (vector <cd> a, vector <cd> b)

rev.resize (n);a.resize (n);b.resize (n);

while (n < tot) n <<= 1,++L;

}

public :

```
4.7 Gaussian Elimination
   vector <vector <double>> a (n + 1, vector <double> (n + 2)); // n * (n + 1)
   for (int i = 1; i <= n; ++i)
       int p = cur, ok = 0;
       while (p \ll n)
           if (a[p][i] != 0) {ok = 1;break;}
       if (!ok) continue;
       for (int j = i; j \le n + 1; ++j) swap (a[p][j],a[cur][j]);
       for (int j = n + 1; j >= i; --j) a[cur][j] /= a[cur][i];
       for (int j = 1; j \le n; ++j)
           if (j == cur) continue;
           for (int k = n + 1; k >= i; --k) a[j][k] -= a[cur][k] * a[j][i];
       ++cur;
   if (cur <= n) puts ("No Solution"); //0 solution or infinte solutions</pre>
   else {for (int i = 1;i <= n;++i) printf ("%.6lf\n",a[i][n + 1]);}</pre>
4.8 FFT
  using cd = complex <double>;
   class FFT
   {
       const double Pi = acos (-1);
       vector <int> rev;int n = 1;
       void fft (vector <cd> &a,int op)
       {
           for (int i = 0; i < n; ++i)
               if (i < rev[i]) swap (a[i],a[rev[i]]);</pre>
           for (int len = 1;len < n;len <<= 1)</pre>
               cd wn (cos (Pi / len),op * sin (Pi / len));
               for (int i = 0; i < n; i += len << 1)
                    cd w (1);
                    for(int j = 0; j < len; ++j)
                        cd u = a[i + j], v = a[i + j + len] * w;
                        a[i + j] = u + v; a[i + j + len] = u - v;
                        w *= wn;
```

int L = 0, tot = (int)a.size () + (int)b.size () - 1;n = 1;

```
for (int i = 0; i < n; ++i) rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (L -
               1));
           fft (a,1); fft (b,1);
           for (int i = 0; i < n; ++i) a[i] = a[i] * b[i];
           fft (a,-1);
           vector <double> ans (tot);
           for (int i = 0; i < tot; ++i) ans[i] = a[i].real ();
           return ans;
       }
  };
4.9 NTT
   class NTT
       vector <int> rev;int n = 1;
       const int P = 1004535809; //998244353
       const int G = 3;
       int qpow (int x,int y)
           int res = 1;
           while (y)
           {
               if (y & 1) res = 111 * res * x % P;
               x = 111 * x * x % P;
               y >>= 1;
           return res;
       void ntt (vector <int> &a,int op)
       {
           for (int i = 0; i < n; ++i)
               if (i < rev[i]) swap (a[i],a[rev[i]]);</pre>
           for (int len = 1;len < n;len <<= 1)</pre>
               int wn = qpow (3,(P-1) / (len << 1));
               if (op == -1) wn = qpow (wn, P - 2);
               for (int i = 0; i < n; i += len << 1)
                   int w = 1;
                   for(int j = 0; j < len; ++j)
                        int u = a[i + j],v = 111 * a[i + j + len] * w % P;
                        a[i + j] = (u + v) \% P;
                        a[i + j + len] = (u - v + P) \% P;
                        w = 111 * w * wn % P;
               }
           }
           if (op == -1)
               int inv_n = qpow (n,P-2);
               for (auto &x : a) x = 111 * x * inv_n % P;
           }
       }
       public :
       vector <int> conv (vector <int> a, vector <int> b)
           int L = 0, tot = (int)a.size () + (int)b.size () - 1;n = 1;
           while (n < tot) n <<= 1,++L;
           rev.resize (n);a.resize (n);b.resize (n);
           for (int i = 0; i < n; i + i) rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (L -
               1));
           ntt (a,1);ntt (b,1);
```

```
for (int i = 0;i < n;++i) a[i] = 1ll * a[i] * b[i] % P;
   ntt (a,-1);a.resize (tot);
   return a;
}
};</pre>
```

5 Computational Geometry

```
using LD = long double;
const LD pi = acos(-1.0);
const LD eps = 1e-8;
int dcmp (LD x) {return x < -eps ? -1 : (x > eps ? 1 : 0);}
struct Point {LD x,y; Point (LD x = 0, LD y = 0) : x(x),y(y) {}};
struct Circle {Point 0;LD r;Circle (Point 0 = Point (),LD r = 0) : 0 (0),r (r)
    {}};
typedef Point Vector;
Vector operator + (Vector A, Vector B) {return Vector (A.x + B.x, A.y + B.y);}
Vector operator - (Vector A, Vector B) {return Vector (A.x - B.x, A.y - B.y);}
Vector operator * (Vector A,LD k) {return Vector (A.x * k,A.y * k);}
Vector operator / (Vector A,LD k) {return Vector (A.x / k,A.y / k);}
LD dot (Vector A, Vector B) {return A.x * B.x + A.y * B.y;}
LD dis (Point A, Point B) {return sqrt ((A.x - B.x) * (A.x - B.x) + (A.y - B.y) *
    (A.y - B.y));
LD cross (Vector A, Vector B) {return A.x * B.y - A.y * B.x;} // A -> B counter-
    clockwise if cross (A,B) > 0
LD len (Point A) {return sqrt (A.x * A.x + A.y * A.y);}
LD angle (Vector A, Vector B) {return acos (dot (A,B) / (len (A) * len (B)));}
Vector proj (Vector A, Vector B) {return A * (dot (A,B) / dot (A,A));} //project
    onto A
Point foot (Point P, Point A, Point B) {Vector AP = P - A, AB = B - A; return A +
   proj (AB,AP);} //foot
Point reflect (Point P, Point A, Point B) {Point F = foot (P,A,B); return F * 2 - P
    ;} //symmetry point
Point rotate (Point P,LD theta) {return (Point){P.x * cos (theta) - P.y * sin (
   theta),P.x * sin (theta) + P.y * cos (theta)};}
bool on_line (Point P,Point A,Point B) {return dcmp (cross (P - A,B - A)) == 0;}
bool on_seg (Point P,Point A,Point B) {return on_line (P,A,B) && dcmp (dot (P - A
   ,P - B)) \leftarrow 0; //judge whether on segment AB
LD dis_seg (Point P,Point A,Point B)
    if (dcmp (dot (B - A,P - A)) < 0) return dis (P,A);</pre>
    if (dcmp (dot (A - B,P - B)) < 0) return dis (P,B);
    return fabs (cross (P - A,P - B)) / dis (A,B);
Point inter_line (Point A, Point B, Point C, Point D) {return A + (B - A) * cross (C
    - A,D - C) / cross (B - A,D - C);}
bool pd_ll_inter (Point A,Point B,Point C,Point D) {return dcmp (cross (B - A,D -
    C)) != 0;} // line - line
bool pd_ls_inter (Point A, Point B, Point C, Point D) {return on_line (inter_line (A
    ,B,C,D),C,D);} //The intersection of AB(line) and CD (line) is on the CD (seg
bool pd_ss_inter (Point A, Point B, Point C, Point D) // seg - seg
    LD c1 = cross (B - A, C - A), c2 = cross (B - A, D - A);
    LD d1 = cross (D - C,A - C),d2 = cross (D - C,B - C);
    if (dcmp (c1) * dcmp (c2) < 0 && dcmp (d1) * dcmp (d2) < 0) return true;
    if (dcmp(c1) == 0 && on_seg (C,A,B)) return true;
    if (dcmp(c2) == 0 && on_seg (D,A,B)) return true;
    if (dcmp(d1) == 0 && on_seg (A,C,D)) return true;
    if (dcmp(d2) == 0 && on_seg (B,C,D)) return true;
    return false;
}
```

```
LD area (vector <Point> P)
    int n = P.size ();
    LD res = 0;
    for (int i = 0; i < n; ++i) res += cross (P[i],P[(i + 1) % n]);
    return res / 2.0;
}
bool is_convex (vector <Point> P)
    int n = P.size ();
    for(int i = 0; i < n - 1; ++i)
        if (dcmp (cross (P[i + 1] - P[i], P[(i + 2) % n] - P[i])) < 0) return
    return true;
}
int in_Poly (vector <Point> P,Point A)
{
    int cnt = 0,n = P.size ();
    for (int i = 0; i < n; ++i)
        int j = (i + 1) \% n;
        if (on_seg (A,P[i],P[j])) return 2;// on the edge
        if (A.y >= min (P[i].y,P[j].y) && A.y < max (P[i].y,P[j].y)) // the
            intersection is on the right
            cnt += dcmp (((A.y - P[i].y) * (P[j].x - P[i].x) / (P[j].y - P[i].y)
                + P[i].x) - A.x) > 0;
    return cnt & 1;
}
auto convex_hull (vector <Point> P) // strict convex hull (<= 0)</pre>
{
    int n = P.size ();
    sort (P.begin (), P.end (), [] (Point &x, Point &y) {return x.x == y.x ? x.y < y
        .y : x.x < y.x; \});
    vector <Point> hull;
    hull.resize (2 * n + 1);
    int k = 0;
    for (int i = 0; i < n; ++i)
        while (k \ge 2 \&\& dcmp (cross (hull[k - 1] - hull[k - 2],P[i] - hull[k - 2])
            2])) <= 0) --k;
        hull[k++] = P[i];
    for (int i = n - 2, t = k; i >= 0; --i)
        while (k > t \& dcmp (cross (hull[k - 1] - hull[k - 2], P[i] - hull[k -
            2])) \leftarrow 0 --k;
        hull[k++] = P[i];
    hull.resize (k - 1);
    return hull;
}
LD diameter (vector <Point> P)
{
    int n = P.size ();
    if (n <= 1) return 0;</pre>
    if (n == 2) return len (P[1] - P[0]);
    LD res = 0;
    for (int i = 0, j = 2; i < n; ++i)
        while (dcmp (cross (P[(i + 1) % n] - P[i], P[j] - P[i]) - cross (P[(i + 1) + 1)))
             % n] - P[i], P[(j + 1) % n] - P[i])) <= 0) j = (j + 1) % n;
```

```
res = max (res, max (len (P[j] - P[i]), len (P[j] - P[(i + 1) \% n]));
    return res;
bool in_cir (Circle C,Point P) {return dcmp (len (P - C.0) - C.r) <= 0;}</pre>
Point get_cir_p (Circle C,LD theta) {return {C.0.x + C.r * cos (theta),C.0.y + C.
   r * sin (theta)};}
int pd_lc_inter (Point A,Point B,Circle C)
    double d = dis_seg (C.O,A,B);
    if (dcmp (d - C.r) == 0) return 0; // tangent
    if (dcmp (d - C.r) > 0) return -1; // separation
    return 1; // intersection
}
int pd_cc_inter (Circle A,Circle B) // the number of tagent lines
{
    LD d = len (A.0 - B.0);
    if (dcmp (A.r + B.r - d) < 0) return 4; // externally separate
    if (dcmp (A.r + B.r - d) == 0) return 3; // externally tangent
    if (dcmp (fabs (A.r - B.r) - d) == 0) return 1; // internally tangent
    if (dcmp (fabs (A.r - B.r) - d) > 0) return 0; // one circle inside the other
    return 2; // intersection
}
auto lc_inter (Point A,Point B,Circle C)
    Point F = \text{foot } (C.0,A,B); LD d = \text{dis } (C.0,F);
    Vector E = (B - A) / dis (A,B);
    Point P1 = F - E * sqrt (C.r * C.r - d * d);
    Point P2 = F + E * sqrt (C.r * C.r - d * d);
    return {P1,P2};
}
auto cc_inter (Circle A, Circle B)
{
    Vector k = B.0 - A.0;
    LD d = len (k);
    LD alpha = atan2 (k.y,k.x), beta = acos ((A.r * A.r + d * d - B.r * B.r) / (2)
       * A.r * d));
    Point P1 = get_cir_p (A,alpha - beta), P2 = get_cir_p (A,alpha + beta);
    return {P1,P2};
}
auto tan_cir (Point P,Circle C)
{
    LD d = len (C.0 - P), theta = asin (C.r / d);
    Vector E = (C.0 - P) / d;
    Vector P1 = P + (rotate (E,theta) * sqrt (d * d - C.r * C.r));
    Vector P2 = P + (rotate (E, -theta) * sqrt (d * d - C.r * C.r));
    return {P1,P2};
}
Circle triangle_incir (Point A,Point B,Point C)
    LD a = dis(B,C), b = dis(A,C), c = dis(A,B);
    Point 0 = (A * a + B * b + C * c) / (a + b + c);
    return {0,dis_seg (0,A,B)};
}
Circle triangle_circum (Point A, Point B, Point C)
{
    LD Bx = B.x - A.x, By = B.y - A.y, Cx = C.x - A.x, Cy = C.y - A.y;
    LD D = 2 * (Bx * Cy - By * Cx);
    LD x = (Cy * (Bx * Bx + By * By) - By * (Cx * Cx + Cy * Cy)) / D + A.x;
    LD y = (Bx * (Cx * Cx + Cy * Cy) - Cx * (Bx * Bx + By * By)) / D + A.y;
    Point P (x,y);
    return Circle (P,dis (A,P));
```

```
}
auto get_tangents (Circle A, Circle B)
    vector <pair <Point,Point>> tangents;
    LD d = len (A.0 - B.0), dif = A.r - B.r, sum = A.r + B.r;
    if (dcmp (d - fabs (dif)) < 0) return tangents;</pre>
    LD base = atan2 (B.0.y - A.0.y, B.0.x - A.0.x);
    if (dcmp (d - fabs (dif)) == 0)
        tangents.push_back ({get_cir_p (A,base + (A.r < B.r ? pi : 0)),get_cir_p</pre>
            (A,base + (A.r < B.r ? pi : 0))));
        return tangents;
    }
    LD theta = acos (dif / d);
    tangents.push_back ({get_cir_p (A,base + theta),get_cir_p (B,base + theta)});
    tangents.push_back ({get_cir_p (A,base - theta),get_cir_p (B,base - theta)});
    if (dcmp (d - sum) == 0) tangents.push_back ({get_cir_p (A,base),get_cir_p (A
        ,base)});
    if (dcmp (d - sum) > 0)
        theta = acos (sum / d);
        tangents.push_back ({get_cir_p (A,base + theta),get_cir_p (B,base + theta
             + pi)}):
        tangents.push_back ({get_cir_p (A,base - theta),get_cir_p (B,base - theta
             + pi)});
    return tangents;
LD tri_ploy_area (Point A, Point B, Circle C)
    Vector 0A = A - C.0, 0B = B - C.0;
    LD S = cross (OA,OB), sign = dcmp (cross (OA,OB)) > 0 ? 1 : -1;
    bool da = dcmp (len (OA) - C.r) < 0, db = dcmp (len (OB) - C.r) < 0;
    if (dcmp (S) == 0) return 0;
    if (da && db) return S * 0.5; // triangle
    if (!da && !db)
    {
        if (pd_lc_inter (A,B,C) == 1)// arc + triangle + arc
            auto [P1,P2] = lc_inter (A,B,C);
            Vector OP1 = P1 - C.O,OP2 = P2 - C.O;
            if (dis (A,P1) > dis (A,P2)) swap (P1,P2);
            return cross (OP1,OP2) * 0.5 + sign * 0.5 * C.r * C.r * (angle (OA,
                OP1) + angle (OB, OP2));
        else return sign * 0.5 * C.r * C.r * angle (0A,0B); // arc
    else // triangle + arc
        auto [P1,P2] = lc_inter (A,B,C);
        if (on_seg (P2,A,B)) swap (P1,P2);
        Vector OP1 = P1 - C.0;
        if (dcmp (len (OA) - C.r) < 0) return cross (OA,OP1) * 0.5 + sign * 0.5 *
             C.r * C.r * angle (OP1,OB);
        else return cross (OP1,OB) * 0.5 + sign * 0.5 * C.r * C.r * angle (OP1,OA
            );
}
LD cc_area (Circle C1, Circle C2)
    int op = pd_cc_inter (C1,C2);
    if (op <= 1) return pi * min (C1.r,C2.r) * min (C1.r,C2.r);</pre>
    else if (op == 4) return 0;
```

```
else
{
    LD d = dis (C1.0,C2.0);
    LD alpha = 2 * acos ((C1.r * C1.r - C2.r * C2.r + d * d) / (2 * C1.r * d)
         );
    LD beta = 2 * acos ((C2.r * C2.r - C1.r * C1.r + d * d) / (2 * C2.r * d))
    ;
    return 0.5 * (C1.r * C1.r * (alpha - sin (alpha)) + C2.r * C2.r * (beta - sin (beta)));
}
```

6 String

6.1 Hash

```
template <unsigned long long base = 13331>
  class Hash
      using u64 = unsigned long long;
      vector <u64> pw,hsh;
      public:
      Hash (char *s)
           int n = strlen (s);
           pw.assign (n + 1,0), hsh.assign (n + 1,0);
           pw[0] = 1; hsh[0] = 0;
           for (int i = 1; i \le n; ++i) pw[i] = pw[i - 1] * base, hsh[i] = hsh[i - 1] *
               base + s[i - 1];
      u64 get (int l,int r) {return hsh[r] - hsh[l - 1] * pw[r - l + 1];}
       u64 link (int 11,int r1,int 12,int r2) {return get (11,r1) * pw[r2 - 12 + 1]
          + get (12,r2);}
      bool same (int 11, int r1, int 12, int r2) {return get (11, r1) == get (12, r2);}
6.2 KMP
   class KMP
       vector <int> fail,ans;
      void getfail (char *s) // Match a with b
           int len = strlen (s);
           fail.assign (len + 1,0);
           fail[0] = -1;
           for (int i = 1; i < len; ++i)
               int cnt = fail[i - 1];
               while (cnt >= 0 && s[cnt + 1] != s[i]) cnt = fail[cnt];
               if (s[cnt + 1] == s[i]) ++cnt;
               fail[i] = cnt;
           }
      }
      public:
       auto get_pos (char *s,char *t)
           getfail (t);
           int lens = strlen (s),lent = strlen (t),cnt = -1;
           for (int i = 0; i < lens; ++i)
               while (cnt >= 0 && t[cnt + 1] != s[i]) cnt = fail[cnt];
               if (t[cnt + 1] == s[i])
                   if (cnt + 1 == lent) ans.push_back (i - lent + 2),cnt = fail[cnt
           return ans;
      }
  }:
```

6.3 Manacher

```
int Manacher (char *s)
       int n = strlen(s), cnt = 0, r = 0, mid = 0, ans = 0;
       vector <char> a (2 * n + 5); vector <int> p (2 * n + 5);
       a[++cnt] = '!';a[++cnt] = '#';
       for (int i = 0; i < n; ++i) a[++cnt] = s[i], a[++cnt] = '#';
       a[++cnt] = '~';
       for (int i = 2; i < cnt; ++i)
           if (i \le r) p[i] = min (r - i + 1, p[mid * 2 - i]);
           else p[i] = 1;
           while (a[i - p[i]] == a[i + p[i]]) ++p[i];
           if (i + p[i] > r) r = i + p[i] - 1, mid = i;
           ans = max (ans,p[i]);
       return ans - 1;
  }
6.4
     Trie
6.4.1 Trie
   struct Trie
       int n,m,cnt;//m total len
       vector <vector <int>> ch;
       vector <int> vis;
       public :
       Trie (int n, int m): n (n), m (m), ch (m, vector < int > (26,0)), vis (m) {cnt = }
          0;}
       void insert (char *s)
           int u = 0,len = strlen (s);
           for (int i = 0; i < len; ++i) m
               int c = s[i] - 'a';
               if (!ch[u][c]) ch[u][c] = ++cnt;
               u = ch[u][c];
           ++vis[u];
       }
       int query (char *s)
           int u = 0,len = strlen (s);
           for (int i = 0; i < len; ++i)
               int c = s[i] - 'a';
               if (!ch[u][c]) return 0;
               u = ch[u][c];
           }
           return vis[u];
       }
   }:
6.4.2 01-Trie
   class Trie
   {
       int n, cnt;
       vector <vector <int>> ch;
       vector <int> val,w;
       public:
       Trie (int n,int lg): n (n),val (2 * lg * n + 1,0),w (2 * lg * n + 1,0),ch (2
            * lg * n + 1, vector <int> (2,0)) {cnt = 1;}
```

```
void pushup (int u)
         w[u] = val[u] = 0;
         //w[u] Number of values (weights) on the edge between node u and its
             parent node
         //val[u] XOR sum maintained by the subtree rooted at u
         if (ch[u][0]) w[u] ^= w[ch[u][0]],val[u] ^= val[ch[u][0]] << 1;
if (ch[u][1]) w[u] ^= w[ch[u][1]],val[u] ^= (val[ch[u][1]] << 1) | w[ch[u]</pre>
             ][1]];
    void modify (int &u,int v,int dep)
         if (!u) u = ++cnt;
         w[u] = 1;
         if (dep < 0) return ;</pre>
         modify (ch[u][v & 1],v >> 1,dep - 1);
         pushup (u);
    void erase (int u,int v,int dep)
         if (!u) return ;
         w[u] ^= 1;
         if (dep < 0) return ;</pre>
         erase (ch[u][v & 1],v >> 1,dep - 1);
         pushup (u);
    void add (int u) // add 1 in [1,n]
         swap (ch[u][0],ch[u][1]);
         if (ch[u][0]) add (ch[u][0]);
         pushup (u);
};
```

6.5 Aho-Corasick Automaton

6.6 SAM

```
class SAM
    class node
        public:int ch[26],len,fa;
        node (const int &L = 0) {memset (ch,0,sizeof (ch)); fa = 0; len = L;}
   };
   public:
   vector <node> t;int lst;
   void GetParentTree (vector <vector <int>>> &G)
        G.resize (t.size ());
        for (unsigned i = 1; i < t.size ();++i) G[t[i].fa].push_back (i);
   void extend (const int &c)
        int p = lst,np = lst = t.size ();
        t.push_back (node (t[p].len + 1));
        for (;p&&!t[p].ch[c];p = t[p].fa) t[p].ch[c] = np;
        if (!p) t[np].fa = 1;
        else
        {
            int v = t[p].ch[c];
            if (t[v].len == t[p].len + 1) t[np].fa = v;
            else
            {
```