

Assignment - 1

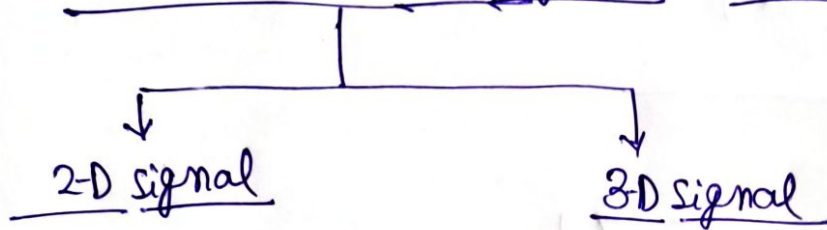
1) Define signal: Signal is anything that is visible, audible, observable or measurable with the help of some machine.

Example: Audio, light, ~~radio~~ radio etc.

2) Types of signals:

A 1) one dimensional signal: Example \Rightarrow Speech, audio

2) Multidimensional signal: Example \Rightarrow Image



B) one channel & Multichannel signals: Example
ECG

C) Continuous & Discrete signals

D) Analog & Digital signals

E) Real & Complex signals

F) Even & Odd signals

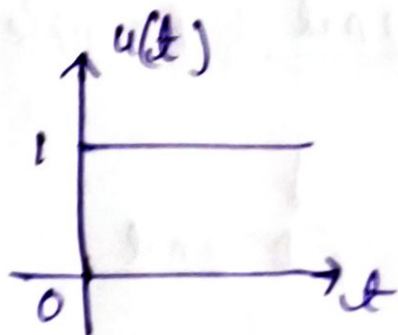
c7) Deterministic & Random signals :

3) What does following signal signifies

i) Step signal :

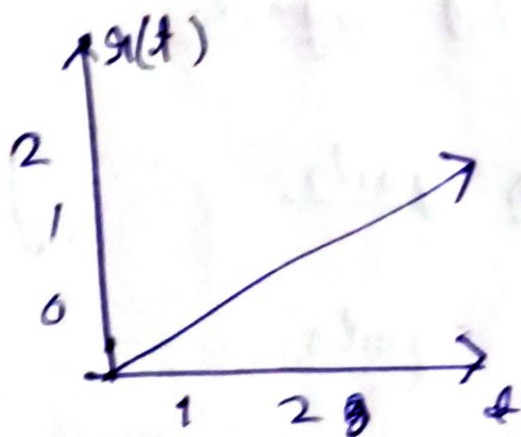
Unit step signal denoted by $u(t)$.

It is defined as $u(t) = \begin{cases} 1 & t \geq 0 \\ 0 & t < 0 \end{cases}$.



ii) Ramp signal :

Ramp signal is denoted by $r(t)$ and it is defined as $r(t) = \begin{cases} t & t \geq 0 \\ 0 & t < 0 \end{cases}$.



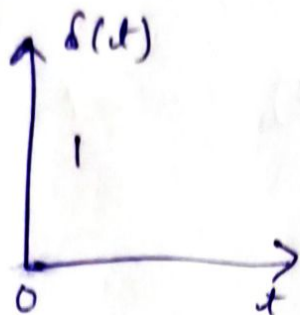
$$\int u(t) = \int 1 = t = r(t)$$

$$u(t) = \frac{dr(t)}{dt}$$

iii) Impulse signal :

Impulse signal is denoted by $\delta(t)$. and

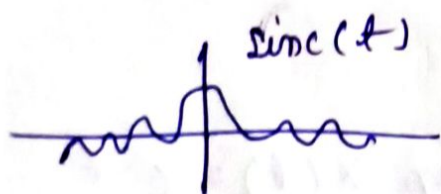
It is defined as $\delta(t) = \begin{cases} 1 & t=0 \\ 0 & t \neq 0 \end{cases}$.



$$\int_{-\infty}^{\infty} \delta(t) dt = 1$$
$$\delta(t) = \frac{d u(t)}{dt}$$

iv) Sinc signal :

It is defined as $\text{sinc}(t)$ and it is defined as ~~sinc~~ sinc.



$$t = \frac{\text{Sinc} \pi t}{\pi t}$$

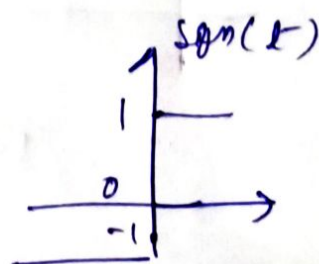
$$= 0 \text{ for } t = \pm 1, \pm 2, \pm 3, \dots$$

v) Signum signal :

Signum function is denoted as $\text{sign}(t)$.

It is defined as $\text{sgn}(t) =$

$$\begin{cases} 1 & t > 0 \\ 0 & t = 0 \\ -1 & t < 0 \end{cases}$$

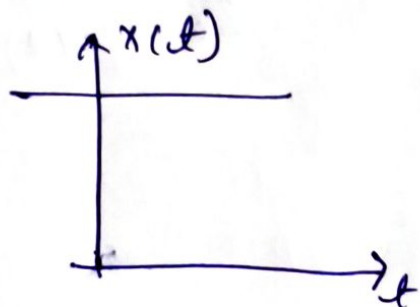


v1) Exponential signal :

It is in the form of $x(t) = e^{\alpha t}$.

The shape of exponential can be defined by α

case 1 : If $\alpha = 0 \rightarrow x(t) = e^0 = 1$.

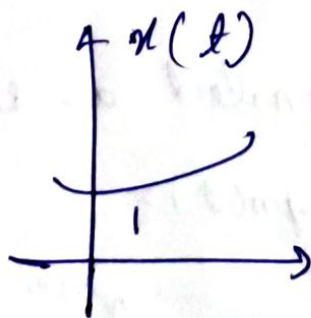


case 2 : If $\alpha < 0$ i.e. -ve then $x(t) = e^{\alpha t}$.

The shape is called decaying exponential.

case 3 : If $\alpha > 0$ i.e. +ve then $x(t) = e^{\alpha t}$.

The shape is called raising appearance.



$$\int \int u(t) dt - \int x(t) dt = \int t dt = \frac{t^2}{2} = \text{Parabolic signal}$$

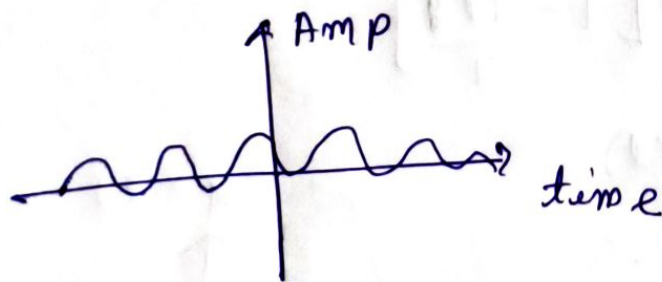
$$\Rightarrow u(t) = \frac{d^2 x(t)}{dt^2}$$

$$\Rightarrow x(t) = \frac{dx(t)}{dt}$$

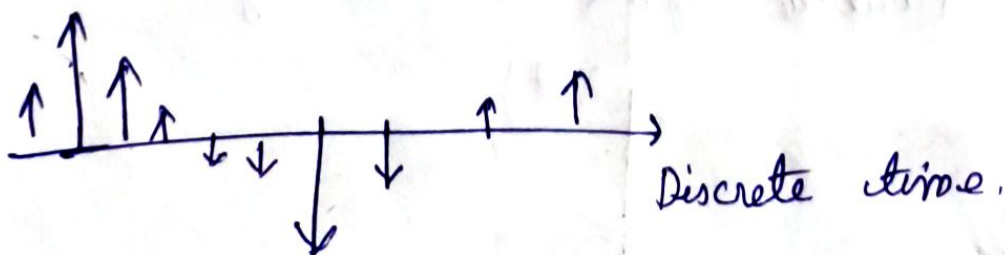
5) Following Signals definition

i) Continuous & Discrete Time Signals :

A signal is said to be continuous when it is defined for all instants of time.



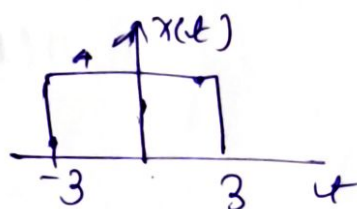
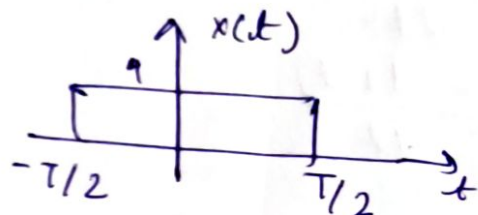
A signal is said to be discrete when it is defined at only discrete instants of time.



vii) Rectangular Signal :

Let it be denoted as $x(t)$ and it is defined as

$$x(t) = A \text{ rect}\left[\frac{t}{T}\right]$$

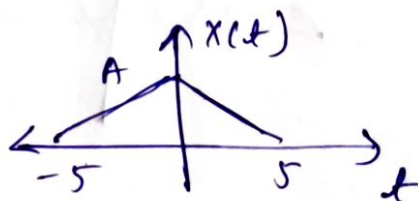
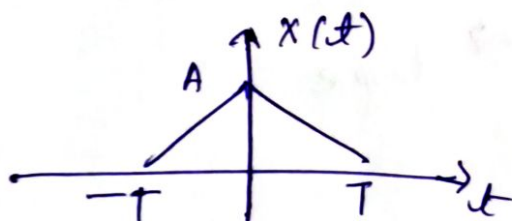


$$A \text{ rect}\left[\frac{t}{6}\right]$$

viii) Triangular Signal

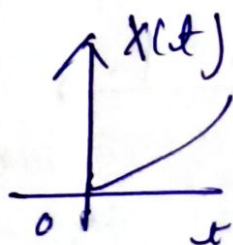
Let it be denoted as $x(t)$

$$x(t) = A \left[1 - \frac{|t|}{T}\right]$$



ix) Parabolic Signal :

Parabolic signal can be defined as $x(t) = \frac{1}{2} P_2(t)$ for $0 \leq t \leq T$



Even & odd signals :

A signal is said to be even when it satisfies the condition $x(t) = x(-t)$

Example : t^2, t^4, \dots and etc.

$$\text{Let } x(t) = t^2$$

$$x(-t) = (-t)^2 = t^2 = x(t)$$

$\therefore t^2$ is even function.

A signal is said to be odd when it satisfies the condition $x(t) = -x(-t)$

Example : t, t^3, \dots And so on.

$$\text{Let } x(t) = \sin t.$$

$$x(-t) = \sin(-t) = -\sin t = -x(t)$$

$\therefore \sin t$ is odd function.

iii) Energy and power signals :

A signal is said to be energy signal when it has finite energy

$$\text{Energy } E = \int_{-\infty}^{\infty} x^2(t) dt$$

A signal is said to be power signal when it has finite ~~time~~ power

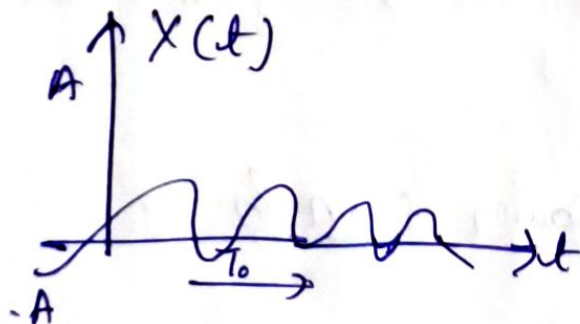
$$\text{power } P = \lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^T x^2(t) dt$$

iv) Periodic and Aperiodic signals :

A signal is said to be periodic if it satisfies the condition $x(t) = x(t+T)$ or $x(n) = x(n+N)$

T = Fundamental time period,

$1/T = f$ = fundamental frequency.

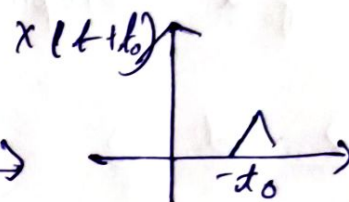
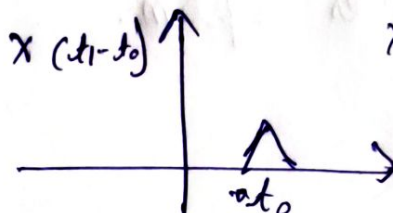
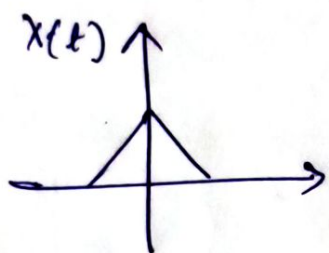


Time Shifting :

i) $x(t \pm t_0)$ is time shifted version of signal $x(t)$

$x(t + t_0) \rightarrow$ negative shift.

$x(t - t_0) \rightarrow$ positive shift.



Time Scaling :

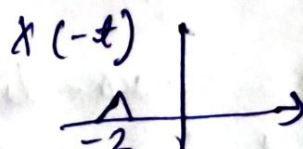
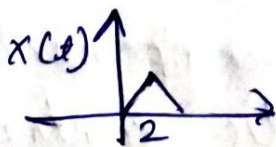
$x(At)$ is time scaled version of the signal $x(t)$. Where A is always positive

$|A| > 1 \rightarrow$ compression of the signal

$|A| < 1 \rightarrow$ Expansion of the signal.

Time Reversal :

$x(-t)$ is the time reversal of the signal $x(t)$



Module II

1) System: A group of components or ~~of~~ Subsystems that integrate & function together in order to achieve specific ~~total~~ goal.

Ex: A dist subsystem is a component/part of a computer system.

2) and 3).

Basic types of systems:

i) Linear or non-linear systems:

A system is linear if it satisfies the following property, where signals $u_1(t)$ and $u_2(t)$ output $y_1(t)$ and $y_2(t)$, respectively

$$T[a_1 u_1(t) + a_2 u_2(t)] = a_1 T[u_1(t)] + a_2 T[u_2(t)] \\ T[u_2(t)] = a_1 y_1(t) + a_2 y_2(t)$$

Linear systems are typically much simpler than their non-linear components. They are automatic control theory, signal

measuring and telecommunication. Specifically ~~on~~ wireless communication can be modeled by Linear systems.

ii) Time variant and Time-invariant Systems :

A system is time-variant if its input and output relationship varies with time. The equations that define these cases are as follows.

When $y(n, t) = T[x(n-t)]$ = input change

and $(y-n, t) =$ output change

$y(n-t) = y(n-t)$ for time-invariant systems.

$y(n, t) \neq y(n-t)$ time-variant system.

iii) Static & Dynamic system :

Static systems are memory less systems.

An example eqⁿ $y[t] = 2x[t]$

Dynamic system might have follows eqⁿ

$$y[t] = 2 \cdot x[t-1]$$

iv) casual and non-casual.

Similar to the disfunction between static & dynamic systems a casual system is one that depends on only present & past inputs.

So $y[t] = 2 \cdot x[t-1]$ still described a casual system. A non-casual system depends on future inputs $y[t] = x[t+1]$, a non-casual system.