

Lecture 3 Numerical Measures

BIO210 Biostatistics

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南方科技大学生命科学学院
SUSTech · SCHOOL OF
LIFE SCIENCES

Summarise data using numbers

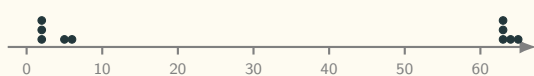
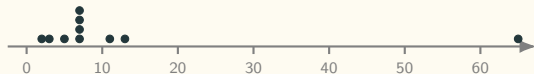
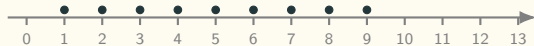
- Central tendency (mean, median, mode)
- Extremes (smallest, largest)
- Range
- Interquartile range (IQR)
- Dispersion (variance, standard deviation)

Central tendency

- Arithmetic mean: $\bar{x} = \frac{x_1 + x_2 + x_3 + \cdots + x_{n-1} + x_n}{n} = \frac{1}{n} \sum_{i=1}^n x_i$
- Median: the 50th percentile
- Mode: the most frequent values

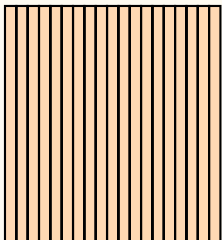
Central tendency

	Mean	Median	Mode
1, 2, 3, 4, 5, 6, 7, 8, 9	5	5	X
2, 3, 5, 7, 7, 7, 7, 11, 13	6.89	7	7
2, 3, 5, 7, 7, 7, 7, 11, 13, 65	12.7	7	7
2, 2, 2, 5, 6, 63, 63, 63, 64, 65	33.5	34.5	2, 63
2, 3, 4, 5, 6, 60, 61, 62, 63	33	33	X

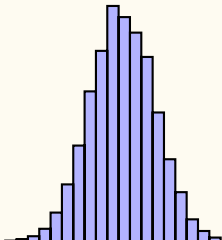


The Shape of The Data

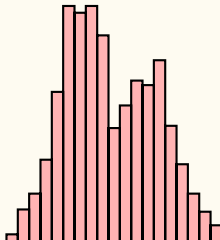
Uniform



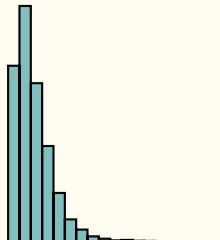
Unimodal



Bimodal



Skewed to the right

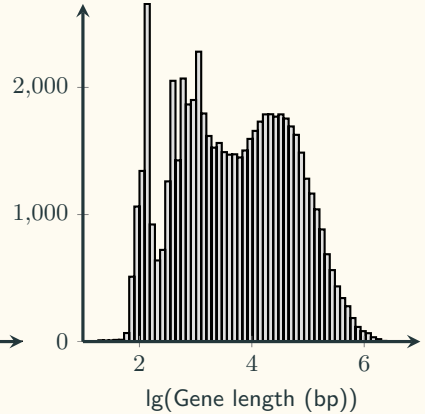
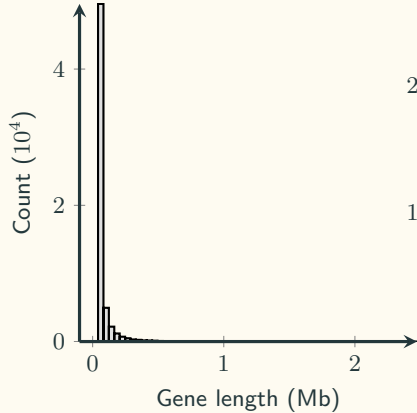
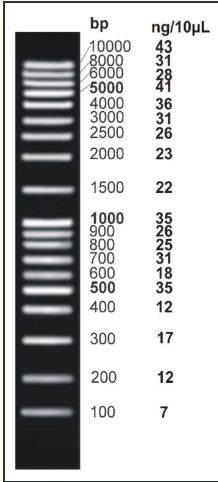


Geometric Mean

$$\text{Geometric mean: } \text{GM} = \sqrt[n]{x_1 x_2 x_3 \cdots x_{n-1} x_n} = \left(\prod_{i=1}^n x_i \right)^{\frac{1}{n}}$$

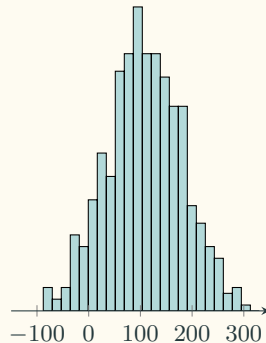
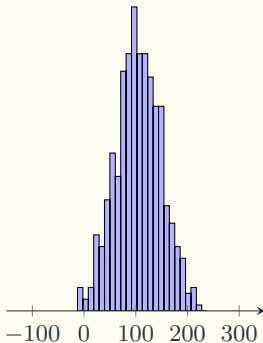
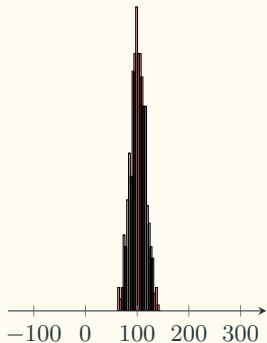
$$\log \text{GM} = \frac{1}{n} \log \left(\prod_{i=1}^n x_i \right) = \frac{1}{n} \sum_{i=1}^n \log x_i$$

Log scale in biology



Dispersion

Mean: 99.95



- Variance: $\mathbb{V}\text{ar} = \frac{1}{n} \sum_{i=1}^n (x_i - \mu)^2$ or $\frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$
- Standard deviation: $\sqrt{\mathbb{V}\text{ar}}$

Grouped data

Transcription factor binding motif length (bp):

[11, 13, 13, 11, 17, 11, 11, 13, 11, 13, 13, 11, 13, 13, 16, 11, 11, 11, 16, 11]

Mean:

$$\bar{x} = \frac{11 + 13 + 13 + 11 + 17 + 11 + 11 + 13 + 11 + 13 + 13 + 11 + 13 + 13 + 16 + 11 + 11 + 11 + 16 + 11}{20}$$

Grouped data

Motif length (bp)	Absolute frequency	Relative frequency
11	10	0.5
13	7	0.35
16	2	0.1
17	1	0.05
Total	20	1

Weighted average

Value	Absolute frequency
x_1	f_1
x_2	f_2
x_3	f_2
\vdots	\vdots
\vdots	\vdots
x_{n-1}	f_{n-1}
x_n	f_n

$$\begin{aligned}\bar{x} &= \frac{x_1 f_1 + x_2 f_2 + \cdots + x_{n-1} f_{n-1} + x_n f_n}{f_1 + f_2 + \cdots + f_{n-1} + f_n} \\&= \frac{x_1 f_1 + x_2 f_2 + \cdots + x_{n-1} f_{n-1} + x_n f_n}{\sum_{i=1}^n f_i} \\&= \frac{f_1}{\sum_{i=1}^n f_i} x_1 + \frac{f_2}{\sum_{i=1}^n f_i} x_2 + \cdots + \frac{f_n}{\sum_{i=1}^n f_i} x_n \\&= w_1 x_1 + w_2 x_2 + \cdots + w_n x_n = \sum_{i=1}^n w_i x_i\end{aligned}$$

Weighted average

Grading system:

Attendance	Assignments	Mid-term exam	Final exam
10%	20%	30%	40%

Pixel luminance:

$$0.2126 \times R + 0.7152 \times G + 0.0722 \times B$$

$$0.299 \times R + 0.587 \times G + 0.114 \times B$$

Weighted average

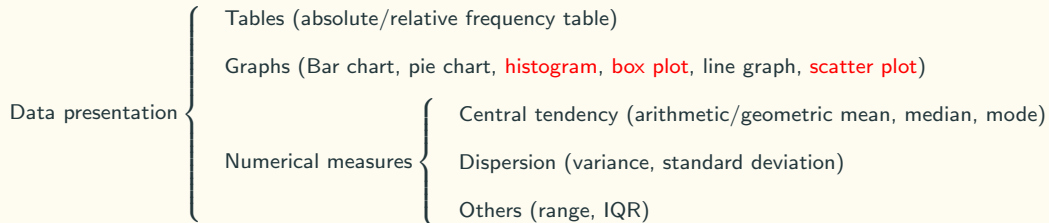
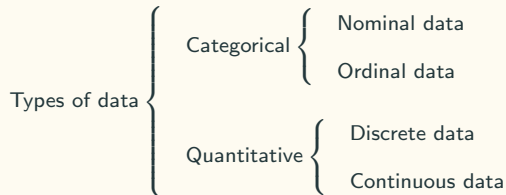
A badly manufactured
dodecahedron die



Values	Relative frequency
1	8%
2	5%
3	5%
4	5%
5	5%
6	10%
7	10%
8	10%
9	10%
10	12%
11	10%
12	10%

We roll the die repeatedly
for a large number of
times. What will be the
average number?

Summary of descriptive statistics



New way of calculating mean: weighted average $\bar{x} = \sum_{i=1}^n w_i x_i$