

Network Effects and Cascading Behavior

CS224W: Machine Learning with Graphs
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<http://cs224w.stanford.edu>



Spreading Through Networks

■ Spreading through networks:

- Cascading behavior
- Diffusion of innovations
- Network effects
- Epidemics

■ Behaviors that cascade from node to node like an epidemic

■ Examples:

■ Biological:

- Diseases via contagion

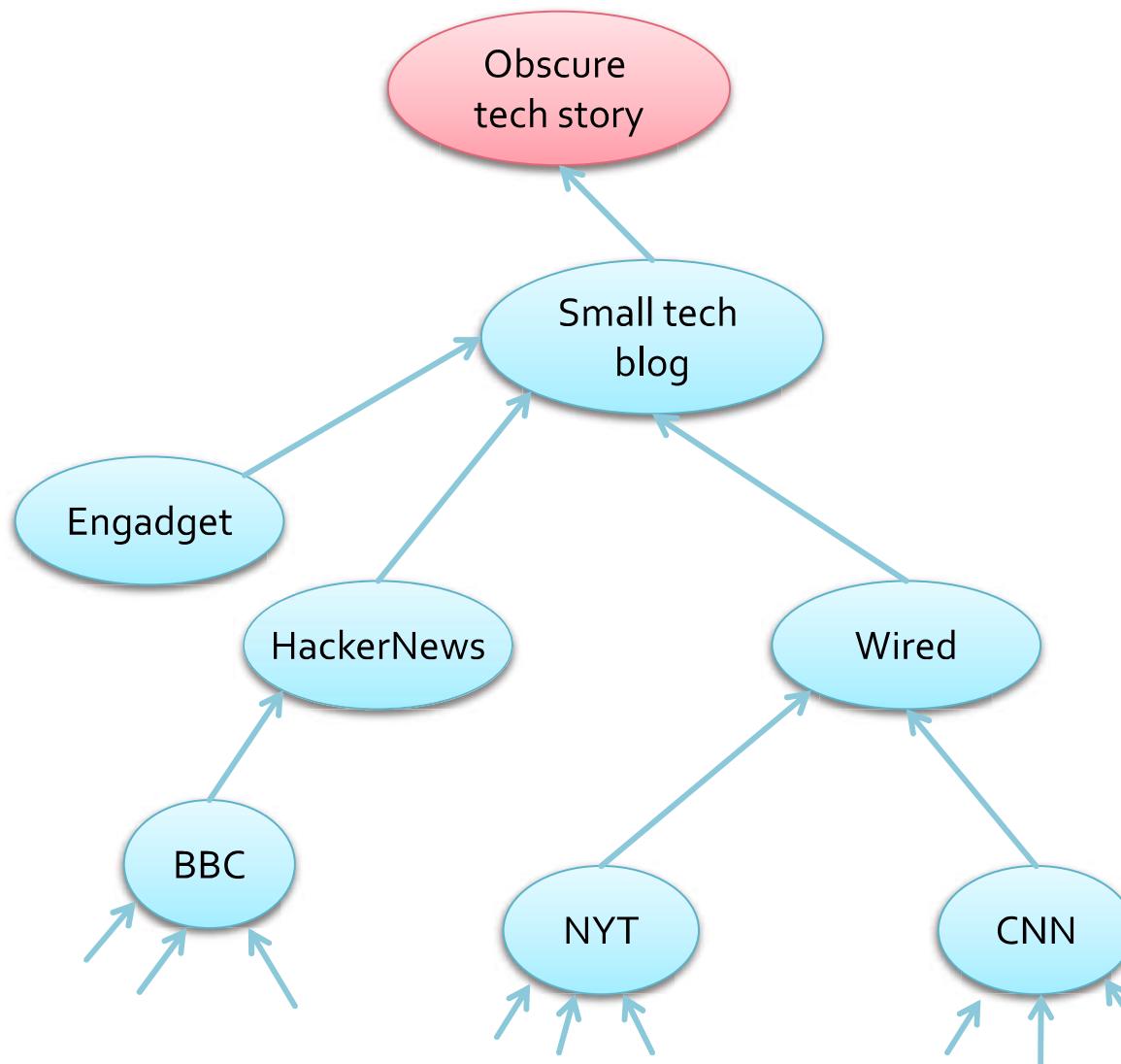
■ Technological:

- Cascading failures
- Spread of information

■ Social:

- Rumors, news, new technology
- Viral marketing

Information Diffusion: Media



Twitter & Facebook post sharing

 **Lada Adamic** shared a link via Erik Johnston.
January 16, 2013 

When life gives you an almost empty jar of nutella, add some ice cream...
(and other useful tips)

 **50 Life Hacks to Simplify your World**
twistedsifter.com

Life hacks are little ways to make our lives easier. These low-budget tips and trick can help you organize and de-clutter space; prolong and preserve your products; or teach you...

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Timeline Photos

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$$V = \pi z^2 a$$

$$V = \text{Pi}(z*z)a$$

[archive](#)



I fucking love science

Seriously. If you have a pizza with radius "z" and thickness "a", its volume is $\text{Pi}(z*z)a$.

Lina von Der Stein, Iman Khalaf, 周明佳 and 73,191 others like this.

27,761 shares

1,470 comments

46 of 1,470

Album: Timeline Photos

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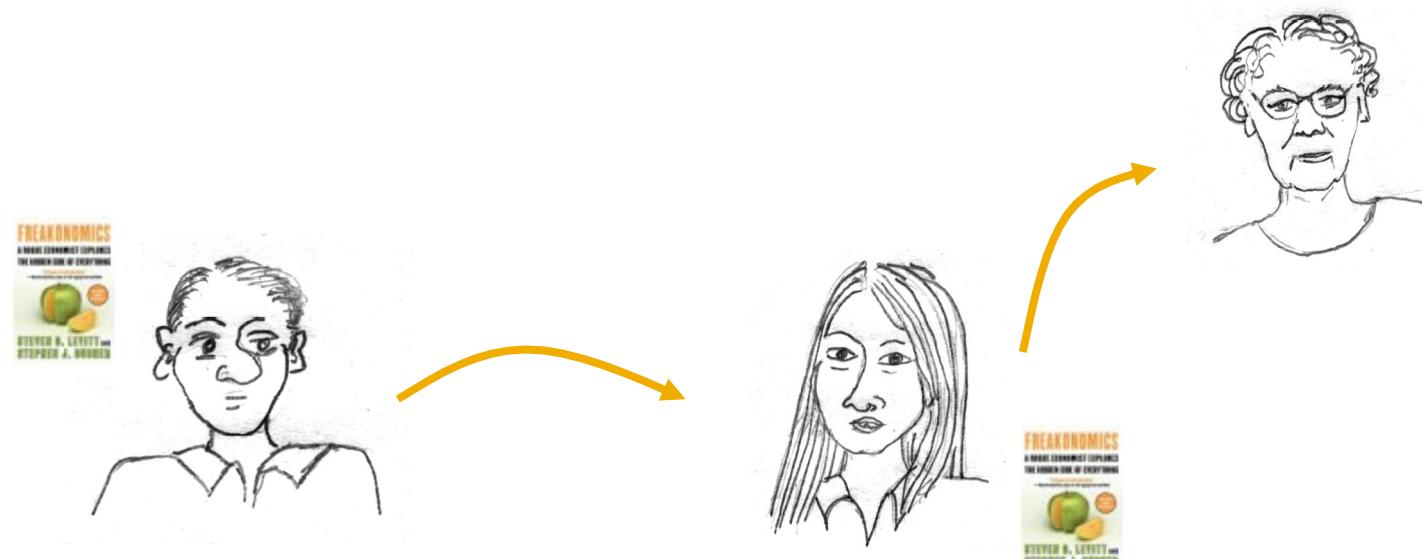
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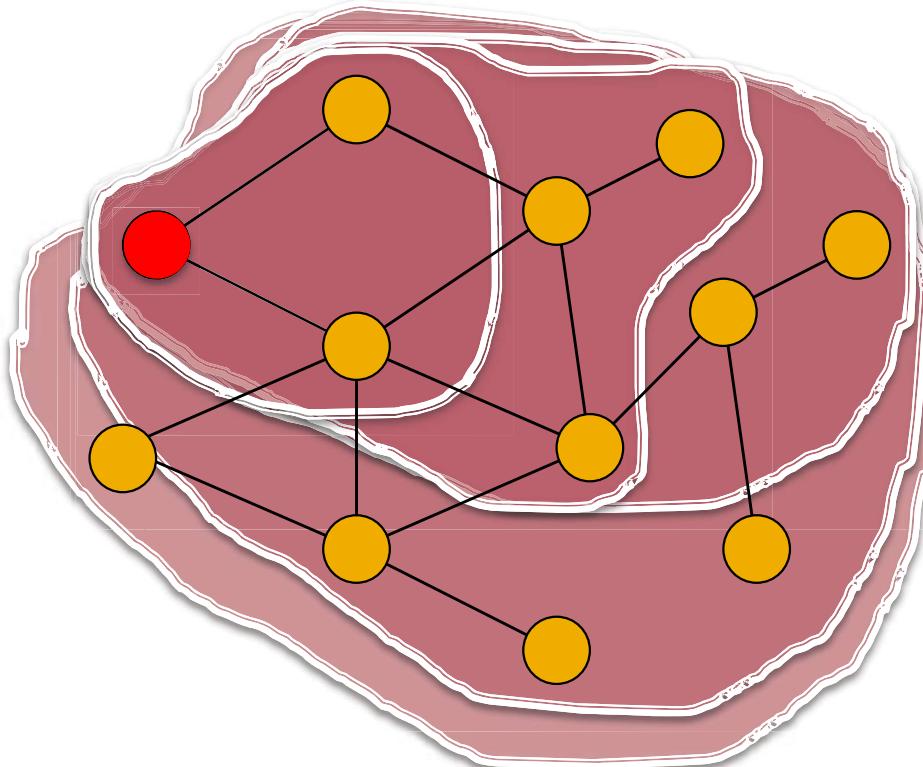
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Diffusion in Viral Marketing

- Product adoption:
 - Senders and followers of recommendations

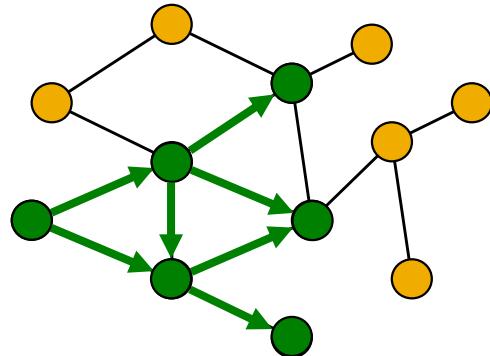


Spread of Diseases (e.g., Ebola)

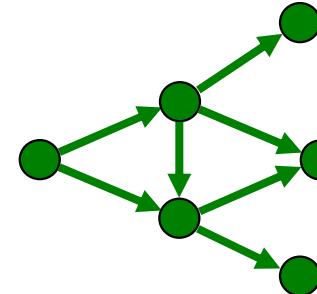


Network Cascades

- Contagion that spreads over the edges of the network
- It creates a propagation tree, i.e., **cascade**



Network



Cascade
(propagation tree)

Terminology:

- What spreads: Contagion
- “Infection” event: Adoption, infection, activation
- Main players: Infected/active nodes, adopters

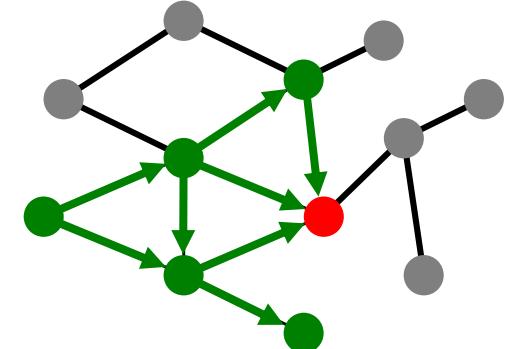
How Do We Model Diffusion?

■ Decision based models (today!):

- Models of product adoption, decision making
 - A node observes decisions of its neighbors and makes its own decision
 - **Example:**
 - You join demonstrations if k of your friends do so too

■ Probabilistic models (on Tuesday):

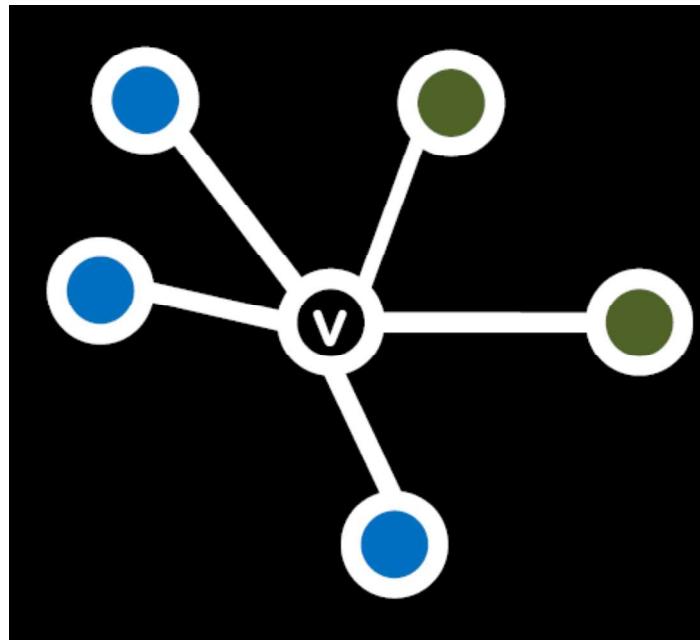
- Models of influence or disease spreading
 - An infected node tries to “push” the contagion to an uninfected node
 - Example:
 - You “catch” a disease with some prob. from each active neighbor in the network



Decision Based Model of Diffusion

Game Theoretic Model of Cascades

- Based on 2 player coordination game
 - 2 players – each chooses technology A or B
 - Each player can only adopt one “behavior”, A or B
 - Intuition: you (node v) gain more payoff if your friends have adopted the same behavior as you



Local view of the network of node v

Example: VHS vs. BetaMax



Example: BlueRay vs. HD DVD



The Model for Two Nodes

■ *Payoff matrix:*

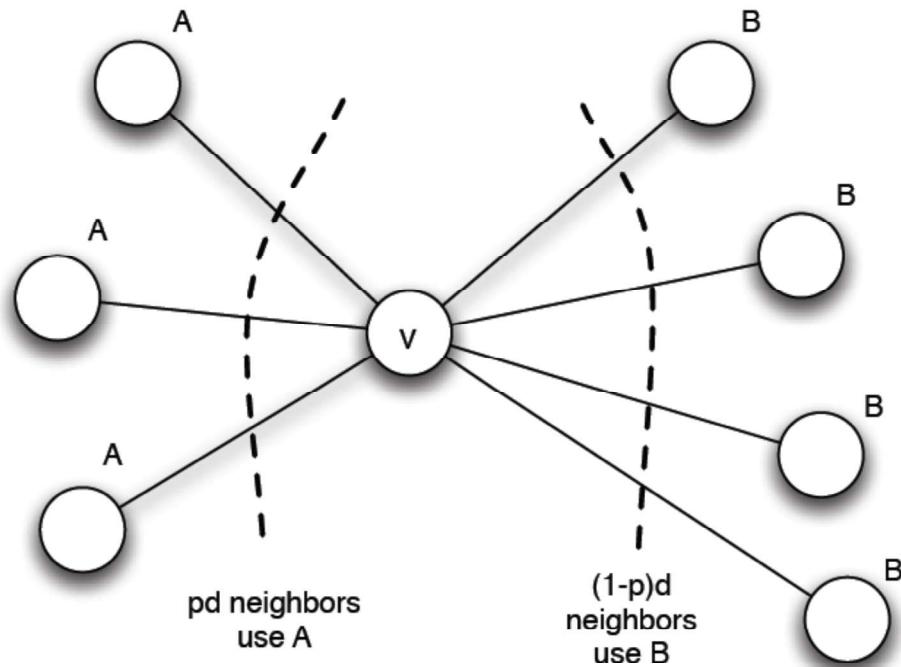
- If both v and w adopt behavior A , they each get payoff $a > 0$
- If v and w adopt behavior B , they each get payoff $b > 0$
- If v and w adopt the opposite behaviors, they each get 0



■ *In some large network:*

- Each node v is playing a copy of the game with each of its neighbors
- **Payoff:** sum of node payoffs over all games

Calculation of Node v



- Let v have d neighbors
- Assume fraction p of v 's neighbors adopt **A**
 - $\text{Payoff}_v = a \cdot p \cdot d$ if v chooses A
 $= b \cdot (1-p) \cdot d$ if v chooses B
- Thus: **v chooses A if: $p > q$**

Threshold:
 v chooses **A** if
$$p > \frac{b}{a + b} = q$$

p ... frac. v 's nbrs. with A
 q ... **payoff threshold**

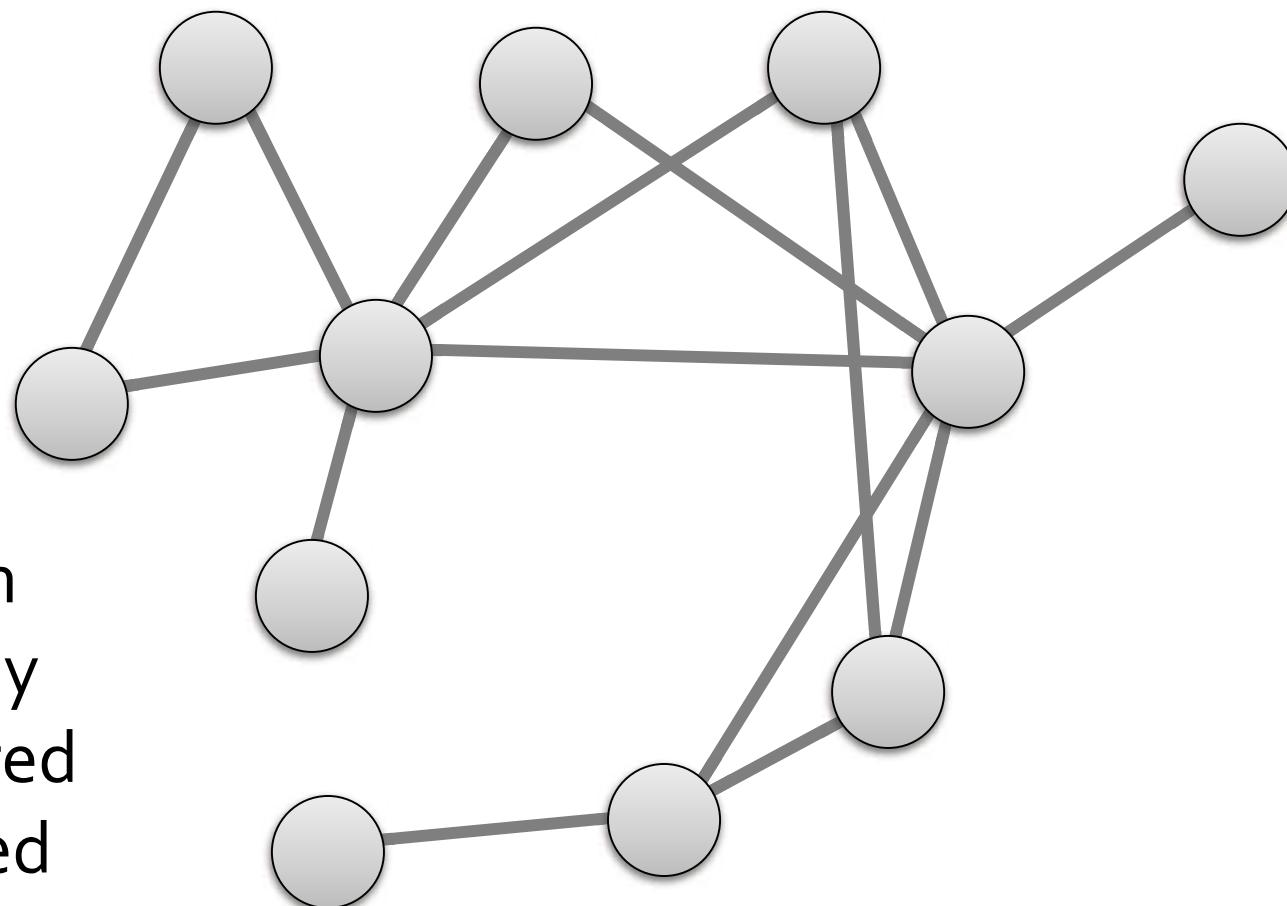
Example Scenario

Scenario:

- Graph where everyone starts with all B
- Small set S of early adopters of A
 - Hard-wire S – they keep using A no matter what payoffs tell them to do
- **Assume payoffs are set in such a way that nodes say:**
If **more than $q=50\%$** of my friends take A
I'll also take A .
This means: $a = b - \epsilon$ ($\epsilon > 0$, small positive constant)
and then $q=1/2$

Example Scenario

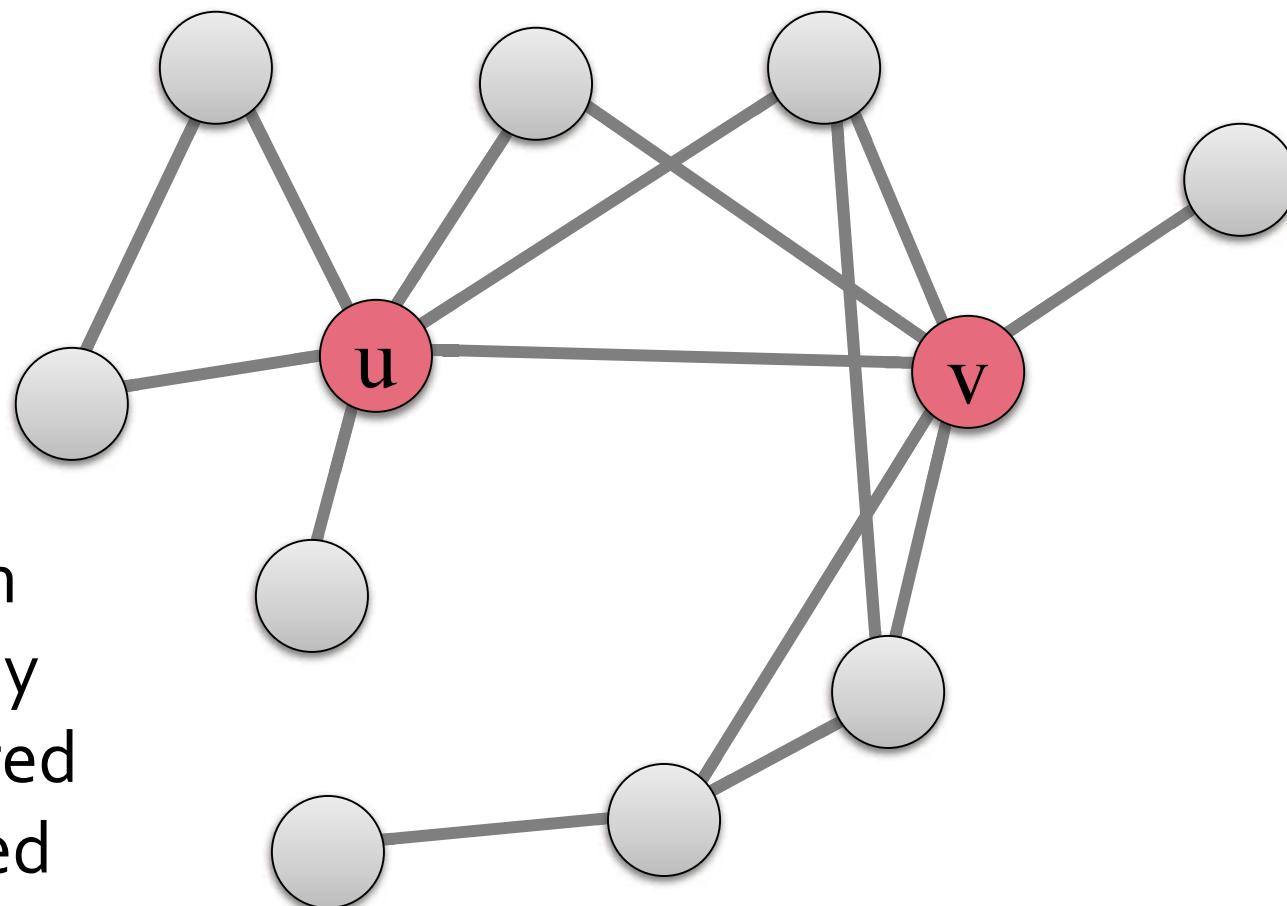
$$S = \{u, v\}$$



If **more** than
q=50% of my
friends are red
I'll also be red

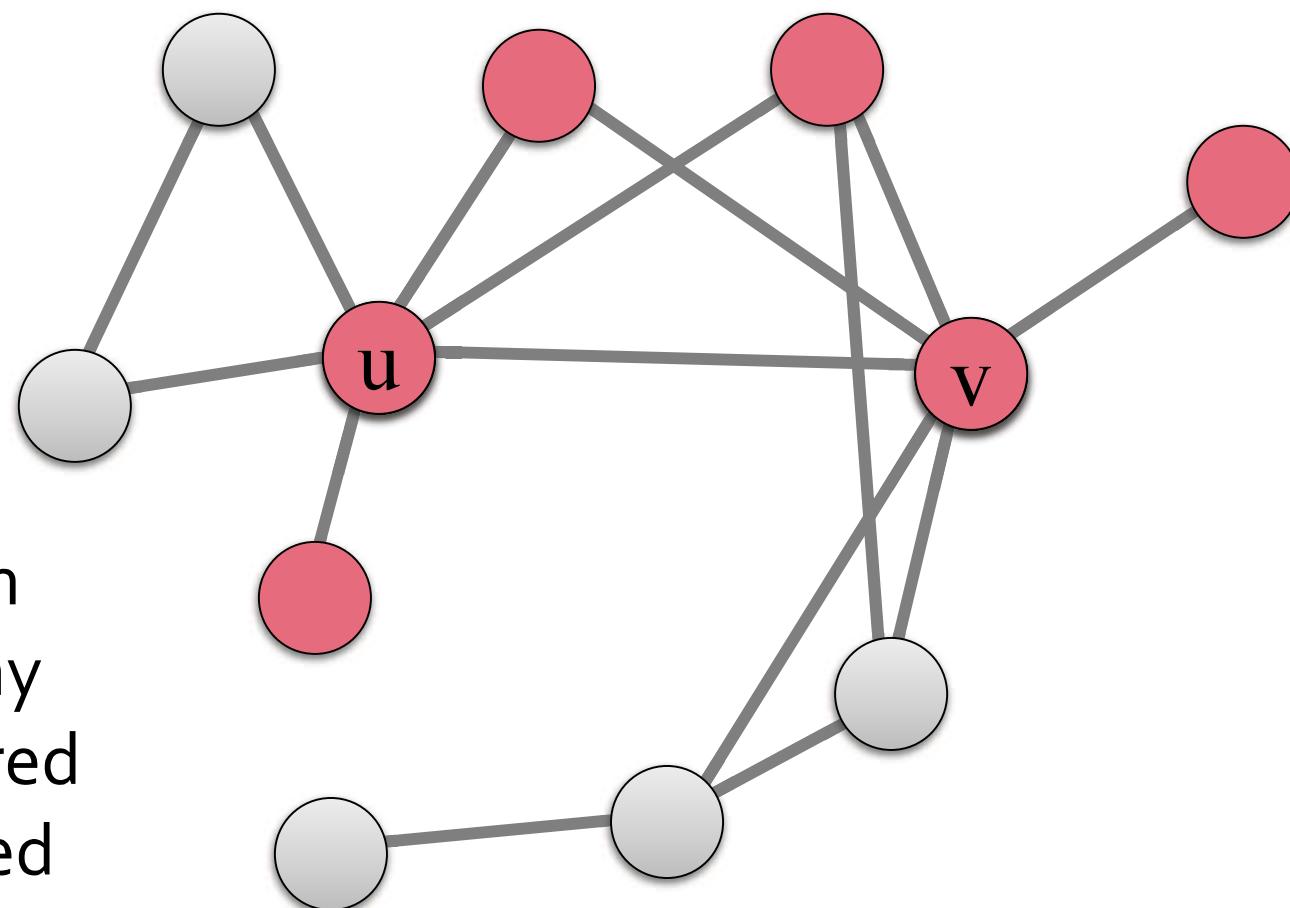
Example Scenario

$$S = \{u, v\}$$



Example Scenario

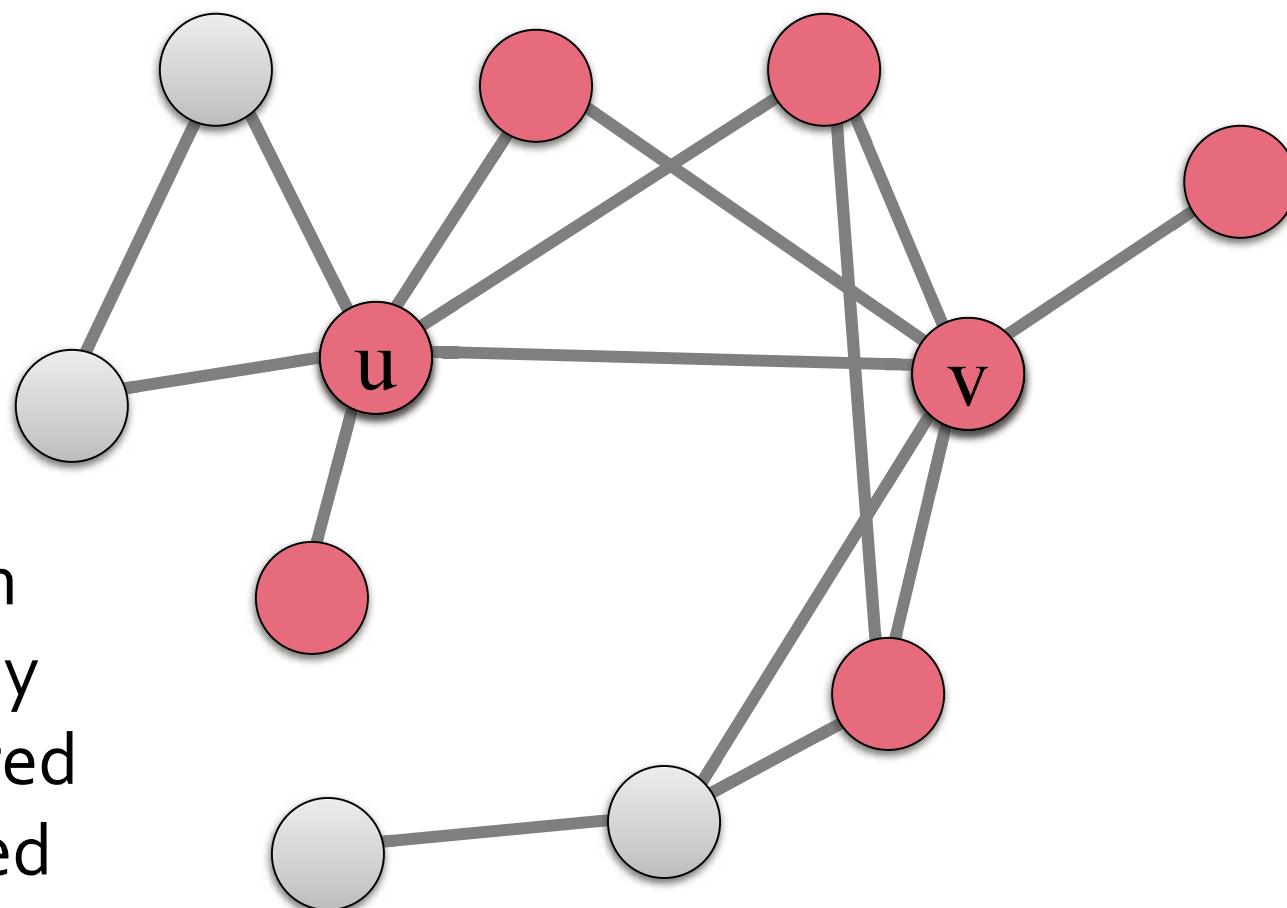
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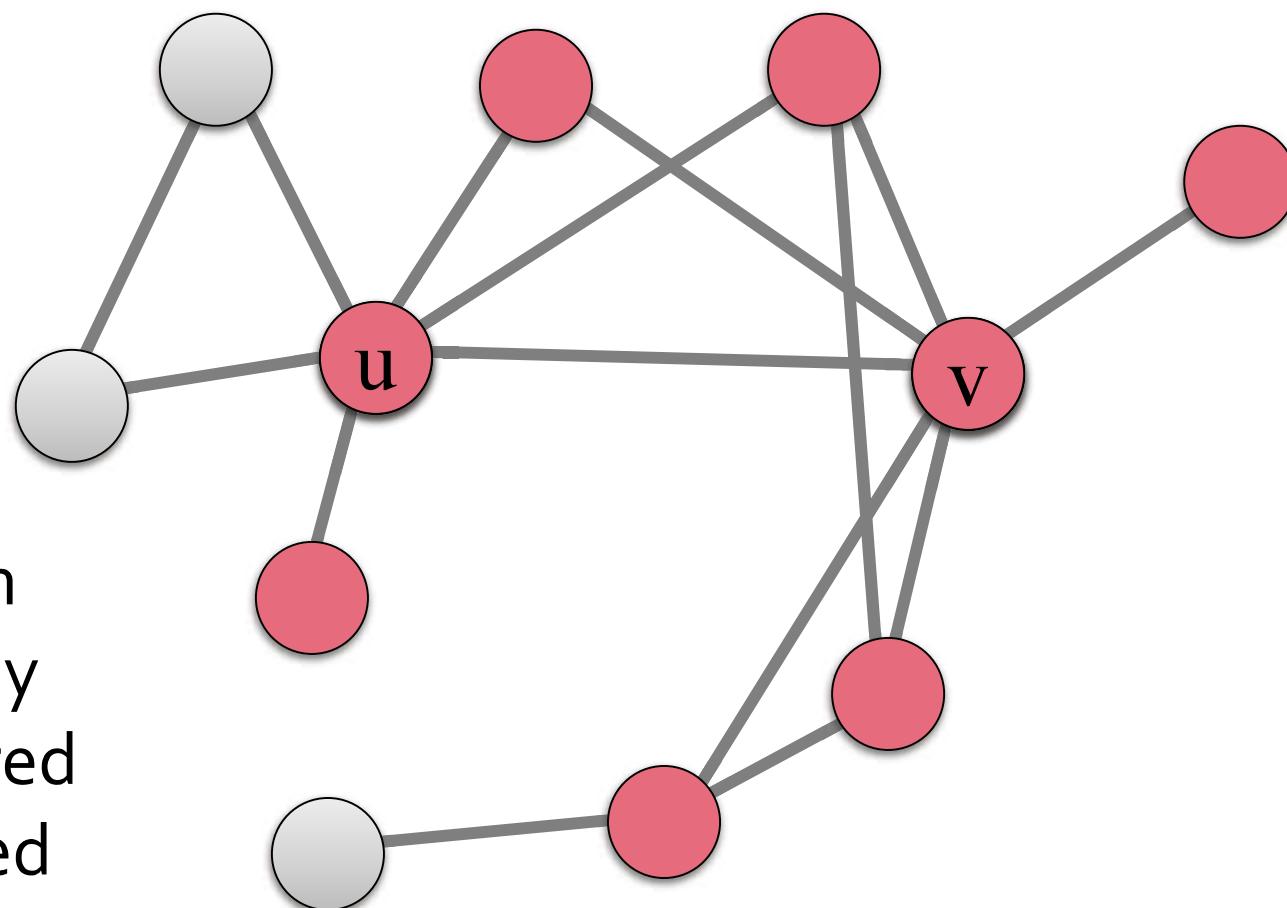
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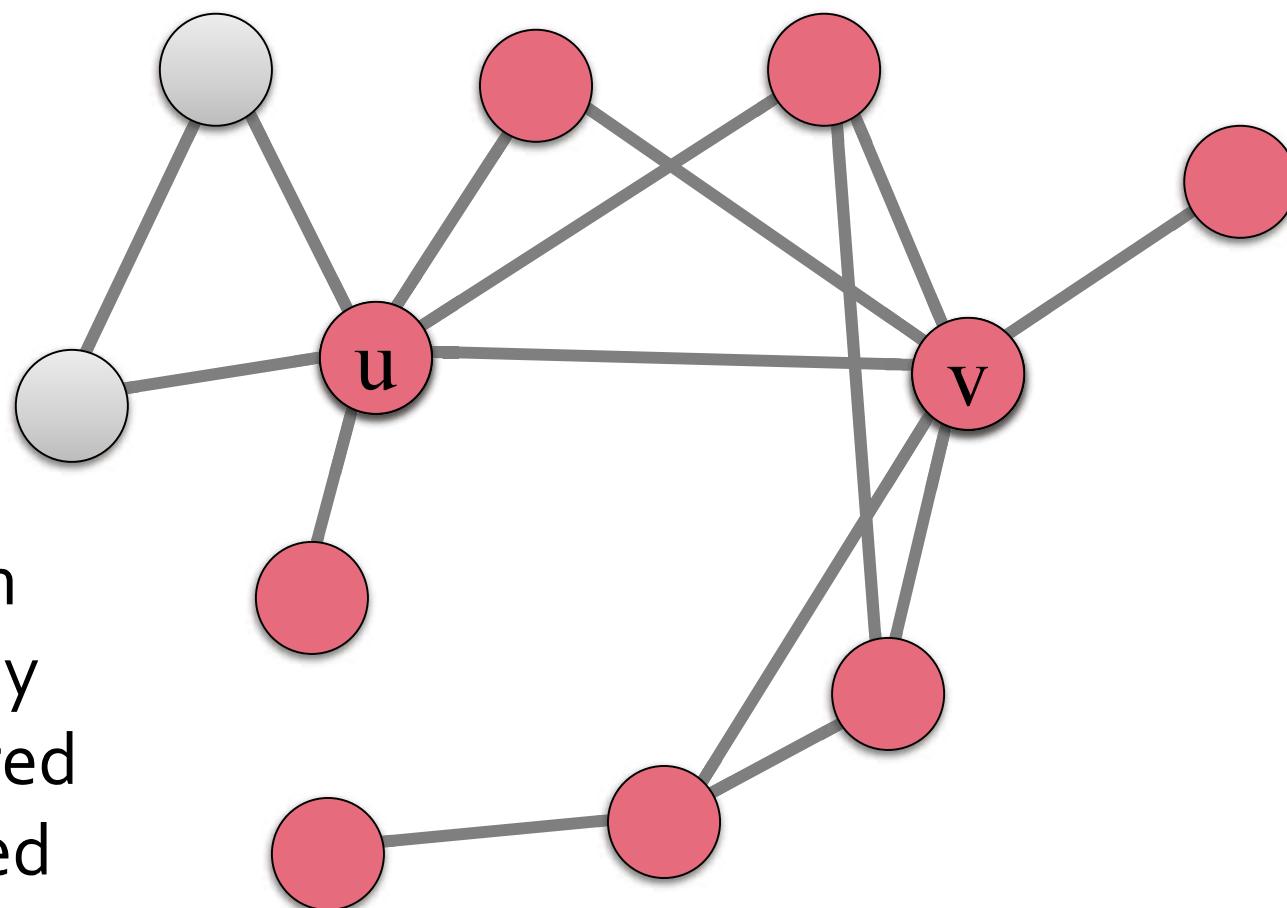
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Example Scenario

$$S = \{u, v\}$$



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Application: Modeling protest recruitment on social networks

[The Dynamics of Protest Recruitment through an Online Network](#)

Bailon et al. Nature Scientific Reports, 2011

The Spanish 'Indignados' Movement

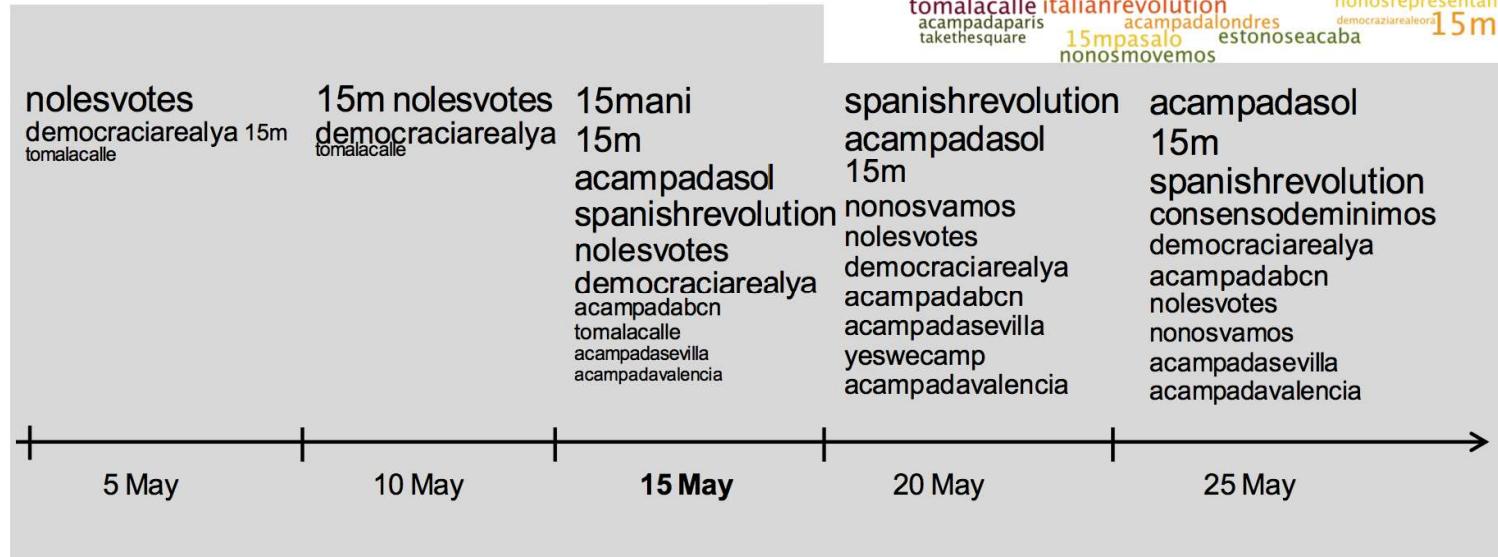
- Anti-austerity protests in Spain May 15-22, 2011 as a response to the financial crisis
- Twitter was used to organize and mobilize users to participate in the protest



Data collected using hashtags

- Researchers identified 70 hashtags that were used by the protesters

#hashtags



Dataset

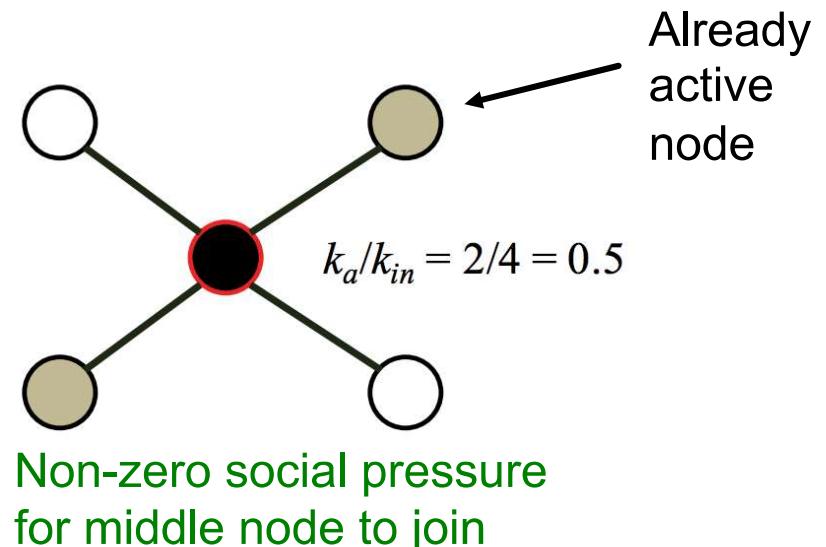
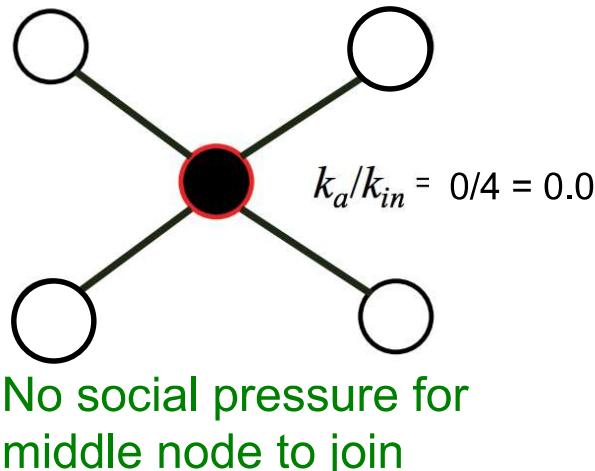
- **70 hashtags were crawled for 1 month period**
 - Number of tweets: 581,750
- **Relevant users:** Any user who tweeted any relevant hashtag and their followers + followees
 - Number of users: 87,569
- **Created two undirected follower networks:**
 1. **Full network:** with all Twitter follow links
 2. **Symmetric network** with only the reciprocal follow links ($i \rightarrow j$ and $j \rightarrow i$)
 - This network represents “strong” connections only.

Definitions

- **User activation time:** Moment when user starts tweeting protest messages
- k_{in} = The total number of neighbors when a user became active
- k_a = Number of active neighbors when a user became active
- **Activation threshold = k_a/k_{in}**
 - The fraction of active neighbors at the time when a user becomes active

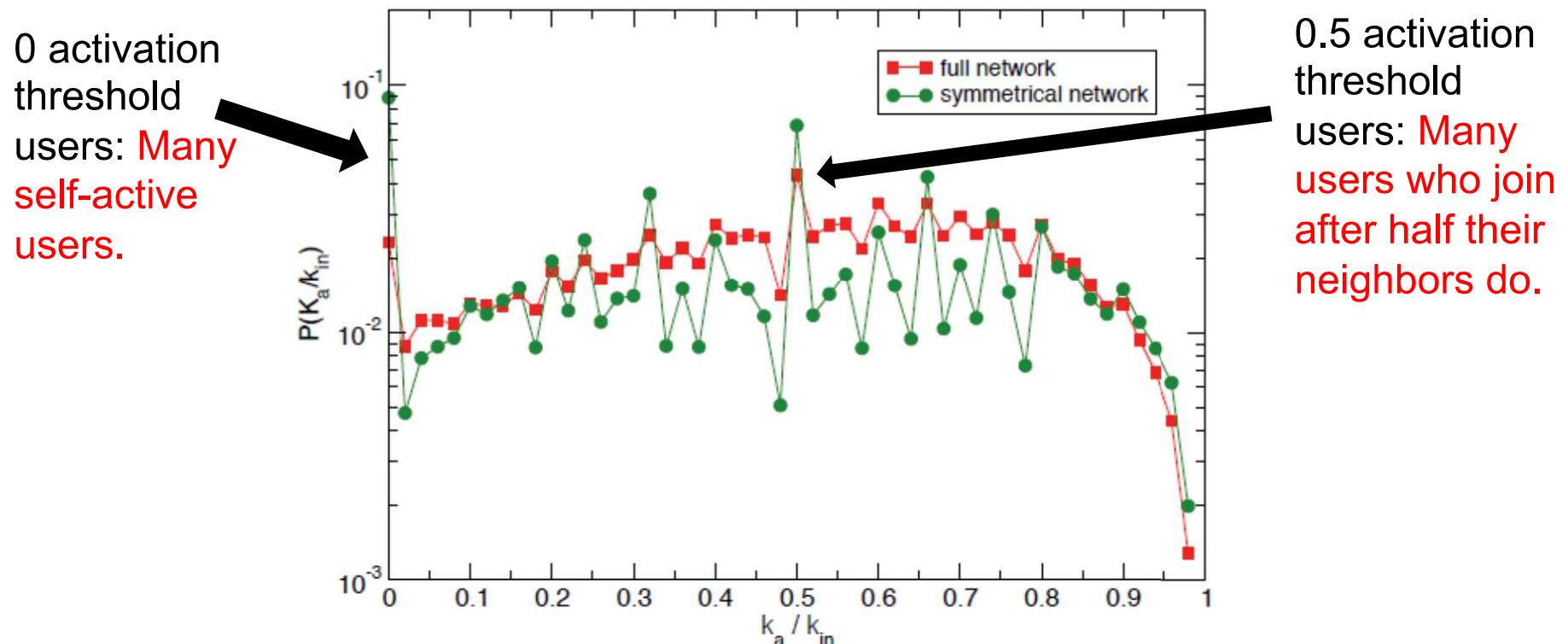
Recruitment & Activation Threshold

- If $k_a/k_{in} \approx 0$, then the user joins the movement when very few neighbors are active \Rightarrow no social pressure
- If $k_a/k_{in} \approx 1$, then the user joins the movement after most of its neighbors are active \Rightarrow high social pressure



Distribution of activation thresholds

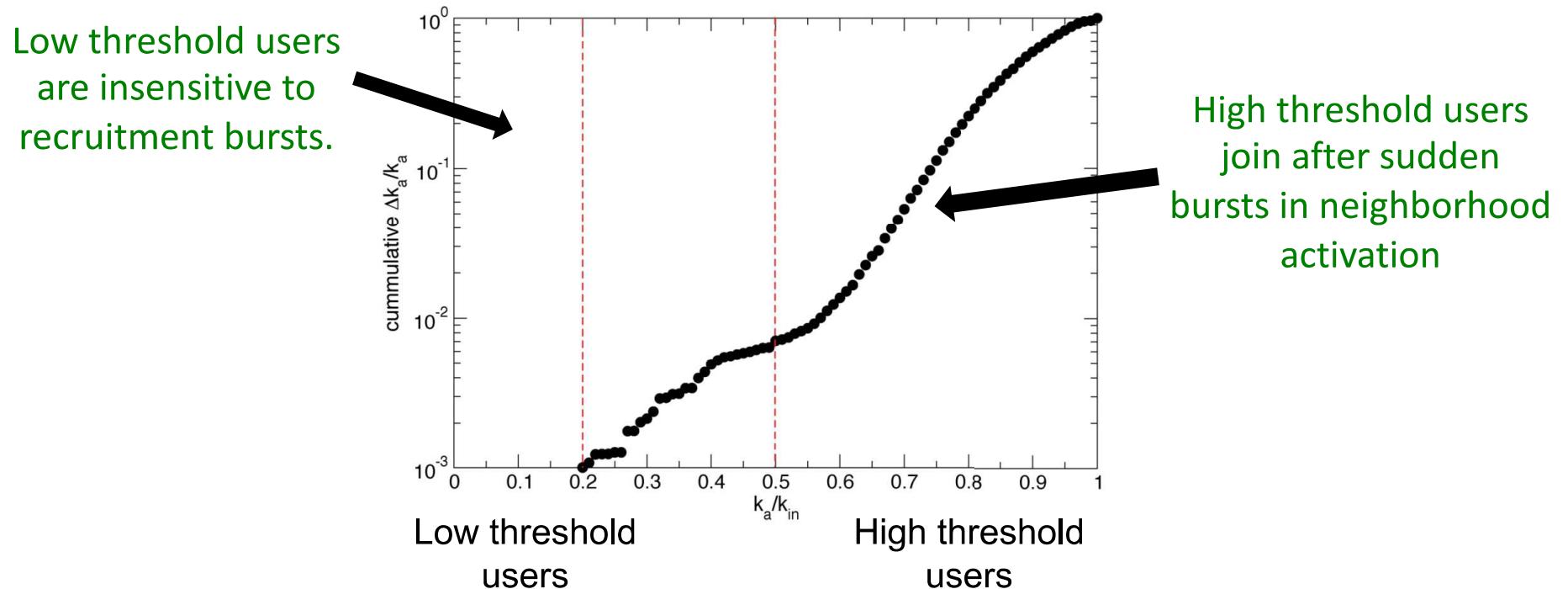
- Mostly uniform distribution of activation threshold in both networks, except for two local peaks



Effect of neighbor activation time

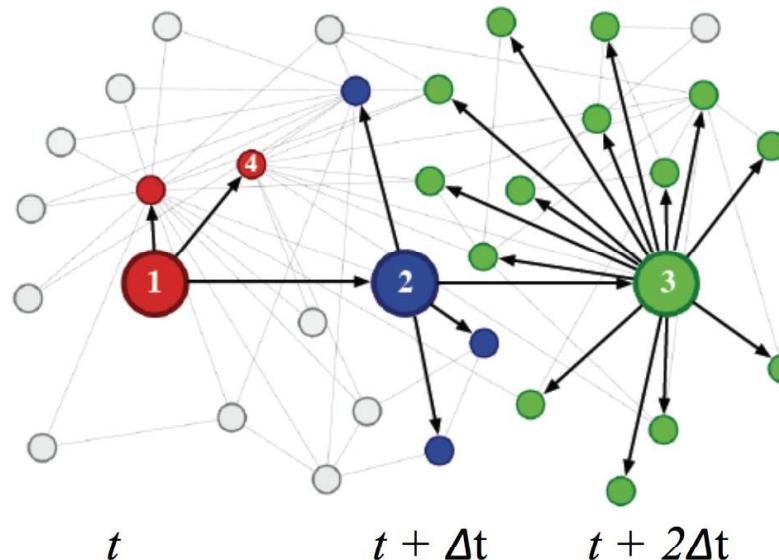
- **Hypothesis:** If several neighbors become active in a short time period, then a user is more likely to become active
- **Method:** Calculate the burstiness of active neighbors as

$$\Delta k_a/k_a = (k_a^{t+1} - k_a^t)/k_a^{t+1}$$



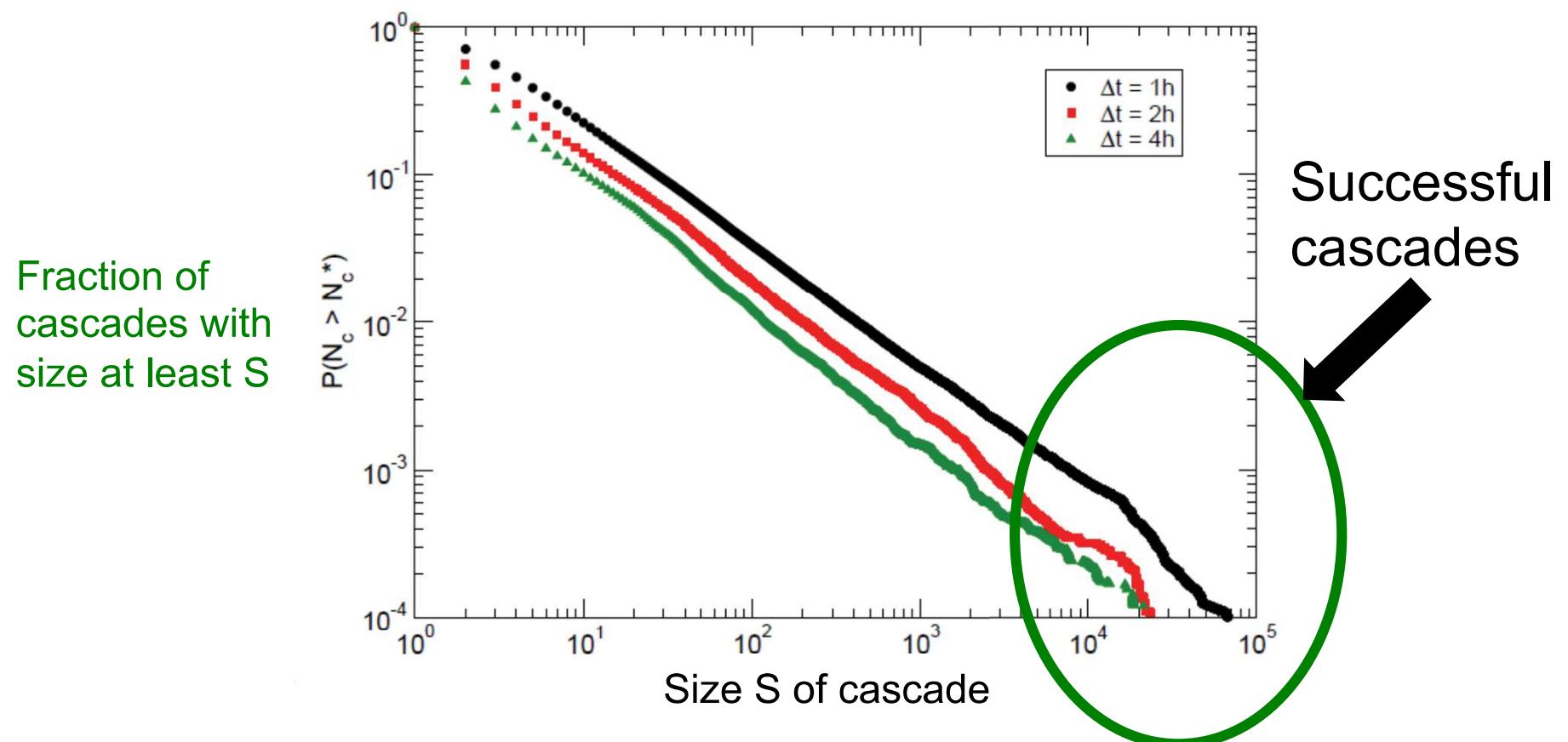
Information cascades

- No cascades are given in the data
- So cascades were identified as follows:
 - If a user tweets a message at time t and one of its followers tweets a message in $(t, t+\Delta t)$, then they form a cascade.
 - E.g., $1 \rightarrow 2 \rightarrow 3$ below form a cascade:



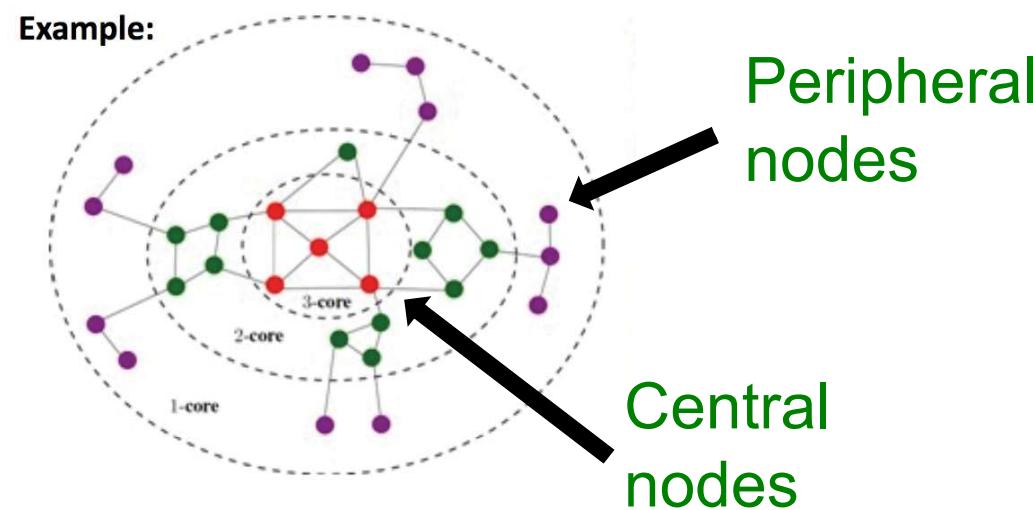
Size of information cascades

- Size = number of nodes in the cascade
- Most cascades are small:



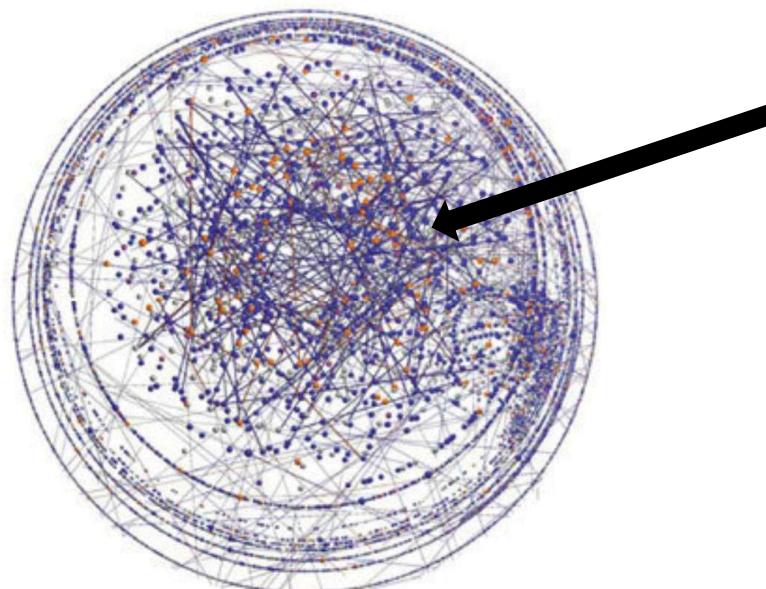
Who starts successful cascades?

- Are starters of successful cascades more central in the network?
- Method: k -core decomposition
 - k -core: biggest connected subgraph where every node has at least degree k
 - Method: repeatedly remove all nodes with degree less than k
 - Higher k -core number of a node means it is more central



Who starts the successful cascades?

- K-core decomposition of follow network
 - Red nodes start successful cascades
 - Red nodes have higher k -core values
 - So, successful cascade starters are central and connected to equally well connected users



Successful
cascade starters
are central (higher
 k -core number)

Summary: Cascades on Twitter

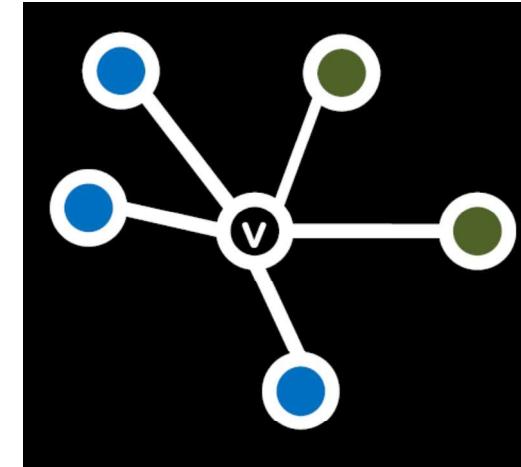
- Uniform activation threshold for users, with two local peaks
- Most cascades are short
- Successful cascades are started by central (more core) users

Models of Cascading Behavior

- So far:

Decision Based Models

- Utility based
- Deterministic
- “Node” centric: A node observes decisions of its neighbors and makes its own decision



- Next: Extending decision based models to multiple contagions

Extending the Model: Allow People to Adopt A and B

Extending the model

- So far:

- Behaviors **A** and **B** compete
- Can only get utility from neighbors of same behavior: **A-A** get **a**, **B-B** get **b**, **A-B** get **0**

- For example:

- Using Skype vs. WhatsApp
 - Can only talk using the same software
- Having a VHS vs. BetaMax player
 - Can only share tapes with people using the same type of tape
- But one can buy 2 players or install 2 programs



Cascades & Compatibility

■ So far:

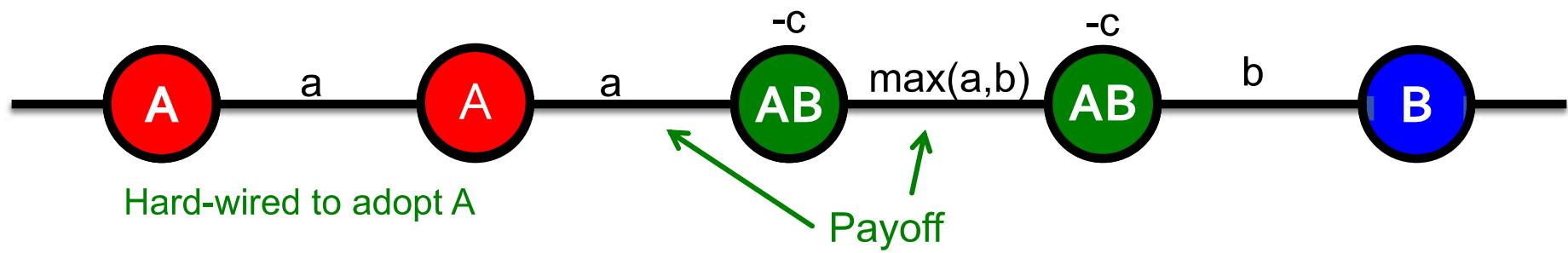
- Behaviors **A** and **B** compete
- Can only get utility from neighbors of same behavior: **A-A** get **a**, **B-B** get **b**, **A-B** get **0**

■ Let's add an extra strategy “**AB**”

- **AB-A** : gets **a**
- **AB-B** : gets **b**
- **AB-AB** : gets **max(a, b)**
- **Also:** Some **cost c** for the effort of maintaining both strategies (summed over all interactions)
 - Note: a given node can receive **a** from one neighbor and **b** from another by playing AB, which is why it could be worth the cost **c**

Cascades & Compatibility: Model

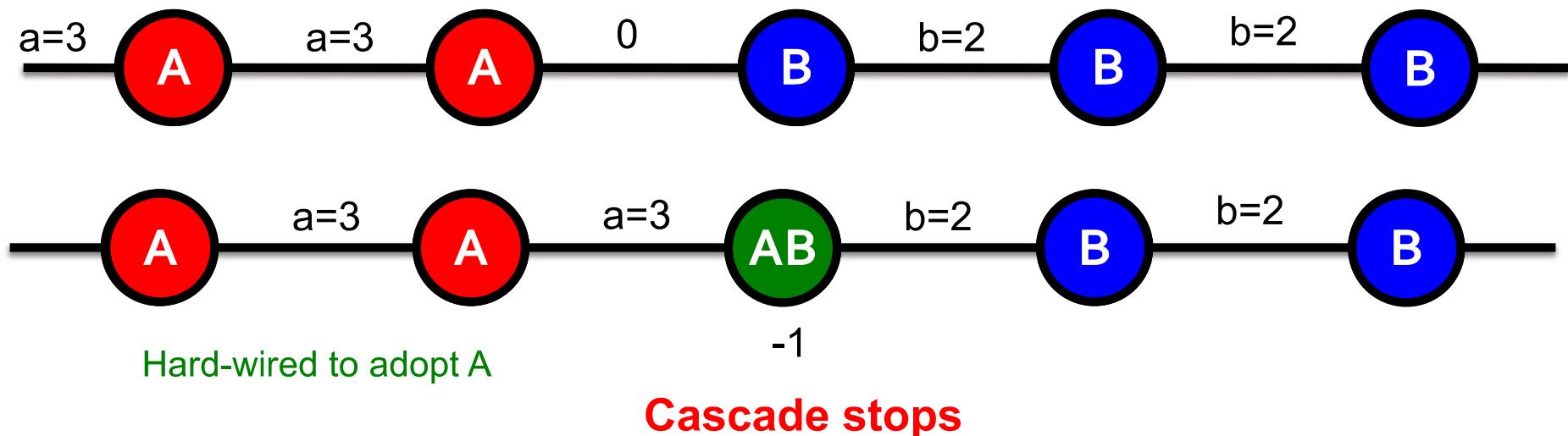
- Every node in an infinite network starts with **B**
- Then a finite set **S** initially adopts **A**
- Run the model for $t=1,2,3,\dots$
 - Each node selects behavior that will optimize payoff (given what its neighbors did in at time $t-1$)



- How will nodes switch from **B** to **A** or **AB**?

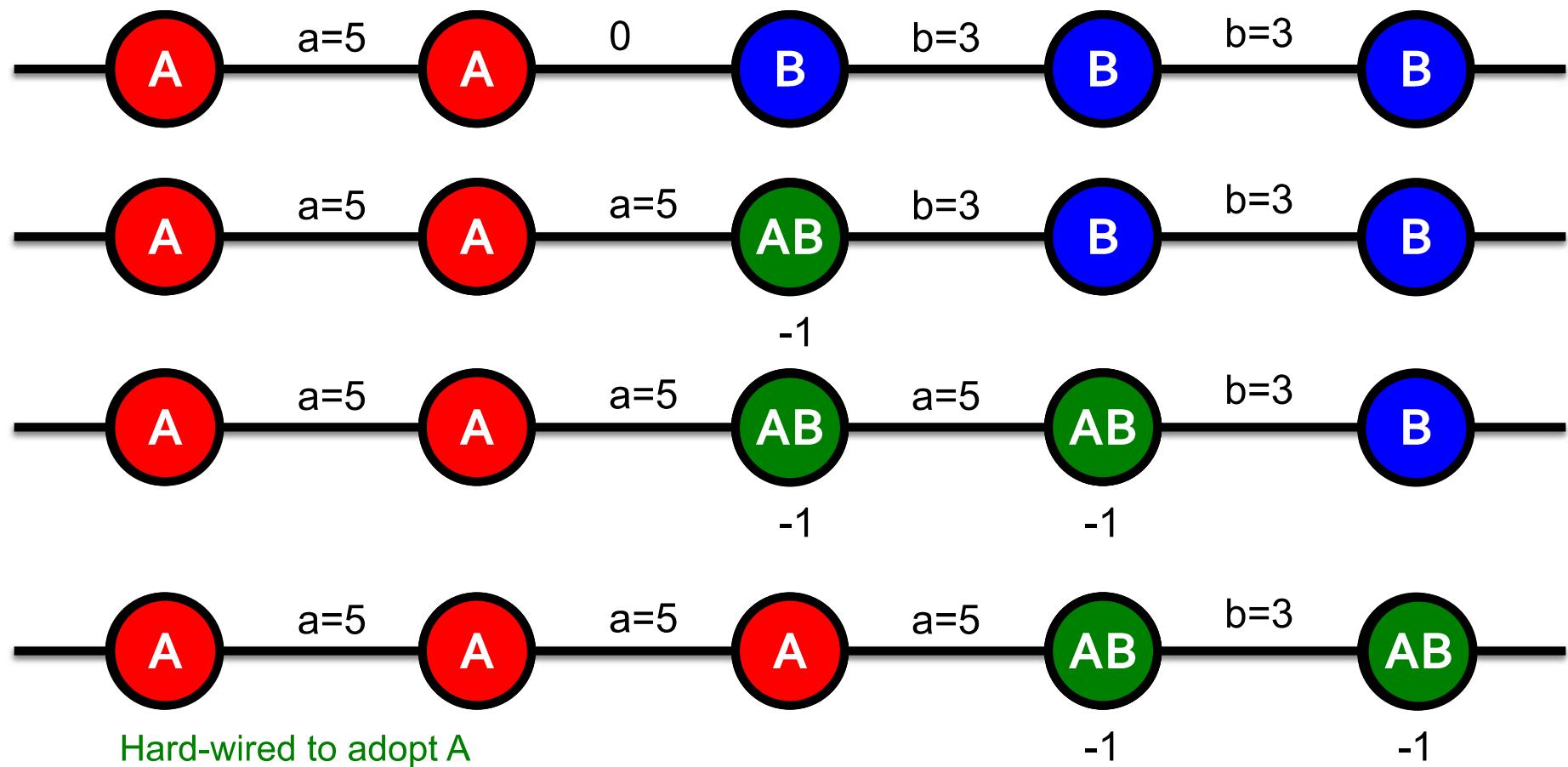
Example: Path Graph (1)

- **Path graph:** Start with Bs, $a > b$ (**A** is better)
- **One node switches to A – what happens?**
 - With just **A**, **B**: **A** spreads if $a > b$
 - With **A**, **B**, **AB**: Does **A** spread?
- **Example: $a=3$, $b=2$, $c=1$**



Example: Path Graph (2)

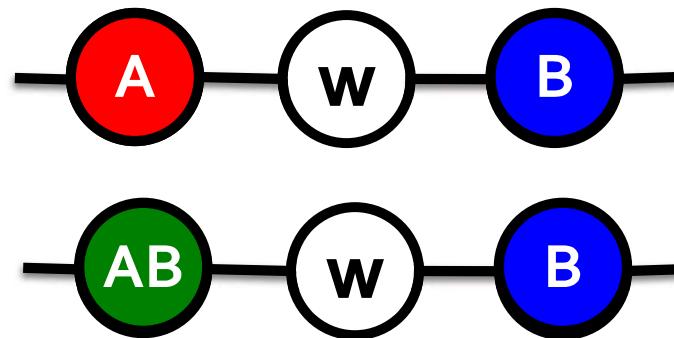
- Example: $a=5$, $b=3$, $c=1$



Cascade never stops!

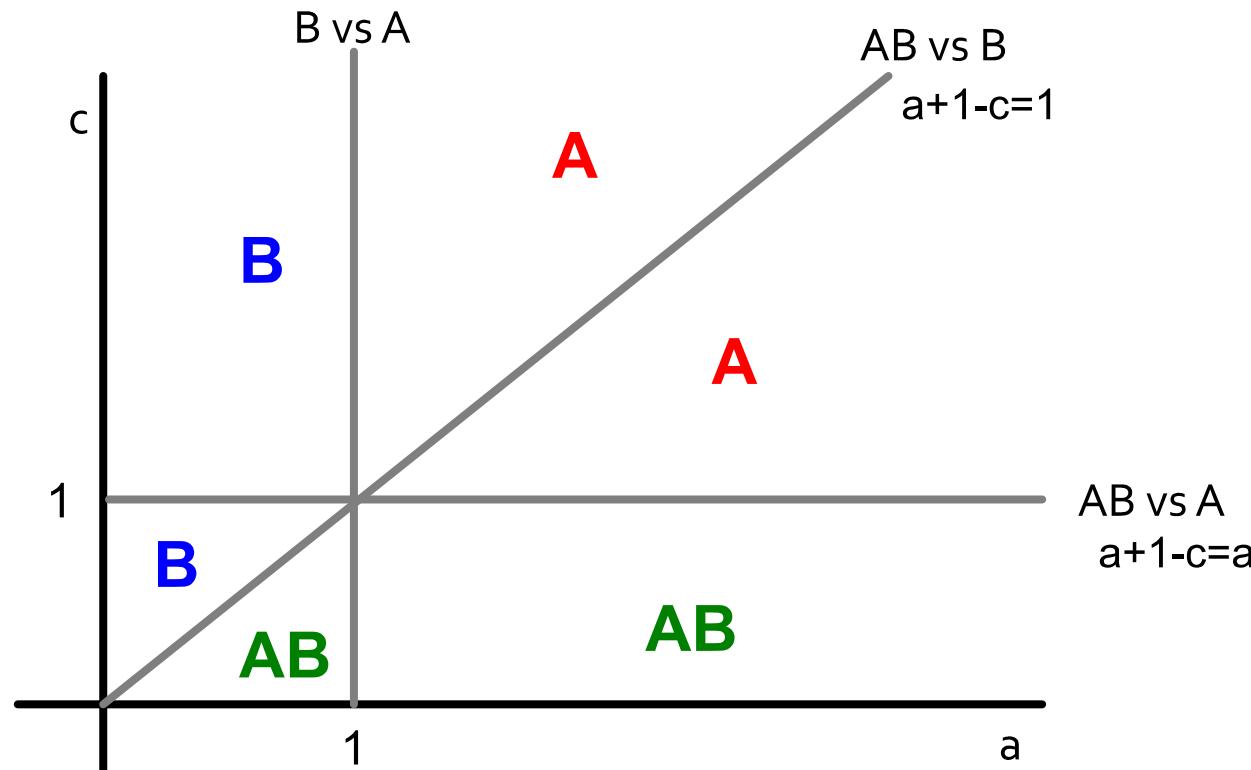
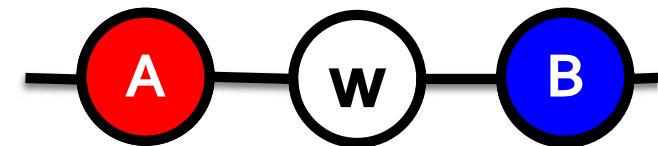
What about in a general case?

- Let's solve the model in a general case:
 - Infinite path, start with all Bs
 - Payoffs for w : A:a, B:1, AB:a+1-c
- For what pairs (c,a) does A spread?
 - We need to analyze two cases for node w : Based on the values of a and c, what would w do?



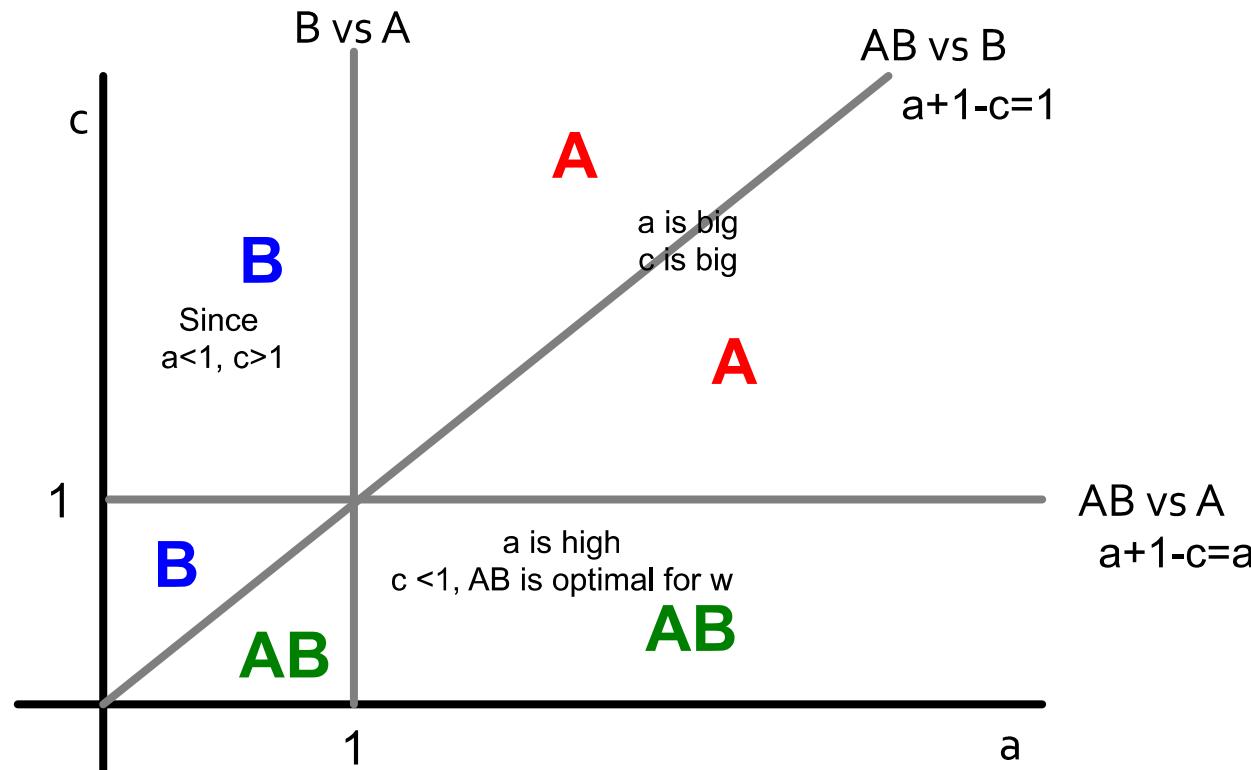
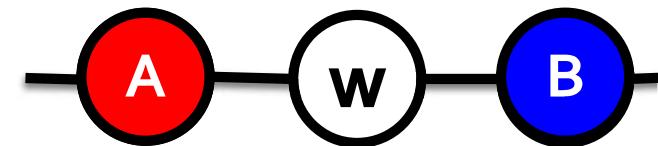
For what pairs (c, a) does A spread?

- Infinite path, start with Bs
- Payoffs for w : A: a , B:1, AB: $a+1-c$
- What does node w adopt?



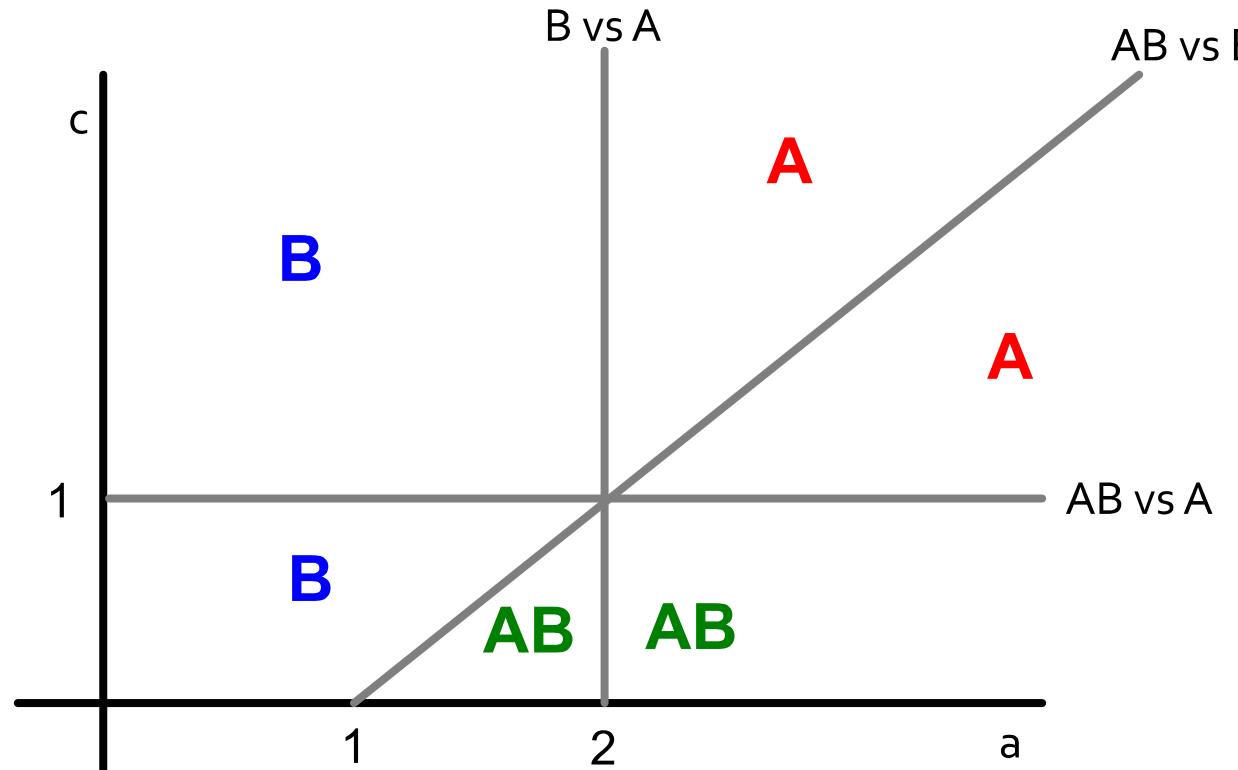
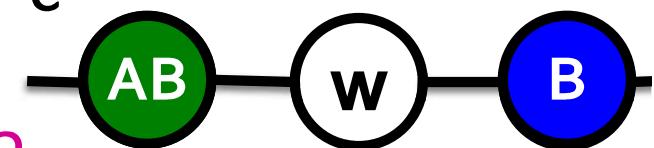
For what pairs (c,a) does A spread?

- Infinite path, start with Bs
- Payoffs for w : A: a , B:1, AB: $a+1-c$
- What does node w in A-w-B do?



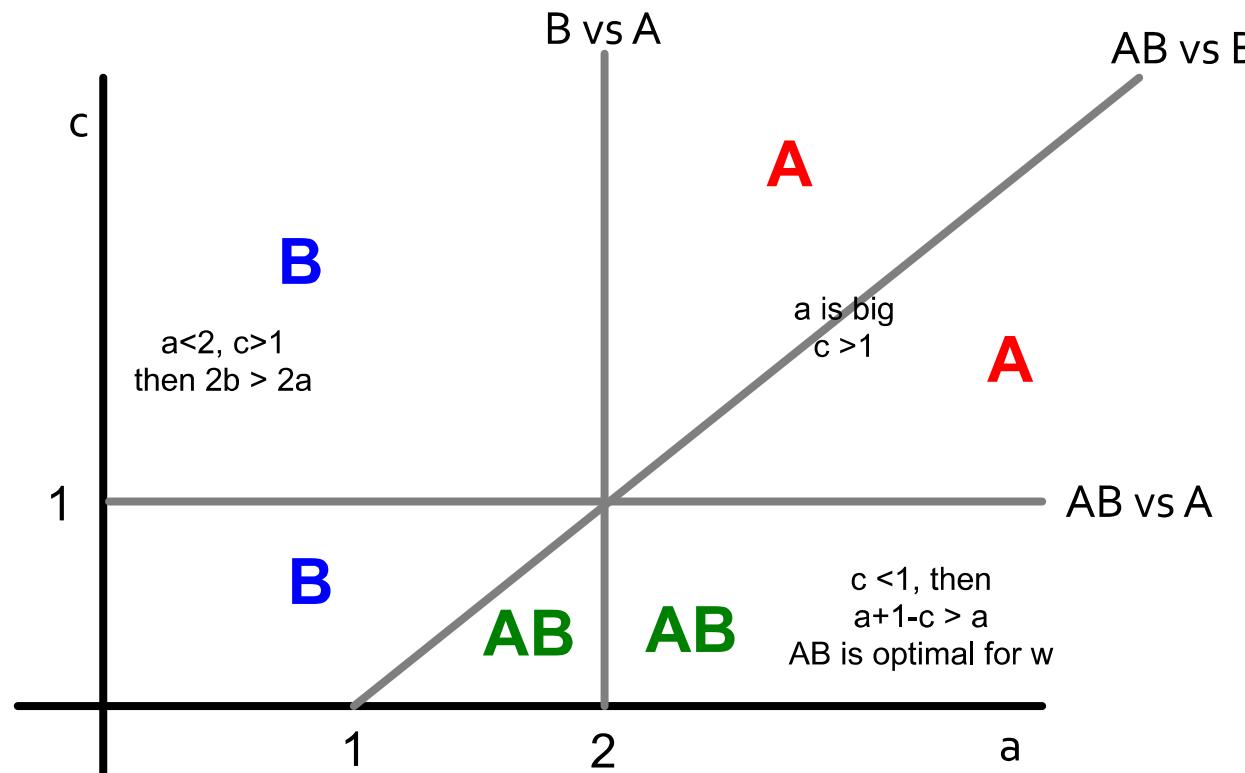
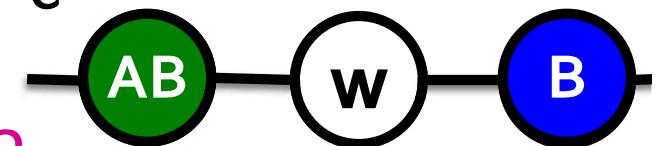
For what pairs (c,a) does A spread?

- Same reward structure as before but now payoffs for w change: $A:a$, $B:1+1$, $AB:a+1-c$
- Notice: Now also AB spreads
- What does node w in $AB-w-B$ do?



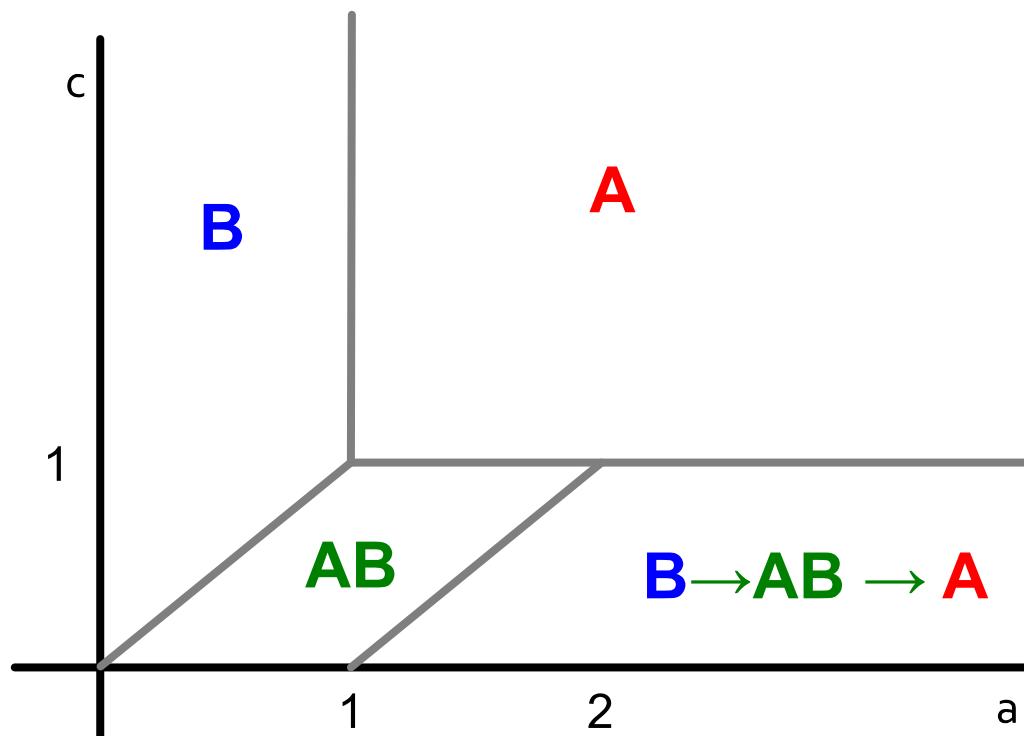
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For what pairs (c,a) does A spread?

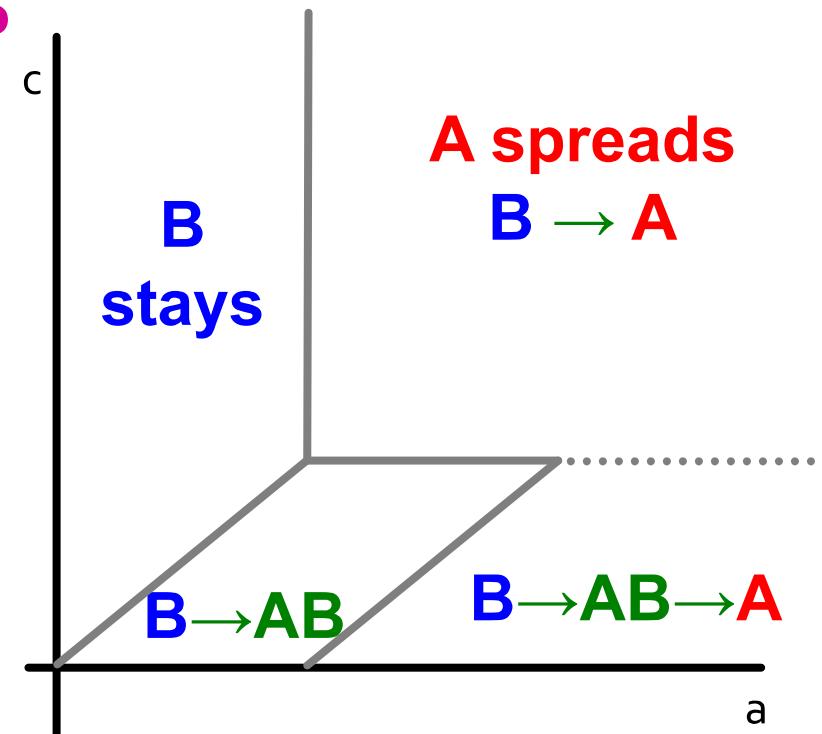
- Joining the two pictures:



Lesson

- ***B is the default throughout the network until new/better A comes along. What happens?***

- **Infiltration:** If B is **too compatible** then people will take on both and then drop the worse one (**B**)
- **Direct conquest:** If A makes itself **not compatible** – people on the border must choose. They pick the better one (**A**)
- **Buffer zone:** If you choose an optimal level then you keep a static “buffer” between **A** and **B**

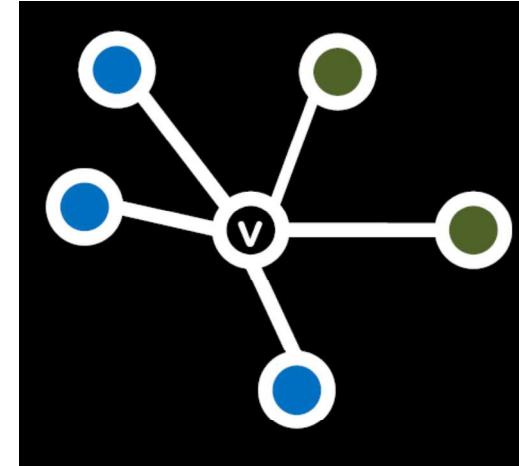


Models of Cascading Behavior

- So far:

Decision Based Models

- Utility based
- Deterministic
- “Node” centric: A node observes decisions of its neighbors and makes its own decision
- Require us to know too much about the data



- Next: Probabilistic Models

- Lets you do things by observing data
- **Limitation:** we can't model causality

