

FORMAL LANGUAGES & AUTOMATA THEORY

(Computer Science & Engineering)

Time: 3 hours

Max. Marks: 70

Answer any FIVE questions

All questions carry equal marks

- 1 Draw a DFA that recognizes the language of all strings of 0's and 1's for length ≥ 1 that, if they were interpreted as binary representations of integers, would represent integers evenly divisible by 3. Leading 0's are permissible.
- 2 Prove the theorem 'Let L be a set accepted by non-deterministic finite automata, then there exists a DFA that accepts L'.
- 3 Using the pumping lemma show that each of these languages is not regular:
 - (a) $L = \{a^n b a^{2n} | n \geq 0\}$.
 - (b) $L = \{a^i b^j c^k | k > i+j\}$.
- 4
 - (a) Construct CFG without ϵ production form $S \rightarrow a|Ab|aBa$, $A \rightarrow b| \epsilon$, $B \rightarrow b|A$.
 - (b) Explain the relationship between derivation and derivation tree with an example.
- 5
 - (a) Show that the Context Free Languages are not closed under intersection.
 - (b) State whether $S \rightarrow aSbS / bSaS / \epsilon$ is ambiguous or not. Support your answer by giving any two examples.
- 6
 - (a) Show that if L is accepted by a PDA in which no symbols are ever removed from the stack, then L is regular.
 - (b) Design a PDA for recognizing $L = \{ a^i b^j / j \leq i \text{ and } i, j > 0 \}$. Show the moves of the PDA for the string 'aabb'.
- 7 Write short notes on:
 - (a) Multitape TMs.
 - (b) Universal TM.
 - (c) Counter machine.
- 8
 - (a) Define P and NP problems with examples.
 - (b) What is PCP? Explain why PCP with two lists $x = (01, 1, 1)$ and $y = (0101, 10, 11)$ has no solution.
