

**FORMAL LANGUAGES & AUTOMATA THEORY**

(Computer Science and Engineering)

Time: 3 hours

Max. Marks: 70

**PART – A**  
(Compulsory Question)

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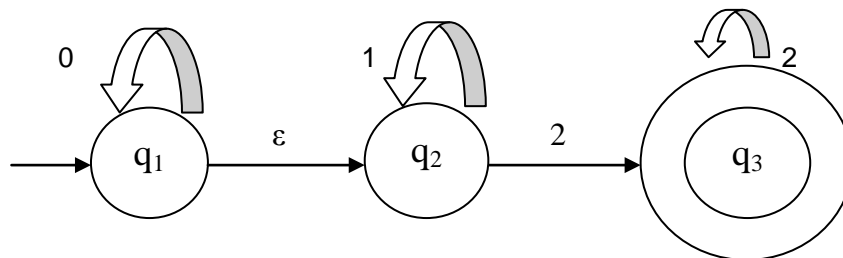
- 1 Answer the following: (10 X 02 = 20 Marks)
- Define the terms symbol, string and Language.
  - Write short notes on proof by contradiction.
  - Differentiate between Kleen closure and positive closure.
  - If  $R_1$  and  $R_2$  are two regular languages,  $R_1 \cup R_2$  and  $\overline{R_1}$  and  $\overline{R_2}$  are also regular languages, prove by DeMorgans rules that  $R_1 \cap R_2$  is also a regular language.
  - For the grammar  $E \rightarrow E+E$ ,  $E \rightarrow E^*E$ ,  $E \rightarrow id$ , construct a parse tree (using leftmost derivation) for the string  $id*id*id+id$ .
  - List the set operators under which CFLs are NOT CLOSED. Justify your answer.
  - Explain how a stack is integrated into the functioning of a PDA.
  - Give the formal definition of a PDA.
  - Explain the functioning of a counter machine.
  - State the closure properties of recursive languages.

**PART – B**

(Answer all five units, 5 X 10 = 50 Marks)

**UNIT – I**

- 2 (a) Construct the NFA for the RE  $(0+1)^*(00+11)(01)^*(0+1)^*$ .
- (b) For the following  $\epsilon$ -NFA, construct its equivalent NFA without  $\epsilon$  transitions.

**OR**

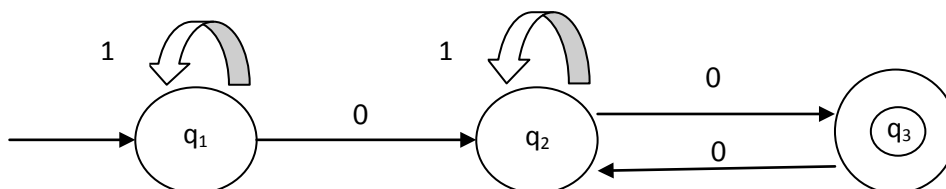
- 3 (a) Construct a Moore machine that takes strings comprising 0, 1, 2 and 3 as input (base 4 number) whose decimal equivalent modulo 7 is given as output.
- (b) How do we determine equivalence of two DFA? Explain with an example

**UNIT – II**

- 4 (a) State and prove Arden's Theorem
- (b) List the closure properties of Regular Languages

**OR**

- 5 Find the regular expression corresponding to the following DFA.



Contd. in page 2

**UNIT – III**

- 6 Convert the following grammar into GNF:  
 $X \rightarrow YZ$      $Y \rightarrow ZX \mid a$      $Z \rightarrow XY \mid b$

**OR**

- 7 (a) Explain the following terms with example:  
 (i) Ambiguous Grammar.  
 (ii) Left Recursion.  
 (iii) Chomsky's Normal Form.  
 (b) Discuss the closure properties of Context free languages.

**UNIT – IV**

- 8 (a) Construct a PDA that recognizes strings (over alphabet 0 and 1) that contain equal number of 0s and 1s.  
 (b) Construct a grammar in Chomsky's Normal Form that is equivalent to:  
 $A \rightarrow aBCb$ ,  $B \rightarrow bC$ ,  $C \rightarrow Cb$ ,  $C \rightarrow b$ .

**OR**

- 9 (a) Construct a PDA that recognizes strings of  $WW^r$  form, where  $W^r$  is the reverse of  $W$ , and strings comprise of 0s and 1s. Give the instantaneous of the PDA also.  
 (b) Construct a PDA that recognizes strings of type  $0^n 1^m \mid n > m$  using final state.

**UNIT – V**

- 10 (a) Explain the concept of Universal Turing Machine.  
 (b) Find a PCP solution for the following sets.

A	B
ab	aba
ba	abb
b	ab
abb	b
a	bab

**OR**

- 11 Construct a Turing Machine that computes the product of two numbers, represented in Unary form.

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