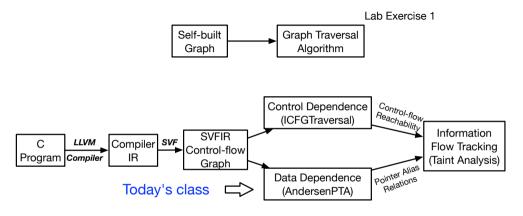
## **Data-Flow and Taint Analysis**

(Week 3)

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## Today's class



Revisiting Andersen's Analysis

- Top-level variables, whose addresses are not taken (ValPN in SVF)
  - Including stack virtual registers (symbols starting with "%") and global variables (symbols starting with "@") are explicit, i.e., directly accessed.

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  - For example, def-use for %a1 from Instruction-1 to Instruction-2.
    - Instruction-1: %a1 = alloca i8, align 1;
    - Instruction-2: store ptr <a>%a1</a>, ptr <a>%a</a>, align 8</a>

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- Address-taken variables (abstract objects), accessed indirectly at load or store instructions via top-level variables (ObjPN in SVF)
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  - A stack object created at an LLVM's 'alloca' instruction or a heap object created via (e.g., 'malloc' callsite) or a global object.
  - Def-use for address-taken variables are computed via pointer analysis.
  - For example, there is a def-use for object o from Instruction-1 to Instruction-2 if pointers %a and %b both point to o.
    - Instruction-1: store ptr %a1, ptr %a, align 8
    - Instruction-2: %c = load ptr %b, align 8

# Pointer Analysis (Revisit Andersen's Analysis in Lab-Exercise-1)

### A typical data-flow analysis

- Points-to Analysis: aims to statically determine the possible runtime values
  of a pointer at compile-time.
  - Compute the points-to set (a set of address-taken variables) of each pointer (top-level variable)
  - For example, p = &a; q = p;
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  - The resulting points-to sets of p and q are: pts(p) = pts(q) = {a}
- Alias Analysis: determines whether two pointer dereferences refer to the same memory location.
  - If the points-to sets of two pointers p and q have overlapping elements (i.e.,  $pts(p) \cap pts(q) \neq \emptyset$ ) then p and q are aliases. The derereferences of p and q may refer to the same memory location.

Why shall we learn pointer analysis?

 Essential for building data-dependence relations between variables (memory objects).

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- Compiler optimizations and bug detection
  - Constant propagation
    - \*p = 1; x = \*q;
       x is a constant value and equals 1, if p and q are must-aliases (always point to the same memory location w.r.t every execution path).
    - \*p = 1; \*q = r; x = \*p;
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    - \*p = 1; \*q = r; x = \*p;
       x is a constant value and equals 1, if p and q do not alias with each other.
  - Taint analysis
    - \*p = taintedInput; x = \*q;
       x is tainted if p and q are aliases.

### **Precision Dimensions**

Can be generally classified into the following precision dimensions at different levels of abstractions.

#### Flow-insensitive analysis:

- Ignores program execution order
- A single solution across whole program

#### Context-insensitive analysis:

 Merges all calling contexts when analysing a program method

#### Path-insensitive analysis:

 Merges all incoming path information at the join points of the control-flow graph

### Flow-sensitive analysis:

- Respects the program execution order
- Separate solution at each program point

### Context-sensitive analysis:

 Distinguishes between different calling contexts of a program method

### Path-sensitive analysis:

Computes a solution per (abstract) program path.

### **Precision Dimensions**

### Levels of Abstractions

### Assume x is a tainted value

$$p = x$$

$$p = y$$

### flow-sensitivity

at which program point

p is tainted?



## context-sensitivity

under which calling context

$$\begin{aligned} &\text{if(cond)}\\ &&p=\mathbf{x}\\ &\text{else}\\ &&p=\mathbf{y} \end{aligned}$$

### path-sensitivity

along which program path p is tainted?

## **Andersen's Pointer Analysis**

A flow-insensitive, context-insensitive and path-insensitive points-to analysis to determine points-to set of a pointer by analyzing the Constraint Graph or Program Assignment Graph (PAG) of a program.

# **Andersen's Pointer Analysis**

A flow-insensitive, context-insensitive and path-insensitive points-to analysis to determine points-to set of a pointer by analyzing the Constraint Graph or Program Assignment Graph (PAG) of a program.

- Also known as inclusion-based points-to analysis, the most popular and widely used pointer analysis.
- Solving constraint edges between ConstraintNodes (SVFVars, which are either pointer types or objects).
- The analysis requires iterative solving of the ConstraintGraph by (1) propagating points-to sets among graph nodes, and (2) adding new edges until a fixed point is reached, i.e., no new edges are added and no points-to sets change. (Lab-Exercise-1)

Andersen, L. O. (1994). Program analysis and specialization for the C programming language (Doctoral dissertation, University of Cophenhagen).

The Ant and the Grasshopper: Fast and Accurate Pointer Analysis for Millions of Lines of Code, PLDI 2007

The analysis operating upon a program's constraint graph which is a subgraph of PAG (program assignment graph).

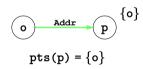
- ConstraintNode represents
  - A pointer (ValVar): (top-level variable) or
  - An object (ObjVar): (address-taken objects, i.e., heap/stack/global/function objs)
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Constraint Edge	LLVM IR	C code	Constraint rules
$p \xleftarrow{\texttt{Addr}} o$	%p = alloca <sub>o</sub>	p = &o	$\mathtt{pts}(\mathtt{p}) = \mathtt{pts}(\mathtt{p}) \cup \{\mathtt{o}\}$
$q \xleftarrow{\texttt{Copy}} p$	%q = bitcast %p	q = p	$\mathtt{pts}(\mathtt{q}) = \mathtt{pts}(\mathtt{q}) \cup \mathtt{pts}(\mathtt{p})$
$q \xleftarrow{\texttt{Load}} p$	%q = load %p	q = *p	$\forall o \in \mathtt{pts}(\mathtt{p}) : add \; edge \; q \xleftarrow{\mathtt{Copy}} o$
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$q \xleftarrow{Gep,fld} p$	%q = gep %p, fld	$\mathtt{q} = \mathtt{\&p} \!\to\! \mathtt{fld}$	$\forall \mathtt{o} \in \mathtt{pts}(\mathtt{p}) : \mathtt{pts}(\mathtt{q}) = \mathtt{pts}(\mathtt{q}) \cup \{\mathtt{o.fld}\}$

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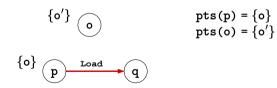
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$$\begin{cases}
o \\
p
\end{cases}
\xrightarrow{\text{copy}} q$$

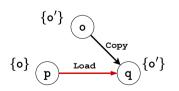
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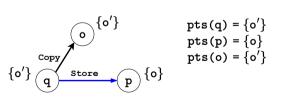
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$$pts(p) = \{o\}$$
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o \\
p
\end{cases}
\xrightarrow{\text{Gep,fld}} q$$

$$pts(p) = \{o\}$$

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# **Constraint Solving Algorithm for Andersen's Analysis**

- A worklist holds a list of constraint graph nodes for iterative processing
  - Initialize the points-to set of the destination node of each address edge. Initialize the worklist with nodes that have incoming address edges.
  - Pop a node p from the worklist.
  - Handle each incoming store edge and each outgoing load edge of node p by adding copy edges.
  - Handle each outgoing copy edge of p by propagating points-to information.
  - A node is pushed into the worklist if (1) its points-to set changes or (2) it is a source node of a new copy edge added to the graph.
- Any new copy edge added needs to be resolved and performs points-to propagation. New points-to sets discovered may trigger introducing new copy edges via load and store edges. The constraint solving should converge to a fixed point, where no new edges are added, and no points-to sets change.

# Compiling a C Program to Its LLVM IR

```
void swap(char **p, char **g){
  char* t = *p:
  *n = *a:
  *a = t:
int main(){
  char al:
                                    Compile
  char *a:
  char b1:
  char *b:
  a = &a1:
  b = &b1:
  swap(&a.&b):
```

swap.c

```
define void @swap(ptr %p, ptr %g) #0 {
entry:
 %0 = load ptr. ptr %p, align 8
 %1 = load ptr. ptr %g, align 8
 store ptr %1, ptr %p, align 8
 store ptr %0, ptr %g, align 8
  ret void
define i32 @main() #0 {
entry:
 %a1 = alloca i8, align 1
 %a = alloca ptr. align 8
 %b1 = alloca i8, align 1
 %b = alloca ptr, align 8
 store ptr %al. ptr %a. align 8
 store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
  ret i32 0
```

swap.ll

\*https://github.com/SVF-tools/Software-Securitv-Analysis/wiki/SVFIR#2-llvm-ir-generation

```
──► Load
                                                          Address
                                                                           → Store
                                                            Copy
define i32 @main() #0 {
                                                        \Omega{O1}
entry:
   %a1 = alloca i8, align 1
                                     // 01
  %a = alloca ptr. align 8
                                                                      {04}
                                                          {O3}
  %b1 = alloca i8. align 1
                                     // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
  ret i32 0
define void @swap(ptr %p, ptr %q) #0 {
entry:
  %0 = load ptr. ptr %p. align 8
  %1 = load ptr, ptr %q, align 8
  store ptr %1, ptr %p, align 8
  store ptr %0, ptr %q, align 8
  ret void
```

https://github.com/svf-tools/SVF/wiki/Analyze-a-Simple-C-Program#5-pag

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──► Load
                                                          Address
                                                            Copy
                                                                           → Store
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                                                                      {04}
                                                          {O3}
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                                     // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
  ret i32 0
define void @swap(ptr %p, ptr %q) #0 {
entry:
  %0 = load ptr. ptr %p. align 8
  %1 = load ptr, ptr %q, align 8
  store ptr %1, ptr %p, align 8
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  ret void
```

<sup>\*</sup>https://github.com/svf-tools/SVF/wiki/Analyze-a-Simple-C-Program#5-pag

→ Load

Address

```
Store
                                                            Copy
define i32 @main() #0 {
entry:
  %a1 = alloca i8, align 1
                                    // 02
  %a = alloca ptr. align 8
                                                                      {04}
                                                          {O3}
  %b1 = alloca i8. align 1
                                    // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
  ret i32 0
define void @swap(ptr %p, ptr %q) #0 {
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  %0 = load ptr. ptr %p. align 8
  %1 = load ptr, ptr %q, align 8
  store ptr %1, ptr %p, align 8
  store ptr %0, ptr %q, align 8
  ret void
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```
Address
                                                                            ► Load
                                                                            → Store
                                                             Copy
define i32 @main() #0 {
                                                                       {02}
entry:
  %a1 = alloca i8, align 1
  %a = alloca ptr. align 8
                                                                        {04}
                                                           {O3}
                                     // O3
  %b1 = alloca i8, align 1
                                                                                     (04)
                                     // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  ret i32 0
define void @swap(ptr %p, ptr %q) #0 {
entry:
  %0 = load ptr, ptr %p, align 8
  %1 = load ptr. ptr %g, align 8
  store ptr %1, ptr %p, align 8
  store ptr %0, ptr %g, align 8
  ret void
```

```
Algorithm 1: 1 Andersen's Pointer Analysis
   Input: G =< V, E >: Constraint Graph
           V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address p do
                                               // Address rule
      pts(p) = o:
      pushIntoWorklist(p):
s while WorkList + @ do
      p := popFromWorklist();
      foreach o ∈ nts(n) do
          foreach ostoren e F do
                                                 // Store rule
8
               if q <sup>Copy</sup> o ∉ E then
                   E := E \sqcup \{a \xrightarrow{Copy} a\}:
10
                                             // Add copy edge
                  nushIntoWorklist(a):
11
          foreach p \stackrel{\text{Load}}{\longrightarrow} r \in E do
                                                   // Load rule
12
              if o copy r ∉ E then
                   E := E \cup \{o \xrightarrow{Copy} r\}:
                                             // Add copy edge
14
                  pushIntoWorklist(o):
15
      foreach p Copy x ∈ F do
16
                                                   // Copy rule
          pts(x) := pts(x) \cup pts(p);
17
          if pts(x) changed then
18
              pushIntoWorklist(x);
      foreach p \xrightarrow{Gep,f1d} x \in E do
                                                    // Gep rule
20
21
          foreach o E pts(p) do
            pts(x) := pts(x) \cup \{o.fld\};
23
          if nto(x) changed then
               pushIntoWorklist(x):
24
```

https://github.com/svf-tools/SVF/wiki/Analyze-a-Simple-C-Program#5-pag

## **Andersen's Pointer Analysis**

```
Address
                                                                          Load
                                                           Copy
                                                                          Store
                                                                     {02}
define i32 @main() #0 {
entry:
  %a1 = alloca i8, align 1
                                                         {O3}
                                                                     {04}
  %a = alloca ptr. align 8
                                      // O3
  %b1 = alloca i8, align 1
                                                                                   (04)
                                      // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
  ret i32 0
define void @swap(ptr %p, ptr %q) #0 {
entry:
  %0 = load ptr, ptr %p, align 8
  %1 = load ptr. ptr %q, align 8
  store ptr %1, ptr %p, align 8
                                                tail
                                                                                head
  store ptr %0, ptr %g, align 8
  ret void
                                                              WorkList
```

```
Algorithm 2: 1 Andersen's Pointer Analysis
  Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o → p do
                                                // Address rule
      pts(p) := pts(p) \cup \{o\}:
      pushIntoWorklist(p):
5 while WorkList ≠ Ø do
       p := popFromWorklist():
       foreach o ∈ pts(p) do
          foreach a \xrightarrow{\text{Store}} p \in E do
                                                  // Store rule
              if a copy o ∉ E then
                   E := E \cup \{q \xrightarrow{Copy} o\}:
                                               // Add copy edge
10
                   pushIntoWorklist(a):
11
          foreach p \xrightarrow{Load} r \in E do
                                                    // Load rule
12
              if o copy r # E then
13
                   E := E \cup \{o \xrightarrow{Copy} r\};
                                              // Add copy edge
14
                   pushIntoWorklist(o);
15
       foreach p \xrightarrow{Copy} x \in F do
16
                                                    // Copy rule
          pts(x) := pts(x) \cup pts(p);
17
          if pts(x) changed then
18
19
              pushIntoWorklist(x):
       foreach p \stackrel{\text{Gep,fld}}{\longrightarrow} x \in F do
                                                     // Gep rule
20
          foreach o ∈ pts(p) do
21
22
              pts(x) := pts(x) \cup \{o.fld\};
23
          if pts(x) changed then
              pushIntoWorklist(x);
24
```

## **Andersen's Pointer Analysis**

```
Address
                                                                           Load
                                                           Copy
                                                                           Store
                                                                      {O2}
define i32 @main() #0 {
entry:
                                      // 01
  %a1 = alloca i8, align 1
                                                                      {04}
                                                          {O3}
  %a = alloca ptr. align 8
                                      // O3
  %b1 = alloca i8, align 1
                                      // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
  ret i32 0
define void @swap(ptr %p, ptr %a) #0 {
entry:
  \%0 = load ptr. ptr \%p. align 8
  %1 = load ptr. ptr %q, align 8
  store ptr %1, ptr %p, align 8
                                                tail
                                                                                 head
  store ptr %0, ptr %g, align 8
  ret void
                                                              WorkList
```

```
Algorithm 3: 1 Andersen's Pointer Analysis
  Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address n do
                                                // Address rule
      pts(p) := pts(p) U {o}:
      pushIntoWorklist(p):
5 while WorkList ≠ Ø do
      p := popFromWorklist():
       foreach o ∈ pts(p) do
          foreach a \xrightarrow{\text{Store}} p \in E do
                                                  // Store rule
              if a copy o ∉ E then
                   E := E \cup \{q \xrightarrow{Copy} o\}:
                                              // Add copy edge
10
                   pushIntoWorklist(a):
11
          foreach p \xrightarrow{Load} r \in E do
                                                    // Load rule
12
              if o copy r # E then
13
                   E := E \sqcup \{o \xrightarrow{Copy} r\}:
                                              // Add copy edge
14
                   pushIntoWorklist(o);
15
       foreach p \xrightarrow{Copy} x \in F do
16
                                                    // Copy rule
          pts(x) := pts(x) \cup pts(p);
17
          if pts(x) changed then
18
19
              pushIntoWorklist(x):
       foreach p \stackrel{\text{Gep,fld}}{\longrightarrow} x \in F do
                                                     // Gep rule
20
          foreach o ∈ pts(p) do
21
22
              pts(x) := pts(x) \cup \{o.fld\};
23
          if pts(x) changed then
              pushIntoWorklist(x);
24
```

```
Address
                                                                          Load
                                                           Copy
                                                                          Store
                                                                     {O2}
define i32 @main() #0 {
entry:
                                      // O1
  %a1 = alloca i8, align 1
                                                                      {04}
                                                          {O3}
  %a = alloca ptr. align 8
                                     // 03
  %b1 = alloca i8, align 1
                                     // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
  ret i32 0
define void @swap(ptr %p, ptr %a) #0 {
entry:
  \%0 = load ptr. ptr \%p. align 8
  %1 = load ptr. ptr %q, align 8
  store ptr %1, ptr %p, align 8
                                                tail
                                                                                head
  store ptr %0, ptr %g, align 8
  ret void
                                                              WorkList
```

```
Algorithm 4: 1 Andersen's Pointer Analysis
  Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address p do
                                                // Address rule
      pts(p) := pts(p) U {o}:
      pushIntoWorklist(p):
5 while WorkList ≠ Ø do
      p := popFromWorklist():
       foreach o ∈ pts(p) do
          foreach a \xrightarrow{\text{Store}} p \in E do
                                                  // Store rule
              if a copy o ∉ E then
                   E := E \cup \{q \xrightarrow{Copy} o\}:
                                              // Add copy edge
10
                   pushIntoWorklist(a):
11
          foreach p \xrightarrow{Load} r \in E do
                                                    // Load rule
12
              if o copy r # E then
13
                   E := E \sqcup \{o \xrightarrow{Copy} r\}:
                                              // Add copy edge
14
                   pushIntoWorklist(o);
15
       foreach p \xrightarrow{Copy} x \in F do
16
                                                    // Copy rule
          pts(x) := pts(x) \cup pts(p);
17
          if pts(x) changed then
18
19
              pushIntoWorklist(x):
       foreach p \stackrel{\text{Gep,fld}}{\longrightarrow} x \in F do
                                                     // Gep rule
20
          foreach o ∈ pts(p) do
22
              pts(x) := pts(x) \cup \{o.fld\};
23
          if pts(x) changed then
              pushIntoWorklist(x);
24
```

```
Address
                                                                           Load
                                                           Copy
                                                                          Store
                                                                      {O2}.
define i32 @main() #0 {
entry:
  %a1 = alloca i8, align 1
                                                          {O3}
                                                                      {04}
  %a = alloca ptr. align 8
                                      // O3
  %b1 = alloca i8, align 1
                                     // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
  ret i32 0
define void @swap(ptr %p, ptr %a) #0 {
entry:
  \%0 = load ptr. ptr \%p. align 8
  %1 = load ptr. ptr %q, align 8
  store ptr %1, ptr %p, align 8
                                                tail
                                                                                 head
  store ptr %0, ptr %g, align 8
  ret void
                                                              WorkWList
```

```
Algorithm 5: 1 Andersen's Pointer Analysis
  Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address p do
                                                // Address rule
      pts(p) := pts(p) U {o}:
      pushIntoWorklist(p):
5 while WorkList ≠ Ø do
       p := popFromWorklist():
       foreach o ∈ pts(p) do
          foreach g \xrightarrow{\text{store}} p \in E do
                                                  // Store rule
              if a copy o ∉ E then
9
                   E := E \cup \{q \xrightarrow{Copy} o\}:
                                              // Add copy edge
10
                   pushIntoWorklist(q);
11
          foreach p \xrightarrow{Load} r \in E do
                                                    // Load rule
12
              if o copy r # E then
13
                   E := E \sqcup \{o \xrightarrow{Copy} r\}:
                                              // Add copy edge
14
                   pushIntoWorklist(o);
15
       foreach p \xrightarrow{Copy} x \in F do
16
                                                    // Copy rule
          pts(x) := pts(x) \cup pts(p);
17
          if pts(x) changed then
18
19
              pushIntoWorklist(x):
       foreach p \stackrel{\text{Gep,fld}}{\longrightarrow} x \in F do
                                                     // Gep rule
20
          foreach o ∈ pts(p) do
21
22
              pts(x) := pts(x) \cup \{o.fld\};
23
          if pts(x) changed then
              pushIntoWorklist(x);
24
```

```
Address
                                                                          Load
                                                           Copy
                                                                          Store
                                                                     {O2}
                                                       %a}{O1}
define i32 @main() #0 {
entry:
  %a1 = alloca i8, align 1
                                      // 01
                                                                      {04}
                                                         {O3}
  %a = alloca ptr, align 8
                                      // O3
  %b1 = alloca i8, align 1
                                                                                  (04
                                     // 04
  %b = alloca ptr, align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
  ret i32 0
                                                       %p)
define void @swap(ptr %p, ptr %g) #0 {
entry:
  %0 = load ptr. ptr %p, align 8
  %1 = load ptr. ptr %q, align 8
  store ptr %1, ptr %p, align 8
                                                tail
                                                                                head
  store ptr %0, ptr %q, align 8
                                                                    %a1
                                                                                    %a
  ret void
                                                              WorkWist
```

```
Algorithm 6: 1 Andersen's Pointer Analysis
  Input: G = < V.E >: Constraint Graph
           V: a set of nodes in graph
          E: a set of edges in graph
 1 WorkList := an empty vector of nodes:
 2 foreach o Address p do
                                               // Address rule
      pts(p) := pts(p) \sqcup \{o\}:
      pushIntoWorklist(p);
 s while WorkList ≠ Ø do
       p := popFromWorklist():
       foreach o e pts(p) do
          for each q \xrightarrow{\text{Store}} p \in E do
                                                  // Store rule
               if a copy o ∉ E then
                   E := E \sqcup \{a \xrightarrow{Copy} o\}:
                                              // Add copy edge
10
                   pushIntoWorklist(g):
           foreach p \xrightarrow{Load} r \in E do
12
                                                    // Load rule
               if o Copy r & E then
                   E := E \cup \{o \xrightarrow{Copy} r\};
                                              // Add copy edge
14
15
                   pushIntoWorklist(o):
       foreach p \xrightarrow{Copy} x \in E do
                                                   // Copy rule
16
           pts(x) := pts(x) \cup pts(p):
           if pts(x) changed then
18
            | pushIntoWorklist(x);
19
       foreach p \xrightarrow{Gep,fld} x \in E do
                                                    // Gep rule
20
21
          foreach o e pts(p) do
22
            | pts(x) := pts(x) ∪ {o.fld};
           if pts(x) changed then
23
              pushIntoWorklist(x):
```

```
Address
                                                                          Load
                                                           Copy
                                                                          → Store
                                                                     {O2},
define i32 @main() #0 {
entry:
  %a1 = alloca i8, align 1
                                                         {O3}
                                                                      {04}
                                      // O(201)
  %a = alloca ptr. align 8
                                      // O3
  %b1 = alloca i8, align 1
                                     // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
                                                          {O3}
                                                                      {04}
  call void @swap(ptr %a, ptr %b)
  ret i32 0
define void @swap(ptr %p, ptr %a) #0 {
entry:
  %0 = load ptr, ptr %p, align 8
  %1 = load ptr. ptr %q, align 8
  store ptr %1, ptr %p, align 8
                                                tail
                                                                                head
  store ptr %0, ptr %g, align 8
                                                              O3 %a %b1 %p
  ret void
                                                              WorkList
```

```
Algorithm 7: 1 Andersen's Pointer Analysis
  Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address n do
                                              // Address rule
      pts(p) := pts(p) U {o}:
      pushIntoWorklist(p):
5 while WorkList ≠ Ø do
      p := popFromWorklist():
      foreach o ∈ pts(p) do
          foreach a \xrightarrow{\text{Store}} p \in E do
                                                // Store rule
              if a copy o ∉ E then
                  E := E \cup \{q \xrightarrow{Copy} o\}:
                                            // Add copy edge
10
                  pushIntoWorklist(a):
11
          foreach p \xrightarrow{Load} r \in E do
                                                  // Load rule
12
              if o copy r # E then
13
                  E := E \cup \{o \xrightarrow{Copy} r\};
                                            // Add copy edge
14
                  pushIntoWorklist(o);
15
      foreach p \xrightarrow{Copy} x \in F do
                                                  // Copy rule
          pts(x) := pts(x) \cup pts(p);
17
          if pts(x) changed then
18
19
              pushIntoWorklist(x):
      foreach p Gep,fld y ∈ F do
                                                   // Gep rule
          foreach o ∈ pts(p) do
22
              pts(x) := pts(x) \cup \{o.fld\};
23
          if pts(x) changed then
              pushIntoWorklist(x);
24
```

16

```
Copy
define i32 @main() #0 {
                                              (01)
entry:
  %a1 = alloca i8, align 1
                                              {01}
  %a = alloca ptr. align 8
                                                           {O3}
                                     // O3
  %b1 = alloca i8, align 1
                                     // 04
                                              (03)
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
                                                           {O3}
  ret i32 0
define void @swap(ptr %p, ptr %g) #0 {
entry:
                                                        (%0)
  %0 = load ptr. ptr %p. align 8
  %1 = load ptr. ptr %g, align 8
  store ptr %1, ptr %p, align 8
                                                 tail
  store ptr %0, ptr %q, align 8
                                                               %1 O3 %g %h
  ret void
                                                                   W
```

Address

Load

head

Store

**{O2}** 

**(04)** 

{04}

```
Algorithm 8: 1 Andersen's Pointer Analysis
  Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address p do
                                                // Address rule
      pts(p) := pts(p) U {o}:
      pushIntoWorklist(p):
5 while WorkList ≠ Ø do
      p := popFromWorklist():
       foreach o ∈ pts(p) do
          foreach g \xrightarrow{\text{store}} p \in E do
                                                  // Store rule
              if a copy o ∉ E then
9
                   E := E \cup \{q \xrightarrow{Copy} o\}:
                                              // Add copy edge
10
                   pushIntoWorklist(q);
11
          foreach p \xrightarrow{Load} r \in E do
                                                    // Load rule
12
              if o copy r # E then
13
                   E := E \cup \{o \xrightarrow{Copy} r\};
                                              // Add copy edge
14
                   pushIntoWorklist(o);
15
       foreach p \xrightarrow{Copy} x \in F do
16
                                                    // Copy rule
          pts(x) := pts(x) \cup pts(p);
17
          if pts(x) changed then
18
19
              pushIntoWorklist(x):
       foreach p \stackrel{\text{Gep,fld}}{\longrightarrow} x \in F do
                                                     // Gep rule
20
          foreach o ∈ pts(p) do
21
22
              pts(x) := pts(x) \cup \{o.fld\};
23
          if pts(x) changed then
              pushIntoWorklist(x);
24
```

```
Address
                                                                             Load
                                                            Copy
                                                                           Store
define i32 @main() #0 {
                                                                      {O2}
                                              (01)
entry:
  %a1 = alloca i8, align 1
                                     // O2,
  %a = alloca ptr. align 8
                                                                       (04)
                                    // 03(01)
                                                          {O3}
  %b1 = alloca i8, align 1
                                     // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
                                                          {O3}
                                                                       {04}
  ret i32 0
                                                       %p
define void @swap(ptr %p, ptr %q) #0 {
entry:
                                                       (%n)
  %0 = load ptr. ptr %p. align 8
  %1 = load ptr. ptr %g, align 8
  store ptr %1, ptr %p, align 8
                                                tail
                                                                                head
  store ptr %0, ptr %q, align 8
                                                           O3 %1 O3 %q %b1
  ret void
                                                                  W
```

```
Algorithm 9: 1 Andersen's Pointer Analysis
  Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address n do
                                               // Address rule
      pts(p) := pts(p) U {o}:
      pushIntoWorklist(p):
5 while WorkList ≠ Ø do
      p := popFromWorklist():
      foreach o ∈ pts(p) do
          foreach a \xrightarrow{\text{Store}} p \in E do
                                                  // Store rule
              if a copy o ∉ E then
                  E := E \cup \{q \xrightarrow{Copy} o\}:
                                              // Add copy edge
10
                  pushIntoWorklist(q);
11
          foreach p \xrightarrow{Load} r \in E do
                                                   // Load rule
12
              if o copy r & E then
13
                   E := E \cup \{o \xrightarrow{Copy} r\}:
                                             // Add copy edge
14
                  pushIntoWorklist(o);
15
      foreach p Copy x ∈ F do
16
                                                   // Copy rule
          pts(x) := pts(x) \cup pts(p);
17
          if pts(x) changed then
18
19
              pushIntoWorklist(x):
      foreach p \stackrel{\text{Gep,fld}}{\longrightarrow} x \in F do
                                                    // Gep rule
20
          foreach o ∈ pts(p) do
22
              pts(x) := pts(x) \cup \{o.fld\};
23
          if pts(x) changed then
              pushIntoWorklist(x);
24
```

```
Address
                                                                             Load
                                                            Copy
                                                                           Store
define i32 @main() #0 {
                                                                      {O2}
                                             (01)
entry:
  %a1 = alloca i8, align 1
                                     // O2,
  %a = alloca ptr. align 8
                                                                       (04)
                                    // 03{01}
                                                          {O3}
                                                                                     {O2}
  %b1 = alloca i8, align 1
                                     // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
                                                          {O3}
                                                                       {04}
  ret i32 0
                                                       %p
define void @swap(ptr %p, ptr %q) #0 {
entry:
                                                       (%n)
  %0 = load ptr. ptr %p. align 8
  %1 = load ptr. ptr %g, align 8
  store ptr %1, ptr %p, align 8
                                                tail
                                                                                head
  store ptr %0, ptr %q, align 8
                                                            O4 O3 %1 O3 %a
  ret void
                                                                  W
```

```
Algorithm 10: 1 Andersen's Pointer Analysis
  Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address p do
                                              // Address rule
      pts(p) := pts(p) U {o}:
      pushIntoWorklist(p):
5 while WorkList ≠ Ø do
      p := popFromWorklist():
      foreach o ∈ pts(p) do
          foreach a \xrightarrow{\text{Store}} p \in E do
                                                // Store rule
              if a copy o ∉ E then
                  E := E \cup \{q \xrightarrow{Copy} o\}:
                                             // Add copy edge
10
                  pushIntoWorklist(a):
11
          foreach p \xrightarrow{Load} r \in E do
                                                  // Load rule
12
              if o copy r # E then
13
                  E := E \cup \{o \xrightarrow{Copy} r\};
                                            // Add copy edge
14
                  pushIntoWorklist(o);
15
      foreach p \xrightarrow{Copy} x \in F do
                                                  // Copy rule
          pts(x) := pts(x) \cup pts(p);
17
18
          if pts(x) changed then
19
              pushIntoWorklist(x):
      foreach p Gep,fld y ∈ F do
                                                   // Gep rule
          foreach o ∈ pts(p) do
22
              pts(x) := pts(x) \cup \{o.fld\};
23
          if pts(x) changed then
              pushIntoWorklist(x);
24
```

16

```
Address
                                                                             Load
                                                            Copy
                                                                           Store
define i32 @main() #0 {
                                                                      {O2}
                                             (01)
entry:
  %a1 = alloca i8, align 1
                                     // O2,
  %a = alloca ptr. align 8
                                                                      (04)
                                    // 03(01)
                                                          {O3}
                                                                                      {O2}
  %b1 = alloca i8, align 1
                                     // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
                                                          {O3}
                                                                      {04}
  ret i32 0
                                                       %p
define void @swap(ptr %p, ptr %q) #0 {
entry:
  %0 = load ptr. ptr %p. align 8
                                                       (%0)
  %1 = load ptr. ptr %g, align 8
  store ptr %1, ptr %p, align 8
                                                tail
                                                                                head
  store ptr %0, ptr %q, align 8
                                                       O4%0 O4 O3 %1 O3
  ret void
                                                                  W
```

```
Algorithm 11: 1 Andersen's Pointer Analysis
  Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address p do
                                              // Address rule
      pts(p) := pts(p) U {o}:
      pushIntoWorklist(p);
5 while WorkList ≠ Ø do
      p := popFromWorklist():
      foreach o ∈ pts(p) do
          foreach a \xrightarrow{\text{Store}} p \in E do
                                                // Store rule
              if a copy o ∉ E then
                  E := E \cup \{q \xrightarrow{Copy} o\};
                                            // Add copy edge
10
                  pushIntoWorklist(q);
11
          foreach p \xrightarrow{Load} r \in E do
                                                  // Load rule
12
              if o copy r & E then
13
                  E := E \cup \{o \xrightarrow{Copy} r\}:
                                            // Add copy edge
14
                  pushIntoWorklist(o);
15
      foreach p Copy x ∈ F do
16
                                                  // Copy rule
          pts(x) := pts(x) \cup pts(p);
17
18
          if pts(x) changed then
19
              pushIntoWorklist(x):
      foreach p \xrightarrow{Gep,fld} x \in E do
                                                   // Gep rule
20
          foreach o ∈ pts(p) do
22
              pts(x) := pts(x) \cup \{o.fld\};
23
          if pts(x) changed then
              pushIntoWorklist(x);
24
```

```
Address
                                                                             Load
                                                            Copy
                                                                           Store
define i32 @main() #0 {
                                                                      {O2}
                                              (01)
entry:
  %a1 = alloca i8, align 1
                                     // O2,
  %a = alloca ptr. align 8
                                                                       (04)
                                    // 03{01}
                                                          {O3}
                                                                                      {O2}
  %b1 = alloca i8, align 1
                                     // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
                                                          {O3}
                                                                       {04}
  ret i32 0
                                                       %p
define void @swap(ptr %p, ptr %q) #0 {
entry:
                                                       (%0) {O1}
  %0 = load ptr. ptr %p. align 8
  %1 = load ptr. ptr %g, align 8
  store ptr %1, ptr %p, align 8
                                                tail
                                                                                head
  store ptr %0, ptr %q, align 8
                                                         %0 O4%0 O4 O3 %1
  ret void
                                                                  W
```

```
Algorithm 12: 1 Andersen's Pointer Analysis
  Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address p do
                                              // Address rule
      pts(p) := pts(p) U {o}:
      pushIntoWorklist(p):
5 while WorkList ≠ Ø do
      p := popFromWorklist():
      foreach o ∈ pts(p) do
          foreach a \xrightarrow{\text{Store}} p \in E do
                                                 // Store rule
              if a copy o ∉ E then
                  E := E \cup \{q \xrightarrow{Copy} o\}:
                                             // Add copy edge
10
                  pushIntoWorklist(a):
11
          foreach p \xrightarrow{Load} r \in E do
                                                  // Load rule
12
              if o copy r # E then
13
                  E := E \sqcup \{o \xrightarrow{Copy} r\}:
                                             // Add copy edge
14
                  pushIntoWorklist(o);
15
      foreach p \xrightarrow{Copy} x \in F do
16
                                                  // Copy rule
          pts(x) := pts(x) \cup pts(p);
17
18
          if pts(x) changed then
19
              pushIntoWorklist(x):
      foreach p Gep,fld y ∈ F do
                                                   // Gep rule
20
          foreach o ∈ pts(p) do
22
              pts(x) := pts(x) \cup \{o.fld\};
23
          if pts(x) changed then
              pushIntoWorklist(x);
24
```

```
Address
                                                                             Load
                                                            Copy
                                                                           Store
define i32 @main() #0 {
                                                                      {O2}
                                              (01)
entry:
  %a1 = alloca i8, align 1
                                     // O2,
  %a = alloca ptr. align 8
                                                                       (04)
                                    // 03(01)
                                                          {O3}
                                                                                      {O2}
  %b1 = alloca i8, align 1
                                     // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
                                                          {O3}
                                                                       {04}
  ret i32 0
                                                       %p
define void @swap(ptr %p, ptr %q) #0 {
entry:
                                                       (%0) {O1}
  %0 = load ptr. ptr %p. align 8
  %1 = load ptr. ptr %g, align 8
  store ptr %1, ptr %p, align 8
                                                tail
                                                                                head
  store ptr %0, ptr %q, align 8
                                                             %0 O4%0 O4 O3
  ret void
                                                                  W
```

```
Algorithm 13: 1 Andersen's Pointer Analysis
  Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address p do
                                              // Address rule
      pts(p) := pts(p) U {o}:
      pushIntoWorklist(p);
5 while WorkList ≠ Ø do
      p := popFromWorklist():
      foreach o ∈ pts(p) do
          foreach a \xrightarrow{\text{Store}} p \in E do
                                                 // Store rule
              if a copy o ∉ E then
                  E := E \cup \{q \xrightarrow{Copy} o\}:
                                             // Add copy edge
10
                  pushIntoWorklist(a):
11
          foreach p \xrightarrow{Load} r \in E do
                                                  // Load rule
12
              if o copy r # E then
13
                  E := E \sqcup \{o \xrightarrow{Copy} r\}:
                                             // Add copy edge
14
                  pushIntoWorklist(o);
15
      foreach p \xrightarrow{Copy} x \in F do
16
                                                  // Copy rule
          pts(x) := pts(x) \cup pts(p);
17
18
          if pts(x) changed then
19
              pushIntoWorklist(x):
      foreach p Gep,fld y \in F do
                                                   // Gep rule
20
          foreach o ∈ pts(p) do
22
              pts(x) := pts(x) \cup \{o.fld\};
23
          if pts(x) changed then
              pushIntoWorklist(x);
24
```

```
Address
                                                                             Load
                                                            Copy
                                                                           Store
define i32 @main() #0 {
                                                                      {O2}
                                              (01)
entry:
  %a1 = alloca i8, align 1
                                     // O2,
  %a = alloca ptr. align 8
                                                                       (04)
                                    // 03(01)
                                                          {O3}
                                                                                      {O2}
  %b1 = alloca i8, align 1
                                     // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
                                                           {O3}
                                                                       {04}
  ret i32 0
                                                        %p
define void @swap(ptr %p, ptr %q) #0 {
entry:
                                                       (%0) {O1}
  %0 = load ptr. ptr %p. align 8
  %1 = load ptr. ptr %g, align 8
  store ptr %1, ptr %p, align 8
                                                tail
                                                                                head
  store ptr %0, ptr %q, align 8
                                                                 %0 O4%0 O4
  ret void
                                                                   W
```

```
Algorithm 14: 1 Andersen's Pointer Analysis
  Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address p do
                                                // Address rule
      pts(p) := pts(p) U {o}:
      pushIntoWorklist(p);
5 while WorkList ≠ Ø do
      p := popFromWorklist():
       foreach o ∈ pts(p) do
          foreach a \xrightarrow{\text{Store}} p \in E do
                                                  // Store rule
              if a copy o ∉ E then
                   E := E \cup \{q \xrightarrow{Copy} o\}:
                                               // Add copy edge
10
                   pushIntoWorklist(a):
11
          foreach p \xrightarrow{Load} r \in E do
                                                    // Load rule
12
              if o copy r # E then
13
                   E := E \sqcup \{o \xrightarrow{Copy} r\}:
                                              // Add copy edge
14
                   pushIntoWorklist(o);
15
       foreach p \xrightarrow{Copy} x \in F do
16
                                                    // Copy rule
          pts(x) := pts(x) \cup pts(p);
17
18
          if pts(x) changed then
19
              pushIntoWorklist(x):
       foreach p \stackrel{\text{Gep,fld}}{\longrightarrow} x \in F do
                                                     // Gep rule
20
          foreach o ∈ pts(p) do
22
              pts(x) := pts(x) \cup \{o.fld\};
23
          if pts(x) changed then
              pushIntoWorklist(x);
24
```

```
Address
                                                                             Load
                                                            Copy
                                                                           Store
define i32 @main() #0 {
                                                                      {O2}
                                              (01)
entry:
  %a1 = alloca i8, align 1
                                     // O2,
  %a = alloca ptr. align 8
                                                                       (04)
                                    // 03(01)
                                                          {O3}
                                                                                      {O2}
  %b1 = alloca i8, align 1
                                     // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
                                                           {O3}
                                                                       {04}
  ret i32 0
                                                        %p
define void @swap(ptr %p, ptr %q) #0 {
entry:
                                                       (%0) {O1}
                                                                      {02} (%
  %0 = load ptr. ptr %p. align 8
  %1 = load ptr. ptr %g, align 8
  store ptr %1, ptr %p, align 8
                                                tail
                                                                                head
  store ptr %0, ptr %q, align 8
                                                                %1 %0 O4%0
  ret void
                                                                   W
```

```
Algorithm 15: 1 Andersen's Pointer Analysis
  Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address p do
                                              // Address rule
      pts(p) := pts(p) U {o}:
      pushIntoWorklist(p):
5 while WorkList ≠ Ø do
      p := popFromWorklist():
      foreach o ∈ pts(p) do
          foreach a \xrightarrow{\text{Store}} p \in E do
                                                // Store rule
              if a copy o ∉ E then
                  E := E \cup \{q \xrightarrow{Copy} o\}:
                                             // Add copy edge
10
                  pushIntoWorklist(a):
11
          foreach p \xrightarrow{Load} r \in E do
                                                  // Load rule
12
              if o copy r # E then
13
                  E := E \sqcup \{o \xrightarrow{Copy} r\}:
                                            // Add copy edge
14
                  pushIntoWorklist(o);
15
      foreach p \xrightarrow{Copy} x \in F do
                                                  // Copy rule
          pts(x) := pts(x) \cup pts(p);
17
18
          if pts(x) changed then
19
              pushIntoWorklist(x):
      foreach p Gep,fld y ∈ F do
                                                   // Gep rule
          foreach o ∈ pts(p) do
22
              pts(x) := pts(x) \cup \{o.fld\};
23
          if pts(x) changed then
              pushIntoWorklist(x);
24
```

16

```
Address
                                                                                Load
                                                              Copy
                                                                              Store
define i32 @main() #0 {
                                                                         {O2}
                                               (01)
entry:
  %a1 = alloca i8, align 1
                                      // O2,
  %a = alloca ptr. align 8
                                                                         (04)
                                     // 03(01)
                                                            {O3}
  %b1 = alloca i8, align 1
                                                                                       (04
                                      // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
                                                                                               10
                                                             {O3}
                                                                         {04}
                                                                                               11
  ret i32 0
                                                         %p
                                                                                               12
                                                                                               13
define void @swap(ptr %p, ptr %q) #0 {
                                                                                               14
                                                                                               15
entry:
                                                         (%0) {O1}
                                                                        {02} (%
  %0 = load ptr. ptr %p. align 8
                                                                                               16
  %1 = load ptr. ptr %g, align 8
                                                                                               17
  store ptr %1, ptr %p, align 8
                                                                                               18
                                                  tail
                                                                                   head
                                                                                               19
  store ptr %0, ptr %q, align 8
                                                                   O4 %1 %0 O4
  ret void
                                                                                               20
                                                                                               21
                                                                     W
                                                                                               22
                                                                                               23
                                                                                               24
```

```
Algorithm 16: 1 Andersen's Pointer Analysis
              Input: G =< V.E >: Constraint Graph
                      V: a set of nodes in graph
                      E: a set of edges in graph
            1 WorkList := an empty vector of nodes:
            2 foreach o Address p do
                                                          // Address rule
                  pts(p) := pts(p) U {o}:
                  pushIntoWorklist(p):
\{O2,O1\}_{5} while WorkList \neq \emptyset do
                  p := popFromWorklist():
                  foreach o ∈ pts(p) do
                      foreach a \xrightarrow{\text{Store}} p \in E do
                                                             // Store rule
                          if a copy o ∉ E then
                              E := E \cup \{q \xrightarrow{Copy} o\}:
                                                         // Add copy edge
                              pushIntoWorklist(a):
                      foreach p \xrightarrow{Load} r \in E do
                                                              // Load rule
                          if o copy r # E then
                              E := E \sqcup \{o \xrightarrow{Copy} r\}:
                                                         // Add copy edge
                              pushIntoWorklist(o);
                  foreach p \xrightarrow{Copy} x \in F do
                                                              // Copy rule
                      pts(x) := pts(x) \cup pts(p);
                      if pts(x) changed then
                          pushIntoWorklist(x):
                  foreach p Gep,fld y ∈ F do
                                                               // Gep rule
                      foreach o ∈ pts(p) do
                          pts(x) := pts(x) \cup \{o.fld\};
                      if pts(x) changed then
                          pushIntoWorklist(x);
```

```
Address
                                                                                Load
                                                              Copy
                                                                              Store
define i32 @main() #0 {
                                                                         {O2}
                                               (01)
entry:
  %a1 = alloca i8, align 1
                                      // O2,
  %a = alloca ptr. align 8
                                                                         (04)
                                     // 03(01)
                                                            {O3}
  %b1 = alloca i8, align 1
                                                                                       (04
                                      // 04
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
                                                                                               10
                                                            {O3}
                                                                         {04}
                                                                                               11
  ret i32 0
                                                         %p
                                                                                               12
                                                                                               13
define void @swap(ptr %p, ptr %q) #0 {
                                                                                               14
                                                                                               15
entry:
                                                         (%0){O1}
                                                                             (%1
  %0 = load ptr. ptr %p. align 8
                                                                                      01}
                                                                                               16
  %1 = load ptr. ptr %g, align 8
                                                                                               17
  store ptr %1, ptr %p, align 8
                                                                                               18
                                                  tail
                                                                                   head
                                                                                               19
  store ptr %0, ptr %q, align 8
  ret void
                                                                                               20
                                                                     W
                                                                                               22
                                                                                               23
```

```
Algorithm 17: 1 Andersen's Pointer Analysis
              Input: G =< V.E >: Constraint Graph
                      V: a set of nodes in graph
                      E: a set of edges in graph
            1 WorkList := an empty vector of nodes:
            2 foreach o Address p do
                                                          // Address rule
                  pts(p) := pts(p) U {o}:
                  pushIntoWorklist(p):
\{O2,O1\}_{5} while WorkList \neq \emptyset do
                  p := popFromWorklist():
                  foreach o ∈ pts(p) do
                      foreach a \xrightarrow{\text{Store}} p \in E do
                                                             // Store rule
                          if a copy o ∉ E then
                              E := E \cup \{q \xrightarrow{Copy} o\}:
                                                         // Add copy edge
                              pushIntoWorklist(a):
                      foreach p \xrightarrow{Load} r \in E do
                                                              // Load rule
                          if o copy r # E then
                              E := E \sqcup \{o \xrightarrow{Copy} r\}:
                                                         // Add copy edge
                              pushIntoWorklist(o);
                  foreach p \xrightarrow{Copy} x \in F do
                                                              // Copy rule
                      pts(x) := pts(x) \cup pts(p);
                      if pts(x) changed then
                          pushIntoWorklist(x);
                  foreach p Gep,fld y ∈ F do
                                                               // Gep rule
                      foreach o ∈ pts(p) do
                          pts(x) := pts(x) \cup \{o.fld\};
                      if pts(x) changed then
                          pushIntoWorklist(x);
```

```
Address
                                                                                Load
                                                              Copy
                                                                              Store
define i32 @main() #0 {
                                                                        {O2}
                                               (01)
entry:
  %a1 = alloca i8, align 1
  %a = alloca ptr. align 8
                                                                         (04)
                                                            {O3}
  %b1 = alloca i8, align 1
                                      // 04
                                               (03
  %b = alloca ptr. align 8
  store ptr %a1, ptr %a, align 8
  store ptr %b1, ptr %b, align 8
  call void @swap(ptr %a, ptr %b)
                                                                                               10
                                                            {O3}
                                                                         {04}
                                                                                               11
  ret i32 0
                                                         %p
                                                                                               12
                                                                                               13
define void @swap(ptr %p, ptr %q) #0 {
                                                                                               14
                                                                                               15
entry:
                                                         (%0){O1}
                                                                             (%1
  %0 = load ptr. ptr %p. align 8
                                                                                     01}
                                                                                               16
  %1 = load ptr. ptr %g, align 8
                                                                                               17
  store ptr %1, ptr %p, align 8
                                                                                               18
                                                  tail
                                                                                   head
                                                                                               19
  store ptr %0, ptr %q, align 8
                                                                    O3 %1 O4
  ret void
                                                                                               20
                                                                    W
                                                                                               22
                                                                                               23
```

```
Algorithm 18: 1 Andersen's Pointer Analysis
              Input: G =< V.E >: Constraint Graph
                      V: a set of nodes in graph
                      E: a set of edges in graph
            1 WorkList := an empty vector of nodes:
            2 foreach o Address p do
                                                          // Address rule
                  pts(p) := pts(p) U {o}:
                  pushIntoWorklist(p):
\{O2,O1\}_{5} while WorkList \neq \emptyset do
                  p := popFromWorklist():
                  foreach o ∈ pts(p) do
                      foreach a \xrightarrow{\text{Store}} p \in E do
                                                             // Store rule
                          if a copy o ∉ E then
                              E := E \cup \{q \xrightarrow{Copy} o\}:
                                                         // Add copy edge
                              pushIntoWorklist(a):
                      foreach p \xrightarrow{Load} r \in E do
                                                              // Load rule
                          if o copy r # E then
                              E := E \sqcup \{o \xrightarrow{Copy} r\}:
                                                         // Add copy edge
                              pushIntoWorklist(o);
                  foreach p \xrightarrow{Copy} x \in F do
                                                              // Copy rule
                      pts(x) := pts(x) \cup pts(p);
                      if pts(x) changed then
                          pushIntoWorklist(x);
                  foreach p Gep,fld y ∈ F do
                                                               // Gep rule
                      foreach o ∈ pts(p) do
                          pts(x) := pts(x) \cup \{o.fld\};
                      if pts(x) changed then
                          pushIntoWorklist(x);
```

```
define i32 @main() #0 {
entry:
%a1 = alloca i8. alian 1
                               // O1
                              // O2 {O1,O2}
%b1 = alloca i8, alian 1
%a = alloca i8*, alian 8
                               // 04
%b = alloca i8*, alian 8
store i8* %a1, i8** %a, alian 8
store i8* %b1, i8** %b, alian 8
call void @swap(i8** %a, i8** %b)
ret i32 0
define void @swap(i8** %p. i8** %a)
#0 {
entry:
\%0 = load i8** \%p, alian 8
%1 = load i8** %q, align 8
store i8* %1, i8** %p, alian 8
store i8* %0, i8** %a, alian 8
ret void
```

```
Load
        Address
                   — Store
          Copy
                 {O2}
        {03}
                  {04}
        {03}
                  {04}
      %р
      (%0
{01.62}
tail
                          head
                              %0
            WorkList
```

10

11

12

13

14

15

16

17

18

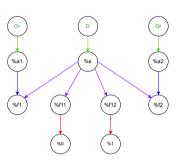
19

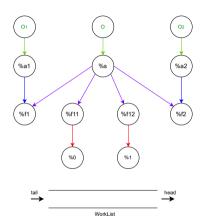
22

23

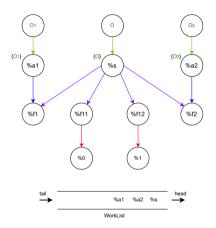
```
Algorithm 19: 1 Andersen's Pointer Analysis
              Input: G =< V.E >: Constraint Graph
                       V: a set of nodes in graph
                       E: a set of edges in graph
             1 WorkList := an empty vector of nodes:
             2 foreach o Address p do
                                                            // Address rule
                   pts(p) := pts(p) U {o}:
                   pushIntoWorklist(p):
{O2.O1}<sub>5</sub> while WorkList ≠ Ø do
                   p := popFromWorklist():
                   foreach o ∈ pts(p) do
                       foreach a \xrightarrow{\text{Store}} p \in E do
                                                               // Store rule
                           if a copy o ∉ E then
                               E := E \sqcup \{a \xrightarrow{Copy} a\}:
                                                           // Add copy edge
                               pushIntoWorklist(a):
                       foreach p \xrightarrow{Load} r \in E do
                                                                // Load rule
                           if o copy r # E then
                               E := E \cup \{o \xrightarrow{Copy} r\};
                                                           // Add copy edge
                               pushIntoWorklist(o);
                   foreach p \xrightarrow{Copy} x \in F do
                                                                // Copy rule
                       pts(x) := pts(x) \cup pts(p);
                       if pts(x) changed then
                           pushIntoWorklist(x):
                   foreach p \stackrel{\text{Gep,fld}}{\longrightarrow} x \in F do
                                                                 // Gep rule
                       foreach o ∈ pts(p) do
                           pts(x) := pts(x) \cup \{o.fld\};
                       if pts(x) changed then
                           pushIntoWorklist(x);
```

```
struct Sf
     int* f1;
     int* f2:
 5 int main(){
      struct S s:
     int a1, a2;
      s.f1 = &a1:
      s.f2 = &a2:
      int* p = s.f1;
11
      int* q = s.f2:
12 }
   define i32 @main() #0 {
   entry:
     %s = alloca %struct.S. align 8
     %a1 = alloca i32, align 4
     %a2 = alloca i32, align 4
     %f1 = getelementptr inbounds %struct.S, ptr %s, i32 0, i32 0
     store ptr %a1, ptr %f1, align 8
     %f2 = getelementptr inbounds %struct.S, ptr %s, i32 0, i32 1
     store ptr %a2, ptr %f2, align 8
     %f11 = getelementptr inbounds %struct.S, ptr %s, i32 0, i32 0
     %0 = load ptr, ptr %f11, align 8
     %f22 = getelementptr inbounds %struct.S. ptr %s, i32 0, i32 1
13
     %1 = load ptr, ptr %f22, align 8
14
     ret i32 0
15 }
```

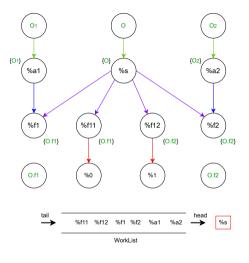




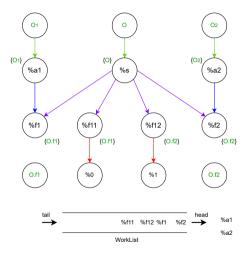
```
Algorithm 20: 1 Andersen's Pointer Analysis
   Input: G =< V.E >: Constraint Graph
           V: a set of nodes in graph
           E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o dddress p do
                                                     // Address rule
      pts(p) = o:
      pushIntoWorklist(p);
5 while WorkList ≠ Ø do
      p := popFromWorklist():
       foreach o ∈ pts(p) do
           foreach a \xrightarrow{\text{Store}} p \in E do
                                                       // Store rule
               if a copy o ∉ E then
                   E := E \cup \{q \xrightarrow{Copy} o\};
                                                   // Add copy edge
10
                  pushIntoWorklist(q);
11
           foreach p \xrightarrow{Load} r \in E do
                                                        // Load rule
12
               if o <sup>Copy</sup> r ∉ E then
                   E := E \cup \{o \xrightarrow{Copy} r\}:
                                                   // Add copy edge
14
                  pushIntoWorklist(o);
15
       foreach p \xrightarrow{Copy} x \in E do
16
                                                        // Copy rule
           pts(x) := pts(x) \cup pts(p);
17
           if pts(x) changed then
18
              pushIntoWorklist(x):
       foreach p \xrightarrow{Gep,fld} x \in E do
                                                         // Gep rule
20
           foreach o ∈ pts(p) do
21
              pts(x) := pts(x) \cup \{o.fld\};
23
           if pts(x) changed then
              pushIntoWorklist(x);
24
```



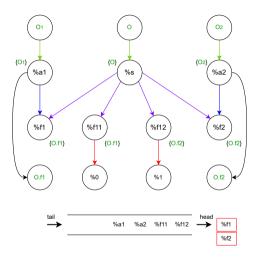
```
Algorithm 21: 1 Andersen's Pointer Analysis
   Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address p do
                                                    // Address rule
      pts(p) = o:
      pushIntoWorklist(p);
5 while WorkList \neq \emptyset do
       p := popFromWorklist();
       foreach o ∈ pts(p) do
          foreach q \xrightarrow{\text{Store}} p \in E do
я
                                                      // Store rule
              if a <sup>Copy</sup> o ∉ E then
9
                  E := E \cup \{a \xrightarrow{Copy} o\}:
                                                  // Add copy edge
10
11
                  pushIntoWorklist(q);
          foreach phoadr ∈ F do
                                                       // Load rule
12
              if o Copy r ∉ E then
13
                  E := E \sqcup \{o \xrightarrow{Copy} r\}:
                                                  // Add copy edge
14
15
                  pushIntoWorklist(o);
       foreach p Gopy x ∈ F do
                                                       // Copy rule
16
          pts(x) := pts(x) \cup pts(p):
17
           if pts(x) changed then
18
              pushIntoWorklist(x);
19
       foreach p \xrightarrow{Gep,fld} x \in E do
                                                        // Gep rule
20
          foreach o ∈ pts(p) do
21
              pts(x) := pts(x) \cup \{o.fld\};
22
          if pts(x) changed then
23
              pushIntoWorklist(x);
```



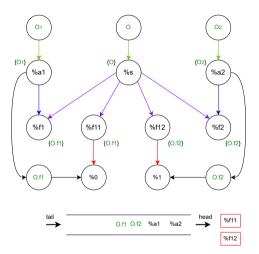
```
Algorithm 22: 1 Andersen's Pointer Analysis
   Input: G =< V.E >: Constraint Graph
           V: a set of nodes in graph
           E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address n do
                                                     // Address rule
       pts(p) = o:
      pushIntoWorklist(p):
5 while WorkList ≠ Ø do
      p := popFromWorklist():
       foreach o ∈ pts(p) do
           foreach a \xrightarrow{\text{Store}} p \in E do
                                                       // Store rule
               if q <sup>Copy</sup> o ∉ E then
                   E := E \cup \{a \xrightarrow{Copy} o\}:
10
                                                   // Add copy edge
                  pushIntoWorklist(a):
11
           foreach p^{Load}r \in E do
12
                                                        // Load rule
               if o <sup>Copy</sup> r ∉ E then
13
                   E := E \sqcup \{o \xrightarrow{Copy} r\}
14
                                                   // Add copy edge
                   pushIntoWorklist(o);
15
       foreach p \xrightarrow{Copy} x \in F do
                                                        // Copy rule
           pts(x) := pts(x) \cup pts(p);
           if pts(x) changed then
18
              pushIntoWorklist(x):
19
       foreach p \xrightarrow{Gep,fld} x \in E do
20
                                                         // Gep rule
           foreach o e pts(p) do
21
22
              pts(x) := pts(x) \cup \{o.fld\};
           if pts(x) changed then
23
              pushIntoWorklist(x);
24
```



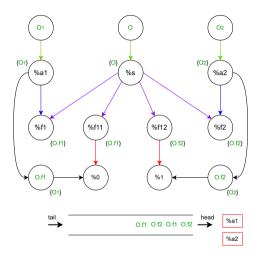
```
Algorithm 23: 1 Andersen's Pointer Analysis
   Input: G =< V.E >: Constraint Graph
           V: a set of nodes in graph
           E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address p do
                                                     // Address rule
      pts(p) = o:
      pushIntoWorklist(p);
5 while WorkList ≠ Ø do
      p := popFromWorklist():
       foreach o ∈ pts(p) do
           foreach a \xrightarrow{\text{Store}} p \in E do
                                                       // Store rule
               if a copy o ∉ E then
                   E := E \cup \{q \xrightarrow{Copy} o\};
                                                   // Add copy edge
10
                  pushIntoWorklist(q);
11
           foreach p \xrightarrow{Load} r \in E do
                                                        // Load rule
12
               if o <sup>Copy</sup> r ∉ E then
13
                   E := E \cup \{o \xrightarrow{Copy} r\}:
                                                   // Add copy edge
14
                  pushIntoWorklist(o);
15
       foreach p \xrightarrow{Copy} x \in E do
16
                                                        // Copy rule
           pts(x) := pts(x) \cup pts(p);
17
           if pts(x) changed then
18
19
              pushIntoWorklist(x):
       foreach p \xrightarrow{Gep,fld} x \in E do
                                                         // Gep rule
20
           foreach o ∈ pts(p) do
21
              pts(x) := pts(x) \cup \{o.fld\};
23
           if pts(x) changed then
              pushIntoWorklist(x);
24
```



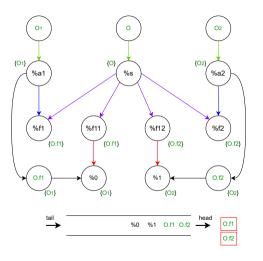
```
Algorithm 24: 1 Andersen's Pointer Analysis
   Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address p do
                                                   // Address rule
      pts(p) = 0
      pushIntoWorklist(p);
s while WorkList ≠ Ø do
      p := popFromWorklist();
       foreach o ∈ pts(p) do
          foreach q \xrightarrow{\text{Store}} p \in E do
                                                     // Store rule
я
              if a copy o ∉ E then
9
                  E := E \cup \{a \xrightarrow{Copy} o\}:
                                                  // Add copy edge
10
11
                  pushIntoWorklist(q);
          foreach p \xrightarrow{Load} r \in E do
12
                                                       // Load rule
              if o copy r ∉ E then
13
                  E := E \sqcup \{o \xrightarrow{Copy} r\}:
                                                  // Add copy edge
14
                  pushIntoWorklist(o);
15
       foreach p \xrightarrow{Copy} x \in E do
                                                       // Copy rule
16
17
          pts(x) := pts(x) \cup pts(p);
18
           if pts(x) changed then
              pushIntoWorklist(x):
19
       foreach p Gep,fld x ∈ E do
20
                                                        // Gep rule
          foreach o ∈ pts(p) do
21
           pts(x) := pts(x) \cup \{o.fld\};
22
          if pts(x) changed then
23
              pushIntoWorklist(x);
24
```



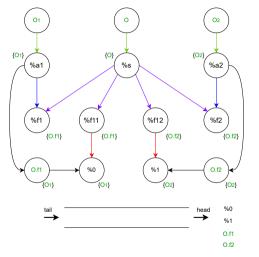
```
Algorithm 25: 1 Andersen's Pointer Analysis
   Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address p do
                                                    // Addrose rulo
      pts(p) = 0
      pushIntoWorklist(p);
s while WorkList ≠ Ø do
      p := popFromWorklist();
       foreach o ∈ pts(p) do
          foreach q \xrightarrow{\text{Store}} p \in E do
                                                      // Store rule
              if q <sup>Copy</sup> o ∉ E then
9
                  E := E \cup \{a \xrightarrow{Copy} o\}:
                                                  // Add copy edge
10
                  pushIntoWorklist(g):
11
           foreach p \xrightarrow{Load} r \in E do
12
                                                       // Load rule
              if o copy r ∉ E then
13
                  E := E \cup \{o \xrightarrow{Copy} r\};
                                                  // Add copy edge
14
                  pushIntoWorklist(o);
15
       foreach p \xrightarrow{Copy} x \in E do
                                                       // Copy rule
16
17
          pts(x) := pts(x) \cup pts(p);
           if pts(x) changed then
              pushIntoWorklist(x):
19
       foreach p Gep,fld x ∈ E do
20
                                                        // Gep rule
          foreach o ∈ pts(p) do
21
            pts(x) := pts(x) \cup \{o.fld\};
22
          if pts(x) changed then
23
              pushIntoWorklist(x);
24
```



```
Algorithm 26: 1 Andersen's Pointer Analysis
   Input: G =< V.E >: Constraint Graph
           V: a set of nodes in graph
           E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address n do
                                                     // Address rule
       pts(p) = o:
      pushIntoWorklist(p):
5 while WorkList ≠ Ø do
       p := popFromWorklist():
       foreach o ∈ pts(p) do
           foreach \underset{p}{\operatorname{g}} \in E do
                                                        // Store rule
               if q <sup>Copy</sup> o ∉ E then
                   E := E \cup \{a \xrightarrow{Copy} o\}:
10
                                                    // Add copy edge
                   pushIntoWorklist(q);
11
           foreach p^{Load}r \in E do
12
                                                         // Load rule
               if o \stackrel{Copy}{\longrightarrow} r \notin E then
13
                   E := E \sqcup \{o \xrightarrow{Copy} r\}
14
                                                    // Add copy edge
                   pushIntoWorklist(o);
15
       foreach p \xrightarrow{Copy} x \in E do
                                                         // Copy rule
16
           pts(x) := pts(x) \cup pts(p);
17
           if pts(x) changed then
18
               pushIntoWorklist(x);
       foreach p Gep,fld x ∈ F do
                                                          // Gep rule
20
           foreach o e pts(p) do
21
              pts(x) := pts(x) \cup \{o.fld\};
22
           if pts(x) changed then
23
24
              pushIntoWorklist(x);
```



```
Algorithm 27: 1 Andersen's Pointer Analysis
   Input: G =< V.E >: Constraint Graph
          V: a set of nodes in graph
          E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address n do
                                                    // Address rule
       pts(p) = o:
      pushIntoWorklist(p):
5 while WorkList ≠ Ø do
      p := popFromWorklist():
       foreach o ∈ pts(p) do
          foreach \underset{p}{\operatorname{g}} \in E do
                                                      // Store rule
              if q <sup>Copy</sup> o ∉ E then
                   E := E \cup \{a \xrightarrow{Copy} o\}:
10
                                                  // Add copy edge
                   pushIntoWorklist(q);
11
          foreach p^{Load}r \in E do
12
                                                        // Load rule
              if o <sup>Copy</sup> r ∉ E then
13
                   E := E \cup \{o \xrightarrow{Copy} r\};
14
                                                  // Add copy edge
                   pushIntoWorklist(o);
       foreach p \xrightarrow{Copy} x \in E do
                                                       // Copy rule
16
           pts(x) := pts(x) \cup pts(p);
17
           if pts(x) changed then
18
              pushIntoWorklist(x);
       foreach p Gep,fld x ∈ F do
                                                         // Gep rule
20
          foreach o e pts(p) do
21
              pts(x) := pts(x) \cup \{o.fld\};
22
           if pts(x) changed then
23
              pushIntoWorklist(x);
```



```
Algorithm 28: 1 Andersen's Pointer Analysis
  Input: G =< V.E >: Constraint Graph
           V: a set of nodes in graph
           E: a set of edges in graph
1 WorkList := an empty vector of nodes:
2 foreach o Address p do
                                                     // Address rule
      pts(p) = o:
      pushIntoWorklist(p);
5 while WorkList ≠ Ø do
      p := popFromWorklist():
       foreach o ∈ pts(p) do
           foreach a \xrightarrow{\text{Store}} p \in E do
                                                       // Store rule
               if a copy o ∉ E then
                   E := E \cup \{q \xrightarrow{Copy} o\};
                                                   // Add copy edge
10
                  pushIntoWorklist(q);
11
           foreach p \xrightarrow{Load} r \in E do
                                                        // Load rule
12
               if o <sup>Copy</sup> r ∉ E then
13
                   E := E \cup \{o \xrightarrow{Copy} r\}:
                                                   // Add copy edge
14
                  pushIntoWorklist(o);
15
       foreach p \xrightarrow{Copy} x \in E do
16
                                                        // Copy rule
           pts(x) := pts(x) \cup pts(p);
17
           if pts(x) changed then
18
              pushIntoWorklist(x):
       foreach p \xrightarrow{Gep,fld} x \in E do
                                                         // Gep rule
20
           foreach o ∈ pts(p) do
21
              pts(x) := pts(x) \cup \{o.fld\};
23
           if pts(x) changed then
              pushIntoWorklist(x);
24
```

# **APIs for Implementing Andersen's analysis**

```
::getPts(NodeID ptr)
                                                              // get points-to set of ptr
                         ::addPts(NodeID ptr, NodeID obi)
                                                              //add obj to point-to set of object ptr
                         ::unionPts(NodeID ptr, NodeID obj)
                                                              // union two point-to set
 SVF:AndersenBase
                                                              // push the node to worklist
                        ::pushIntoWorklist(NodeID id)
                         ::popFromWorklist()
                                                              // pop a node from the worklist
                                                              // return true if the node in the worklist
                         ::isInWorklist(NodeTD id)
                         ::isWorklistEmptv(NodeID id)
                                                              // return true if worklist is empty
 SVF:AndersenPTA
                        ::addCopyEdge(NodeID src. NodeID dst)// add a copy edge from src to dst
                         ::getConstraintNode(NodeID id)
                                                          //get the node based on its id
SVF:ConstraintGraph -----
                         :: dump()
                                                          //dump the ConsG
                         ::getStoreInEdge()
                                                         // get incoming store edges of the node
                        ::getStoreOutEdge()
                                                        //get outgoing store edges of the node
SVF:ConstraintNode -----
                         ::getCopyInEdges()
                                                        // get incoming copy edges of the node
                                                        // get outgoing copy edges of the node
                         :: getCopyOutEdges()
```

```
https://github.com/SVF-tools/Software-Security-Analysis/wiki/SVF-CPP-API#worklist-operations
https://github.com/SVF-tools/Software-Security-Analysis/wiki/SVF-CPP-API#points-to-set-operations
https://github.com/SVF-tools/Software-Security-Analysis/wiki/SVF-CPP-API#alias-relations
https://github.com/SVF-tools/Software-Security-Analysis/wiki/SVF-CPP-API#constrainteraph-constraintpode-and-constraintedge
```

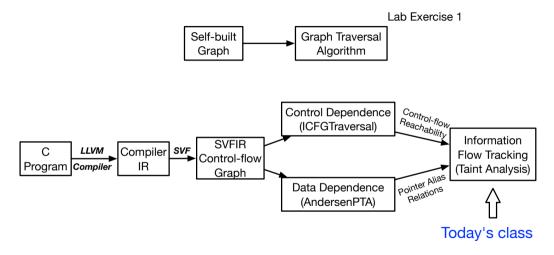
## **Information Flow Tracking**

(Week 3)

Yulei Sui

School of Computer Science and Engineering University of New South Wales, Australia

### **Today's Class**



#### **Taint Analysis**

- Taint analysis aims to reason about the control and data dependence from a source (statement/node) to a sink (statement/node).
- Taint analysis can also be seen as information flow tracking analysis.
  - Static taint analysis: taint tracking at compile time (this course)
  - Dynamic taint analysis: taint tracking during runtime.

### **Taint Analysis**

- Taint analysis aims to reason about the control and data dependence from a source (statement/node) to a sink (statement/node).
- Taint analysis can also be seen as information flow tracking analysis.
  - Static taint analysis: taint tracking at compile time (this course)
  - Dynamic taint analysis: taint tracking during runtime.

#### Why learn Taint Analysis?

- Detect information leakage
  - sensitive data stored in a heap object and manipulated by pointers can be passed around and stored to an unchecked memory (untrusted third-party APIs)
- Detect code vulnerability
  - There is a vulnerability if an unchecked tainted source (e.g., return value from an untrusted third party function) flows into one of the following sinks, where the tainted variable being used as
    - a parameter passed to a sensitive function or
    - a bound access (array index) or
    - a termination condition (loop condition)

• . . .

#### **Tainted Information Flows**

Let us use what we have learned about control-flow and data-flow to develop an information flow checker to validate tainted flows from a source to a sink.

- A source v<sub>src</sub>@s<sub>src</sub> is a tuple consisting of a variable v<sub>src</sub> and a statement s<sub>src</sub> where v<sub>src</sub> is defined.
- A sink v<sub>snk</sub>@s<sub>snk</sub> is also a tuple consisting of a variable v<sub>snk</sub> and a statement s<sub>snk</sub> where v<sub>snk</sub> is used.
- In SVF, variables  $v_{src}$  and  $v_{snk}$  are SVFVars. Statements  $s_{src}$  and  $s_{snk}$  are ICFGNodes.

#### **Tainted Information Flows**

Let us use what we have learned about control-flow and data-flow to develop an information flow checker to validate tainted flows from a source to a sink.

- A source v<sub>src</sub>@s<sub>src</sub> is a tuple consisting of a variable v<sub>src</sub> and a statement s<sub>src</sub> where v<sub>src</sub> is defined.
- A sink v<sub>snk</sub>@s<sub>snk</sub> is also a tuple consisting of a variable v<sub>snk</sub> and a statement s<sub>snk</sub> where v<sub>snk</sub> is used.
- In SVF, variables  $v_{src}$  and  $v_{snk}$  are SVFVars. Statements  $s_{src}$  and  $s_{snk}$  are ICFGNodes.
- Given a tainted source v<sub>src</sub>@s<sub>src</sub>, we say that a sink v<sub>snk</sub>@s<sub>snk</sub> is also tainted
  if both of the following two conditions satisfy:
  - s<sub>src</sub> reaches s<sub>snk</sub> on the ICFG (reachability in Assignment-1),
  - $v_{src}$  and  $v_{snk}$  are aliases, (i.e.,  $pts(v_{src}) \cap pts(v_{snk})$ )  $\neq \emptyset$  (solveWorklist in Assignment-1)

#### **Example 1**

```
int main(){
char* secretToken = tgetstr();  // source
char* a = secretToken;
char* b = a;
broadcast(b);  // sink
}
```

What is the tainted flow?

#### Example 1

```
int main(){
char* secretToken = tgetstr();  // source
char* a = secretToken;
char* b = a;
broadcast(b);  // sink
}
```

#### What is the tainted flow?

- Line 2 reaches Line 5 along the ICFG (control-dependence holds)
   secretToken and b are aliases (data-dependence holds)
- Both control-dependence and data-dependence hold. Therefore, secretToken@Line 2 flows to b@Line 5.

#### Example 2

```
int main(){
char* secretToken = tgetstr(...);  // source
char* a = secretToken;
char* b = a;
char* publicToken = "hello";
broadcast(publicToken);  // sink
}
```

#### Example 2

```
int main(){
char* secretToken = tgetstr(...); // source
char* a = secretToken;
char* b = a;
char* publicToken = "hello";
broadcast(publicToken); // sink
}
```

- Line 2 reaches Line 6 along the ICFG (control-dependence holds),
- secretToken and publicToken are not aliases (data-dependence does not hold),
- secretToken@Line 2 does not flow to publicToken@Line 6.

#### Example 3

```
char* foo(char* token){ return token: }
    int main(){
        if(condition){
3
            char* secretToken = tgetstr(...); // source
            char* b = foo(secretToken);
5
        else{
            char* publicToken = "hello";
            char* a = foo(publicToken);
            broadcast(a):
                                                 // sink
10
11
12
```

#### Example 3

```
char* foo(char* token){ return token: }
    int main(){
        if(condition){
3
            char* secretToken = tgetstr(...); // source
            char* b = foo(secretToken);
5
        else{
            char* publicToken = "hello";
            char* a = foo(publicToken);
            broadcast(a):
                                                 // sink
10
11
12
```

- secretToken and a are aliases due to callee foo (data-dependence holds),
- Line 4 does not reach Line 10 on ICFG (control-dependence does not hold),
- secretToken@Line 4 does not flow to a@Line 10.

#### Example 4

```
int main(){
        char* secretToken = tgetstr(...);
                                                            // source
        while(loopCondition){
            if(BranchCondition){
                char* a = secretToken;
                broadcast(a):
                                                          // sink
            else{
                char* b = "hello":
10
11
12
```

How many tainted flows from source to sink?

#### **Example 4**

```
int main(){
        char* secretToken = tgetstr(...);
                                                             // source
        while(loopCondition){
            if (BranchCondition) {
                char* a = secretToken;
                broadcast(a):
                                                           // sink
            else{
                char* b = "hello":
10
11
12
```

#### How many tainted flows from source to sink?

- (At least) two paths from Line 2 to Line 6 on ICFG (control-dependence holds),
- secretToken and a are aliases (data-dependence holds),
- secretToken@Line 2 has two tainted paths flowing to a@Line 6.

# **Configuring Sources and Sinks for Taint Analysis**

**Aim**: enable different taint tracking patterns by defining/configuring sources and sinks.

Given a source v<sub>src</sub>@s<sub>src</sub> and a sink v<sub>snk</sub>@s<sub>snk</sub>, in this class, we are interested in the case that s<sub>src</sub> and s<sub>snk</sub> are both API calls, i.e., CallBlockNode in SVF.

# **Configuring Sources and Sinks for Taint Analysis**

**Aim**: enable different taint tracking patterns by defining/configuring sources and sinks.

- Given a source v<sub>src</sub>@s<sub>src</sub> and a sink v<sub>snk</sub>@s<sub>snk</sub>, in this class, we are interested in the case that s<sub>src</sub> and s<sub>snk</sub> are both API calls, i.e., CallBlockNode in SVF.
- v<sub>src</sub> is a return value from the call statement s<sub>src</sub>.
- $\mathbf{v}_{\mathbf{snk}}$  is a parameter being passed to a call statement  $\mathbf{s}_{\mathbf{snk}}$ .

# **Configuring Sources and Sinks for Taint Analysis**

**Aim**: enable different taint tracking patterns by defining/configuring sources and sinks.

- Given a source v<sub>src</sub>@s<sub>src</sub> and a sink v<sub>snk</sub>@s<sub>snk</sub>, in this class, we are interested in the case that s<sub>src</sub> and s<sub>snk</sub> are both API calls, i.e., CallBlockNode in SVF.
- v<sub>src</sub> is a return value from the call statement s<sub>src</sub>.
- $\mathbf{v}_{\mathbf{snk}}$  is a parameter being passed to a call statement  $\mathbf{s}_{\mathbf{snk}}$ .
- We can identify s<sub>src</sub> and s<sub>snk</sub> according to different APIs, so as to configure sources and sinks.
- In Example 1, variable secretToken is  $\mathbf{v}_{src}$  and b is  $\mathbf{v}_{snk}$ . The call statement tgetstr(...) represents  $\mathbf{s}_{src}$  and broadcast(...) are used for  $\mathbf{s}_{snk}$ .
- In Assignment-1, you will need to implement readSrcSnkFromFile to identify sources and sinks configured by SrcSnk.txt.

#### What's next?

- (1) Understand data-flow and points-to analysis in today's slides
- (2) Finish the implementation of the four methods readSrcSnkFromFile, reachability, solveWorklist, aliasCheck in Assignment-1
- (3) Submit Assignment-1.cpp by 23:59 Tuesday, Week 4.