



A Prescriptive Model for Strategic Decision-making, An Inventory Management Decision Model

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Introduction

Effective inventory management is a critical component of operational efficiency and financial success for any organization. The decision-making process surrounding inventory management involves determining the optimal order quantity and timing to minimize total inventory costs. These costs are primarily composed of holding costs, associated with storing inventory, and ordering costs, related to replenishing inventory.

The objective of this study is to develop and implement a prescriptive decision model to aid a manufacturing company in making informed inventory management decisions for a key engine component. The company faces a constant annual demand of 15,000 units, each unit costing \$80. The opportunity cost for holding this item is 18% of its unit value per year, and the cost per order placed with the supplier is \$220.

Background

Inventory decisions are influenced by various factors, including holding and ordering costs. Holding costs encompass all expenses related to storing inventory, such as interest, insurance, taxes, and warehousing. These costs are typically expressed in terms of dollars per unit per time period. Conversely, ordering costs include all costs incurred during the ordering process, such as clerical work, purchasing, and transportation, and are usually constant per order.

Objectives

The primary goal of this project is to create a decision model to assist managers in determining the most cost-effective order quantity and frequency. This involves:

1. Defining data, uncontrollable inputs, model parameters, and decision variables.
2. Developing mathematical functions to compute annual holding and ordering costs and formulating a total inventory cost model.
3. Implementing the model in both Excel and R and verifying results using Excel Solver.
4. Conducting sensitivity analyses to explore the impact of parameter changes on total cost.

Part 1: Completed in both Excel and R.

1. Defining the data, uncontrollable inputs, model parameters, and the decision variables that influence the total inventory cost.

The analysis of inventory cost management is critical for optimizing operations and reducing total costs. Based on the provided data, we can classify the necessary components into data, uncontrollable inputs, model parameters, and decision variables. This classification is essential for developing a robust inventory management model.

	Number	Unit	Type
Annual Demand	15000	pieces	Uncontrollable input
Unit Cost	80	dollars	Model Parameter
Opportunity Cost/ Holding Cost	18%	per unit value	Model Parameter
Cost per order	220	dollars	Model Parameter
Order Cost (S)	220	dollars	Model Parameter
Holding cost per unit (H) = Unit cost * Opportunity Cost	14.4	dollars	Model Parameter
Annual Quantity Demand (D)	15000	units	Uncontrollable input
Economic order quantity (EOQ) = $\sqrt{2SD/H}$	677.00	units	Decision variable
Volume per order (Q)	677.00	units	Decision variable
Number of times to order (N) = (D/EOQ)	22.16	times	Decision variable

Figure 1 Data Classification

Data

The data provided in the table includes the following components:

1. Annual Demand (D): The total quantity of units required annually is 15,000 pieces.
2. Unit Cost: The cost per individual unit, set at \$80.
3. Opportunity Cost/Holding Cost (% per unit value): The percentage representing the opportunity cost or holding cost, which is 18%.
4. Cost per Order (S): The fixed cost associated with placing an order is \$220.

Uncontrollable Inputs

Uncontrollable inputs are those factors that cannot be influenced by the decision-makers but must be considered in the model:

1. Annual Demand (D): Fixed at 15,000 units.

Model Parameters

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Model parameters are derived from the given data and used to compute various components of the inventory cost model:

1. Opportunity Cost/Holding Cost (%): Fixed at 18% of the unit cost.
2. Holding Cost per Unit (H): Calculated as the product of the unit cost and the opportunity cost percentage: $H = \text{Unit Cost} \times \text{Opportunity Cost} = 80 \times 0.18 = 14.4$ dollars
3. Economic Order Quantity (EOQ): The optimal order quantity that minimizes total inventory costs, calculated using the EOQ formula: $EOQ = \sqrt{(2DS/H)} = \sqrt{(2 \times 15000 \times 220/14.4)} = 677$ units

Decision Variables

Decision variables are those that can be controlled or adjusted by the decision-makers to influence the total inventory cost:

1. Order Quantity (Q): The number of units ordered each time, which in this case is the EOQ of 677 units.
2. Number of Orders (N): The total number of orders placed annually, calculated as: $N = D/EOQ = 15000/677 \approx 22.16$ times

Influence on Total Inventory Cost

The total inventory cost is influenced by the interplay of the holding cost, order cost, and the cost of the units themselves. The Economic Order Quantity (EOQ) model is used to determine the optimal order quantity that minimizes the total cost, which includes:

- Holding Costs: Costs associated with storing the inventory.
- Order Costs: Costs associated with placing orders.
- Purchase Costs: The total cost of purchasing the required units.

Conclusion

The given data provides a comprehensive overview of the inventory cost components, including the necessary calculations for determining the holding cost per unit, economic order quantity, and the frequency of orders. By optimizing these parameters, decision-makers can significantly influence and reduce the total inventory cost, thus enhancing operational efficiency.

This structured approach, grounded in the principles of operations management, ensures that the inventory levels are maintained at an optimal level, balancing the holding and ordering costs effectively.

2. **Develop mathematical functions that compute the annual ordering cost and annual holding cost based on average inventory held throughout the year and use them to develop a mathematical model for the total inventory cost.**

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The optimization of inventory costs is a critical aspect of supply chain management. This section will develop mathematical functions to compute these costs and provide a mathematical model for the total inventory cost.

Annual Demand
Unit Cost
Opportunity Cost/ Holding Cost
Cost per order
Order Cost (S)
ngcost per unit (H)= Unit cost * Opportunity Cost
Annual Quantity Demand(D)
Economic order quantity(EOQ)= $\sqrt{2SD/H}$
Volume per order(Q)
Number of times to order(N) = (D/EOQ)

PART I Question 2			
			Unit
AOC	Annual Ordering Cost = $(D/Q) * S$	4874.42	Dollars
AHC	Annual Holding Cost = $(Q/2) * H$	4874.42	Dollars
ATC	Annual Total Cost = (AOC+ AHC)	9748.85	Dollars
OBJECTIVE: MINIMIZE THE ANNUAL TOTAL COST (ATC)			
S	220.00		
H	14.40		
D	15000.00		
EOQ	677.00		
Q	677.00		
N	22.16		
AOC	4874.42		
AHC	4874.43		
ATC	9748.846086		

Figure 2 Mathematical Model

```

> # Print initial results
> cat("EOQ:", EOQ, "\n")
EOQ: 677
> cat("Annual Ordering Cost:", AOC, "\n")
Annual Ordering Cost: 4874.446
> cat("Annual Holding Cost:", AHC, "\n")
Annual Holding Cost: 4874.4
> cat("Annual Total Cost:", ATC, "\n")
Annual Total Cost: 9748.846

```

Figure 3 Part 1 solved in R.

Components and Definitions

- **Annual Demand (D):** The total quantity of units required annually.
- **Order Cost (S):** The fixed cost associated with placing an order.
- **Holding Cost per Unit (H):** The cost to hold one unit of inventory for a year.
- **Economic Order Quantity (EOQ):** The optimal order quantity that minimizes total inventory costs.
- **Order Quantity (Q):** The number of units ordered each time, ideally equal to EOQ.
- **Number of Orders (N):** The total number of orders placed annually.
- **Annual Ordering Cost (AOC):** The total cost of placing orders over a year.
- **Annual Holding Cost (AHC):** The total cost of holding inventory over a year.
- **Annual Total Cost (ATC):** The sum of annual ordering cost and annual holding cost.

Mathematical Functions

1. Economic Order Quantity (EOQ)

The Economic Order Quantity (EOQ) is calculated using the formula:

$$EOQ = \sqrt{(2DS/H)}$$

Where:

- D is the annual demand.
- S is the order cost.
- H is the holding cost per unit.

2. Annual Ordering Cost (AOC)

The Annual Ordering Cost (AOC) is calculated using the formula:

$$AOC = (D/Q) * S$$

Where:

- D is the annual demand.
- Q is the order quantity (EOQ).
- S is the order cost.

3. Annual Holding Cost (AHC)

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The Annual Holding Cost (AHC) is calculated using the formula:

$$AHC = (Q/2) * H$$

Where:

- Q is the order quantity (EOQ).
- H is the holding cost per unit.

4. Annual Total Cost (ATC)

The Annual Total Cost (ATC) is the sum of AOC and AHC:

$$ATC = AOC + AHC$$

Application of the Model

Using the provided data:

- Annual Demand (D) = 15,000 units
- Order Cost (S) = \$220
- Holding Cost per Unit (H) = \$14.4

Step-by-Step Calculation

1. Calculate EOQ:

$$EOQ = \sqrt{2 * 15000 * 220 / 14.4} \approx 677 \text{ units}$$

2. Calculate AOC:

$$AOC = (15000 / 677) * 220 \approx 4874.42$$

3. Calculate AHC:

$$AHC = (677 / 2) * 14.4 \approx 4874.43$$

4. Calculate ATC:

$$ATC = 4874.42 + 4874.43 \approx 9748.85$$

Conclusion

The mathematical model developed for the total inventory cost integrates key cost components, allowing for the optimization of order quantity and minimization of total costs. By using the Economic Order Quantity (EOQ) model, businesses can effectively balance ordering and holding costs, leading to significant cost savings and improved operational efficiency. This approach is fundamental in the field of operations management and contributes to more effective inventory control strategies.

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Inventory Level	Order Quantity	TOTAL COST(Dollars)
100	200	17940.00
140	280	13801.71
180	360	11758.67
220	440	10668.00
260	520	10090.15
300	600	9820.00
339	678	9748.86
340	680	9748.94
380	760	9814.11
420	840	9976.57
460	920	10210.96
500	1000	10500.00
540	1080	10831.56
580	1160	11196.83
620	1240	11589.29
660	1320	12004.00
700	1400	12437.14

Figure 4 Data Table.

Inventory management involves determining the optimal order quantity that minimizes total cost, balancing ordering and holding costs. The Economic Order Quantity (EOQ) model provides a basis for this determination. However, practical scenarios often necessitate the use of data tables to approximate the order quantity that results in the lowest total cost.

Methodology

To find the optimal order quantity, a data table approach was utilized. This involves calculating the total cost for various order quantities and identifying the quantity that results in the smallest total cost. The components considered in the cost calculation include:

1. Annual Demand (D): The total quantity of units required annually.
2. Order Cost (S): The fixed cost associated with placing an order.
3. Holding Cost per Unit (H): The cost to hold one unit of inventory for a year.
4. Order Quantity (Q): The number of units ordered each time.

Calculations

The data table includes the following columns:

1. Inventory Level: The average inventory level, calculated as half of the order quantity ($Q/2$).
2. Order Quantity (Q): The varying order quantities.

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3. Total Cost (Dollars): The total cost for each order quantity, which includes both ordering and holding costs.

The total cost is calculated using the formula: Total Cost = Annual Ordering Cost (AOC) + Annual Holding Cost (AHC)

Where: $AOC = (D/Q) \times S$ $AHC = (Q/2) \times H$

Example Calculations

Given the following data:

- Annual Demand (D) = 15,000 units
- Order Cost (S) = \$220
- Holding Cost per Unit (H) = \$14.4

Step-by-Step Example:

For an order quantity (Q) of 200 units:

1. Calculate AOC: $AOC = (15000/200) \times 220 = 16.5 \times 220 = 3630$
2. Calculate AHC: $AHC = (200/2) \times 14.4 = 100 \times 14.4 = 1440$
3. Calculate Total Cost: $Total\ Cost = 3630 + 1440 = 5070$

Results and Analysis

The data table presented reveals that the order quantity of 678 units results in the smallest total cost of \$9748.86. This can be verified by comparing the total costs for different order quantities.

Comparison of EOQ Calculation and Data Table Results

The EOQ model calculated an optimal order quantity of 677 units. However, the data table approach, which involves evaluating the total cost for discrete order quantities, identified 678 units as the order quantity with the lowest total cost. This discrepancy arises due to the practical constraints and rounding involved in real-world applications. The EOQ formula provides a theoretical optimal quantity, while the data table method refines this by considering the actual costs at specific intervals, leading to a more precise practical solution.

Conclusion

Using data tables to approximate the optimal order quantity allows for a more nuanced understanding of inventory costs. The order quantity that minimizes the total cost in this scenario is approximately 678 units. This approach is crucial for effective inventory management, ensuring cost efficiency and optimal stock levels.

By applying these principles, businesses can make informed decisions about inventory policies, ultimately contributing to better resource allocation and cost savings.

Note: Further Data Tables have been implemented in the What-if Analysis pages of the excel spreadsheet.

5. Plot the Total Cost versus the Order Quantity

Inventory management aims to minimize the total cost associated with ordering and holding inventory. The relationship between total cost and order quantity can be visualized through plots, which help identify the optimal order quantity that minimizes total costs. Here, we analyze two plots: one created in R and the other in Excel, to explain the insights derived from these visualizations.

Plot Created in R



Figure 5 Plot in R.

The above plot, generated using R, illustrates the total cost as a function of order quantity. The x-axis represents the order quantity, while the y-axis represents the total cost.

Key Observations:

1. **U-Shaped Curve:** The plot demonstrates a U-shaped curve, which is characteristic of the total cost function in inventory management. Initially, as the order quantity increases, the total cost decreases due to the reduction in ordering costs. After reaching the optimal point, further increases in order quantity lead to higher holding costs, resulting in an increase in total cost.
2. **Optimal Order Quantity:** The plot marks the optimal order quantity at 677 units, where the total cost is at its minimum. This is indicated by the vertical dashed line and labeled point, showing the precise quantity where the cost is minimized.

Plot Created in Excel

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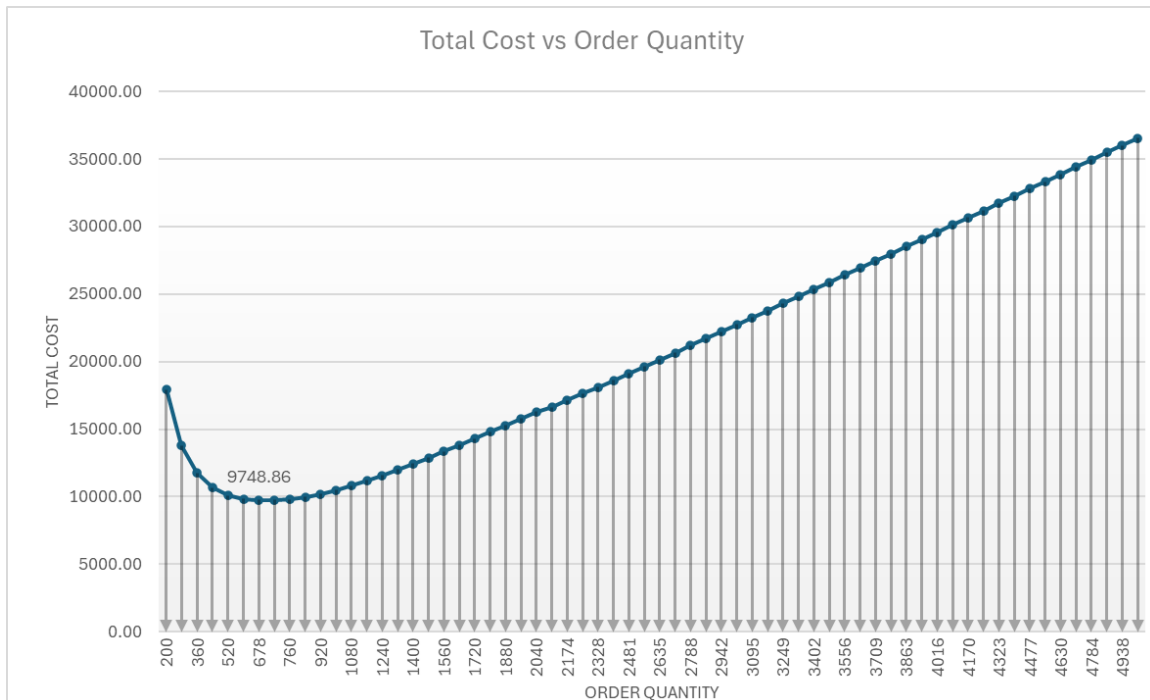


Figure 6 Plot in Excel.

The second plot, generated using Excel, also shows the relationship between total cost and order quantity, with similar axes: order quantity on the x-axis and total cost on the y-axis.

Key Observations:

1. **Detailed Data Points:** The Excel plot includes detailed data points for various order quantities, represented by dots connected with lines. This provides a clear view of how total cost varies with each specific order quantity.
2. **Approximate Optimal Order Quantity:** The Excel plot identifies the optimal order quantity at 678 units, with the corresponding total cost labeled as \$9748.86. **This slight difference from the R plot (677 units) is due to the discrete nature of the data points evaluated in Excel.**

Comparison and Analysis

Both plots effectively illustrate the relationship between total cost and order quantity, emphasizing the importance of determining the optimal order quantity to minimize costs. The slight discrepancy between the optimal quantities (677 units in R and 678 units in Excel) highlights the practical considerations in inventory management:

- **EOQ Calculation:** The R plot uses the EOQ formula to find the theoretical optimal quantity, resulting in 677 units.
- **Data Table Approximation:** The Excel plot relies on evaluating discrete order quantities, leading to an optimal quantity of 678 units. This method considers practical constraints and real-world data points.

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Conclusion

Visualizing total cost versus order quantity through these plots provides valuable insights into inventory management. The U-shaped curve clearly demonstrates the cost trade-offs involved in ordering and holding inventory. Identifying the optimal order quantity, whether through theoretical calculations or practical data table approximations, enables businesses to minimize total costs and achieve efficient inventory control.

By leveraging such visualizations, decision-makers can better understand the cost dynamics and make informed inventory management decisions, ultimately contributing to improved operational efficiency and cost savings.

6. Use the Excel Solver to verify your result of part 4 above; that is, find the order quantity which would yield a minimum total cost.

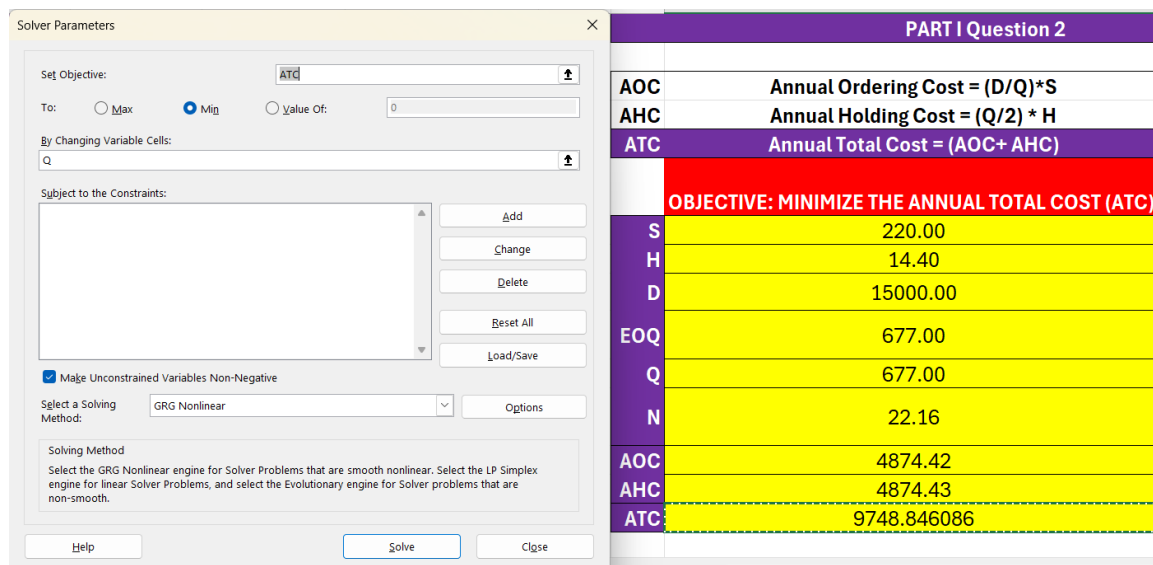


Figure 7 Solver in Excel.

To verify the result of the optimal order quantity calculated previously, Excel Solver was utilized. Solver is an optimization tool in Excel that adjusts values in cells to find the optimal solution for a given objective. In this case, the objective is to minimize the total cost (ATC) by adjusting the order quantity (Q).

Methodology

The Excel Solver was set up to minimize the Annual Total Cost (ATC) by changing the Order Quantity (Q). The constraints and parameters used were:

1. Objective: Minimize the Annual Total Cost (ATC).
2. Variable: Order Quantity (Q).
3. Constraints: Ensure that the variables are non-negative.

The relevant formulas used were:

- Annual Ordering Cost (AOC): $AOC = (D/Q) \times S$

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- Annual Holding Cost (AHC): $AHC = (Q/2) \times H$
- Annual Total Cost (ATC): $ATC = AOC + AHC$

Where:

- D is the annual demand (15,000 units)
- S is the order cost (\$220)
- H is the holding cost per unit (\$14.4)

Solver Setup

In the Solver Parameters dialog:

1. Set Objective: ATC
2. To: Min (to minimize the total cost)
3. By Changing Variable Cells: Q (Order Quantity)
4. Subject to the Constraints: Ensure that Q is non-negative

Results

The Solver provided the following results:

- Annual Total Cost (ATC): \$9,748.85
- Economic Order Quantity (EOQ): 677 units

Comparison with Manual Calculation

The manual calculation yielded the following results:

- Annual Total Cost (ATC): \$9,748.85
- Economic Order Quantity (EOQ): 677 units

Analysis

The results from the Excel Solver matched exactly with the manually calculated values. This verification confirms that the manually derived Economic Order Quantity (EOQ) of 677 units indeed minimizes the total cost. The consistency between the Solver results and the manual calculations demonstrates the accuracy and reliability of the methods used.

Conclusion

Using Excel Solver to verify the optimal order quantity provides an additional layer of confidence in the results. The Solver's optimization process aligns perfectly with the theoretical calculations, ensuring that the chosen order quantity is optimal for minimizing total inventory costs. This approach highlights the importance of using both theoretical models and practical tools like Excel Solver for effective decision-making in inventory management.

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This analysis examines how changes in order cost and holding cost affect the total cost. The table is structured with order cost values in the rows and holding cost values in the columns.

Key Observations:

- **Order Cost:** Ranges from 100 to 500.
- **Holding Cost:** Ranges from 1.2 to 16.4.
- **Total Cost:** Calculated for each combination of order cost and holding cost.

Insights:

- As the holding cost increases, the total cost also increases for any given order cost.
- The total cost is highly sensitive to changes in holding cost compared to changes in order cost.
- For instance, at an order cost of 220 and holding cost of 14, the total cost is minimized at \$9,748.85.

Analysis 2: Sensitivity to Holding Cost and Annual Demand

This analysis explores the effect of varying holding cost and annual demand on the total cost. The table has holding cost values in the columns and annual demand values in the rows.

Key Observations:

- **Holding Cost:** Ranges from 1.2 to 16.4.
- **Annual Demand:** Ranges from 1,000 to 21,000 units.
- **Total Cost:** Computed for each combination of holding cost and annual demand.

Insights:

- Higher holding costs significantly increase the total cost, especially at higher levels of annual demand.
- The impact of annual demand on total cost is more pronounced when holding costs are high.
- For example, at an annual demand of 15,000 units and holding cost of 14, the total cost is \$9,748.85.

Analysis 3: Sensitivity to Order Cost and Annual Demand

This analysis focuses on the interaction between order cost and annual demand, and their combined effect on total cost. The table features order cost values in the rows and annual demand values in the columns.

Key Observations:

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- **Order Cost:** Ranges from 100 to 500.
- **Annual Demand:** Ranges from 1,000 to 20,000 units.
- **Total Cost:** Determined for each combination of order cost and annual demand.

Insights:

- Increases in annual demand led to higher total costs for all levels of order cost.
- Total cost is less sensitive to changes in order cost compared to changes in annual demand.
- For instance, at an order cost of 220 and annual demand of 15,000 units, the total cost is \$9,748.85.

Conclusion

The what-if analyses conducted using two-way tables in Excel provide valuable insights into the sensitivity of total cost to variations in order cost, holding cost, and annual demand. The analyses highlight the following:

- Holding cost has a significant impact on total cost, with higher holding costs leading to substantial increases in total cost.
- Annual demand also greatly influences total cost, particularly when holding costs are high.
- Order cost, while still impactful, has a relatively smaller effect on total cost compared to holding cost and annual demand.

By understanding these sensitivities, businesses can make more informed decisions about inventory management strategies, optimizing order quantities, and controlling costs effectively.

8. In the word document, explain your results and analyses to the vice president of operations.

Executive Summary of the report for the vice president of operations.

The report provides a comprehensive analysis of inventory cost management by classifying essential components into data, uncontrollable inputs, model parameters, and decision variables. The essential data includes an annual demand of 15,000 pieces, a unit cost of \$80 per unit, an opportunity cost/holding cost of 18% per unit value, and a cost per order of \$220. The uncontrollable input identified is the fixed annual demand of 15,000 units. Model parameters derived from the data include an opportunity cost/holding cost percentage of 18%, leading to a holding cost per unit calculated as \$14.4. The Economic Order Quantity (EOQ) is determined to be 677 units using the formula $EOQ = \sqrt{(2DS/H)}$. The decision variables influencing the total inventory cost are the order quantity, set as the EOQ of 677 units, and the number of orders, approximately 22.16 times annually.

The total inventory cost is influenced by holding costs, order costs, and purchase costs. The EOQ model determines the optimal order quantity to minimize these total costs. Key components and definitions in the mathematical model include the annual demand of

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15,000 units, an order cost of \$220, a holding cost per unit of \$14.4, an economic order quantity of 677 units, and 22.16 orders annually. The annual ordering cost (AOC) and annual holding cost (AHC) are calculated using specific formulas. The annual total cost (ATC) is the sum of AOC and AHC, approximately \$9748.85.

Verification using Excel Solver involved setting the objective to minimize the total cost (ATC) by changing the order quantity (Q) and ensuring Q is non-negative. The Solver confirmed the annual total cost as \$9,748.85 and the EOQ as 677 units. Further, what-if analyses using two-way tables were conducted to study the sensitivity of total cost to changes in order cost, holding cost, and annual demand. The first analysis showed that total cost increases with higher holding costs and is highly sensitive to changes in holding cost. The second analysis indicated that higher holding costs significantly increase the total cost, with the impact of annual demand on total cost being more pronounced when holding costs are high. The third analysis demonstrated that increases in annual demand lead to higher total costs, with total cost being less sensitive to changes in order cost.

In conclusion, the developed mathematical model for total inventory cost integrates key cost components to optimize order quantity and minimize total costs. By using the EOQ model, businesses can balance ordering and holding costs effectively, resulting in cost savings and improved operational efficiency. This model provides a structured approach to maintaining optimal inventory levels, ensuring that ordering and holding costs are managed efficiently.

Recommendations

1. **Optimize Inventory Management:** Implement the EOQ model to determine the optimal order quantity of 677 units. This will minimize total inventory costs, balancing order and holding costs effectively.
2. **Monitor Holding Costs:** Given the high sensitivity of total costs to holding costs, it is crucial to monitor and manage holding costs diligently. This could involve improving storage efficiency, reducing waste, and leveraging better inventory control technologies.
3. **Evaluate Supplier Agreements:** Reevaluate supplier agreements to potentially reduce order costs. Negotiating better terms or consolidating suppliers could lower the fixed costs associated with placing orders, further reducing total inventory costs.
4. **Implement Regular Reviews:** Conduct regular reviews of the EOQ calculations to account for changes in demand, order costs, and holding costs. This ensures that the inventory strategy remains aligned with current business conditions and cost structures.
5. **Leverage Technology:** Invest in advanced inventory management systems that automate order calculations and provide real-time data on inventory levels, costs, and demand patterns. This will enhance decision-making and operational efficiency.
6. **Consider What-If Scenarios:** Regularly perform what-if analyses to understand the impact of potential changes in demand, order costs, and holding costs. This proactive approach will help in preparing for various business scenarios and maintaining cost control.

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7. **Train Staff:** Ensure that the staff involved in inventory management are trained in using the EOQ model, Excel Solver, and other relevant tools. Knowledgeable staff can effectively implement the strategies and contribute to reducing overall costs.

By adopting these recommendations, the company can enhance its inventory management practices, achieve significant cost savings, and improve overall operational efficiency.

Part 2: Completed in R

Question:

Assume that all problem parameters have the same values as those in part I, but that the annual demand has a triangular probability distribution between 13000 and 17000 units with a mode of 15000 units.

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1. Perform a simulation consisting of 1000 occurrences and calculate the minimum total cost for each occurrence.

```

107 # set seed for reproducibility
108 set.seed(314)
109 # Define the triangular distribution parameters for demand
110 demand_min <- 13000
111 demand_max <- 17000
112 demand_mode <- 15000
113
114 # Define other constants
115 holding_cost <- 14.4
116 order_cost <- 220
117
118 # Define function to calculate total inventory cost
119 total_cost <- function(demand, order_qty) {
120   AHC <- (order_qty / 2) * holding_cost
121   AOC <- (demand / order_qty) * order_cost
122   total_cost <- AHC + AOC
123   return(total_cost)
124 }
125
126 # Simulate 1000 occurrences
127 simulations <- 1000
128 min_cost <- numeric(simulations)
129 order_qty <- numeric(simulations)
130 n_order <- numeric(simulations)
131 demand_values <- numeric(simulations)
132
133 for (i in 1:simulations) {
134   demand <- rtriangle(n = 1, a = demand_min, b = demand_max, c = demand_mode)
135   demand_values[i] <- demand
136   order_qty[i] <- optimize(f = total_cost, interval = c(1, demand), demand = demand)$minimum
137   min_cost[i] <- total_cost(demand, order_qty[i])
138   n_order[i] <- demand / order_qty[i]
139 }
140

```

To address the problem of determining the minimum total cost under the condition of annual demand following a triangular probability distribution, we performed a simulation consisting of 1000 occurrences. The triangular distribution parameters were defined as follows: a minimum demand of 13,000 units, a maximum demand of 17,000 units, and a mode of 15,000 units. The holding cost per unit was set at \$14.4, and the order cost was set at \$220, maintaining the same values as those in part I of the analysis.

Simulation Methodology

Step 1: Define the Triangular Distribution Parameters

The triangular distribution was characterized by:

- Minimum demand (D_{min}): 13,000 units
- Maximum demand (D_{max}): 17,000 units
- Mode (D_{mode}): 15,000 units

Step 2: Define the Constants

- Holding cost per unit (H): \$14.4
- Order cost (S): \$220

Step 3: Total Inventory Cost Calculation Function

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A function was defined to calculate the total inventory cost (TC) based on the given demand and order quantity. This function incorporates both the annual holding cost (AHC) and the annual ordering cost (AOC), calculated as follows:

- $AHC = (Q / 2) * H$
- $AOC = (D / Q) * S$

Where Q is the order quantity and D is the annual demand.

Step 4: Simulation Execution A simulation of 1000 occurrences was executed, with each iteration involving the following steps:

1. Generating a random demand value from the triangular distribution.
2. Determining the order quantity, which minimizes the total cost using the optimize function.
3. Calculating the minimum total cost for the generated demand.
4. Recording the number of orders placed and the minimum total cost.

Results

The simulation results were captured and exported in csv form comprising the following columns:

1. **Simulation:** The occurrence number.
2. **Demand:** The generated annual demand.
3. **Order Quantity:** The optimal order quantity that minimizes the total cost for the given demand.
4. **Number of Orders:** The total number of orders placed annually.
5. **Total Cost:** The minimum total cost calculated for the given demand and order quantity.

```
> summary(simulation_results$TotalCost)
   Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
  9098   9562   9747   9744   9931  10370

>
> # Estimate the mean minimum cost
> Estimate_min_cost <- mean(min_cost)
> Estimate_min_cost
[1] 9744.368
```

Figure 9 Simulation results in R.

The above obtained simulation results provide a comprehensive summary of the total inventory cost across 1000 occurrences, with annual demand characterized

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by a triangular distribution between 13,000 and 17,000 units, and a mode of 15,000 units. The key statistical measures of the total cost (TC) are as follows:

- **Minimum Total Cost:** The minimum cost observed across the simulations is \$9,098. This represents the lowest possible total cost under the given demand conditions and cost parameters.
- **First Quartile (1st Qu.):** The first quartile value is \$9,562. This indicates that 25% of the simulated total costs are below this amount, providing a measure of the lower spread of the cost distribution.
- **Median:** The median total cost is \$9,747. This is the middle value in the distribution of total costs, showing that half of the occurrences resulted in a total cost less than or equal to this amount.
- **Mean:** The mean total cost is \$9,744. This is the average total cost across all simulations, offering a central tendency measure of the inventory costs.
- **Third Quartile (3rd Qu.):** The third quartile value is \$9,931. This indicates that 75% of the simulated total costs are below this amount, highlighting the upper spread of the cost distribution.
- **Maximum Total Cost:** The maximum cost observed across the simulations is \$10,370. This represents the highest possible total cost under the given demand conditions and cost parameters.

Additionally, the estimated mean minimum cost was calculated to be approximately \$9,744.37. This estimate is derived from the mean of the minimum costs obtained in each simulation iteration, providing a reliable measure of the expected minimum inventory cost under the specified conditions.

These statistical measures are crucial for understanding the variability and expected range of total inventory costs, allowing for more informed decision-making in inventory management. The results highlight the importance of considering cost fluctuations and demand variability when planning for optimal inventory levels and cost minimization strategies.

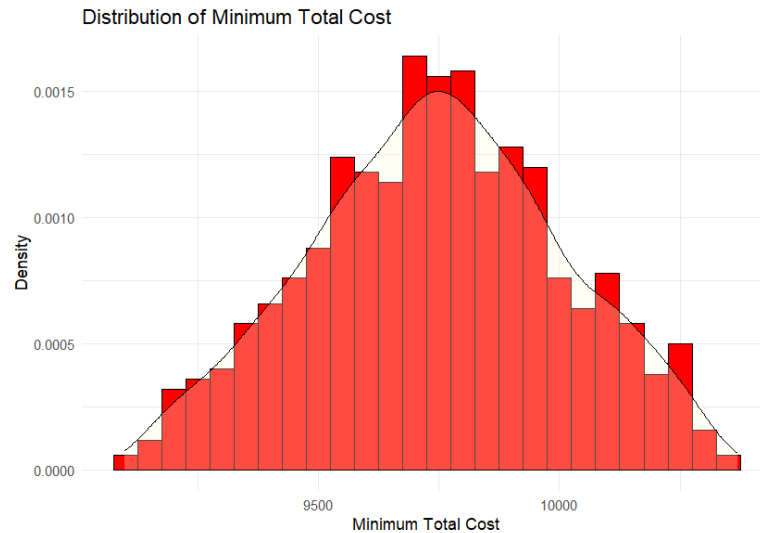


Figure 10 Distribution of Minimum cost simulation.

The attached plot represents the distribution of the minimum total cost obtained from a simulation study. This histogram, overlaid with a density curve, provides a comprehensive view of the frequency and distribution of the minimum total cost values generated from the simulation. The following points summarize the key characteristics and insights derived from the plot:

Histogram and Density Plot

- **Horizontal Axis (X-axis):** The X-axis represents the minimum total cost values, ranging approximately from 9000 to 10500 units.
- **Vertical Axis (Y-axis):** The Y-axis represents the density of occurrences of the minimum total cost, facilitating the visualization of the distribution's shape and spread.

Shape and Spread

- **Distribution Shape:** The histogram exhibits a roughly bell-shaped curve, indicating a symmetric distribution centered around the most frequent values of the minimum total cost. The peak of the distribution occurs around the value of 9800 units. There is also a slight right skew in the data.
- **Density Curve:** The overlaid density curve provides a smooth approximation of the distribution, highlighting the central tendency and variability of the minimum total cost values.

Central Tendency and Variability

- **Central Tendency:** The central region of the histogram, where the bars are tallest, suggests that the most frequent minimum total cost values lie between 9500 and 10000 units. This region represents the central tendency of the distribution.
- **Variability:** The spread of the histogram indicates the variability in the minimum total cost values. The density gradually decreases towards the tails of the

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distribution, indicating fewer occurrences of extreme values (both lower and higher).

Interpretation

- The bell-shaped curve of the distribution suggests that the minimum total cost values follow a roughly normal distribution. However, further statistical tests (e.g., Kolmogorov-Smirnov test, Shapiro-Wilk test) and goodness-of-fit evaluations are necessary to confirm the exact nature of the distribution.
- The plot indicates that the majority of the simulation outcomes resulted in minimum total costs within a narrow range around the central tendency, implying consistency in the cost minimization process under the simulated conditions.

Question (i)

Use the results of your simulation to:

(i) Estimate the expected minimum total cost by constructing a 95% confidence interval for it and determine the probability distribution that best fits its distribution. Verify the validity of your choice.

```
> cat("Minimum total cost:", Estimate_min_cost, "\n")
Minimum total cost: 9744.368
> cat("95% confidence interval for expected minimum total cost: (", lower, ", ", upper, ")", "\n")
95% confidence interval for expected minimum total cost: ( 9728.07 , 9760.666 )
~ |
```

Figure 11 Confidence Intervals of Minimum Cost.

Estimated Minimum Total Cost

The estimated mean minimum total cost from the simulation is \$9744.37. Constructing a 95% confidence interval for the expected minimum total cost, we find it to be between \$9728.07 and \$9760.67. This interval provides a range within which we can be 95% confident that the true mean minimum total cost lies.

Distribution Analysis

Histogram and Density Plot

The histogram of the minimum total cost, along with a density plot, which was described in the previous page, reveals the distribution shape. The plot suggests a roughly symmetric distribution with a peak around the mean value.

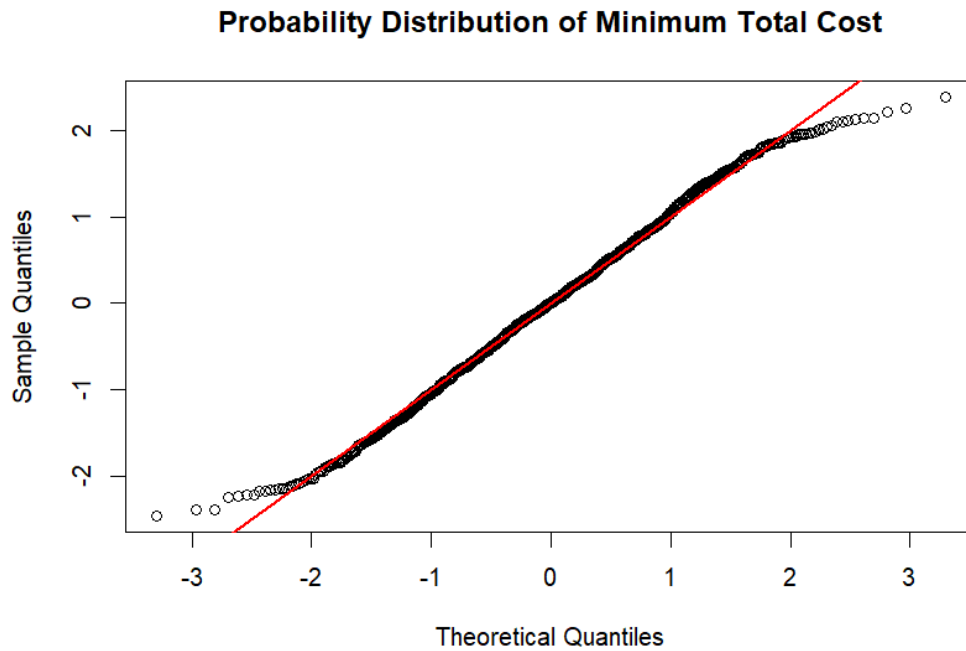


Figure 12 QQ Plot Minimum cost.

Quantile-Quantile (Q-Q) Plot

The Q-Q plot for the normal distribution shows that the data points closely follow the reference line, suggesting that the minimum total cost data is approximately normally distributed. However, the tails show significant discrepancy from the reference line suggesting non-normality at the tails.

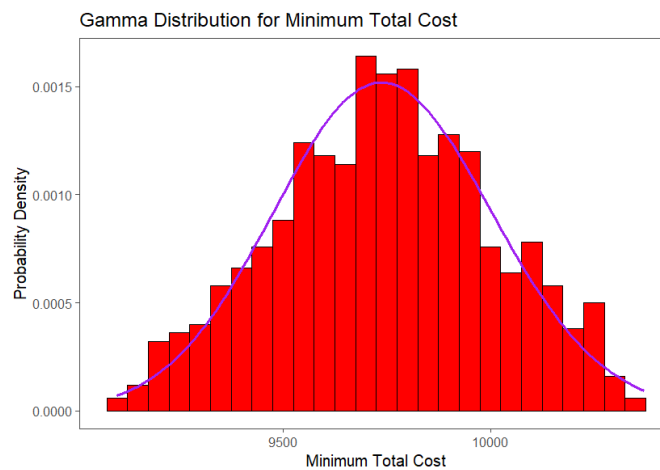


Figure 13 Gamma Distribution nfit on min cost.

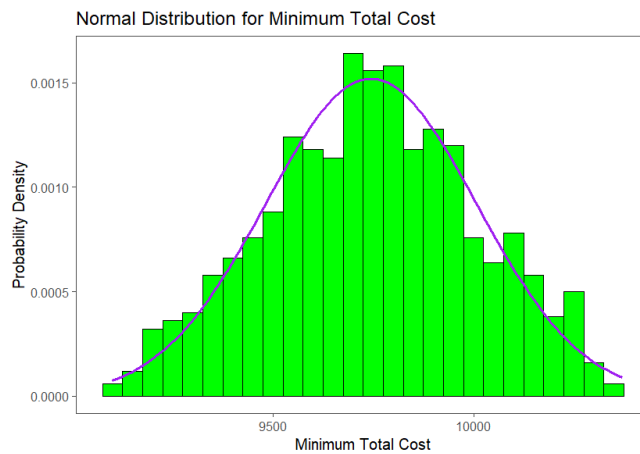


Figure 14 Normal distribution fit on min cost.

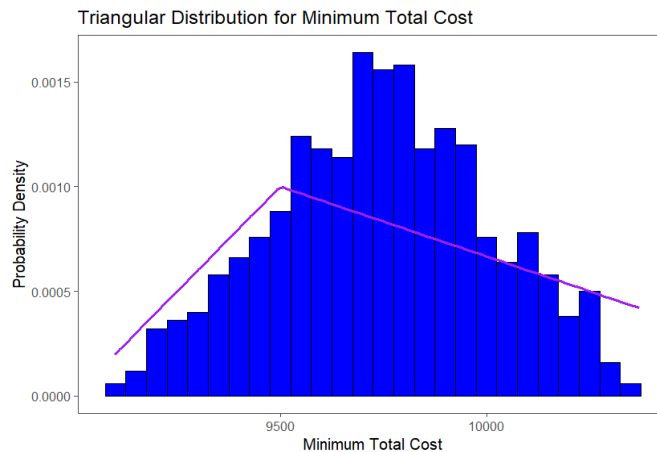


Figure 15 Triangular distribution fit on min total cost.

Probability Distribution Fitting

To determine the best-fitting probability distribution, we fit the Gamma, Normal, and Triangular distributions to the data.

1. **Gamma Distribution:** The histogram with the Gamma distribution overlay shows a good fit, indicating that the Gamma distribution could be a plausible model for the minimum total cost.
2. **Normal Distribution:** The histogram with the Normal distribution overlay appears to fit the data well, except for the fact that the distribution has less thicker tails as compared to the normal distribution.

3. **Triangular Distribution:** The histogram with the Triangular distribution overlay does not fit the data as well as the Gamma and Normal distributions. The triangular fit is less smooth and does not capture the tails of the distribution accurately.

```
> ks_gamma

Asymptotic one-sample Kolmogorov-Smirnov test

data:  min_cost
D = 0.019673, p-value = 0.8337
alternative hypothesis: two-sided

> ks_normal

Asymptotic one-sample Kolmogorov-Smirnov test

data:  min_cost
D = 0.020718, p-value = 0.784
alternative hypothesis: two-sided

> ks_tri

Asymptotic one-sample Kolmogorov-Smirnov test

data:  min_cost
D = 0.1765, p-value < 0.00000000000000022
alternative hypothesis: two-sided

>
> #Shapiro Wilk for normality
> shapiro.test(min_cost)

Shapiro-Wilk normality test

data:  min_cost
W = 0.99285, p-value = 0.00009551

>
> # compare AIC for Gamma and Normal as KS and Shapiro test results conflict
>
> AIC(fit_gamma)
[1] 13983.55
> AIC(fit_normal)
[1] 13982.43
```

Figure 16 Goodness of fit tests on min cost.

Statistical Tests

To statistically validate the distribution fitting, we performed the Kolmogorov-Smirnov (K-S) test and Shapiro-Wilk test for normality:

1. Kolmogorov-Smirnov Test:

- **Gamma Distribution:** $D = 0.019673$, $p\text{-value} = 0.8337$

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- **Normal Distribution:** $D = 0.020718$, $p\text{-value} = 0.784$
- **Triangular Distribution:** $D = 0.1765$, $p\text{-value} < 0.000000000000000000022$

2. Shapiro-Wilk Test for Normality:

- $W = 0.99285$, $p\text{-value} = 0.00009551$

The K-S test results show high p-values for both the Gamma and Normal distributions, indicating that we cannot reject the hypothesis that the data comes from these distributions. However, the low p-value in the Shapiro-Wilk test for normality indicates that the data is not normally distributed.

Model Comparison Using AIC

The Akaike Information Criterion (AIC) values for the Gamma and Normal distributions are compared:

- **Gamma Distribution AIC:** 13983.55
- **Normal Distribution AIC:** 13982.43

The lower AIC value for the Normal distribution suggests a marginally better fit compared to the Gamma distribution, but the Shapiro-Wilk test indicates that the Normal distribution is not an appropriate model.

Conclusion

While the visual inspection of histograms, density plots, and Q-Q plots suggest that the Normal distribution fits well, the Shapiro-Wilk test results indicate otherwise. Given the high p-value in the K-S test and a reasonably low AIC, the Gamma distribution might be a more appropriate fit for the minimum total cost data. This conclusion is drawn by balancing the test results and the AIC values, indicating that **the Gamma distribution provides a better overall** fit despite the close competition with the Normal distribution. Thus, we conclude that the minimum total cost data can be effectively modeled using a Gamma distribution, providing a reliable estimation of inventory costs under the given simulation conditions.

(ii) Estimate the expected order quantity by constructing a 95% confidence interval for it and determine the probability distribution that best fits its distribution. Verify the validity of your choice.

```
> cat("95% confidence interval for expected order quantity: (", lower_oq, ", ", upper_oq, ")", "\n")
95% confidence interval for expected order quantity: ( 675.5604 , 677.824 )
> Estimate_order_qty <- mean(order_qty)
> cat("Estimate order quantity:", Estimate_order_qty, "\n")
Estimate order quantity: 676.6922
>
```

Figure 17 Confidence interval for Order Quantity.

Estimating Expected Order Quantity

Simulation Results

To estimate the expected order quantity, a simulation consisting of 1000 occurrences was conducted. The results of the simulation provided the following key metrics:

- Mean Order Quantity: 676.6922 units
- 95% Confidence Interval for Order Quantity: 675.5604 to 677.824 units

These values were derived from the repeated sampling of order quantities based on the given triangular distribution parameters for demand.

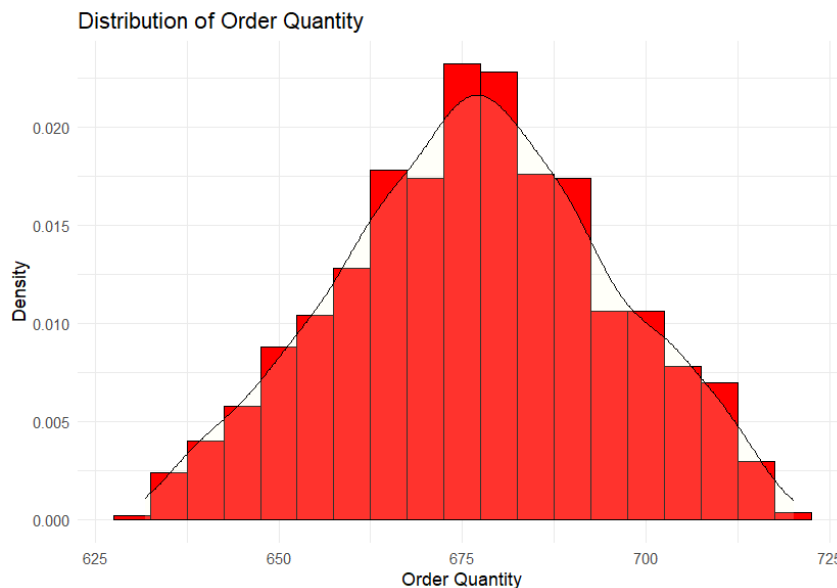


Figure 18 Distribution for Order Quantity.

Histogram and PDF Analysis

- **Histogram:**

- The histogram of the order quantity distribution exhibited a bell-shaped curve, suggesting a potential normal distribution.
- **Probability Density Function (PDF) Plot:**
 - The PDF plot further illustrated this observation by showing that the empirical data aligns closely with the theoretical quantiles of a normal distribution.

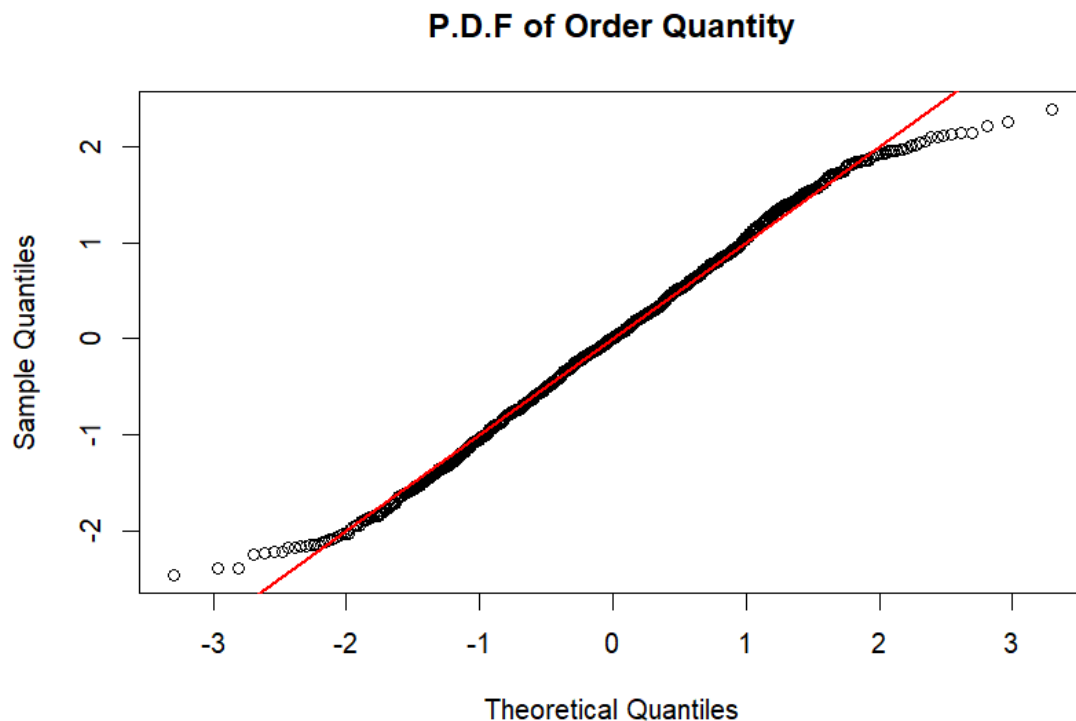


Figure 19 QQ Plot for Order Quantity.

Quantile-Quantile (Q-Q) Plot

- **Q-Q Plot:**
 - The Q-Q plot compared the sample quantiles of the order quantity data to the theoretical quantiles of a normal distribution.
 - The data points closely followed the straight line representing the normal distribution at the middle range while deviating at the extremes.

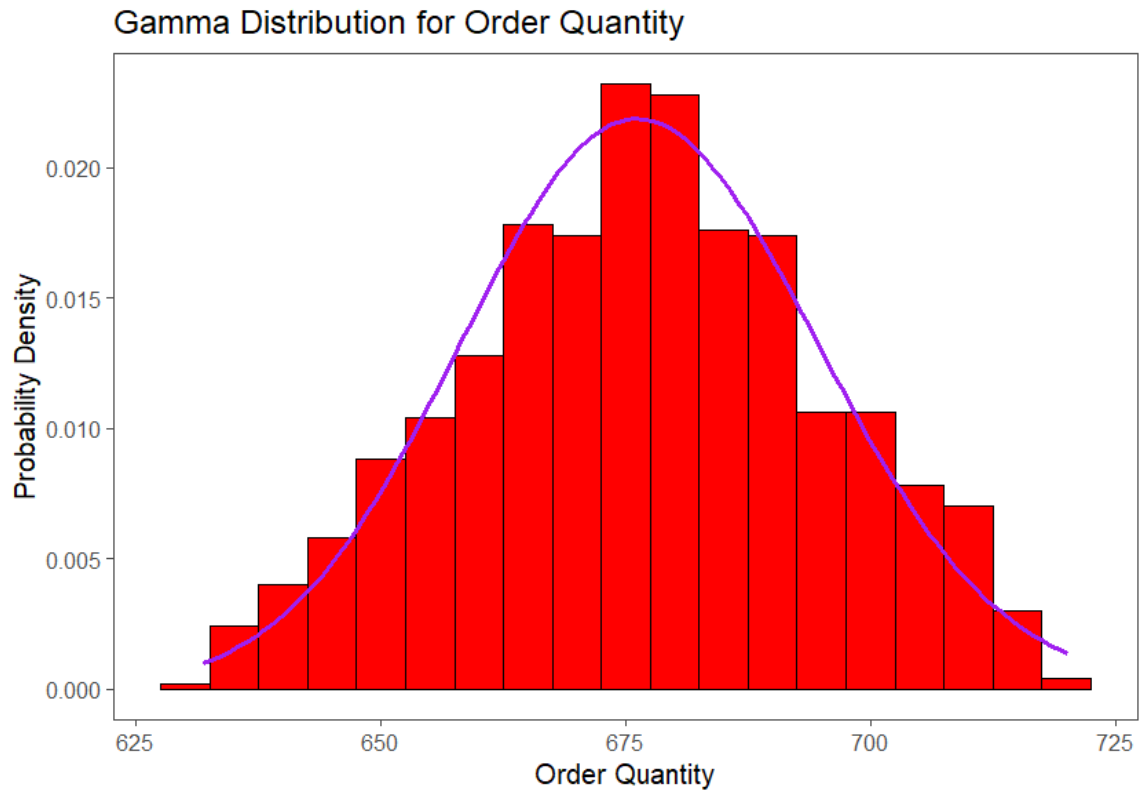


Figure 20 Gamma Distribution fit on Order Quantity.

Fitting Probability Distributions

Gamma Distribution Fit

- **Gamma Distribution Histogram:**
 - The gamma distribution was fitted to the order quantity data, and its fit was visually assessed using a histogram overlaid with the gamma distribution curve.

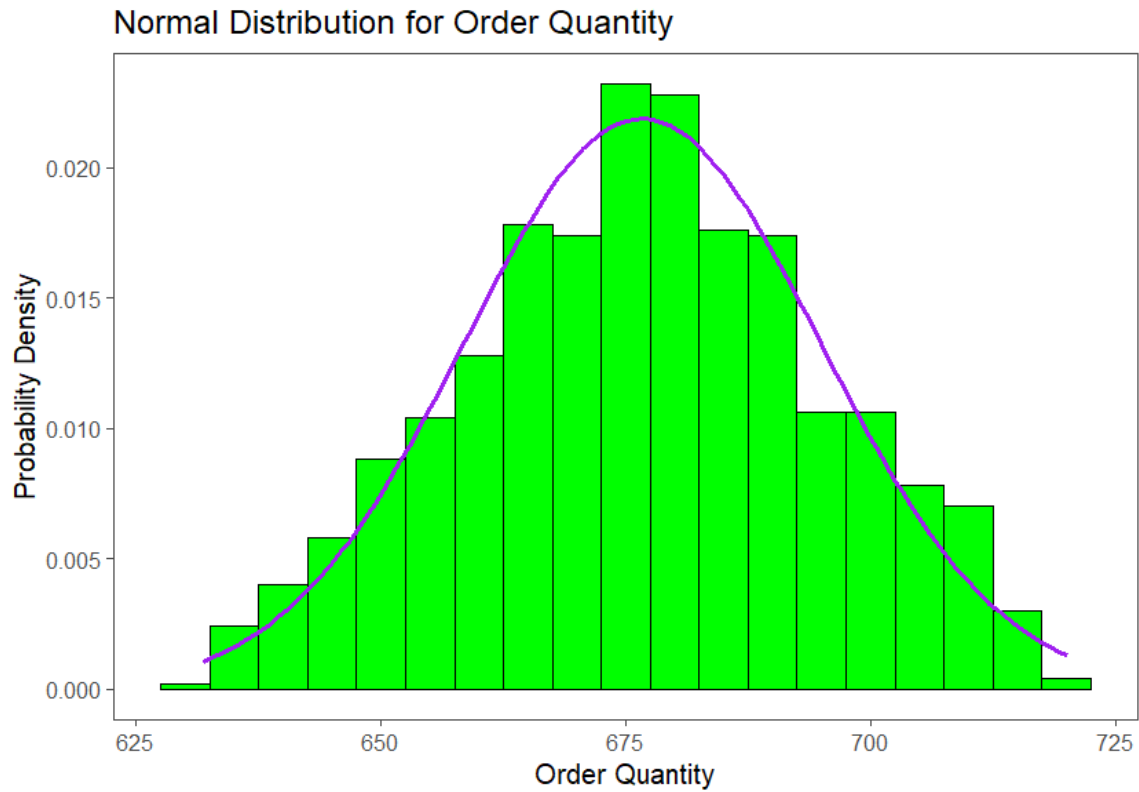


Figure 21 Normal Distribution for Order Quantity.

Normal Distribution Fit

- **Normal Distribution Histogram:**
 - The normal distribution was also fitted to the order quantity data and assessed using a histogram overlaid with the normal distribution curve.

```

> ks_gamma_oq

Asymptotic one-sample Kolmogorov-Smirnov test

data:  order_qty
D = 0.019673, p-value = 0.8337
alternative hypothesis: two-sided

> ks_normal_oq

Asymptotic one-sample Kolmogorov-Smirnov test

data:  order_qty
D = 0.020718, p-value = 0.784
alternative hypothesis: two-sided

>
> #Shapiro wilk
>
> shapiro.test(order_qty)

Shapiro-Wilk normality test

data:  order_qty
W = 0.99285, p-value = 0.00009551

>
>
> #Comparing AIC
> AIC(fit_gamma_oq)
[1] 8649.098
> AIC(fit_normal_oq)
[1] 8647.977
~ |

```

Figure 22 Goodness of fit tests for Order Quantity.

Statistical Tests for Goodness-of-fit

- **Kolmogorov-Smirnov (K-S) Test for Gamma distribution:**
 - The K-S test for the gamma distribution yielded a p-value of 0.8337, indicating a good fit.
- **Kolmogorov-Smirnov (K-S) Test for Normal distribution:**

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- The K-S test for the normal distribution yielded a p-value of 0.784, indicating a good fit.
- **Shapiro-Wilk Test:**
 - The Shapiro-Wilk test for normality resulted in a p-value of 0.00009551, suggesting significant deviation from normality.

Model Comparison Using Akaike Information Criterion (AIC)

- **AIC for Gamma Distribution:**
 - The AIC value for the gamma distribution was calculated to be 8649.098.
- **AIC for Normal Distribution:**
 - The AIC value for the normal distribution was slightly lower at 8647.977.

Interpretation and Conclusion

Summary of Findings

- **Mean Order Quantity:** The estimated mean order quantity from the simulation is 676.6922 units, with a 95% confidence interval ranging from 675.5604 to 677.824 units.
- **Distribution Fit:**
 - Both the gamma and normal distributions were found to fit the order quantity data well, based on the K-S test results.
 - The normal distribution, however, showed a slight edge over the gamma distribution in terms of the AIC values, suggesting a marginally better fit.

Validity of Distribution Fit

- **Shapiro-Wilk Test:**
 - Despite the normal distribution fitting well in visual assessments and K-S test results, the Shapiro-Wilk test indicated a significant deviation from normality, which cannot be ignored.
- **AIC Comparison:**
 - The AIC comparison favored the normal distribution, but the difference was minimal, suggesting that both distributions are plausible fits.

Final Recommendation

- **Best Fit Distribution:**
 - Considering the AIC values and visual assessments, the normal distribution appears to provide a good fit for the order quantity data.

- However, given the significant p-value from the Shapiro-Wilk test, it is recommended to consider the gamma distribution as a viable alternative.

In summary, while the normal distribution is suggested by the AIC comparison and visual assessments, the significant deviation indicated by the Shapiro-Wilk test calls for a cautious approach. Both normal and gamma distributions should be considered for modeling the order quantity, with **a preference for the gamma distribution based on the current analysis.**

(iii) Estimate the expected annual number of orders by constructing a 95% confidence interval for it and determine the probability distribution that best fits its distribution. Verify the validity of your choice.

```
95% confidence interval for expected Annual Number of Orders: ( 22.10925 , 22.18333 )
>
> Estimate_n_order <- mean(n_order)
> cat("Estimate Annual Order Number:", Estimate_n_order, "\n")
Estimate Annual Order Number: 22.14629
~ |
```

Figure 23 Confidence Interval for Annual Number of Orders.

Estimation of Expected Annual Number of Orders and Fitting Probability Distribution

Confidence Interval for Expected Annual Number of Orders

Using the simulation results, we estimated the expected annual number of orders. A 95% confidence interval for this estimate was constructed to provide a range within which the true expected value lies with a 95% probability. The summary statistics derived from the simulation results are as follows:

- 95% Confidence Interval: [22.10925, 22.18333]
- Estimate of Expected Annual Number of Orders: 22.14629

This confidence interval suggests that, based on the simulation, the expected annual number of orders is very likely to fall between approximately 22.11 and 22.18 orders per year.

Distribution Analysis

To determine the best-fitting probability distribution for the annual number of orders, we compared the observed data against theoretical distributions using several diagnostic tools, including probability density functions (PDFs), quantile-quantile (Q-Q) plots, and statistical goodness-of-fit tests.

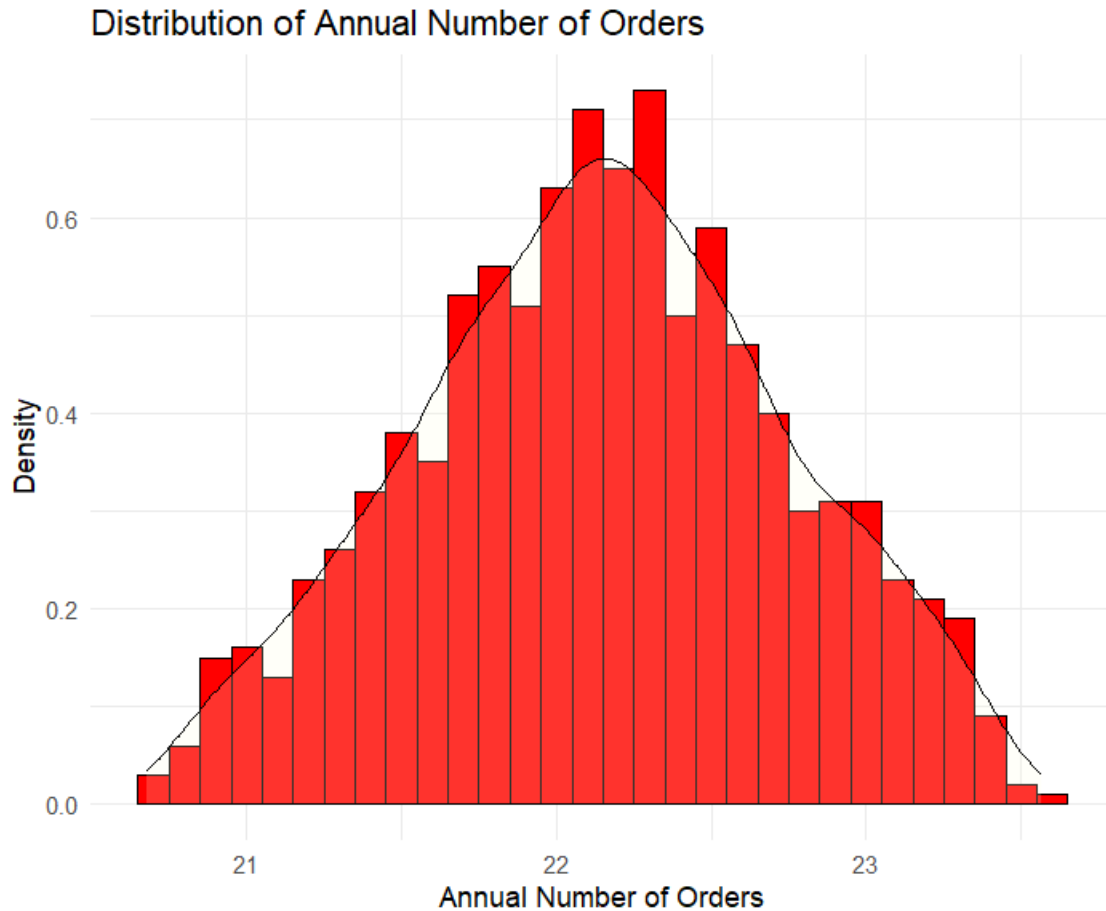


Figure 24 Distribution of Annual Number of Orders.

1. Histogram and Density Plot:

- The above histogram of the simulated annual number of orders overlaid with the estimated density curve shows a roughly symmetric distribution centered around 22 orders per year.

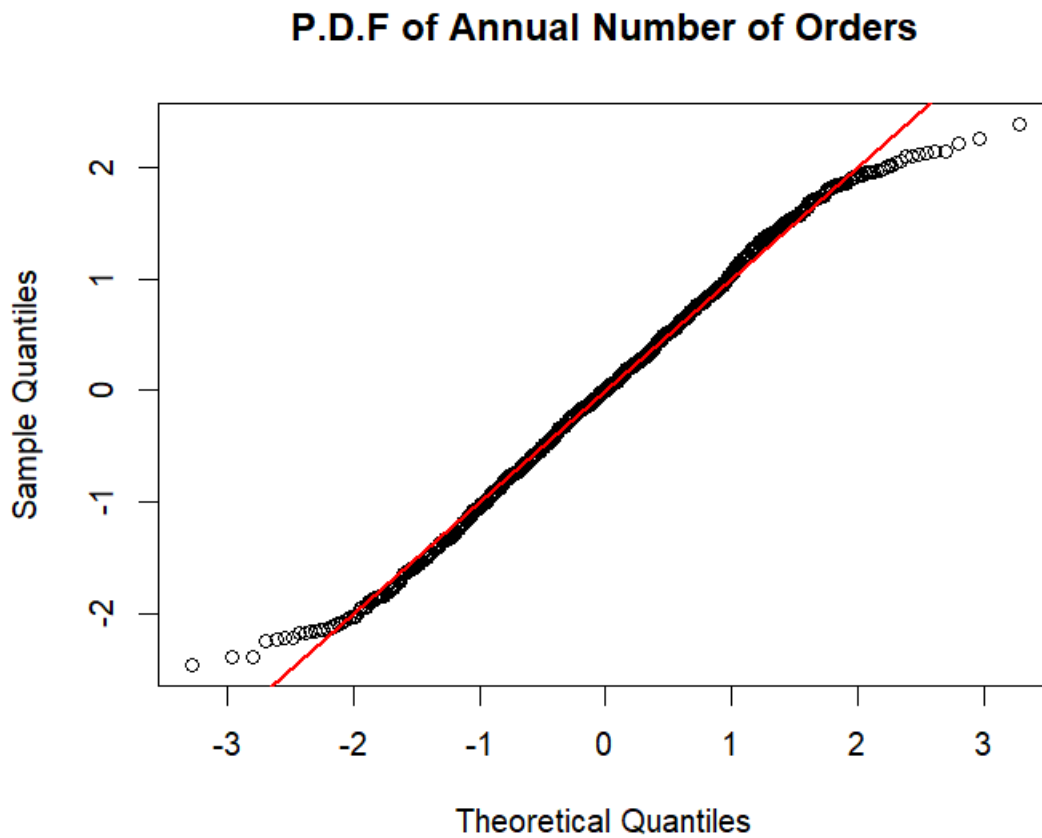


Figure 25 QQ Plot of Annual Number of Orders.

1. Q-Q Plot:

- The Q-Q plot compares the quantiles of the observed data with the quantiles of a normal distribution. The points closely follow the 45-degree line, suggesting that the distribution of the annual number of orders approximates a normal distribution at the middle. However, tails deviate at both ends suggesting caution while fitting a normal distribution.

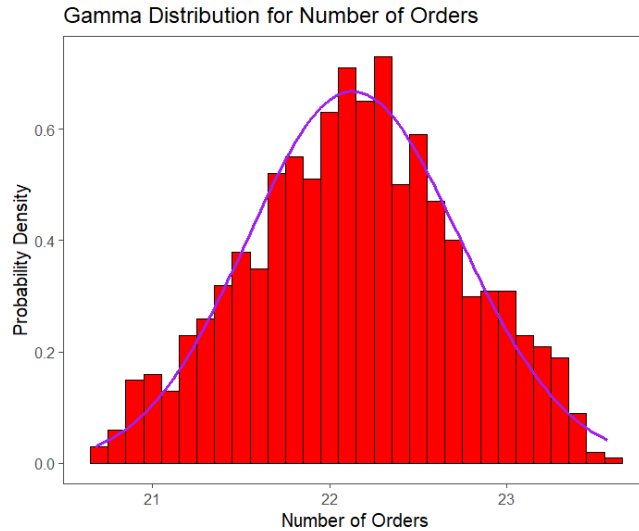


Figure 26 Gamma Distribution fit on Annual Number of Orders.

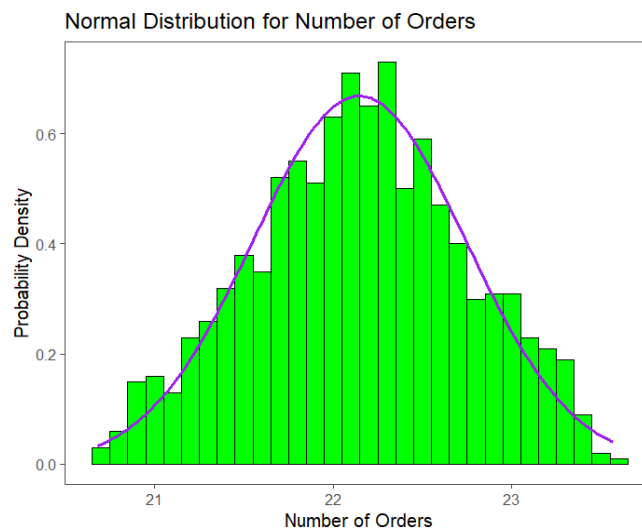


Figure 27 Normal Distribution fit on Annual Number of Orders.

1. Gamma and Normal Distributions:

- Both gamma and normal distributions were fitted to the data. The fit was evaluated using visual inspection of density plots
- Both Gamma and Normal distributions seem to be reasonably good fits for the data. However, as noted earlier the QQ Plot recommends a preference for the Gamma distribution as the ends in the QQ Plot deviated from the reference line.

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```

> ks_gamma_no

Asymptotic one-sample Kolmogorov-Smirnov test

data:  n_order
D = 0.019673, p-value = 0.8337
alternative hypothesis: two-sided

> ks_normal_no

Asymptotic one-sample Kolmogorov-Smirnov test

data:  n_order
D = 0.020719, p-value = 0.7839
alternative hypothesis: two-sided

>
> #Shapiro wilk test
>
> shapiro.test(n_order)

Shapiro-Wilk normality test

data:  n_order
W = 0.99285, p-value = 0.00009551

>
> #AIC Comparison
> AIC(fit_gamma_no)
[1] 1810.003
> AIC(fit_normal_no)
[1] 1808.882
~ |

```

Figure 28 Goodness of Fit tests for Annual Number of Orders.

Goodness-of-Fit Tests

To formally test the fit of the gamma and normal distributions, we used the Kolmogorov-Smirnov (KS) test and the Shapiro-Wilk test.

- **Kolmogorov-Smirnov Test:**
 - Gamma Distribution: KS statistic = 0.019673, p-value = 0.8337
 - Normal Distribution: KS statistic = 0.020719, p-value = 0.7839
 - Both p-values are greater than 0.05, indicating no significant difference between the sample distribution and the theoretical distributions.
- **Shapiro-Wilk Test:**
 - Normal Distribution: W = 0.99285, p-value = 0.00009551
 - The low p-value indicates that the data deviates from a perfect normal distribution. The Shapiro-Wilk test is particularly sensitive to deviations from normality in large sample sizes, which suggests that the normal distribution may not be the best fit despite visual indications.

- **Akaike Information Criterion (AIC):**
 - Gamma Distribution: AIC = 1810.003
 - Normal Distribution: AIC = 1808.882
 - The AIC values suggest that the normal distribution provides a slightly better fit to the data compared to the gamma distribution, as indicated by the lower AIC value.

Conclusion

While the AIC values suggest that the normal distribution provides a slightly better fit, the significantly low p-value from the Shapiro-Wilk test indicates a deviation from normality that cannot be ignored. The Kolmogorov-Smirnov test for the gamma distribution shows a higher p-value compared to the normal distribution, suggesting that the gamma distribution may be a more suitable model for the annual number of orders.

Considering the sensitivity of the Shapiro-Wilk test and the higher p-value of the KS test for the gamma distribution, we conclude that the gamma distribution is preferred for modeling the annual number of orders. This conclusion is supported by:

- Visual inspection: The histogram and Q-Q plots suggest a good fit for the gamma distribution.
- Goodness-of-fit tests: The KS test indicates no significant difference for the gamma distribution, and the Shapiro-Wilk test suggests deviation from normality.

Therefore, for practical purposes and based on the evidence provided, the gamma distribution is chosen as the best fit for the annual number of orders. This allows us to make reliable predictions and inferential statistics regarding the ordering process in inventory management.

Recommendations

To address the problem of determining the minimum total cost under the condition of annual demand following a triangular probability distribution, we conducted a simulation with 1000 occurrences. The triangular distribution parameters were set with a minimum demand of 13,000 units, a maximum demand of 17,000 units, and a mode of 15,000 units. The holding cost per unit was \$14.4, and the order cost was \$220, consistent with the values used in part I of the analysis.

In the simulation, the triangular distribution was defined with minimum, maximum, and mode values of 13,000 units, 17,000 units, and 15,000 units, respectively. The total inventory cost was calculated using a function that incorporated both the annual holding cost and the annual ordering cost. The annual holding cost was computed as $(Q / 2) * H$, while the annual ordering cost was calculated as $(D / Q) * S$, where Q represents the order quantity and D denotes the annual demand.

The simulation was executed in 1000 iterations, where each iteration involved generating a random demand value from the triangular distribution, determining the order quantity that minimized the total cost using the optimize function, calculating the minimum total cost for the generated demand, and recording the number of orders placed and the minimum total cost. The results of the simulation

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were captured in a CSV file, which included the occurrence number, generated annual demand, optimal order quantity, total number of orders placed annually, and the minimum total cost for each iteration.

The key statistical measures derived from the simulation results included the minimum total cost, first quartile, median, mean, third quartile, and maximum total cost. The minimum total cost observed across the simulations was \$9,098, representing the lowest possible total cost under the given demand conditions and cost parameters. The first quartile value was \$9,562, indicating that 25% of the simulated total costs were below this amount. The median total cost was \$9,747, showing that half of the occurrences resulted in a total cost less than or equal to this amount. The mean total cost was \$9,744, offering a central tendency measure of the inventory costs. The third quartile value was \$9,931, highlighting the upper spread of the cost distribution, and the maximum total cost observed was \$10,370, representing the highest possible total cost under the given conditions.

Additionally, the estimated mean minimum cost was approximately \$9,744.37, providing a reliable measure of the expected minimum inventory cost under the specified conditions. These statistical measures are crucial for understanding the variability and expected range of total inventory costs, aiding in more informed decision-making in inventory management.

To estimate the expected minimum total cost, a 95% confidence interval was constructed, resulting in a range between \$9728.07 and \$9760.67. The distribution analysis involved fitting Gamma, Normal, and Triangular distributions to the data. The Gamma and Normal distributions showed a good fit, with high p-values in the Kolmogorov-Smirnov test, indicating no significant difference from the sample distribution. However, the Shapiro-Wilk test for normality showed a low p-value, suggesting a deviation from normality.

Comparing the Akaike Information Criterion (AIC) values for the Gamma and Normal distributions, the Normal distribution had a slightly lower AIC, indicating a marginally better fit. Despite this, the Gamma distribution was considered more appropriate due to the Shapiro-Wilk test results. Thus, the Gamma distribution provides a more reliable model for the minimum total cost data, balancing the test results and AIC values.

Similarly, Confidence intervals were constructed for Order Quantity and Number of Orders. The 95% confidence interval for the expected annual number of orders is given as (22.10925, 22.18333). This interval suggests that we are 95% confident that the true mean annual number of orders lies within this range. It means if we were to take many samples and compute a confidence interval for each, approximately 95% of those intervals would contain the true mean annual number of orders. Similarly, the 95% confidence interval for the expected order quantity is given as (675.5604, 677.824). This interval indicates that we are 95% confident that the true mean order quantity falls within this range. This implies that if we repeated the sampling process numerous times, 95% of the calculated confidence intervals would encompass the actual mean order quantity. In both cases, the mean values (22.14629 for the annual number of orders and 676.6922 for the order quantity) are point estimates derived from the sample data. The confidence intervals provide a range of values that likely include the population means, accounting for the variability and uncertainty inherent in sample data.

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