

**Table 4 | Computational cost and runtime (practicality) for MXene EIS fitting.** Benchmark comparison of the three inference routes, classical nonlinear least squares (NLLS), continuous VQE/VQA (bounded decoding + COBYLA outer loop), and discrete QAOA (surrogate QUBO/Ising +  $\gamma$ - $\beta$  search + best-shot decoding), reporting wall-time, number of objective evaluations, average time per evaluation, and sampling budget (shots = 4096 where applicable) in a fixed software/hardware environment (platform + Python/NumPy/SciPy versions and number of frequency points  $N$ ). The table also summarizes scaling-relevant factors (e.g.,  $O(N)$  circuit-model evaluation, dependence on angle-grid size for QAOA) and provides a practical breakdown highlighting the dominant QAOA costs from surrogate finite-difference construction, Ising-energy precomputation, and angle-evaluation/sampling.

Method	Algorithm	Wall-time (s)	Objective evals	Avg time / eval (s)	Shots	Key scaling	Notes	Breakdown
Classical NLLS	SciPy least_squares (TRF)	0.01391208 39999691	6	0.0023186806 66661521	—	$\approx O(N_{freq})$ per eval; convergence -dependent nfev	Deterministic baseline; direct complex residual fit	—
VQE/VQA (continuous)	COBYLA (bounded $u \in [0,1]^7$ )	0.01001976 49999813	53	0.0001890521 698109691	4096	Hardware: $O(\text{shots} \cdot \text{depth})$ per eval; here classical model $O(N_{freq})$	Continuous search; no discretization; optimizer settings affect $n_{fev}$	—
QAOA (discrete)	$p = 1 +$ $\gamma$ - $\beta$ grid (25+81) + best-shot decode	269.589276 98999923	99 (surrogate ) + 106 (angles)	2.432 (per $\langle H \rangle$ eval)	4096	Angle- search $\propto$ #evals; qubits=7×bi ts; $\Delta$ sets local window	$\Delta = 0.08$ ; $\gamma^*=2.8667$ , $\beta^*=0.6676$ ; reference implementat ion	Surrogate FD + energy precomp $ute +$ $106 \times$ $\langle H \rangle$ eval + sampling