

**Table S2B | Parameter distribution statistics across noise levels for MXene EIS inference.** For the same noise-injection and multi-start refit protocol as Table S2A, this table reports parameter-wise distributions of the recovered  $\theta$  at each noise level, including mean, standard deviation, coefficient of variation (CV%), median, and P5–P95 quantiles. These statistics quantify noise-driven drift, dispersion, and heteroscedastic sensitivity across parameters (including the CPE exponents  $\alpha_1, \alpha_2$ ), and provide the distribution-level evidence used in the identifiability and robustness discussion.

Noise (%)	Parameter	Mean	Std	CV (%)	Median	P5	P95
0.00	$R_s$	1.065	0.3482	32.69	1.044	0.6662	1.508
0.00	$L$	$1.950 \times 10^{-7}$	$4.229 \times 10^{-8}$	21.69	$1.906 \times 10^{-7}$	$1.442 \times 10^{-7}$	$2.457 \times 10^{-7}$
0.00	$R_{ct}$	17.48	4.386	25.08	16.33	12.55	22.74
0.00	$Q_1$	0.003278	$7.980 \times 10^{-4}$	24.35	0.003355	0.002265	0.004135
0.00	$\alpha_1$	0.8228	0.03089	3.75	0.8145	0.7874	0.862
0.00	$Q_2$	0.002111	$2.772 \times 10^{-5}$	1.31	0.002116	0.002072	0.002139
0.00	$\alpha_2$	0.9077	0.01615	1.78	0.9073	0.8885	0.9254
0.50	$R_s$	1.133	0.4397	38.81	1.16	0.6449	1.687
0.50	$L$	$1.989 \times 10^{-7}$	$3.085 \times 10^{-8}$	15.51	$1.978 \times 10^{-7}$	$1.652 \times 10^{-7}$	$2.339 \times 10^{-7}$
0.50	$R_{ct}$	19.53	5.601	28.68	19.73	12.39	26.26
0.50	$Q_1$	0.003469	$9.675 \times 10^{-4}$	27.89	0.00314	0.002549	0.004689
0.50	$\alpha_1$	0.8247	0.05065	6.14	0.8038	0.7784	0.8964
0.50	$Q_2$	0.002113	$6.554 \times 10^{-5}$	3.10	0.002107	0.002029	0.002188
0.50	$\alpha_2$	0.9154	0.03689	4.03	0.9159	0.8709	0.9612
1.00	$R_s$	1.204	0.3336	27.69	1.073	0.8701	1.635
1.00	$L$	$2.127 \times 10^{-7}$	$6.469 \times 10^{-8}$	30.41	$1.979 \times 10^{-7}$	$1.481 \times 10^{-7}$	$2.927 \times 10^{-7}$
1.00	$R_{ct}$	19.48	3.42	17.55	20.41	14.84	22.81
1.00	$Q_1$	0.003467	0.001224	35.31	0.003025	0.002495	0.005231
1.00	$\alpha_1$	0.823	0.05583	6.78	0.8331	0.7439	0.8776
1.00	$Q_2$	0.002125	$6.453 \times 10^{-5}$	3.04	0.002143	0.002034	0.002188
1.00	$\alpha_2$	0.9139	0.02038	2.23	0.9163	0.889	0.9355
2.00	$R_s$	0.8799	0.1632	18.55	0.92	0.6465	1.04

2.00	$L$	$1.779 \times 10^{-7}$	$4.314 \times 10^{-8}$	24.25	$1.604 \times 10^{-7}$	$1.431 \times 10^{-7}$	$2.410 \times 10^{-7}$
2.00	$R_{ct}$	22.26	12.6	56.61	17.43	12.37	41.05
2.00	$Q_1$	0.003239	0.001018	31.44	0.003225	0.002028	0.004311
2.00	$\alpha_1$	0.8598	0.04164	4.84	0.8745	0.8048	0.9007
2.00	$Q_2$	0.002158	$7.696 \times 10^{-5}$	3.57	0.002152	0.002066	0.002254
2.00	$\alpha_2$	0.9079	0.03206	3.53	0.9078	0.8694	0.9478
3.00	$R_s$	1.015	0.3394	33.44	0.9803	0.61	1.434
3.00	$L$	$2.189 \times 10^{-7}$	$5.604 \times 10^{-8}$	25.60	$1.917 \times 10^{-7}$	$1.729 \times 10^{-7}$	$2.964 \times 10^{-7}$
3.00	$R_{ct}$	19.72	2.559	12.98	18.74	17.48	23.04
3.00	$Q_1$	0.003089	$9.982 \times 10^{-4}$	32.32	0.003039	0.002054	0.004437
3.00	$\alpha_1$	0.8153	0.01957	2.40	0.8186	0.7885	0.8348
3.00	$Q_2$	0.002088	$5.138 \times 10^{-5}$	2.46	0.002106	0.002018	0.002139
3.00	$\alpha_2$	0.9273	0.02177	2.35	0.919	0.9089	0.9594
5.00	$R_s$	1.368	0.5745	42.01	1.494	0.6247	1.949
5.00	$L$	$1.820 \times 10^{-7}$	$3.285 \times 10^{-8}$	18.05	$1.844 \times 10^{-7}$	$1.407 \times 10^{-7}$	$2.163 \times 10^{-7}$
5.00	$R_{ct}$	20.56	3.148	15.32	20.23	16.97	24.13
5.00	$Q_1$	0.003564	0.00152	42.65	0.003686	0.001781	0.005169
5.00	$\alpha_1$	0.8115	0.06823	8.41	0.8246	0.7153	0.8761
5.00	$Q_2$	0.002098	$8.417 \times 10^{-5}$	4.01	0.002095	0.002003	0.00221
5.00	$\alpha_2$	0.9197	0.03437	3.74	0.9228	0.8758	0.9613
8.00	$R_s$	1.404	0.488	34.76	1.325	0.9166	2.086
8.00	$L$	$1.880 \times 10^{-7}$	$2.556 \times 10^{-8}$	13.60	$1.833 \times 10^{-7}$	$1.636 \times 10^{-7}$	$2.177 \times 10^{-7}$
8.00	$R_{ct}$	21.51	5.499	25.56	20.4	15.78	28.92
8.00	$Q_1$	0.003377	$6.307 \times 10^{-4}$	18.68	0.003315	0.002691	0.004119
8.00	$\alpha_1$	0.8435	0.05029	5.96	0.8468	0.7842	0.8949
8.00	$Q_2$	0.002139	$8.094 \times 10^{-5}$	3.78	0.002144	0.002032	0.00223
8.00	$\alpha_2$	0.9166	0.02322	2.53	0.9099	0.8957	0.9503