

Table 4 | Computational cost and runtime (practicality) for MXene EIS fitting. Benchmark comparison of the three inference routes, classical nonlinear least squares (NLLS), continuous VQE/VQA (bounded decoding + COBYLA outer loop), and discrete QAOA (surrogate QUBO/Ising + γ - β search + best-shot decoding), reporting wall-time, number of objective evaluations, average time per evaluation, and sampling budget (shots = 4096 where applicable) in a fixed software/hardware environment (platform + Python/NumPy/SciPy versions and number of frequency points N). The table also summarizes scaling-relevant factors (e.g., O(N) circuit-model evaluation, dependence on angle-grid size for QAOA) and provides a practical breakdown highlighting the dominant QAOA costs from surrogate finite-difference construction, Ising-energy precomputation, and angle-evaluation/sampling.

Method	Algorithm	Wall-time (s)	Objective evals	Avg time / eval (s)	Shots	Key scaling	Notes	Breakdown
Classical	SciPy least_squares	0.01391208 39999691	6	0.0023186806 66661521	—	$\approx O(N_{freq})$ per eval; convergence -dependent nfev	Deterministi c baseline; direct complex residual fit	—
VQE/VQA (continuous)	COBYLA (bounded $u \in [0,1]^7$)	0.01001976 49999813	53	0.0001890521 698109691	4096	Hardware: $O(\text{shots} \cdot \text{dep})$ th) per eval; here classical model $O(N_{freq})$	Continuous search; no discretizatio n; optimizer settings affect n_{fev}	—
QAOA (discrete)	$p = 1 + \gamma - \beta$ grid (25+81) + best-shot decode	269.589276 98999923	99 (surrogate) + 106 (angles)	2.432 (per (H) eval)	4096	Angle- search \propto #evals; qubits=7×bi ts; Δ sets local	$\Delta = 0.08;$ $\gamma^* = 2.8667,$ $\beta^* = 0.6676;$ reference ute + implementat ion window	Surrogate FD + energy precomp + 106 × $\langle H \rangle$ eval + sampling