

# University Physics A(1)

## Worksheet #7

Name (名字):

Student number (学号):

**New words:** Write the Chinese next to these words as you learn them.

elastic collision

rotational angular momentum

inelastic collision

torque

internal energy

relative to...

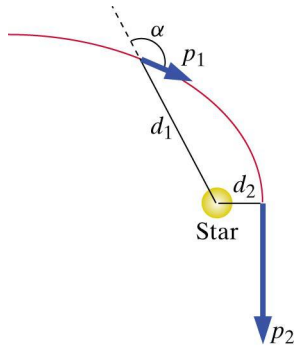
translational angular momentum

**Problems** Show all working.

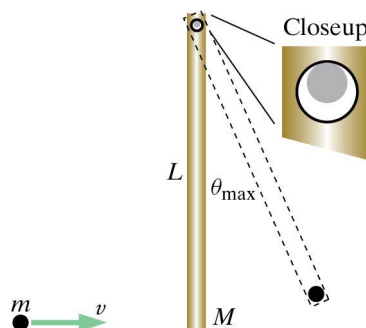
(1) [10.P.21] A car of mass 2300 kg collides with a truck of mass 4300 kg, and just after the collision the car and truck slide along, stucktogether, with no rotation. The car's velocity just before the collision was  $\langle 38, 0, 0 \rangle$  m/s, and the truck's velocity just before the collision was  $\langle -16, 0, 27 \rangle$  m/s.

- (a) What is the velocity of the stuck-together car and truck just after the collision? Write clearly which fundamental principle you are using, and what objects you choose to be in your system.
- (b) In your analysis in part (a), why can you neglect the effect of the force of the road on the car and truck?
- (c) What is the increase in internal energy of the car and truck (thermal energy and deformation)?
- (d) Is this collision elastic or inelastic?

(2) [11.P.50] A small rock passes a massive star, following the path shown in red on the diagram. When the rock is a distance  $4.5 \times 10^{13}$  m (indicated as  $d_1$  in the figure below) from the center of the star, the magnitude  $p_1$  of its momentum is  $1.35 \times 10^{17}$  kg · m/s, and the angle is  $126^\circ$ . At a later time, when the rock is a distance  $d_2 = 1.3 \times 10^{13}$  m from the center of the star, it is heading in the  $-y$  direction. There are no other massive objects nearby. What is the magnitude  $p_2$  of the final momentum?



(3) [11.P.36] A stick of length  $L$  and mass  $M$  hangs from a low-friction axle (see the figure below). A bullet of mass  $m$  traveling at a high speed  $v$  strikes near the bottom of the stick and quickly buries itself in the stick.



- During the brief impact, is the *linear* momentum of the stick + bullet system constant? Explain why or why not. Include in your explanation a sketch of how the stick shifts on the axle during the impact.
- During the brief impact, around what point does the *angular* momentum of the stick + bullet system remain constant?
- Just after the impact, what is the angular speed  $\omega$  of the stick (with the bullet embedded in it)? (*Hint:* the center of mass of the stick has a speed  $\omega L/2$ . The moment of inertia of a uniform rod about its center of mass is  $\frac{1}{12}ML^2$ .)
- Calculate the change in kinetic energy from just before to just after the impact. Where has this energy gone?

## 第七周作业

(1) (a) 小车、卡车系统中, 由动量守恒原理:

$$\vec{p}_{\text{初}} = \vec{p}_{\text{末}} \quad \text{即} \quad m_{\text{小车}} \vec{v}_{\text{小车}} + m_{\text{卡车}} \vec{v}_{\text{卡车}} = (m_{\text{小车}} + m_{\text{卡车}}) \vec{v}_{\text{共}}$$

代入数据得:  $\vec{v}_{\text{共}} = (2.82, 0, 17.59) \text{ m/s}$

(b) 道路对系统中小车和卡车支持力与重力抵消, 摩擦力因接触时间短也可忽略.

(c) 由能量守恒定律有:

$$K_{\text{初}} = K_{\text{末}} + E_{\text{增}}$$

即  $E_{\text{增}} = K_{\text{末}} - K_{\text{初}} = \frac{1}{2}(m_{\text{小车}} + m_{\text{卡车}}) |\vec{v}_{\text{共}}|^2 - \frac{1}{2} m_{\text{小车}} |\vec{v}_{\text{小车}}|^2 - \frac{1}{2} m_{\text{卡车}} |\vec{v}_{\text{卡车}}|^2$

代入数据得:  $E_{\text{增}} = 2.73 \times 10^6 \text{ J}$

(d) 非弹性碰撞, 因为  $E_{\text{增}} \neq 0$

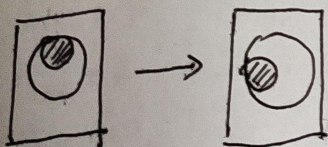
(2) 因为  $\vec{r} \parallel \vec{F}$ , 所以  $\vec{r} \times \vec{F} = \vec{0}$

又  $\frac{d\vec{L}_A}{dt} = \vec{\tau}_A = \vec{0}$  则  $\vec{L}_{A,2} - \vec{L}_{A,1} = \vec{0}$  即  $\vec{L}_{A,2} = \vec{L}_{A,1}$

所以  $\vec{r}_{A,2} \times \vec{p}_2 = \vec{r}_{A,1} \times \vec{p}_1$  在  $-z$  分量上,  $d_2 \cdot p_2 = d_1 \cdot p_1 \cdot \sin \alpha$

所以  $p_2 = \frac{d_1}{d_2} \cdot p_1 \sin \alpha$ . 代入数据, 解得  $p_2 = 3.8 \times 10^{17} \text{ kg} \cdot \text{m/s}$

(3) (a) 棍+子弹系统动量不是常数.  $\Delta \vec{p} = \vec{F} \cdot \Delta t$ . 当子弹击中杆时, 杆向右移动, 击中杆轴, 轴上有很大的力作用在棍上, 大多数系统动量被转移到轴上, 所以不是常数.



(b) 在木棍中心位置, 木棍+子弹系统角动量保持不变.

(c) 由  $\vec{L}_{A,i} = \vec{L}_{A,f}$  得:  $m |\vec{v}_i| L = (I_{\text{棍}} + I_{\text{子弹}}) \cdot |\vec{\omega}_f|$

$|\vec{\omega}_f| \cdot I_{\text{棍}} = \frac{1}{2} \cdot M \cdot \omega \cdot \frac{L}{2} + \frac{1}{2} M L^2 \omega = \frac{1}{3} M L^2 \omega = \frac{1}{3} M L^2 |\vec{\omega}_f|$

$|\vec{\omega}_f| \cdot I_{\text{子弹}} = m L^2 |\vec{\omega}_f|$  则  $|\vec{\omega}_f| = \frac{m}{\frac{1}{3} M + m} \cdot \frac{|\vec{v}_i|}{L}$

(d) 因为  $K_i = \frac{1}{2} m |\vec{v}_i|^2$ ,  $K_f = \frac{1}{2} (I_{\text{棍}} + I_{\text{子弹}}) \cdot |\vec{\omega}_f|^2 = \frac{1}{2} |\vec{v}_i|^2 \cdot \left( \frac{m^2}{\frac{1}{3} M + m} \right)$

所以  $\Delta K = K_f - K_i = \frac{1}{2} m |\vec{v}_i|^2 \cdot \left( \frac{m}{M + 3m} \right)$  这些能量使木棍和子弹温度升高并变形.