

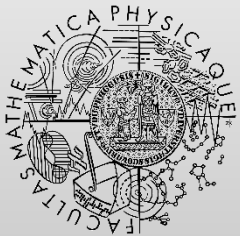
Advanced Usage of Z: Objects & Refinement

<http://d3s.mff.cuni.cz>

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Object-Z



- Main features
 - Classes & instances
 - Operations (methods)
 - Inheritance
 - History invariants
 - Dot notation
- Benefits
 - OOP: structure, modularity, reuse

Refinement

- Goal: specification → design → code
- Operation refinement
- Data refinement

Operation refinement

- Abstract operation OpA
- Concrete operation OpC
- Weaker precondition
 - $\text{pre OpA} \Rightarrow \text{pre OpC}$
- Stronger postcondition
 - $\text{post OpC} \Rightarrow \text{post OpA}$
- Analogy: inheritance & method overriding
 - Object-oriented development

Data refinement

- Goal: design concrete data structures
- Abstract schemas \rightarrow abstract states
- Concrete schemas \rightarrow concrete states
- Abstraction schema: abstract \leftrightarrow concrete
- Correct data refinement
 - $\text{pre OpA} \wedge \text{Abs} \Rightarrow \text{pre OpC}$
 - $\text{pre OpA} \wedge \text{Abs} \wedge \text{OpC} \Rightarrow \text{Abs}' \wedge \text{post OpA}$
 - $\text{InitC} \Rightarrow \text{InitA} \wedge \text{Abs}$

Iterative step-wise refinement

- Target: complex systems
- Step
 - Refine some parts of the system model
 - Create procedures → modular design

Example

- Bank account system
- Abstract data structures
 - Mathematical model (clarity)
- Concrete data structures
 - Computer representation (performance)

- G. Smith. The Object-Z Specification Language
 - <http://doi.org/10.1007/978-1-4615-5265-9>