8E and 8F: Finding the Probability P(Y==1|X)

8E: Implementing Decision Function of SVM RBF Kernel

After we train a kernel SVM model, we will be getting support vectors and their corresponsing coefficients α_i

Check the documentation for better understanding of these attributes:

https://scikit-learn.org/stable/modules/generated/sklearn.svm.SVC.html

Attributes:

support_ : *array-like, shape = [n_SV]*
Indices of support vectors.

support_vectors_ : *array-like, shape = [n_SV, n_features]*
Support vectors.

n_support_ : *array-like, dtype=int32, shape = [n_class]*
Number of support vectors for each class.

dual_coef_ : *array, shape = [n_class-1, n_SV]*
Coefficients of the support vector in the decision function. For multiclass, coefficient for all 1-vs-1 classifiers. The layout of the coefficients in the multiclass case is somewhat non-trivial. See the section about multi-class classification in the SVM section of the User Guide for details.

coef_ : *array, shape = [n_class * (n_class-1) / 2, n_features]*
Weights assigned to the features (coefficients in the primal problem). This is only available in the case of a linear kernel.

coef_ is a readonly property derived from `dual_coef_` and `support_vectors_`.

intercept_ : *array, shape = [n_class * (n_class-1) / 2]*
Constants in decision function.

fit_status_ : *int*
0 if correctly fitted, 1 otherwise (will raise warning)

probA_ : *array, shape = [n_class * (n_class-1) / 2]*

probB_ : *array, shape = [n_class * (n_class-1) / 2]*
If probability=True, the parameters learned in Platt scaling to produce probability estimates from decision values. If probability=False, an empty array. Platt scaling uses the logistic function `1 / (1 + exp(decision_value * probA_ + probB_))` where `probA_` and `probB_` are learned from the dataset [R20c70293ef72-2]. For more information on the multiclass case and training procedure see section 8 of [R20c70293ef72-1].

As a part of this assignment you will be implementing the `decision_function()` of kernel SVM, here decision_function() means based on the value return by `decision_function()` model will classify the data point either as positive or negative

Ex 1: In logistic regression After traning the models with the optimal weights w we get, we will find the value $\frac{1}{1+\exp(-(wx+b))}$, if this value comes out to be < 0.5 we will mark it as negative class, else its positive class

Ex 2: In Linear SVM After traning the models with the optimal weights w we get, we will find the value of $sign(wx+b)$, if this value comes out to be -ve we will mark it as negative class, else its positive class.

Similarly in Kernel SVM After traning the models with the coefficients α_i we get, we will find the value of $sign(\sum_{i=1}^{n}(y_i\alpha_i K(x_i,x_q)) + intercept)$, here $K(x_i,x_q)$ is the RBF kernel. If this value comes out to be -ve we will mark x_q as negative class, else its positive class.

RBF kernel is defined as: $K(x_i,x_q)$ = $exp(-\gamma||x_i - x_q||^2)$

For better understanding check this link: https://scikit-learn.org/stable/modules/svm.html#svm-mathematical-formulation

Task E

> 1. Split the data into X_{train}(60), X_{cv}(20), X_{test}(20)
> 2. Train $SVC(gamma = 0.001, C = 100.)$ on the (X_{train}, y_{train})
> 3. Get the decision boundry values f_{cv} on the X_{cv} data i.e. f_{cv} `= decision_function(` X_{cv} `)` you need to implement this decision_function()

In [160…
```python
import numpy as np
import pandas as pd
from sklearn.datasets import make_classification
from sklearn.model_selection import train_test_split
import numpy as np
from sklearn.svm import SVC
from tqdm.notebook import tqdm
```

In [161…
```python
X, y = make_classification(n_samples=5000, n_features=5, n_redundant=2,
                           n_classes=2, weights=[0.7], class_sep=0.7, random_state=15)
```

Pseudo code

clf = SVC(gamma=0.001, C=100.)
clf.fit(Xtrain, ytrain)

def decision_function(Xcv, ...): #use appropriate parameters
  for a data point x_q in Xcv:
    #write code to implement $(\sum_{i=1}^{\text{all the support vectors}}(y_i\alpha_i K(x_i,x_q)) + intercept)$, here the values y_i, α_i, and $intercept$ can be obtained from the trained model
return *# the decision_function output for all the data points in the Xcv*

fcv = decision_function(Xcv, ...) *# based on your requirement you can pass any other parameters*

Note: Make sure the values you get as fcv, should be equal to outputs of clf.decision_function(Xcv)

In [162…
```python
X_train, X_test, Y_train, Y_test = train_test_split(X,y,test_size=0.2, random_state=0)
X_train, X_cv, Y_train, Y_cv = train_test_split(X_train,Y_train,test_size=0.25, random_state=0)
```

In [163…
```python
svm_clf = SVC(kernel='rbf', gamma=0.001, C=100, random_state = 0)
svm_clf.fit(X_train,Y_train)
```

Out[163…
```
SVC(C=100, gamma=0.001, random_state=0)
```

In [164…
```python
support_vectors = svm_clf.support_vectors_
intercept = svm_clf.intercept_
y_i_alpha_i = svm_clf.dual_coef_     #dual_coef_ = y_i*alpha_i
```

In [165…
```python
def decision_function(X_cv,gamma):
    decision=[]
    for x_q in X_cv:
        decision_fun = 0
        for i in range(len(support_vectors)):
            k = np.exp(-gamma*((np.linalg.norm(support_vectors[i]-x_q))**2))   #k = exp(-gamma ||x_i - x_q||^2)
            decision_fun = decision_fun + (y_i_alpha_i[0,i]*k)
        decision_fun = decision_fun + intercept
        decision.append(decision_fun)
    return np.array(decision)
```

In [166…
```python
f_cv = decision_function(X_cv, 0.001)   #gamma = 0.001
```

In [167…
```python
f_cv = f_cv[:,0]
```

In [168…
```python
f_cv.shape
```

Out[168…
```
(1000,)
```

In [169…
```python
f_cv
```

Out[169…
```
array([-4.16849194e+00, -2.34894292e+00, -7.75767116e-01,  1.86859998e+00,
        1.05466075e+00, -2.20643803e+00, -1.28060150e+00, -3.25420095e+00,
       -2.24829480e-01,  1.03902965e-01, -3.16532463e+00, -2.03106676e+00,
       -2.02504137e+00, -2.35177029e+00, -3.18361576e+00, -2.05109166e+00,
       -1.53876582e+00, -1.69240186e+00,  1.65243447e+00, -1.09625346e+00,
        1.02338767e+00, -1.53430697e+00, -2.33920116e+00,  5.18458451e-01,
       -3.19610556e+00,  6.18589817e-01, -2.98274764e+00,  7.05536018e-02,
       -1.53914038e-01,  1.71592358e+00, -2.25508890e+00,  1.95288295e+00,
       -1.70628594e+00, -3.65295851e+00, -2.81932287e+00,  1.82775238e+00,
       -2.26225632e+00, -1.96585813e+00, -1.88925705e+00, -7.10400139e-01,
       -1.75454813e+00, -2.29105560e+00, -1.10961485e+00,  1.31582783e+00,
       -1.11547834e+00, -7.69598754e-01, -3.19636658e-01,  1.84646153e+00,
       -2.08098129e+00, -1.74515203e+00, -6.15279613e-01, -3.40574850e+00,
       -2.70457611e+00, -5.73558421e-01, -4.38241552e+00, -1.92243520e+00,
       -3.37968523e+00, -1.64651761e+00, -3.06468442e+00, -2.68183795e+00,
       -2.43367141e+00,  3.58739535e+00, -1.05885247e+00, -3.54755840e+00,
       -3.50452571e+00,  1.87747767e+00, -2.97615944e+00,  1.79172456e+00,
       -3.31351171e+00, -3.66825872e+00, -2.34912441e-01, -2.01069526e+00,
        2.01303242e+00, -2.92478723e+00, -8.16357983e-01,  1.94045289e+00,
       -2.37229021e+00, -1.96509596e+00,  1.73161599e+00,  1.68282173e+00,
       -3.49079693e+00, -8.62657879e-02, -2.75122526e+00, -2.31481107e+00,
        2.01795762e+00,  3.39994514e-01,  2.66712465e-01,  5.42989943e-01,
       -1.83612381e+00, -2.02276733e+00,  1.95695184e+00, -3.53851202e+00,
       -1.88197534e+00, -3.34723356e+00, -5.32437031e+00,  2.04387481e+00,
       -2.88587366e+00, -3.10771786e+00, -3.45629890e+00, -1.98369733e+00,
       -1.61237334e-01, -2.43925011e+00, -2.44896256e+00, -2.52781334e+00,
       -1.50237998e+00, -3.31532929e+00, -2.32819411e+00, -2.11105979e+00,
        1.64193625e+00, -2.58660795e+00, -3.05472597e+00, -2.62203184e+00,
        1.85072951e+00, -2.86709411e+00,  5.36908396e-01,  2.56040315e+00,
        1.39006035e+00, -2.52529463e+00, -1.58530550e+00, -3.08372812e+00,
        1.83589464e+00, -1.64896725e+00, -1.83701511e+00, -2.22172106e+00,
        1.57514457e+00, -2.57421145e+00,  1.24319293e+00,  8.58983200e-01,
       -2.07304561e-01,  1.62849031e+00,  2.01845009e+00, -3.25474391e+00,
       -4.62625599e+00,  1.76885722e+00, -5.34834886e+00,  5.96888940e-01,
       -3.49579027e+00, -3.57141809e+00, -1.37718496e+00, -4.16808612e+00,
       -1.93885620e+00,  1.61476195e+00, -6.06650382e+00, -4.36210868e+00,
       -2.89047418e+00,  4.28526820e+00, -3.01541972e+00, -3.15614413e+00,
       -2.78929575e+00, -2.34826697e+00,  1.05201011e+00, -5.58902528e-01,
        9.89488781e-01, -1.31034459e+00, -2.78030302e+00, -3.30298475e+00,
       -2.78743958e+00, -2.21492469e+00, -3.84862892e-01, -3.15917976e+00,
        1.54479842e+00, -3.12687775e+00, -2.51575558e+00, -2.57396225e+00,
       -2.56516945e+00, -3.77254246e+00,  1.85582050e+00, -1.30769491e+00,
       -2.35962855e+00, -1.50060127e+00,  4.39512865e-01, -1.27792868e+00,
       -1.31346758e+00,  2.54487414e+00, -8.22895550e-01, -4.08278271e+00,
       -2.40704035e+00, -4.50364917e-02,  1.80420859e+00, -1.49567802e+00,
       -3.76919977e+00, -1.58035298e+00, -2.27985705e+00,  1.95120220e+00,
       -3.10908331e+00, -3.97823899e+00, -1.64629259e+00,  2.04699631e+00,
       -2.86663082e-01, -1.95420244e+00, -2.18851958e+00,  1.89160727e+00,
        1.22175358e+00, -3.08100015e+00,  3.09555782e+00,  1.59829256e+00,
        3.00380191e+00,  1.74528788e+00, -3.56686568e+00, -3.65984261e+00,
       -2.44990021e+00, -1.44390112e+00, -2.02531153e+00, -4.59795541e+00,
       -3.31050658e+00, -1.43707626e+00, -2.13380871e+00, -2.60848218e+00,
        1.80332424e+00, -3.90872374e-01, -6.63607581e-01, -2.97959612e+00,
        1.96110218e+00, -2.91042682e+00, -3.08508599e+00,  1.31356782e+00,
       -3.04458335e+00, -2.68718183e+00, -2.73271599e+00, -1.08840496e+00,
       -3.57330412e+00, -1.83902830e+00, -2.88425232e+00, -1.59391057e+00,
       -2.99215975e+00, -1.49822940e+00,  1.71896392e+00, -5.14933511e+00,
       -2.61294183e+00, -1.99727046e+00, -2.02428411e+00, -1.77757432e+00,
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       -1.04025002e-01, -4.06029774e+00, -2.76173011e+00, -2.66238695e+00,
       -1.69664027e+00,  1.57413635e+00, -4.07361518e+00,  1.97905700e+00,
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       -4.22011021e-01, -1.38686204e+00,  7.38030889e-01, -3.05135919e+00,
       -2.28383743e+00, -3.16978524e+00, -2.07724187e+00, -2.55733878e+00,
        1.13370192e+00,  2.48859789e-01,  2.24779356e+00, -2.20294788e+00,
       -3.08743144e+00, -1.52208391e+00, -1.51996027e+00, -1.91698205e+00,
       -1.41411378e+00, -2.08966991e+00, -1.68713330e+00, -3.78052461e+00,
       -7.68140529e-02,  2.44736251e+00, -2.46257799e+00, -2.28886195e+00,
       -2.49727728e+00,  1.89792157e+00,  3.98347099e-01,  3.65390186e-01,
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       -3.55307394e+00, -8.97882699e-01,  1.34138676e+00, -2.47993579e+00,
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       -1.77234497e+00, -3.06422712e+00, -2.88339558e+00,  1.35292144e+00,
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       -3.13077927e+00, -3.48184732e+00,  4.77684748e-02, -1.63857779e+00,
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        1.62242105e+00, -2.74820457e-01,  1.70637788e+00,  1.62229744e+00,
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       -3.12060001e+00, -2.59426925e+00, -3.61206970e+00, -1.71776063e+00,
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       -2.03830449e+00, -2.36776058e+00, -1.72114738e+00, -2.70951858e+00,
       -2.30499252e+00, -2.98234595e+00,  9.49961604e-01, -2.48206809e+00,
        1.18405202e+00, -3.11717633e+00,  2.09080209e-03, -4.04154364e+00,
        1.87118023e+00, -2.26139962e-01, -4.03066729e+00, -1.46812682e+00,
       -2.09730699e+00, -1.48780625e+00,  1.73531994e+00, -1.82663482e+00,
       -2.19311343e+00, -3.66869795e+00,  3.11472211e-01, -3.20794456e+00,
        2.07701354e-01, -3.19319295e+00,  1.47357864e+00, -2.41890409e+00,
        1.56896526e+00, -7.14835106e-01, -1.49186406e+00,  8.70643094e-01,
        1.84110297e+00, -4.17674474e+00, -3.64177229e+00,  1.93317215e-03,
       -3.09995795e+00, -2.97078315e+00, -3.16049353e+00,  1.56339007e+00,
       -3.20504021e+00, -2.45891411e+00,  1.62957297e+00, -8.71749201e-01,
        2.15457113e+00, -7.71516540e-01, -1.19061686e+00, -3.08598415e+00,
       -1.02596581e+00, -2.93332845e+00,  1.37737009e+00, -2.48799395e+00,
       -3.91008182e+00, -3.21071691e+00,  3.79258996e-01, -3.11589648e+00,
       -4.65656460e+00,  9.30675914e-01, -2.59511768e+00, -6.81624287e-01,
       -1.97880230e+00, -2.50829547e+00, -1.97504900e+00,  7.19686988e-01,
        3.65916581e-01, -1.73012168e+00, -2.21666772e+00, -2.29778770e+00,
       -3.70587316e+00, -1.73172186e+00,  1.39459498e+00,  1.99594797e+00,
        3.98228639e-01, -6.94875475e-02, -1.05771456e+00, -2.02730352e+00,
       -7.42631379e-01,  1.02617610e+00, -1.02644122e+00,  1.36210331e+00,
       -5.18819053e-01, -3.06562478e+00, -1.71447026e+00, -2.97677852e+00,
       -1.11200092e+00, -2.58682680e-01, -3.00682613e+00,  1.73681020e+00,
       -2.72088424e+00, -9.13412212e-01,  4.02218284e-01,  1.25502003e+00,
       -2.97303317e+00, -2.16629760e+00, -2.40390433e+00, -2.69092285e+00,
        1.41063468e+00,  1.16698008e+00, -1.88140994e+00, -2.87048220e+00,
       -1.66353000e+00, -2.24612444e+00, -2.98267187e+00,  2.67884901e-01,
        2.84537783e+00, -2.25283647e+00,  1.24428009e+00,  1.62407683e+00,
       -1.00597086e+00, -3.53702111e+00, -3.54113243e-01, -1.81210694e+00,
       -1.46790097e-01, -1.91896265e+00, -1.59508055e+00,  2.72038698e+00,
        1.79777233e+00, -2.07677046e+00, -3.08852456e+00, -3.11073866e+00,
       -3.79834211e-02, -2.30467592e+00, -1.77188693e+00,  1.96812904e+00,
        9.04941020e-01, -3.21910997e+00,  1.46476110e+00, -3.14924969e+00,
        1.36264241e+00, -4.08843533e-01, -3.17827117e+00, -4.22622395e+00,
       -2.97072585e+00, -1.71884523e+00, -2.28916402e+00,  8.03565256e-01,
       -3.14183103e+00,  1.10461538e+00, -2.41309656e+00, -3.55475513e+00,
        2.00110250e+00,  1.83268035e+00, -1.92882821e+00, -9.10602065e-01,
        1.63102610e+00, -1.87131627e+00, -3.70707958e+00, -1.73690467e+00,
       -1.60147569e+00,  1.01348299e+00, -3.75733518e+00,  3.59060228e+00,
       -5.91065200e-01, -3.17505287e+00, -3.82771227e+00, -1.16758070e+00,
       -5.92718433e-01,  1.96624933e+00, -1.45762841e+00,  5.73778104e-01,
       -1.74733000e+00, -2.66113607e+00, -2.90585123e+00, -7.86136238e-01,
        2.40286742e+00,  8.39859895e-01,  2.19680865e+00, -3.10347195e-01,
        1.71894826e+00, -2.63182510e+00, -3.34974870e+00,  2.13194594e+00,
        1.75825465e+00, -6.43244432e-02, -3.26878169e+00,  2.13096064e+00,
       -2.59580906e+00, -2.17449642e+00, -2.89744908e+00, -2.68777286e+00,
       -2.72515714e+00, -3.33336195e+00, -4.37044675e+00, -4.63677393e+00,
       -3.07132053e+00, -3.20736821e+00, -2.50833573e+00, -1.60920008e+00,
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       -3.13871643e+00, -2.20452907e+00, -3.10462169e-01, -2.46453849e+00,
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       -1.69193950e+00,  1.29540169e+00,  1.39312830e+00,  1.90107903e+00,
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        2.40707591e+00, -1.75463361e+00, -2.96937334e+00, -4.87070724e-01,
       -3.71023281e+00,  9.84372337e-01, -2.33733671e+00, -1.71546530e+00,
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       -2.74424870e+00,  2.01599676e+00,  4.65305814e-01, -1.52375120e+00,
        1.49382071e+00,  1.04288253e+00,  3.42268570e-01,  2.59545814e+00,
       -3.07547102e+00, -2.55386804e+00,  1.17784013e+00,  1.74906429e+00,
        1.95616148e-01,  2.94136017e+00,  1.70892632e+00, -2.39059966e+00,
        2.32494958e+00, -2.20128542e+00,  1.68278943e+00, -4.51141349e+00,
       -2.66638231e+00, -3.07657870e+00,  1.34122382e+00, -2.28722277e+00,
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       -1.75373684e+00, -3.04450693e+00, -3.39051292e+00, -2.81538384e+00,
       -3.94947133e+00, -3.79108284e+00, -2.55211974e+00, -2.08227150e+00,
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       -2.08225022e+00, -2.61046052e+00,  1.43429589e+00,  5.44487864e-01,
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       -3.45560651e+00,  8.86933900e-01, -3.36226408e+00,  1.83188198e+00,
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       -2.77752450e+00, -1.16960924e+00, -1.59936092e+00, -2.48810326e+00,
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       -1.65066941e+00, -2.99548196e+00, -4.09361038e+00, -1.95867231e+00,
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       -2.29248581e+00, -2.44499093e+00, -2.64647914e+00, -2.90645298e+00,
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       -1.01885499e+00, -3.04909430e+00, -2.27020543e+00,  1.39313542e+00,
       -1.07574289e+00, -1.17959130e+00, -1.91062283e-01, -1.54634811e+00,
       -3.20048596e+00,  1.30489295e+00, -2.48119445e+00,  1.36011518e+00,
       -1.74624556e+00,  2.02323572e+00, -1.17487225e+00, -3.20041960e-01,
       -3.97723705e-01, -1.51127867e+00, -3.10301571e+00, -2.10668995e+00,
       -3.53165138e+00, -3.33931250e+00, -2.86862591e+00,  1.53147897e+00,
       -5.65530224e+00,  1.51572975e+00,  1.00872762e+00,  3.74216530e-02])
```

In [170…
```python
sklearn_decision_fun = svm_clf.decision_function(X_cv)
```

In [171…
```python
sklearn_decision_fun.shape
```

Out[171…
```
(1000,)
```

In [172…
```python
sklearn_decision_fun
```

Out[172…
```
array([-4.16849194e+00, -2.34894292e+00, -7.75767116e-01,  1.86859998e+00,
        1.05466075e+00, -2.20643803e+00, -1.28060150e+00, -3.25420095e+00,
       -2.24829480e-01,  1.03902965e-01, -3.16532463e+00, -2.03106676e+00,
       -2.02504137e+00, -2.35177029e+00, -3.18361576e+00, -2.05109166e+00,
       -1.53876582e+00, -1.69240186e+00,  1.65243447e+00, -1.09625346e+00,
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       -1.70628594e+00, -3.65295851e+00, -2.81932287e+00,  1.82775238e+00,
       -2.26225632e+00, -1.96585813e+00, -1.88925705e+00, -7.10400139e-01,
       -1.75454813e+00, -2.29105560e+00, -1.10961485e+00,  1.31582783e+00,
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       -2.70457611e+00, -5.73558421e-01, -4.38241552e+00, -1.92243520e+00,
       -3.37968523e+00, -1.64651761e+00, -3.06468442e+00, -2.68183795e+00,
       -2.43367141e+00,  3.58739535e+00, -1.05885247e+00, -3.54755840e+00,
       -3.50452571e+00,  1.87747767e+00, -2.97615944e+00,  1.79172456e+00,
       -3.31351171e+00, -3.66825872e+00, -2.34912441e-01, -2.01069526e+00,
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       -2.37229021e+00, -1.96509596e+00,  1.73161599e+00,  1.68282173e+00,
       -3.49079693e+00, -8.62657879e-02, -2.75122526e+00, -2.31481107e+00,
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```

In [173…
```python
np.subtract(f_cv,sklearn_decision_fun)
```

Out[173…

```
array([ 0.00000000e+00,  0.00000000e+00,  0.00000000e+00,  0.00000000e+00,
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```

As shown above, the values we got as fcv are equal to outputs of clf.decision_function(Xcv)

8F: Implementing Platt Scaling to find P(Y==1|X)

Let the output of a learning method be $f(x)$. To get calibrated probabilities, pass the output through a sigmoid:

$$P(y = 1|f) = \frac{1}{1 + exp(Af + B)} \tag{1}$$

where the parameters A and B are fitted using maximum likelihood estimation from a fitting training set (f_i, y_i). Gradient descent is used to find A and B such that they are the solution to:

$$\underset{A,B}{argmin}\{-\sum_i y_i log(p_i) + (1 - y_i)log(1 - p_i)\}, \tag{2}$$

where

$$p_i = \frac{1}{1 + exp(Af_i + B)} \tag{3}$$

Two questions arise: where does the sigmoid train set come from? and how to avoid overfitting to this training set?

If we use the same data set that was used to train the model we want to calibrate, we introduce unwanted bias. For example, if the model learns to discriminate the train set perfectly and orders all the negative examples before the positive examples, then the sigmoid transformation will output just a 0,1 function. So we need to use an independent calibration set in order to get good posterior probabilities. This, however, is not a draw back, since the same set can be used for model and parameter selection.

To avoid overfitting to the sigmoid train set, an out-of-sample model is used. If there are N_+ positive examples and N_- negative examples in the train set, for each training example Platt Calibration uses target values y_+ and y_- (instead of 1 and 0, respectively), where

$$y_+ = \frac{N_+ + 1}{N_+ + 2}; \; y_- = \frac{1}{N_- + 2} \tag{4}$$

For a more detailed treatment, and a justification of these particular target values see (Platt, 1999).

Check this PDF

TASK F

1. Apply SGD algorithm with (f_{cv}, y_{cv}) and find the weight W intercept b `Note: here our data is of one dimensional so we will have a one dimensional weight vector i.e W.shape (1,)`

   Note1: Don't forget to change the values of y_{cv} as mentioned in the above image. you will calculate y+, y- based on data points in train data

   Note2: the Sklearn's SGD algorithm doesn't support the real valued outputs, you need to use the code that was done in the `'Logistic Regression with SGD and L2'` Assignment after modifying loss function, and use same parameters that used in that assignment.

```python
def log_loss(w, b, X, Y):
    N = len(X)
    sum_log = 0
    for i in range(N):
        sum_log += Y[i]*np.log10(sig(w, X[i], b)) + (1-Y[i])*np.log10(1-sig(w, X[i], b))
    return -1*sum_log/N
```

   if Y[i] is 1, it will be replaced with y+ value else it will replaced with y- value

1. For a given data point from X_{test}, $P(Y = 1|X) = \frac{1}{1+exp(-(W*f_{test}+b))}$ where f_{test} = `decision_function(` X_{test} `)`, W and b will be learned as metioned in the above step

Note: in the above algorithm, the steps 2, 4 might need hyper parameter tuning, To reduce the complexity of the assignment we are excluding the hyerparameter tuning part, but intrested students can try that

If any one wants to try other calibration algorithm istonic regression also please check these tutorials

1. http://fa.bianp.net/blog/tag/scikit-learn.html#fn:1
2. https://drive.google.com/open?id=1MzmA7QaP58RDzocB0RBmRiWfl7Co_VJ7
3. https://drive.google.com/open?id=133odBinMOIVb_rh_GQxxsyMRyW-Zts7a
4. https://stat.fandom.com/wiki/Isotonic_regression#Pool_Adjacent_Violators_Algorithm

In [174…

```python
#Sigmoid function
def sigmoid(w,x,b):
    val=1/(1+np.exp(-(np.dot(x,w.T)+b)))
    return val
```

In [175…

```python
#Log Loss function
# Log loss= -((1/N)*[(y*log(p))+((1-y)*log(1-p))])
def log_loss_fun(w,x,b,y):
    sigmoid_val=sigmoid(w,x,b)
    first_term=y*np.log10(sigmoid_val)
    second_term=(1-y)*np.log10(1-sigmoid_val)
    val=-((first_term+second_term)/(len(x)))
    return np.sum(val)
```

In [176…

```python
class_one = list(Y_train).count(1)
class_zero = list(Y_train).count(0)
Y_plus = (class_one+1)/(class_one+2)
Y_minus = 1/(class_zero+2)
```

In [177…

```python
def convert(Y_cv, Y_plus, Y_minus):
    Y_probabilities = []
    for p in Y_cv:
        if p==1:
            Y_probabilities.append(Y_plus)
        else:
            Y_probabilities.append(Y_minus)
    return (np.array(Y_probabilities))
```

In [178…

```python
modified_Y_cv = convert(Y_cv, Y_plus, Y_minus)
```

In [179…

```python
w = np.zeros_like(f_cv[0])
b = 0
eta0  = 0.0001
alpha = 0.0001
```

In [180…

```python
def SGD(w,b,epoch,x,y):
    log_loss_test=[]
    N=len(x)
    #Calculate initial log loss and storing the values
    loss = log_loss_fun(w,x,b,y)
    log_loss_test.append(loss)

    for epo in tqdm(range(epoch)):
        for i in range(N):
            w= ((1-(alpha*eta0)/N)*w)+((alpha*x[i])*(y[i]-sigmoid(w,x[i],b)))
            b= (b+(alpha*(y[i]-sigmoid(w,x[i],b))))
        log_loss_value=log_loss_fun(w,x,b,y)
        log_loss_test.append(log_loss_value)
        if abs((np.sum(log_loss_test[epo+1]-log_loss_test[epo])))<=0.0001:
            print('Updation is completed in {} epochs'.format(epo+1))
            break

    return w,b,log_loss_test,epo+1
```

In [181…

```python
epochs = 50
updated_w,updated_b,loss,convergence_epoch=SGD(w,b,epochs,f_cv,modified_Y_cv)
print("Weight = {}".format(updated_w))
print("Intercept = {}".format(updated_b))
```

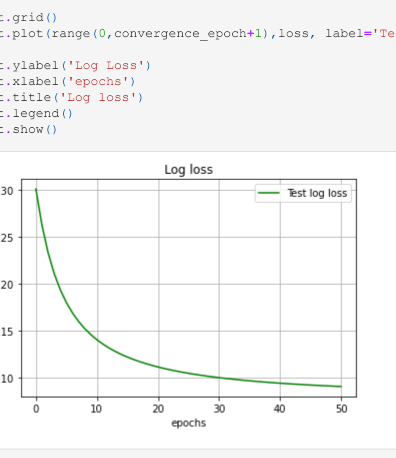
```
Weight = 1.184267476983368
Intercept = -0.1822208677249477
```

In [182…

```python
import matplotlib.pyplot as plt

plt.grid()
plt.plot(range(0,convergence_epoch+1),loss, label='Test log loss', color='green')

plt.ylabel('Log Loss')
plt.xlabel('epochs')
plt.title('Log loss')
plt.legend()
plt.show()
```



In [183…

```python
f_test = decision_function(X_test, 0.001)
```

In [184…

```python
X_test.shape
```

Out[184…

```
(1000, 5)
```

In [185…

```python
def y_probability(f_test, w , b):
    return( 1/(1+np.exp(-((w*f_test)+b))))
```

In [186…

```python
probability = y_probability(f_test, updated_w, updated_b)
print(probability.shape,X_test.shape)
print(probability)
```

```
(1000, 1) (1000, 5)
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