

Assignment 4

CMPT354

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Question 1

1. $isrc \rightarrow mln$

this cannot be implied from F, because mln is only in two functional dependencies which are kind of isolated from others and there isn't any attribute in those two to/from other FDs.

2. $isrc, rep \rightarrow end$

It can be implied from F:

- a. we know $rep \rightarrow label$ using augmentation we have:
 $end, rep \rightarrow end, label$
- b. we also know that $artist, label \rightarrow end, rep$
- c. transitivity on a and b, we have:
 $artist, label \rightarrow end, label$
- d. augmentation on c we get:
 $artist \rightarrow end$
- e. from $isrc \rightarrow artist, genre$ and decomposition
 $isrc \rightarrow artist$
- f. transitivity on e and d:
 $isrc \rightarrow end$
- g. from reflexivity we know:
 $isrc, rep \rightarrow isrc$
- h. transitivity on f and g:
 $isrc, rep \rightarrow end$

3. $label, msin, artist \rightarrow inst, mfn, rep$

It can be implied from F:

- a. we know:
 $msin \rightarrow mln, inst$
- b. Decomposition on a:
 $Msin \rightarrow inst$
 $Msin \rightarrow mln$
- c. We know:
 $Msin, mln \rightarrow msin, mfn$
- d. Augmentation on c:
 $Mln \rightarrow mfn$
- e. Transitivity on b and d:
 $Msin \rightarrow mfn$
- f. Union on b and e:
 $Msin \rightarrow inst, mfn$

- g. We know:
Artist, label -> end, rep
 - h. Decomposition on g:
Artist, label -> rep
 - i. From reflexivity we have:
Artist, label, msin -> msin
Artist, label, msin -> artist, label
 - j. Transitivity on f and i:
Artist, label, msin -> inst, mfn
 - k. Transitivity on h and i:
Artist, label, msin -> rep
 - l. Union on j and k:
Artist, label, msin -> inst mfn, rep
4. *wsin, artist -> genre, royalty*

this cannot be implied from F, we have these FDs

- *isrc, wsin, title -> royalty, title, album*
- *isrc, wsin -> royalty, album*
- *isrc, wsin -> royalty*
- *artist -> genre*

there's no way to get the required FD from these ones, so it cannot be implied.

Question 2

1. attribute closure of (msin, wsin):
{msin, wsin, mln, inst, mfn, wfn, wln}
2. attribute closure of (isrc, label):
{isrc, label, icity, icountry, artist, genre, member, title, album, syear, end, rep}
3. minimal super key:
{msin, isrc, wsin}

Question 3

In order to get canonical cover of F, we'll follow these three steps:

1. apply decomposition rule to the ones possible
2. remove extraneous attributes
3. remove redundant FDs

step 1:

artist → member
artist → genre
msin → mln
msin → inst

$msin, mln \rightarrow msn$ (will be discard for step 2, because we can always conclude $X.Y \rightarrow X$)
 $msin, mln \rightarrow mfn$
 $isrc, title, album, artist \rightarrow syear$
 $isrc, artist \rightarrow title$
 $isrc, artist \rightarrow album$
 $artist, label \rightarrow end$
 $artist, label \rightarrow rep$
 $rep \rightarrow label$
 $label \rightarrow icity$
 $label \rightarrow icountry$
 $isrc, wsin, title \rightarrow royalty$
 $isrc, wsin, title \rightarrow title$ (will be discard for step 2, because we can always conclude $X.Y \rightarrow X$)
 $isrc, wsin, title \rightarrow album$
 $wsin \rightarrow wfn$
 $wsin \rightarrow wln$
 $isrc \rightarrow artist$
 $isrc \rightarrow genre$

step 2: remove extraneous attributes

$artist \rightarrow member$
 $artist \rightarrow genre$
 $msin \rightarrow mln$
 $msin \rightarrow inst$
 $msin \rightarrow mfn$ (mln extraneous)
 $isrc \rightarrow syear$ ($title, album, artist$ extraneous)
 $isrc \rightarrow title$ ($artist$ extraneous)
 $isrc \rightarrow album$ ($artist$ extraneous)
 $artist, label \rightarrow end$
 $artist, label \rightarrow rep$
 $rep \rightarrow label$
 $label \rightarrow icity$
 $label \rightarrow icountry$
 $isrc, wsin \rightarrow royalty$ ($title$ extraneous)
 $isrc \rightarrow album$ ($wsin, title$ extraneous)
 $wsin \rightarrow wfn$
 $wsin \rightarrow wln$
 $isrc \rightarrow artist$
 $isrc \rightarrow genre$

step 3:

$artist^* = \{artist, member, genre\}$

$F_c = \{\text{artist} \rightarrow \text{member}\}$

$F_c = \{\text{artist} \rightarrow \text{member}, \text{artist} \rightarrow \text{genre}\}$

$M_{sin}^* = \{\text{Msin}, \text{mln}, \text{inst}, \text{mfn}\}$

$F_c = \{\text{artist} \rightarrow \text{member}, \text{artist} \rightarrow \text{genre}, \text{msin} \rightarrow \text{mln}, \text{msin} \rightarrow \text{inst}, \text{msin} \rightarrow \text{mfn}\}$

$Isrc^* = \{\text{isrc}, \text{year}, \text{title}, \text{album}, \text{artist}, \text{genre}, \text{member}\}$

$F_c = \{\text{artist} \rightarrow \text{member}, \text{artist} \rightarrow \text{genre}, \text{msin} \rightarrow \text{mln}, \text{msin} \rightarrow \text{inst}, \text{msin} \rightarrow \text{mfn}, \text{isrc} \rightarrow \text{year}, \text{isrc} \rightarrow \text{title}, \text{isrc} \rightarrow \text{album}, \text{isrc} \rightarrow \text{artist}\}$

$Label^* = \{\text{label}, \text{icity}, \text{icountry}\}$

$F_c = \{\text{artist} \rightarrow \text{member}, \text{artist} \rightarrow \text{genre}, \text{msin} \rightarrow \text{mln}, \text{msin} \rightarrow \text{inst}, \text{msin} \rightarrow \text{mfn}, \text{isrc} \rightarrow \text{year}, \text{isrc} \rightarrow \text{title}, \text{isrc} \rightarrow \text{album}, \text{isrc} \rightarrow \text{artist}, \text{label} \rightarrow \text{icity}, \text{label} \rightarrow \text{icountry}\}$

$(\text{Artist}, \text{label})^* = \{\text{artist}, \text{member}, \text{genre}, \text{label}, \text{icity}, \text{icountry}, \text{end}, \text{rep}\}$

$F_c = \{\text{artist} \rightarrow \text{member}, \text{artist} \rightarrow \text{genre}, \text{msin} \rightarrow \text{mln}, \text{msin} \rightarrow \text{inst}, \text{msin} \rightarrow \text{mfn}, \text{isrc} \rightarrow \text{year}, \text{isrc} \rightarrow \text{title}, \text{isrc} \rightarrow \text{album}, \text{isrc} \rightarrow \text{artist}, \text{label} \rightarrow \text{icity}, \text{label} \rightarrow \text{icountry}, \text{artist}, \text{label} \rightarrow \text{end}, \text{artist}, \text{label} \rightarrow \text{rep}\}$

$Rep^* = \{\text{rep}, \text{label}, \text{icity}, \text{icountry}\}$

$F_c = \{\text{artist} \rightarrow \text{member}, \text{artist} \rightarrow \text{genre}, \text{msin} \rightarrow \text{mln}, \text{msin} \rightarrow \text{inst}, \text{msin} \rightarrow \text{mfn}, \text{isrc} \rightarrow \text{year}, \text{isrc} \rightarrow \text{title}, \text{isrc} \rightarrow \text{album}, \text{isrc} \rightarrow \text{artist}, \text{label} \rightarrow \text{icity}, \text{label} \rightarrow \text{icountry}, \text{artist}, \text{label} \rightarrow \text{end}, \text{artist}, \text{label} \rightarrow \text{rep}, \text{rep} \rightarrow \text{label}\}$

$W_{sin}^* = \{\text{wsin}, \text{wfn}, \text{wln}\}$

$F_c = \{\text{artist} \rightarrow \text{member}, \text{artist} \rightarrow \text{genre}, \text{msin} \rightarrow \text{mln}, \text{msin} \rightarrow \text{inst}, \text{msin} \rightarrow \text{mfn}, \text{isrc} \rightarrow \text{year}, \text{isrc} \rightarrow \text{title}, \text{isrc} \rightarrow \text{album}, \text{isrc} \rightarrow \text{artist}, \text{label} \rightarrow \text{icity}, \text{label} \rightarrow \text{icountry}, (\text{artist}, \text{label}) \rightarrow \text{end}, (\text{artist}, \text{label}) \rightarrow \text{rep}, \text{rep} \rightarrow \text{label}, \text{wsin} \rightarrow \text{wfn}, \text{wsin} \rightarrow \text{wln}, (\text{isrc}, \text{wsin}) \rightarrow \text{royalty}\}$

Question 4

Lossless join decomposition:

First, we check and make sure that we have all attributes of F if we get the union of the sub relations which is true in this case.

Artist (artist, member, genre)

Plays (artist, msin)

Artist is the common attribute and $\text{Artist} \rightarrow \text{member}, \text{genre}$

So, artist is a candidate Key for Artist.

Musician (msin, mfn, mln, inst)

Plays (artist, msin)

msin is the common attribute and $\text{msin} \rightarrow \text{mln}, \text{inst} \ \& \ \text{msin}, \text{mln} \rightarrow \text{msin}, \text{mfn}$

So, msin is a candidate Key for Musician.

Publishes (artist, rep, end)

Reps (label, rep)

rep is the common attribute and $\text{Rep} \rightarrow \text{label}$

So, rep is a candidate Key for Reps.

Label (label, icity, icountry)

Reps (label, rep)

rep is the common attribute and $\text{Label} \rightarrow \text{icity, icountry}$

So, label is a candidate Key for Label.

Writes (isrc, wsin, royalty)

Song (isrc, title, album, syear, artist)

rep is the common attribute and $\text{Isrc, title, album, artist} \rightarrow \text{syear} \ \& \ \text{Isrc, artist} \rightarrow \text{title, album} \ \& \ \text{isrc} \rightarrow \text{artist}$

So, isrc is a candidate Key for Song.

Writer (wsin, wln, wfn)

Writes (isrc, wsin, royalty)

rep is the common attribute and $\text{Wsin} \rightarrow \text{wfn, wln}$

So, wsin is a candidate Key for Writer.

So, as we can see they're all connected together and the common attributes is key for either X or Y. so, this is lossless.

Dependency preservation:

Artist (artist, member, genre)

$\text{Artist} \rightarrow \text{member, genre}$

Musician (msin, mfn, mln, inst)

$\text{msin} \rightarrow \text{mln, inst}$

$\text{msin, mln} \rightarrow \text{msin, mfn}$

Song (isrc, title, album, syear, artist)

$\text{Isrc, title, album, artist} \rightarrow \text{syear}$

$\text{Isrc, artist} \rightarrow \text{title, album}$

Plays (artist, msin)

Label (label, icity, icountry)

$\text{Label} \rightarrow \text{icity, icountry}$

Publishes (artist, rep, end)

Reps (label, rep)

$\text{Rep} \rightarrow \text{label}$

Writer (wsin, wln, wfn)

$\text{Wsin} \rightarrow \text{wfn, wln}$

Writes (isrc, wsin, royalty)

NONE?

$\text{artist, label} \rightarrow \text{end, rep}$

$\text{isrc, wsin, title} \rightarrow \text{royalty, title, album}$

isrc → artist, genre

based on this schema F is not dependency preservation because as we can see there are 3 FD that can't be fit into anything.

BCNF

Artist (artist, member, genre)

Key: artist

Prime: artist

Non-prime: member, genre

Musician (msin, mfn, mln, inst)

Key: msin

Prime: msin

Non-prime: mfn, mln, inst

Song (isrc, title, album, syear, artist)

Key: isrc

Prime: isrc

Non-prime: title, album, syear, artist

Plays (artist, msin)

N/A

Label (label, icity, icountry)

Key: label

Prime: label

Non-prime: icity, icountry

Publishes (artist, rep, end)

Key: artist

Prime: artist

Non-prime: end, rep

Reps (label, rep)

Key: rep

Prime: rep

Non-prime: label

Writer (wsin, wln, wfn)

Key: wsin

Prime: wsin

Non-prime: wln, wfn

Writes (isrc, wsin, royalty)

Key: isrc, wsin

Prime: isrc, wsin

Non-prime: royalty

- artist → member, genre **Superkey**
- msin → mln, inst **Superkey**

- *msin, mln* → *msin, mfn* **Superkey**
- *isrc, title, album, artist* → *syear* **Superkey**
- *isrc, artist* → *title, album* **Superkey**
- *artist, label* → *end, rep* **Superkey**
- *rep* → *label* **Superkey**
- *label* → *lcity, lcountry* **Superkey**
- *isrc, wsin, title* → *royalty, title, album* **Superkey**
- *wsin* → *wfn, wln* **Superkey**
- *isrc* → *artist, genre* **Superkey**

it is BCNF because the RHS of all are superkey.

3NF

Every BCNF FD is also 3NF, because it satisfies the 3NF requirements too. So it is also 3NF

Question 5

Lossless join decomposition:

Artist (artist, members, genre, msin, mfn, mln, inst)

Song (isrc, title, album, syear, wsin, wln, wfn, royalty, artist)

artist is the common attribute but it's not key in any of them.

So, it's not lossless join decomposition.

Dependency preservation:

Artist (artist, members, genre, msin, mfn, mln, inst)

Artist → member, genre

msin → mln, inst

msin, mln → msn, mfn

Song (isrc, title, album, syear, wsin, wln, wfn, royalty, artist)

Isrc, title, album, artist → syear

Isrc, artist → title, album

isrc, wsin, title → royalty, title, album

Wsin → wfn, wln

Label (label, icity, icountry)

Label → icity, icountry

Publishes (label, artist, rep, end)

artist, label → end, rep

Rep → label

NONE?

isrc \rightarrow artist, genre

this is the only one which is not fitting we can decompose this as

isrc \rightarrow artist

isrc \rightarrow genre

we also know that

artist \rightarrow genre

so instead of isrc \rightarrow genre

if we write

isrc \rightarrow artist

artist \rightarrow genre

we can fit these two in Song and Artist respectively.

In this case we can say this is dependency preservation.

BCNF

Artist (artist, members, genre, msin, mfn, mln, inst)

Key: artist, msin

Prime: artist, msin

Non-prime: member, genre, mfn, mln, inst

In a lot of FDs, super key is not in LHS, like:

- *artist \rightarrow members, genre*
- *msin \rightarrow mln, inst*
- *msin, mln \rightarrow msin, mfn*

So it is not BCNF.

3NF

Artist (artist, members, genre, msin, mfn, mln, inst)

Key: artist, msin

Prime: artist, msin

Non-prime: member, genre, mfn, mln, inst

Song (isrc, title, album, syeal, wsin, wln, wfn, royalty, artist)

Key: isrc, wsin

Prime: isrc, wsin

Non-prime: title, album, syeal, wln, wfn, royalty, artist

Label (label, icity, icountry)

Key: label

Prime: label

Non-prime: icity, icountry

Publishes (label, artist, rep, end)

Key: label, artist

Prime: label, artist

Non-prime: rep, end

- *artist* → *members*, *genre* **Not satisfied**
- *msin* → *mln*, *inst* **Not satisfied**
- *msin*, *mln* → *msin*, *mfn* **Not satisfied**
- *isrc*, *title*, *album*, *artist* → *syear* **satisfied**
- *isrc*, *artist* → *title*, *album* **satisfied**
- *artist*, *label* → *end*, *rep* **satisfied**
- *rep* → *label* **satisfied**
- *label* → *lcity*, *lcountry* **satisfied**
- *isrc*, *wsin*, *title* → *royalty*, *title*, *album* **satisfied**
- *wsin* → *wfn*, *wln* **Not satisfied**
- *isrc* → *artist*, *genre* **Not satisfied**

so, this is not 3NF, as we see.

Question 6

Lossless join decomposition:

Artist (artist, member, genre)

Song (isrc, title, album, syear, artist)

artist is the common attribute and Artist → member, genre

So, artist is a candidate Key for Artist.

Label (label, icity, icountry)

Publishes (label, artist, rep, end)

label is the common attribute and Label → icity, icountry

So, label is a candidate Key for Label.

Writer (wsin, wln, wfn)

Writes (isrc, wsin, royalty)

wsin is the common attribute and Wsin → wfn, wln

So, wsin is a candidate Key for Writes.

It's lossless decomposition.

Dependency preservation:

Artist (artist, member, genre)

Artist → member, genre

Musician (msin, mfn, mln, inst)

msin → mln, inst

msin, mln → msin, mfn

Song (isrc, title, album, syear, artist)

Isrc, title, album, artist \rightarrow syear

Isrc, artist \rightarrow title, album

Label (label, icity, icountry)

Label \rightarrow icity, icountry

Publishes (label, artist, rep, end)

artist, label \rightarrow end, rep

Rep \rightarrow label

Writer (wsin, wln, wfn)

Wsin \rightarrow wfn, wln

Writes (isrc, wsin, royalty)

NONE

isrc, wsin, title \rightarrow royalty, title, album

isrc \rightarrow artist, genre

there's two FD that won't fit in any, for the second one we can apply what we discussed in Q5 and have it in Song and Artist which works,

we can rewrite isrc, wsin, title \rightarrow royalty, title, album

as isrc, wsin \rightarrow royalty, album using augmentation

using these two relations from Songs:

isrc, artist \rightarrow album

and

isrc \rightarrow artist.

we can say

isrc \rightarrow album

Now, we have these two:

isrc \rightarrow album

isrc, wsin \rightarrow royalty, album

which can be written as

isrc, wsin \rightarrow royalty

and this can be fit in Writes

doing these calculations, we can say there's dependency preservation.

BCNF

Artist (artist, member, genre)

Key: artist

Prime: artist
 Non-prime: member, genre
 Musician (msin, mfn, mln, inst)
 Key: msin
 Prime: msin
 Non-prime: mfn, mln, inst
 Song (isrc, title, album, syeal, artist)
 Key: isrc
 Prime: isrc
 Non-prime: title, album, syeal, artist
 Label (label, icity, icountry)
 Key: label
 Prime: label
 Non-prime: icity, icountry
 Publishes (label, artist, rep, end)
 Key: artist, label
 Prime: artist, label
 Non-prime: end, rep
 Writer (wsin, wln, wfn)
 Key: wsin
 Prime: wsin
 Non-prime: wln, wfn
 Writes (isrc, wsin, royalty)
 Key: isrc, wsin
 Prime: isrc, wsin
 Non-prime: royalty

- *artist -> members, genre **satisfied***
- *msin -> mln, inst **satisfied***
- *msin, mln -> msin, mfn **satisfied***
- *isrc, title, album, artist -> syeal **satisfied***
- *isrc, artist -> title, album **satisfied***
- *artist, label -> end, rep **satisfied***
- *rep -> label **not satisfied***
- *label -> icity, icountry **satisfied***
- *isrc, wsin, title -> royalty, title, album **satisfied***
- *wsin -> wfn, wln **satisfied***
- *isrc -> artist, genre **satisfied***

only because of *rep -> label* this is not BCNF.

3NF

- *artist* -> *members*, *genre* **satisfied**
- *msin* -> *mln*, *inst* **satisfied**
- *msin*, *mln* -> *msin*, *mfn* **satisfied**
- *isrc*, *title*, *album*, *artist* -> *syecar* **satisfied**
- *isrc*, *artist* -> *title*, *album* **satisfied**
- *artist*, *label* -> *end*, *rep* **satisfied**
- *rep* -> *label* **satisfied**
- *label* -> *lcity*, *lcountry* **satisfied**
- *isrc*, *wsin*, *title* -> *royalty*, *title*, *album* **satisfied**
- *wsin* -> *wfn*, *wln* **satisfied**
- *isrc* -> *artist*, *genre* **satisfied**

3NF requirement is satisfied in all of them, and because on the RHS of *rep* -> *label* there is prime attribute this FD is also satisfied, and it is 3NF