

ASSIGNMENT #4

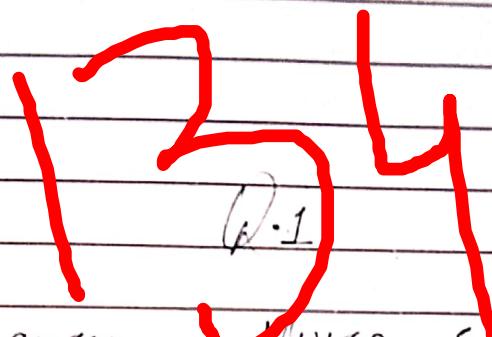
Date _____ 20 _____

NAME : SAAD - UR - REHMAN

Pg # ①

ID : 19K-0218

Sec : C.



DIRECTED

UNDIRECTED

MULTIPLE EDGES

ONE MORE THAN 1 loop

3

3.	No	Yes	No	No
4.	No	Yes	Yes	No
5.	No	Yes	Yes	Yes
6.	No	Yes	Yes	No
7.	Yes	No	Yes	Yes
8.	Yes	No	Yes	Yes
9.	Yes	No	Yes	Yes

Q.2

$$I) \quad d(N_i) = 2E$$

$$d(a) = 2$$

$$\text{sum of degree} = 12$$

$$d(b) = 4$$

$$\text{no. of edges} = 6$$

$$d(c) = 1$$

$$d(d) = 0$$

$$\Rightarrow 12 = 2 \times 6$$

$$d(e) = 2$$

$$\boxed{12 = 12} \quad \text{Proven}$$

$$d(f) = 3$$

2-

Pg # (2)

$$\deg(a) = 6$$

$$\deg(b) = 6$$

$$\deg(c) = 6$$

$$d(d) = 5$$

$$d(e) = 3.$$

Sum of deg = 26

No. of edges = 13 -

$$26 = 2 \times E$$

$$26 = 2 \times 13$$

$$\boxed{\underline{26 = 26}}$$

3-

$$d(a) = 3$$

$$d(b) = 2.$$

$$d(c) = 4$$

$$d(d) = 0.$$

$$d(e) = 6.$$

$$d(f) = 0.$$

$$d(g) = 4.$$

$$d(h) = 2.$$

$$d(i) = 3.$$

Sum of degrees = 24

No. of edges = 12.

$$24 = 2 \times 12$$

$$\boxed{\underline{24 = 24}}$$

Q. 3

Pg # 3.

$$\begin{aligned}\sum d(v) &= \sum d(e) + \sum d(b) \\ &= e + 0 \\ &= e.\end{aligned}$$

→ It conclude that whenever we add two even no. or two odd no. or one even & one odd, it will always give even NO. sum.

Q. 1.

No. of vertices = 4.

No. of edges = 7.

$\deg^-(a) = 3$	$\deg^+(a) = 1$
$\deg^-(b) = 1$	$\deg^+(b) = 2$
$\deg^-(c) = 2$	$\deg^+(c) = 1$
$\deg^-(d) = 1$	$\deg^+(d) = 3$
$\Rightarrow 2 = \deg^-(V) + \deg^+(V)$	$\Rightarrow 7$
$\boxed{7 = 7 = 7}$	$\Rightarrow 7$

$$\begin{aligned}\therefore 2 &= \deg^-(V) + \deg^+(V) \\ \boxed{7} &= \boxed{7} = \boxed{7}\end{aligned}$$

Q. 2) No. of vertices = 4

No. of edges = 8.

$\deg^-(a) = 2$	$\deg^+(a) = 2$
$\deg^-(b) = 3$	$\deg^+(b) = 3$
$\deg^-(c) = 2$	$\deg^+(c) = 1$
$\deg^-(d) = 1$	$\deg^+(d) = 1$
$\Rightarrow 8$	$\Rightarrow 8$

No. of vertices = 5

No. of edges = 13

$\deg^-(a) = 6$	$\deg^+(a) = 1$
$\deg^-(b) = 1$	$\deg^+(b) = 5$
$\deg^-(c) = 2$	$\deg^+(c) = 5$
$\deg^-(d) = 4$	$\deg^+(d) = 2$
$\deg^-(e) = 0$	$\deg^+(e) = 0$
$\Rightarrow 13$	$\Rightarrow 13$

Q.4

Pg # ④

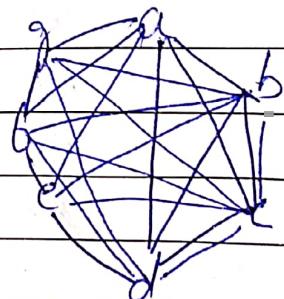
7) $f = \deg^-(V) = \deg^+(N)$
 $f = f^- + f^+$
 equal.

8) $f = \deg^-(V) = \deg^+(N)$
 $8 = 8^- - 8$
 equal.

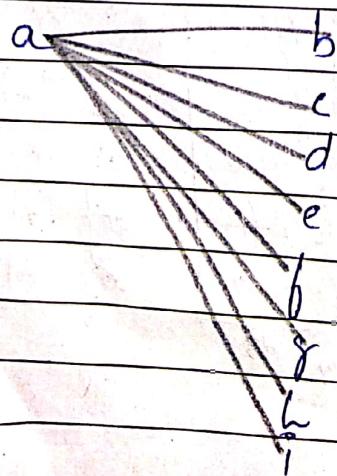
9) $f = \deg^-(V) = \deg^+(N)$
 $13 = 13^- - 13$
 equal.

Q.5

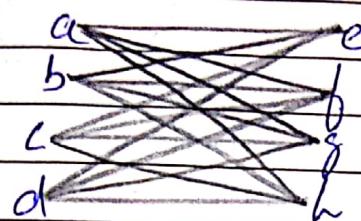
a) K7.



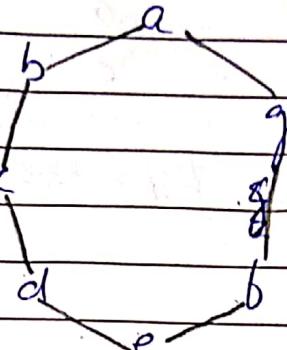
b) K1,8.



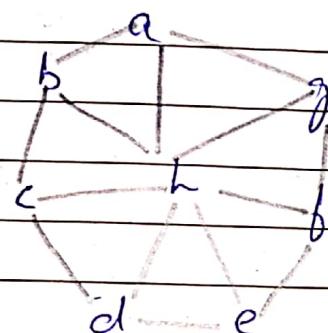
(c) K4,4



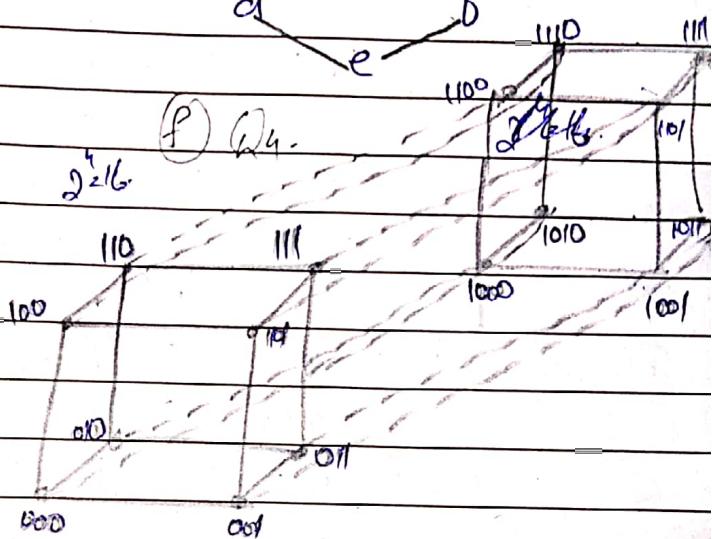
(d) C7

~~B4~~(S)

(e) VJ2.



(f) Q4.



(Q.6)

21-

V1

V2.

a

e

b

c

d

Yes, it is bipartite.

22-

V1

V2.

a

d

Yes, it is bipartite

c

b

e

Pg 56 (6).

23-

	V ₁	V ₂
a		b
c		b
d		

Not bipartite as f is creating problem -

24-

	V ₁	V ₂
a		f
c		c
b		
d		

Yes, it is Bipartite.

25-

	V ₁	V ₂
a		b
c		f
e		

It is not bipartite.

Q. 8

Pg No. ⑧

ADJACENCY LIST:-

a : b, c, d

b : a, d

c : a, d

d : a, b, c

ADJACENCY MATRIX

	a	b	c	d
a	0	1	1	1
b	1	0	0	1
c	1	0	0	1
d	1	1	1	0

INCIDENCE MATRIX:-

a	1	1	0	0
b	1	0	1	0
c	0	0	0	1
d	0	1	1	0

ADJACENCY MATRIX:

- a : b, c, d, e
b : a, d, e
c : d, e
d : a, b, c
e : b, c

	a	b	c	d	e
a	0	1	0	1	0
b	1	0	0	1	1
c	0	0	0	1	1
d	1	1	1	0	0
e	0	1	1	0	0

INCIDENCE MATRIX:-

	e ₁	e ₂	e ₃	e ₄	e ₅	e ₆
a	1	1	0	0	0	0
b	1	0	1	1	0	0
c	0	0	0	1	1	0
d	0	1	1	0	0	0
e	0	0	0	1	0	1

Date _____
Pg # ⑧

3-)

ADJACENCY LIST:-

- a: a, b, c, d.
- b: d.
- c: a, b.
- d: d, c, b.

ADJACENCY MATRIX:-

	a	b	c	d
a	1	1	1	1
b	0	0	0	1
c	1	1	0	0
d	0	1	1	1

INCIDENCE MATRIX:-

	e_1	e_2	e_3	e_4	e_5	e_6	e_7	e_8	e_9	e_{10}
a	1	1	0	1	1	0	0	0	0	0
b	0	0	0	0	0	0	0	0	0	0
c	0	0	1	0	0	1	0	0	0	0
d	0	0	0	0	0	0	1	1	0	0

4) ADJACENCY LIST:-

- a: b, d.
- b: a, d, e, c.
- c: c, b
- d: a, e.
- e: e, c.

ADJACENCY MATRIX:-

	a	b	c	d	e
a	0	1	0	1	0
b	1	0	1	1	1
c	0	1	1	0	0
d	1	0	0	0	1
e	0	0	1	0	1

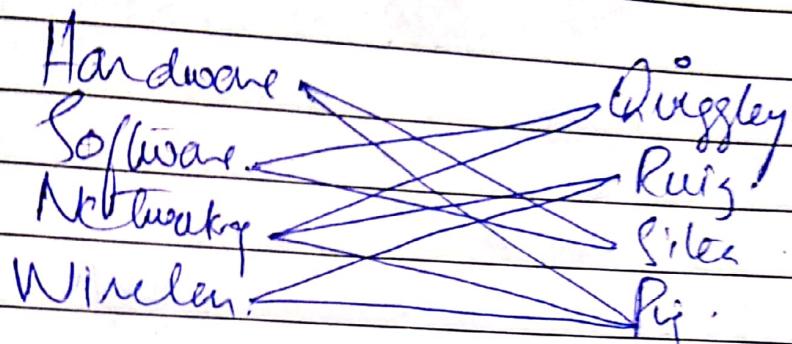
INCIDENCE MATRIX:-

1	-1	1	-1	0	0	0	0	0	0	0
0	0	0	0	-1	0	-1	-1	-1	0	0
0	0	0	0	0	0	0	-1	1	1	0
-1	1	0	0	-1	-1	0	0	0	0	0
0	0	0	0	0	1	0	0	0	1	1

Qst

Pg # (7)

a).



SOL

b) The Hall's theorem is valid if big is assigned hardware, Quigley is assigned networking, Ruiz is assigned wireless & Siles is assigned software.

→

c) There are multiple possible assignments of employees to support areas.

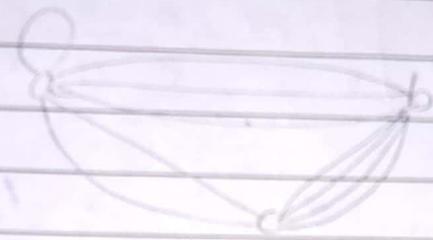
Let us choose big for hardware there are only one possible area for each of other three employees.

Date _____

B# ⑩

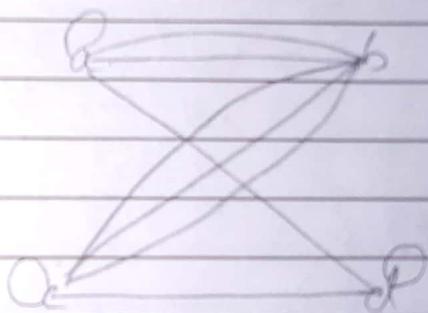
Q9

16. α [a b c]
a [1 3 2]
b [3 0 4]
c [2 4 0]



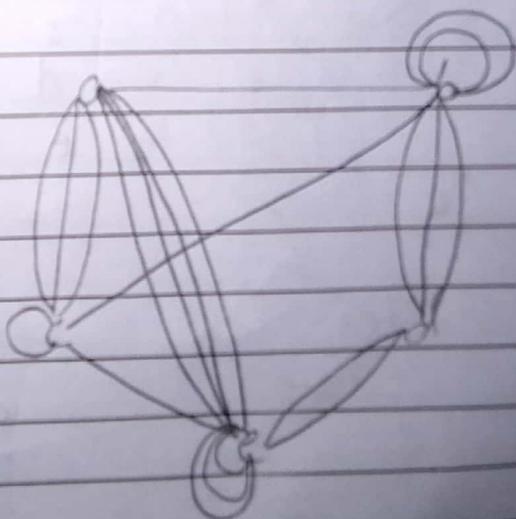
7- 17! a b c d

$$\begin{array}{l} a \left[\begin{array}{cccc} 1 & 2 & 0 & 1 \end{array} \right] \\ b \left[\begin{array}{cccc} 2 & 0 & 3 & 1 \end{array} \right] \\ c \left[\begin{array}{cccc} 0 & 3 & 1 & 1 \end{array} \right] \\ d \left[\begin{array}{cccc} 1 & 0 & 1 & 0 \end{array} \right] \end{array}$$



8- 18! a b c d e

$$\begin{array}{l} a \left[\begin{array}{ccccc} 0 & 1 & 3 & 0 & 4 \end{array} \right] \\ b \left[\begin{array}{ccccc} 1 & 2 & 1 & 3 & 0 \end{array} \right] \\ c \left[\begin{array}{ccccc} 3 & 1 & 1 & 0 & 1 \end{array} \right] \\ d \left[\begin{array}{ccccc} 0 & 3 & 0 & 0 & 2 \end{array} \right] \\ e \left[\begin{array}{ccccc} 4 & 0 & 1 & 2 & 3 \end{array} \right] \end{array}$$



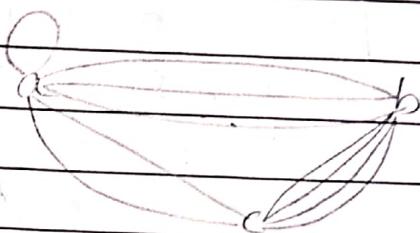
Date _____

Pg # (10)

Q.9

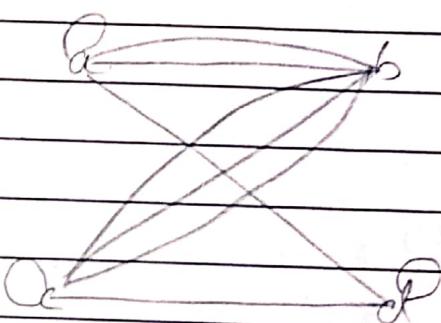
a b c.

16.	a	1 3 2]
	b	3 0 4	
	c	2 4 0	



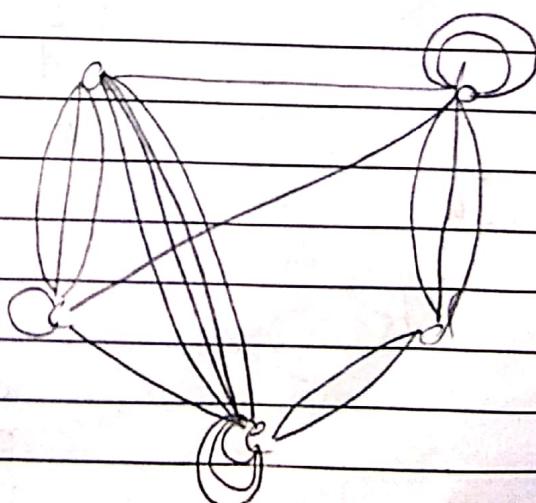
Q. 17! a b c d

a	1 2 0 1]
b	2 0 3 1	
c	0 3 1 1	
d	1 0 1 0	



Q. 18! a b c d e

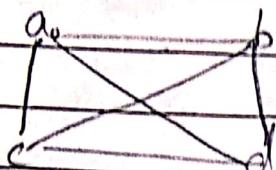
a	0 1 3 0 4]
b	1 2 1 3 0	
c	3 1 1 0 1	
d	0 3 0 0 2	
e	4 0 1 2 3	



Q.10

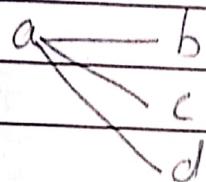
D
Pg. No. 10

a) K₄



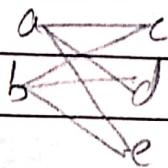
	a	b	c	d
a	0	1	1	1
b	1	0	1	1
c	1	1	0	1
d	1	1	1	0

b) K_{1,4}.



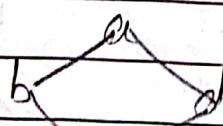
	a	b	c	d
a	0	1	1	1
b	1	0	0	0
c	1	0	0	0
d	1	0	0	0

c) K_{2,3}.



	a	b	c	d	e
a	0	0	1	1	1
b	0	0	1	1	1
c	1	1	0	0	0
d	1	1	0	0	0
e	1	1	0	0	0

d) C₄.

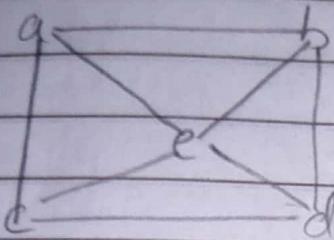


	a	b	c	d
a	0	1	0	1
b	1	0	1	0
c	0	1	0	1
d	1	0	1	0

Date _____

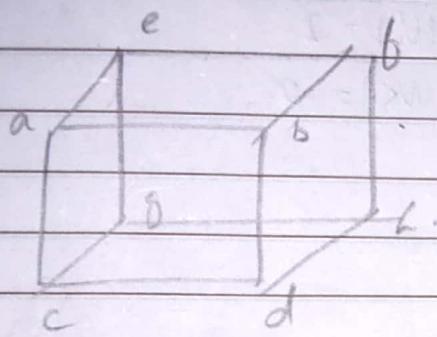
Pg # ⑩

(e) W4.



	a	b	c	d	e
a	0	1	1	0	1
b	1	0	0	1	1
c	1	0	0	1	1
d	0	1	1	0	1
e	1	1	1	0	0

1 Q3-



	a	b	c	d	e	f	g	h	i
a	0	1	1	0	1	0	0	0	0
b	1	0	0	1	0	1	0	0	0
c	1	0	0	1	0	0	1	0	0
d	0	1	0	0	0	0	1	0	0
e	1	0	0	0	0	1	1	0	0
f	0	1	0	0	1	0	0	1	0
g	0	0	1	0	1	0	0	1	0
h	0	0	0	1	0	1	1	0	0
i	0	0	0	1	0	1	1	0	0

Q3

Q. 11

	a	b	c	d
a	0	1	0	0
b	0	1	1	0
c	0	1	1	1
d	1	0	0	0

	a	b	c	d
a	1	1	1	1
b	0	1	0	1
c	1	0	1	0
d	1	1	1	1

	a	b	c	d
a	1	1	2	1
b	1	0	0	2
c	1	0	1	1
d	0	2	1	0

Q. 12

38.

$$\deg(U_1) = 1.$$

$$\deg(U_2) = 2.$$

$$\deg(W_1) = 2.$$

$$\deg(U_3) = 2.$$

$$\deg(U_4) = 1.$$

$$\deg(V_1) = 1.$$

$$\deg(V_2) = 2.$$

$$\deg(W_3) = 1.$$

$$\deg(W_4) = 2.$$

$$\deg(W_5) = 2.$$

$$f(U_1) = V_1.$$

$$f(U_2) = V_2.$$

$$f(U_3) = V_4.$$

$$f(U_4) = V_5.$$

$$f(U_5) = V_3.$$

It is isomorphic.

39.

$$\deg(U_1) = 2.$$

$$\deg(U_2) = 2.$$

$$\deg(U_3) = 2.$$

$$\deg(U_4) = 2.$$

$$\deg(U_5) = 2.$$

$$\deg(W_1) = 2.$$

$$\deg(W_2) = 2.$$

$$\deg(W_3) = 2.$$

$$\deg(W_4) = 2.$$

$$\deg(W_5) = 2.$$

H is isomorphic.

40.

$$\deg(U_1) = 3.$$

$$\deg(U_2) = 2.$$

$$\deg(U_3) = 3.$$

$$\deg(U_4) = 3.$$

$$\deg(U_5) = 3.$$

$$\deg(V_1) = 2.$$

$$\deg(V_2) = 3.$$

$$\deg(V_3) = 2.$$

$$\deg(V_4) = 3.$$

$$\deg(V_5) = 3.$$

Not isomorphic as degrees of vertices
are not same.

41.

$$\deg(U_1) = 3. 2$$

$$\deg(U_2) = 4. 2$$

$$\deg(U_3) = 2$$

$$\deg(U_4) = 3$$

$$\deg(U_5) = 2$$

$$\deg(U_6) = 2$$

$$\deg(U_7) = 2$$

$$\deg(V_1) = 2$$

$$\deg(V_2) = 2$$

$$\deg(V_3) = 2$$

$$\deg(V_4) = 2$$

$$\deg(V_5) = 2$$

$$\deg(V_6) = 2$$

$$\deg(V_7) = 2$$

Yes, it is isomorphic.

42.

$$d(U_1) = 3$$

$$d(U_2) = 4$$

$$d(U_3) = 2$$

$$d(U_4) = 4$$

$$d(U_5) = 3$$

$$\cancel{d(U_6)}$$

$$d(V_1) = 3$$

$$d(V_2) = 2$$

$$d(V_3) = 4$$

$$d(V_4) = 3$$

$$d(V_5) = 4$$

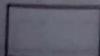
$$f(U_1) = V_1$$

$$f(U_2) = V_5. 3$$

$$f(U_3) = V_2.$$

$$f(U_4) = V_5$$

$$f(U_5) = V_4.$$



43.

$$d(U_1) = 3$$

$$d(U_2) = 3$$

$$d(U_3) = 3$$

$$d(U_4) = 3$$

$$d(U_5) = 3$$

$$d(U_6) = 3$$

$$d(N_1) = 3$$

$$d(N_2) = 3$$

$$d(N_3) = 3$$

$$d(N_4) = 3$$

$$d(N_5) = 3$$

$$d(N_6) = 3$$

It is isomorphic.

44 - degree of vertices are not same, hence
not isomorphic.

$$45 - d(U_1) = 1$$

$$d(U_2) = 2$$

$$d(U_3) = 3$$

$$d(U_4) = 1$$

$$d(U_5) = 2$$

$$d(U_6) = 3$$

$$d(U_7) = 1$$

$$d(U_8) = 1$$

$$d(N_1) = 1$$

$$d(N_2) = 3$$

$$d(N_3) = 1$$

$$d(N_4) = 2$$

$$d(N_5) = 2$$

$$d(N_6) = 3$$

$$d(N_7) = 1$$

$$d(N_8) = 1$$

Not isomorphic.

Q. 13.

1. \rightarrow Not Euler path because there are more than two vertices with odd degree.
 \rightarrow Not a Euler circuit as well.

2. Not Euler path & Euler circuit.

3. If has a Euler path.

$a \rightarrow b \rightarrow e \rightarrow b \rightarrow d \rightarrow e \rightarrow c \rightarrow e \rightarrow a \rightarrow e \rightarrow d$.

\hookrightarrow Not a Euler circuit.

4. If has an Euler path as only two vertices have odd degree.

$a \rightarrow b \rightarrow d \rightarrow a \rightarrow e \rightarrow f \rightarrow b \rightarrow c \rightarrow d \rightarrow e \rightarrow c$.

5. Euler circuit : $a \rightarrow b \rightarrow c \rightarrow d \rightarrow c \rightarrow e \rightarrow b \rightarrow d \rightarrow e \rightarrow a \rightarrow e \rightarrow a$.

\rightarrow Not Euler path as it doesn't contain any odd degree of vertices.

6. Extra Euler path.

$b \rightarrow i \rightarrow c \rightarrow d \rightarrow f \rightarrow e \rightarrow d \rightarrow a \rightarrow l \rightarrow i \rightarrow g \rightarrow o$
 $\rightarrow i \rightarrow o \rightarrow b$.

Q-15

Date _____

18- $d(a) = 3, d(b) = 4, d(c) = 4, d(d) = 5$.

Euler path exists.

$$\rightarrow a \rightarrow b \rightarrow d \rightarrow c \rightarrow a \rightarrow d \rightarrow b \rightarrow c \rightarrow d.$$

19- $d(a) = 3, d(b) = 4, d(c) = 4, d(d) = 3$.

Neither path nor circuit.

20- $d(a) = 2, d(b) = 6, d(c) = 2, d(d) = 4, d(e) = 4$.

Euler circuit exists:

$$(a \rightarrow d \rightarrow b \rightarrow d \rightarrow e \rightarrow b \rightarrow e \rightarrow c \rightarrow b \rightarrow a).$$

21- $d(a) = 3, d(b) = 6, d(c) = 4, d(d) = 4, d(e) = 7$.

Euler path exists.

$$a \rightarrow d \rightarrow e \rightarrow b \rightarrow a \rightarrow e \rightarrow d \rightarrow b \rightarrow e \rightarrow c \rightarrow b \rightarrow c \rightarrow e \rightarrow b.$$

22- $d(a) = 4, d(b) = 7, d(c) = 5, d(d) = 4, d(e) = 6$,

 $d(f) = 6$.

Euler path exists.

$$b \rightarrow d \rightarrow e \rightarrow b \rightarrow c \rightarrow e \rightarrow b \rightarrow f \rightarrow e.$$

$$c \rightarrow b \rightarrow c \rightarrow b \rightarrow f.$$

$$c \rightarrow e \rightarrow b \rightarrow c \rightarrow d \rightarrow d \rightarrow c \rightarrow b \rightarrow f \rightarrow a \rightarrow f \rightarrow e \rightarrow f$$

$$\rightarrow d \rightarrow e \rightarrow a \rightarrow b$$

Q. 16

30. It is not hamilton circuit because vertex are repeating when moving $e \rightarrow f$.

31. It is a hamilton circuit.

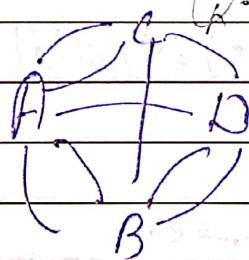
(a, b, c, d, e, f)

32. Not hamilton circuit. because once it reaches vertex f, no way to return, in this way vertex is repeating.

33. Not hamilton circuit.

e, g, f vertex can't be returned without repeating a edge.

Q. 14.



$$d(A) = 5, d(B) = 5, d(C) = 4, d(D) = 4.$$

No, it is not possible for an euler circuit degree of each vertex should be even.

